## 750 GeV Diphoton Excess May Not Imply a 750 GeV Resonance

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We discuss nonstandard interpretations of the 750 GeV diphoton excess recently reported by the ATLAS and CMS Collaborations which do *not* involve a new, relatively broad resonance with a mass near 750 GeV. Instead, we consider the sequential cascade decay of a much heavier, possibly quite narrow, resonance into two photons along with one or more additional particles. The resulting diphoton invariant mass signal is generically rather broad, as suggested by the data. We examine three specific event topologies—the "antler," the "sandwich," and the two-step cascade decay—and show that they all can provide a good fit to the observed published data. In each case, we delineate the preferred mass parameter space selected by the best fit. In spite of the presence of extra particles in the final state, the measured diphoton  $p_T$  spectrum is moderate due to its anticorrelation with the diphoton invariant mass. We comment on the future prospects of discriminating with higher statistics between our scenarios, as well as from more conventional interpretations.

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Introduction.—Recently, the ATLAS and Collaborations have reported first results with data obtained at the Large Hadron Collider (LHC) operating at 13 TeV. The data show an intriguing excess in the inclusive diphoton final state [1,2]. The ATLAS Collaboration further reported that about 15 events in the diphoton invariant mass distribution are observed above the standard model (SM) expectation at  $3.9\sigma$  local significance ( $2.3\sigma$ global significance) with 3.2 fb<sup>-1</sup> of data. The excess appears as a bump at  $M \sim 750$  GeV with a relatively broad width  $\Gamma \sim 45$  GeV, resulting in  $\Gamma/M \sim 0.06$  [1]. Similar results are reported by the CMS Collaboration for 2.6 fb<sup>-1</sup> of data-there are about ten excess events at a local significance of  $2.6\sigma$  ( $2.0\sigma$ ) assuming a narrow (wide) width [2]. The anomalous events are not accompanied by significant extra activity, e.g., missing transverse energy  $E_T$  [3]. The required cross section for the excess is ~10 fb at 13 TeV, and, so far, no indication of a similar excess has been observed in other channels.

While waiting for the definitive verdict on this anomaly from additional LHC data, it is fun to speculate on new physics scenarios which are consistent with the current data. Since the excess was seen in the diphoton invariant mass spectrum, the most straightforward interpretation would involve the production of a resonance with mass near 750 GeV, which decays directly to two photons. The relative broadness of the observed feature would imply that this resonance has a relatively large width, creating some tension with its nonobservation in other channels. Since the initial announcement, many models along those lines have

been proposed, e.g., in the context of extended Higgs sectors [4], supersymmetry [5], extra dimensions [6], strong dynamics [7], or effective field theory [8].

In this Letter, we entertain a different interpretation of the diphoton excess in the context of a sequential cascade decay of a much heavier, possibly quite narrow, resonance, resulting in a final state with two photons and one or two *additional* particles (see, also, Ref. [9]). Three specific examples of such simplified model [10] event topologies are exhibited in Fig. 1: an "antler" topology [14] in Fig. 1(a), a "sandwich" topology [15] in Fig. 1(b), and a two-step cascade decay in Fig. 1(c). In such scenarios, the resulting diphoton invariant mass  $m_{\gamma\gamma}$  is typically characterized by a somewhat broad distribution, which eliminates the necessity of an intrinsically broad resonance. Furthermore, the peak of the  $m_{\gamma\gamma}$  distribution is found near the upper kinematic end point, making it likely that the first signal events will be seen at large invariant mass, while

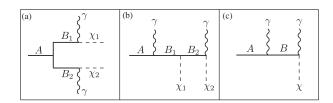


FIG. 1. The event topologies with two photons  $\gamma$  (wavy lines) and up to two additional particles  $\chi_i$  (dashed lines) under consideration in this Letter: (a) antler, (b) sandwich, and (c) two-step cascade decay. Solid lines correspond to heavier resonances  $(A, B_i)$ .

the low mass tail remains buried under the steeply falling SM background. Interestingly, for signal events with the required extreme values of  $m_{\gamma\gamma}$ , the transverse momentum of the diphoton system  $p_T^{\gamma\gamma}$  turns out to be rather moderate due to its anticorrelation with the diphoton mass  $m_{\gamma\gamma}$ . Given the small signal statistics [O(10)] events, such cascade decays may easily fake the standard diphoton resonance signature and deserve further scrutiny. We note that this observation is not restricted to the diphoton channel but is quite general and applicable to any inclusive resonance search in a two-body final state.

