Chiral Three-Nucleon Interactions in Light Nuclei, Neutron- α Scattering, and Neutron Matter

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We present quantum Monte Carlo calculations of light nuclei, neutron- α scattering, and neutron matter using local two- and three-nucleon (3N) interactions derived from chiral effective field theory up to next-tonext-to-leading order (N²LO). The two undetermined 3N low-energy couplings are fit to the ⁴He binding energy and, for the first time, to the spin-orbit splitting in the neutron- α P-wave phase shifts. Furthermore, we investigate different choices of local 3N-operator structures and find that chiral interactions at N²LO are able to simultaneously reproduce the properties of A = 3, 4, 5 systems and of neutron matter, in contrast to commonly used phenomenological 3N interactions.

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Three-nucleon (3N) interactions are essential for a reliable prediction of the properties of light nuclei and nucleonic matter [1–5]. In quantum Monte Carlo (QMC) calculations, phenomenological 3N interactions such as the Urbana [6] and Illinois [7] models have been used with great success [3,8]. However, such models suffer from certain disadvantages: They are not based on a systematic expansion and it was found that the Illinois forces tend to overbind neutron matter [9,10]. It is therefore unlikely that these phenomenological models can be used to correctly predict the properties of heavy neutron-rich nuclei.

An approach which addresses these shortcomings is chiral effective field theory (EFT) [2,11–14]. Chiral EFT is a lowenergy effective theory consistent with the symmetries of quantum chromodynamics and provides a systematic expansion for nuclear forces. It includes contributions from longrange pion-exchange interactions explicitly and expands the short-distance interactions into a systematic set of contact operators accompanied by low-energy couplings fit to experimental data. Chiral EFT enables the determination of theoretical uncertainties and systematic order-by-order improvement; for recent work see Refs. [15–18].

Chiral EFT also predicts consistent many-body interactions. In Weinberg power counting, 3N forces first enter at next-to-leading order (N²LO) [19,20] and contain three contributions: a two-pion-exchange interaction V_C , a one-pion-exchange-contact interaction V_D , and a 3Ncontact interaction V_E . While the first is accompanied by the couplings c_i from the pion-nucleon sector, the latter two are accompanied by the couplings c_D and c_E , which have to be determined in A > 2 systems.

In addition to systematic nuclear forces, reliable manybody methods are required to describe properties of light nuclei and of dense neutron matter. QMC approaches, which solve the many-body Schrödinger equation stochastically, are such a class of methods. Both the Green's function Monte Carlo (GFMC) method and the auxiliaryfield diffusion Monte Carlo (AFDMC) method rely on projection in imaginary time τ ,

$$\lim_{\tau \to \infty} e^{-H\tau} |\Psi_T\rangle \to |\Psi_0\rangle, \tag{1}$$

with H the Hamiltonian of the system and $|\Psi_T\rangle$ a trial wave function not orthogonal to the many-body ground state $|\Psi_0\rangle$. For a recent review of developments and applications of QMC methods in nuclear physics, see Ref. [3]. Recently, we have developed local chiral EFT interactions for use with QMC methods [21-24], thereby producing nonperturbative results for testing the chiral expansion scheme [22] and benchmarks for neutron matter up to high density [21,23]. However, these studies were limited to twonucleon (NN) interactions only or to an exploratory study of neutron matter with only the long-range parts of the 3Ninteraction.

In this Letter, we include consistent 3N interactions at N²LO in coordinate space [24] in GFMC calculations of light nuclei and $n-\alpha$ scattering, and in AFDMC calculations of neutron matter. We fit the two couplings c_D and c_E to the ⁴He binding energy and low-energy n- α scattering P-wave phase shifts. The latter system has been studied using various approaches; see, for example, Refs. [25-27]. These observables are expected to be less correlated than fits to structure properties of A = 3, 4 systems because the spin-orbit and $T = \frac{3}{2}$ components of the 3N interaction enter directly.