Diphoton invariant mass spectrum.—We first review the diphoton invariant mass distributions corresponding to the above-mentioned three event topologies from Fig. 1. The differential distribution of the diphoton invariant mass  $m \equiv m_{\gamma\gamma}$ ,

$$\frac{dN}{dm} \equiv f(m; M_A, M_{B_i}, M_{\chi_i}) \tag{1}$$

is known analytically (see, e.g., Ref. [16]) and is simply a function of the unknown masses  $M_A$ ,  $M_{B_i}$ , and  $M_{\chi_i}$ . The kinematic end point (henceforth, denoted as E) is defined as the maximum value of m allowing a nonzero f(m), i.e.,  $E \equiv \max\{m\}$ .

Ignoring for the moment spin correlations and assuming pure phase space distributions, the shape in the case of the antler topology of Fig. 1(a) is given by [14]

$$f(m) \sim \begin{cases} \eta m, & 0 \le m \le e^{-\eta} E, \\ m \ln(E/m), & e^{-\eta} E \le m \le E, \end{cases}$$
 (2)

where the end point E and the parameter  $\eta$  are defined in terms of the mass parameters as

$$E = \sqrt{e^{\eta} (M_{B_1}^2 - M_{\chi_1}^2) (M_{B_2}^2 - M_{\chi_2}^2) / (M_{B_1} M_{B_2})},$$
 (3)

$$\eta = \cosh^{-1}[(M_A^2 - M_{B_1}^2 - M_{B_2}^2)/(2M_{B_1}M_{B_2})]. \eqno(4)$$

The corresponding shape for the sandwich topology is given by the same expression (2); only this time, E and  $\eta$  are defined as follows [16]:

$$E = \sqrt{e^{\eta} (M_A^2 - M_{B_1}^2) (M_{B_2}^2 - M_{\chi_2}^2) / (M_{B_1} M_{B_2})}, \quad (5)$$

$$\eta = \cosh^{-1}[(M_{B_1}^2 + M_{B_2}^2 - M_{\chi_1}^2)/(2M_{B_1}M_{B_2})]. \quad (6)$$

In both cases, for small enough values of  $\eta$ , the peak location  $e^{-\eta}E$  can be arbitrarily close to the end point E.

Finally, the two-step cascade decay has the well-known triangular shape

$$f(m) \sim m,\tag{7}$$

where the distribution extends up to

$$E = \sqrt{(M_A^2 - M_B^2)(M_B^2 - M_\chi^2)/M_B^2}.$$
 (8)

For all three event topologies in Fig. 1 [assuming small enough values of  $\eta$  in Eq. (2)], the distributions are characterized by a relatively broad peak near the kinematic end point and a continuously falling tail to lower values of m. Given that the SM background distribution for  $m_{\gamma\gamma}$  is a very steeply falling function, the low m tail can be easily hidden in the background, and the only feature of the signal distribution which would be visible in the early data is the peak itself.

Signal models.—For the numerical studies below, we choose the following signal models realizing the topologies of Fig. 1. In the antler topology of Fig. 1(a), the particle  $A(B_i, \chi_i)$  is a scalar (fermion, fermion), and the fermion coupling to the photon is vectorlike,  $\sim \bar{B}_i \sigma^{\mu\nu} \chi_i F_{\mu\nu}$ , where  $F_{\mu\nu}$  is the photon field strength tensor. For the sandwich topology of Fig. 1(b), particle A is a heavy U(1) vector boson with field strength tensor  $F'_{\mu\nu}$ , which couples to a scalar  $B_1$  as  $\sim B_1 F'_{\mu\nu} F^{\mu\nu}$ , while  $B_2$  and  $\chi_i$  are fermions with vectorlike couplings to photons as before. Finally, in the two-step cascade decay of Fig. 1(c), A and  $\chi$  are vector particles coupling to a scalar B as above. In all three cases, the diphoton invariant mass distribution is given by the analytical results of the previous section [17].

Data analysis.—Given the analytical results (2)–(8), we now try to fit the three models from Fig. 1 to the  $m_{\gamma\gamma}$  spectrum data reported by the ATLAS Collaboration [1] (black dots in Fig. 2). To describe the background portion in the data, we introduce the same background model function as in Ref. [1],

$$f_{\text{hg}}(x;b,a) = (1-x^{1/3})^b x^a,$$
 (9)

where a and b are fit parameters to be determined by the data and  $x = m/\sqrt{s}$  with  $\sqrt{s} = 13$  TeV. We then perform likelihood fits using combined signal + background templates using f(m) from Eqs. (2) and (7) and  $f_{bg}(m)$  from Eq. (9). Our fit results for the case of Figs. 1(a) and 1(b) [Fig. 1(c)] are shown in the upper (lower) panel of Fig. 2. The red solid curves represent the best-fit models (i.e., signal + background), while the red dashed (blue solid) curves describe their background (signal) components. To estimate parameter errors more carefully with low statistics, we generate 10 000 pseudo-data-sets via random samplings of the data point in each bin, assuming a Poisson distribution with its mean value parameter set to the number of events in each bin reported by the ATLAS Collaboration (any zero bins in the real data were always sampled to be 0). We then conduct the same fit procedure explained above for all pseudo-data-sets and obtain distributions of fitted model parameters, from which we extract mean values and  $1\sigma$ confidence intervals, along with reduced  $\chi^2$  distributions.

For the antler and sandwich cases, the relevant reduced  $\chi^2$  distribution yields a mean (median) value of 0.98 (0.93) with

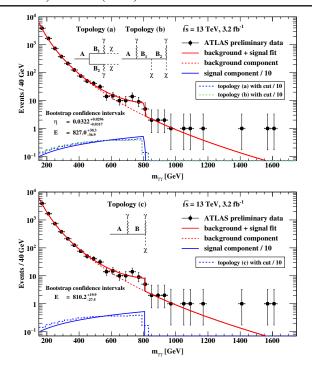


FIG. 2. Upper panel: The ATLAS diphoton data (black dots) and our fit results with the antler and sandwich event topologies, Eq. (2). The red solid curve represents the best-fit signal plus background distribution. The blue dashed (green dashed) curve represents the best-fit Monte Carlo event distribution in the antler (sandwich) case after incorporating the ATLAS analysis cuts. Lower panel: The same but for the two-step cascade decay of Fig. 1(c).

the Gaussian width around 1, indicating that our fitting template accommodates pseudo-data-samples well enough. The extracted best-fit parameter values and their  $1\sigma$  errors are

$$\eta = 0.0322^{+0.0296}_{-0.0317}, \qquad E = 827.0^{+30.3}_{-36.9} \text{ GeV}. \quad (10)$$

Because of the set of cuts applied in the ATLAS analysis to suppress the SM backgrounds, the resulting signal distributions could be distorted. In order to account for those effects, we simulate single production of particle A at LHC13 with MadGraph5\_aMC@NLO [18], followed by PYTHIA 6.4 [19] and DELPHES 3 [20]. We take  $M_A=1.7$  TeV, and the remaining masses are chosen in accordance with the best-fit E and  $\eta$  from Eq. (10). Since the antler and the sandwich scenarios have, in principle, different cut sensitivity, we show the corresponding distributions with the blue (antler) and green (sandwich) dashed curves in the upper panel of Fig. 2.

For the two-step cascade scenario, the relevant reduced  $\chi^2$  distribution shows a mean (median) value of 0.69 (0.67) with the Gaussian width around 0.5, indicating that this model also reproduces the data well enough. The best-fit value for E and its  $1\sigma$  error are reported as

$$E = 810.2^{+19.9}_{-27.5} \text{ GeV}.$$
 (11)

As before, the signal distribution after cuts is shown by the blue dashed curve in the lower panel of Fig. 2.