In phenomenological 3N models, any short-range parts which arise from the Fourier transformation of pion exchanges are typically absorbed into other short-distance structures: We retain these explicitly. We choose the 3N cutoff $R_{3N} = R_0$, where R_0 is the NN cutoff, and vary the cutoff in the range $R_0 = 1.0-1.2$ fm [21–24]. Note that with a finite cutoff certain ambiguities appear, including the specific operator form associated with the shorter-range interactions. In the Fourier transformation of V_D , two possible operator structures arise:

$$\begin{aligned} V_{D1} &= \frac{g_A c_D m_\pi^2}{96\pi \Lambda_\chi F_\pi^4} \sum_{i < j < k} \sum_{\text{cyc}} \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_k \bigg[X_{ik}(\mathbf{r}_{kj}) \delta_{R_{3N}}(\mathbf{r}_{ij}) \\ &+ X_{ik}(\mathbf{r}_{ij}) \delta_{R_{3N}}(\mathbf{r}_{kj}) - \frac{8\pi}{m_\pi^2} \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_k \delta_{R_{3N}}(\mathbf{r}_{ij}) \delta_{R_{3N}}(\mathbf{r}_{kj}) \bigg], \end{aligned}$$

$$(2a)$$

$$V_{D2} = \frac{g_A c_D m_{\pi}^2}{96\pi \Lambda_{\chi} F_{\pi}^4} \sum_{i < j < k} \sum_{\text{cyc}} \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_k \Big[X_{ik}(\mathbf{r}_{ik}) \\ - \frac{4\pi}{m_{\pi}^2} \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_k \delta_{R_{3N}}(\mathbf{r}_{ik}) \Big] [\delta_{R_{3N}}(\mathbf{r}_{ij}) + \delta_{R_{3N}}(\mathbf{r}_{kj})], \quad (2b)$$

where $X_{ik}(\mathbf{r}) = [S_{ik}(\mathbf{r})T(r) + \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_k]Y(r)$ is the coordinatespace pion propagator, $S_{ik}(\mathbf{r}) = 3\boldsymbol{\sigma}_i \cdot \hat{\mathbf{r}}\boldsymbol{\sigma}_k \cdot \hat{\mathbf{r}} - \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_k$ is the tensor operator, and the tensor and Yukawa functions are defined as $T(r) = 1 + 3/(m_{\pi}r) + 3/(m_{\pi}r)^2$ and $Y(r) = e^{-m_{\pi}r}/r$. The smeared-out delta function $\delta_{R_{3N}}(\mathbf{r}) =$ $[1/\pi\Gamma(3/4)R_{3N}^3]e^{-(r/R_{3N})^4}$ and the long-range regulator multiplying *Y*, $f_{\text{long}}(r) = 1 - e^{-(r/R_{3N})^4}$, are consistent with the choices made in the *NN* interaction [21–24]. The sum i < j < k runs over all particles 1 to *A*, and the cyclic sum runs over the cyclic permutations of a given triple.

The two possible V_D structures agree in the limit of $R_{3N} \rightarrow 0$, because the delta functions then enforce i = j (k = j) in the first (second) term, in which case Eqs. (2a) and (2b) would coincide. The V_D interaction does not distinguish which of the two nucleons in the contact participates in the pion exchange. The second choice, V_{D2} , can be obtained with the exchange of a fictitious heavy scalar particle between the two nucleons in the contact. This ambiguity was also pointed out in Ref. [28]. The differences between Eqs. (2a) and (2b) are regulator effects and therefore higher order in the chiral expansion, but it is important to investigate how they affect different observables at this order.

Similar effects arise in the 3N contact interaction V_E . Here, the main ambiguity is the choice of the 3N contact operator. The same Fierz-rearrangement freedom that allows for a selection of (mostly) local contact operators in the NN sector up to N²LO exists in the 3N sector at this order. Symmetry considerations allow the choice of one of the following six operators [20]:

$$\{\mathbb{1}, \boldsymbol{\sigma}_{i} \cdot \boldsymbol{\sigma}_{j}, \boldsymbol{\tau}_{i} \cdot \boldsymbol{\tau}_{j}, \boldsymbol{\sigma}_{i} \cdot \boldsymbol{\sigma}_{j} \boldsymbol{\tau}_{i} \cdot \boldsymbol{\tau}_{j}, \\ \boldsymbol{\sigma}_{i} \cdot \boldsymbol{\sigma}_{j} \boldsymbol{\tau}_{i} \cdot \boldsymbol{\tau}_{k}, [(\boldsymbol{\sigma}_{i} \times \boldsymbol{\sigma}_{j}) \cdot \boldsymbol{\sigma}_{k}] [(\boldsymbol{\tau}_{i} \times \boldsymbol{\tau}_{j}) \cdot \boldsymbol{\tau}_{k}] \}.$$
(3)

The usual choice is $\tau_i \cdot \tau_j$. Here, we investigate two other choices: first the operator 1, and second a projector operator \mathcal{P} on to triples with $S = \frac{1}{2}$ and $T = \frac{1}{2}$:

$$\mathcal{P} = \frac{1}{36} \left(3 - \sum_{i < j} \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j \right) \left(3 - \sum_{k < l} \boldsymbol{\tau}_k \cdot \boldsymbol{\tau}_l \right), \quad (4)$$

where the sums are over pairs in a given triple. In the infinite-momentum cutoff limit, only these $S = \frac{1}{2}$, $T = \frac{1}{2}$ triples would contribute to V_E due to the Pauli principle. Thus, in the following we will explore three possible structures:

$$V_{E\tau} = \frac{c_E}{\Lambda_{\chi} F_{\pi}^4} \sum_{i < j < k} \sum_{\text{cyc}} \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_k \delta_{R_{3N}}(\mathbf{r}_{kj}) \delta_{R_{3N}}(\mathbf{r}_{ij}), \quad (5a)$$

$$V_{E1} = \frac{c_E}{\Lambda_{\chi} F_{\pi}^4} \sum_{i < j < k} \sum_{\text{cyc}} \delta_{R_{3N}}(\mathbf{r}_{kj}) \delta_{R_{3N}}(\mathbf{r}_{ij}), \qquad (5b)$$

$$V_{E\mathcal{P}} = \frac{c_E}{\Lambda_{\chi} F_{\pi}^4} \sum_{i < j < k} \sum_{\text{cyc}} \mathcal{P} \delta_{R_{3N}}(\mathbf{r}_{kj}) \delta_{R_{3N}}(\mathbf{r}_{ij}).$$
(5c)

We stress that there exist other operator-structure possibilities for V_D and V_E which will be investigated in future work.

Having specified all 3N structures, we vary the values of the couplings c_D and c_E to fit the ⁴He binding energy, as shown in Fig. 1(a). We display curves for V_{D1} and V_{D2} using $V_{E\tau}$ and both cutoffs $R_0 = 1.0$ fm and $R_0 = 1.2$ fm. In addition, we show curves for V_{D2} using the other two possible V_E structures and the cutoff $R_0 = 1.0$ fm. For all of these possibilities, the stars give the values for the couplings which also fit *P*-wave *n*- α scattering phase shifts, as shown in Fig. 1(b). The resulting couplings c_D and c_E are given in Table I. In all cases $\langle V_E \rangle$ is repulsive in ⁴He, except for the case with $(D2, E\tau)$ with the softer cutoff $(R_0 = 1.2$ fm), where it is mildly attractive.

For $R_0 = 1.0$ fm and $V_{E\tau}$, $c_D \approx 0$ and both forms of V_D simultaneously fit the ⁴He binding energy and the *P*-wave n- α scattering phase shifts [see Fig. 1(b)]. However, in the softer-cutoff case $R_0 = 1.2$ fm, V_{D1} and V_{D2} lead to different couplings. For V_{D1} , the splitting between the two *P* waves appears to saturate in c_D for values of $c_D > 2$; e.g., the $\frac{3}{2}^-$ phase shift for $c_D = 2.0, 3.0$, and 5.0 at $E_{\rm cm} = 1.3$ MeV are each ~75 deg, which is ~35 deg below the *R*-matrix value. Since we cannot fit the *P*-wave n- α scattering phase shifts in this case (V_{D1} and $R_0 = 1.2$ fm), we do not consider it in the following. Instead, for V_{D2} and $R_0 = 1.2$ fm, the splitting can be fit, as is evident from Fig. 1(b). For V_{D2} using V_{E1} or V_{EP} and



FIG. 1. (a) Couplings c_E vs c_D obtained by fitting the ⁴He binding energy for different 3*N*-operator forms. Triangles are obtained by using V_{D1} and $V_{E\tau}$, while the other symbols are obtained for V_{D2} and three different V_E -operator structures. The blue and green lines (lower and upper) correspond to $R_0 = 1.0$ fm, while the red lines (central) correspond to $R_0 = 1.2$ fm. The GFMC statistical errors are smaller than the symbols. The stars correspond to the values of c_D and c_E which simultaneously fit the *n*- α *P*-wave phase shifts (see Table I and the right panel). No fit to both observables can be obtained for the case with $R_0 = 1.2$ fm and V_{D1} . (b) *P*-wave *n*- α elastic scattering phase shifts compared with an *R*-matrix analysis of experimental data. Colors and symbols correspond to the left panel. We also include phase shifts calculated at NLO which clearly indicate the necessity of 3*N* interactions to fit the *P*-wave splitting.