Discussion and outlook.—Since the number of experimentally measurable parameters for the antler topology is two (namely,  $\eta$  and E) [16], the underlying mass spectrum is not fully determined. However, a phenomenologically motivated scenario is the case where the decay is symmetric, i.e.,  $B_1 = B_2$  and  $\chi_1 = \chi_2$ . We then have three input mass parameters, two of which can be given as functions of the third mass, using the measured values for  $\eta$  and E. Taking  $M_{\chi}$  as a free parameter, we find that  $M_A$  and  $M_B$  can be expressed as follows:

$$M_B = (e^{-\eta/2}E + \sqrt{e^{-\eta}E^2 + 4M_\chi^2})/2,$$
 (12)

$$M_A = \sqrt{2M_B^2(\cosh \eta + 1)}. (13)$$

The upper-left panel of Fig. 3 displays the corresponding  $1\sigma$  mass ranges for the A (blue region and curves) and B (red region and curves) particles as a function of  $M_{\nu}$ .

For the sandwich topology of Fig. 1(b), we can similarly reduce the number of input mass degrees of freedom by considering the simple case of  $\chi_1 = \chi_2$  as a well-motivated phenomenological scenario. Then, using the measurements (10), we can predict the masses of two of the unknown particles, say,  $M_{B_1}$  and  $M_{B_2}$ , as a function of the other two,  $M_A$  and  $M_\chi$ , as shown in the middle left panel of Fig. 3 ( $M_{B_1}$  only for illustration).

Finally, for the two-step cascade topology of Fig. 1(c), only one parameter, Eq. (11), can be measured from the data. This provides one relation among the three unknown masses  $M_A$ ,  $M_B$ , and  $M_\chi$ , which is depicted in the bottom-left panel of Fig. 3.

We have seen that the cascade event topologies from Fig. 1 can provide a good fit to the diphoton invariant mass spectrum in Fig. 2. It is, therefore, natural to ask what other kinematic variables of the diphoton system can be used to test our hypothesis. One such possibility is the transverse momentum of the diphoton system  $p_T^{\gamma\gamma}$ , since it is sensitive to other objects recoiling against the two photons. However, there exists an inverse correlation between the two diphoton kinematic variables  $m_{\gamma\gamma}$  and  $p_T^{\gamma\gamma}$ , as illustrated in the right panels of Fig. 3: events with extreme values of  $m_{\gamma\gamma}$  have relatively small  $p_T^{\gamma\gamma}$  and vice versa. The anticorrelation trend is especially pronounced for the antler event topology, as demonstrated in the left panel of Fig. 4, where we show the  $p_T^{\gamma\gamma}$  distribution of simulated events near the bump,  $m_{\gamma\gamma} \in (700, 800)$  GeV, for 3.2 fb<sup>-1</sup> of data with the ATLAS selection cuts [1]. For such events, the typical angular separation (in the laboratory frame) between the two photons is anticipated to be large, and if the photons are almost back to back, then so must be the two  $\chi$ 's, yielding a relatively small net  $p_T^{\gamma\gamma}$ . Figure 4 is consistent with Ref. [3] and shows that the signal events lead to a rather featureless tail in the  $p_T^{\gamma\gamma}$  distribution. With the

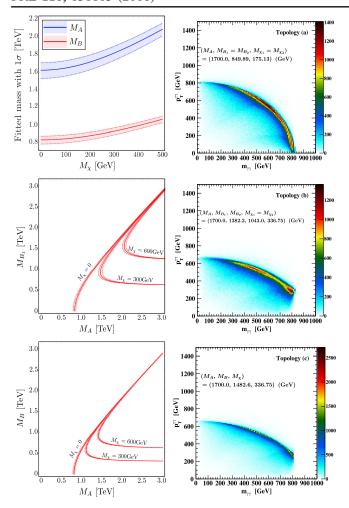


FIG. 3. Left panels: The allowed mass regions at  $1\sigma$ , selected by the best fit. Right panels: Temperature plots showing the correlation between  $m_{\gamma\gamma}$  and  $p_T^{\gamma\gamma}$ , using parton-level Monte Carlo events with a representative mass spectrum consistent with the best-fit values in Eqs. (10) and (11).

accumulation of more data,  $p_T^{\gamma\gamma}$  will eventually be a good discriminator between the conventional resonance scenario (with relatively soft  $p_T^{\gamma\gamma}$ ) and the cascade decay scenarios considered here.

Another handle to discriminate among the competing interpretations of Fig. 1 is provided by the photon energy spectrum. In the conventional case of a single resonance with a large decay width [4–8], the photon energy spectrum has a single peak at half the resonance mass [21,22], which may show a sharp kink structure if the heavy resonance is singly produced [23]. On the other hand, the energy distribution for the (symmetric) antler scenario develops a peak at a *different* position,

$$E_{\gamma} = (M_B^2 - M_{\chi}^2)/(2M_B). \tag{14}$$

For the other two cases, the corresponding photon spectrum could develop a *double-bump* structure depending on the

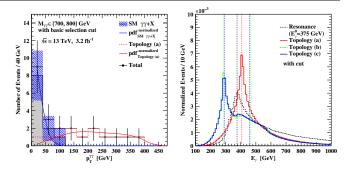


FIG. 4. Left:  $p_T^{\gamma\gamma}$  distribution of events (in a single pseudoexperiment) near the bump,  $m_{\gamma\gamma} \in (700, 800)$  GeV, for the event topology of Fig. 1(a), with the mass spectrum from Fig. 3. Solid lines show the expected distributions. Right: Unit-normalized photon energy distributions for the conventional scenario with a heavy resonance of mass 750 GeV and width 45 GeV (black dotted line), and the three cascade decay scenarios: the antler topology (red solid), the sandwich topology (blue solid), and the two-step cascade (green dotted). The dashed vertical lines mark the expected energy peaks.

underlying mass spectrum [24]. These expectations are summarized in the right panel of Fig. 4.

As the excess was observed in the *inclusive* diphoton channel [1–3], we have focused our attention primarily on the kinematics of the diphoton system itself. Of course, more *exclusive* studies could target the detector signatures of the additional particles  $\chi_i$ . For example, if the particles  $\chi_i$  are stable and weakly interacting, they will be invisible in the detector and cause missing transverse energy  $E_T$ . The predicted  $E_T$  distribution would be similar to the  $p_T^{\gamma\gamma}$  distribution shown in Fig. 4 and, at this point, seems to be disfavored by the data [3] (another constraint would be provided by the inclusive diphoton plus  $E_T$  search for new physics [25]). Of course, the particles  $\chi_i$  could be visible or further decay visibly themselves. The exact nature of their signatures (and kinematic distributions) is rather model dependent and beyond the scope of this Letter.

Finally, we note the potential impact of spin correlations on our analysis. It is well known that the overall shape of invariant mass distributions can be distorted by the introduction of nontrivial spin correlations [26,27]. One could then repopulate most of the signal events in a (relatively) narrow region around the peak, which would further improve the fit. Let  $f_s(m)$  be the relevant  $m_{\gamma\gamma}$  distribution in the presence of spin correlations. For the antler and sandwich cases, one can write [15,17]

$$f_{S}(m) \sim \begin{cases} m(c_{1} + c_{2}t + c_{3}t^{2}), & 0 \leq m \leq e^{-\eta}E, \\ m[c_{4} + c_{5}t + c_{6}t^{2}, & (15) \\ +(c_{7} + c_{8}t + c_{9}t^{2})\ln t], & e^{-\eta}E \leq m \leq E. \end{cases}$$

Here,  $t \equiv m^2/E^2$  and  $c_i$  (i = 1, ..., 9) represent coefficients encoding the underlying spin information. For the decay

topology in Fig. 1(c), the relevant expression is given by the first line of Eq. (15) [15,26]:

$$f_S(m) \sim m(d_1 + d_2t + d_3t^2)$$
 for  $0 \le m \le E$ , (16)

and the presence of the additional terms beyond Eq. (7) can also favorably sculpt the distribution in the vicinity of the peak.

In conclusion, we investigated the nature of the anomalous excesses reported by the ATLAS and CMS Collaborations in terms of cascade decay topologies from a heavy, possibly quite narrow resonance. Our scenarios can generically accommodate a (relatively) large width of the peak accompanied with a (relatively) small diphoton transverse momentum. We also discussed the potential of distinguishing the competing interpretations with more data, using the diphoton transverse momentum and photon energy distributions. We eagerly await the resolution of this puzzle with new data from the LHC.

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