 $R_0 = 1.0$ fm, both the ⁴He binding energy and the *P*-wave n- α scattering phase shifts can be simultaneously fit: we show only the case with V_{EP} in Fig. 1(b). There, we also show the next-to-leading order (NLO) results which are a clear indication that 3N forces are necessary to properly describe n- α scattering. Similar results have been found in Refs. [29–31]. Because A = 3, 4 systems (further discussed below) are largely insensitive to odd-parity partial waves, we find no significant dependence on the choice of structures in V_D . However, our results in n- α *P*-wave scattering show a substantial sensitivity: V_{D1} appears to have a smaller effect than V_{D2} .

In Fig. 2, we show ground-state energies and point proton radii for A = 3, 4 nuclei at NLO and N²LO using V_{D2} and $V_{E\tau}$ for $R_0 = 1.0$ fm and $R_0 = 1.2$ fm, in comparison with experiment. The ground-state energies of the A = 3 systems compare well with experimental values. The

TABLE I. Fit values for the couplings c_D and c_E for different choices of 3N forces and cutoffs.

V_{3N}	R_0 (fm)	c_E	c_D
N ² LO $(D1, E\tau)$	1.0	-0.63	0.0
	1.2		
N ² LO $(D2, E\tau)$	1.0	-0.63	0.0
	1.2	0.09	3.5
$N^2LO(D2, E1)$	1.0	0.62	0.5
$N^{2}LO(D2, E\mathcal{P})$	1.0	0.59	0.0

ground-state energy of ⁴He is used in fitting c_D and c_E , and so it is forced to match the experimental value to within ≈ 0.03 MeV. The point proton radii also compare well with values extracted from experiment. The theoretical uncertainty at each order is estimated through the expected size of higher-order contributions; see Ref. [32] for details. We



FIG. 2. Ground-state energies and point proton radii for A = 3, 4 nuclei calculated at NLO and N²LO (with V_{D2} and $V_{E\tau}$) compared with experiment. Blue (red) symbols correspond to $R_0 = 1.0$ fm ($R_0 = 1.2$ fm). The errors are obtained as described in the text and also include the GFMC statistical uncertainties.

include results from LO, NLO, and N²LO in the analysis using the Fermi momentum and the pion mass as the small scales for neutron matter (discussed below) and nuclei, respectively. The error bars presented here are comparable to those shown in Ref. [33], although it is worth emphasizing that our calculations represent a complete estimate of the uncertainty at N²LO since we include 3N interactions. Other choices for 3N structures give similar results.

It is noteworthy that *NN* and 3*N* interactions derived from chiral EFT up to N²LO have sufficient freedom such that *n*- α scattering phase shifts in Fig. 1(b) and properties of light nuclei in Fig. 2 can be simultaneously described. The failures of the Urbana IX model in underbinding nuclei and underpredicting the spin-orbit splitting in neutron-rich systems, including the *n*- α system, were among the factors motivating the addition of the threepion exchange diagrams in the Illinois 3*N* models [7]. Our results show that chiral 3*N* forces at N²LO, including the shorter-range parts in the pion exchanges, allow the simultaneous fit. These interactions should be tested further in light *p*-shell nuclei.

Finally, we study the full chiral N²LO forces, including all 3N contributions, in neutron matter to extend the results from Ref. [24]. More specifically, we examine the effects of different V_D and V_E structures on the equation of state of neutron matter. Although these terms vanish in the limit of infinite cutoff, they contribute for finite cutoffs. In Fig. 3 we show results for the neutron matter energy per particle as a function of the density calculated with the



FIG. 3. The energy per particle in neutron matter as a function of density for the *NN* and full 3*N* interactions at N²LO with $R_0 = 1.0$ fm. We use V_{D2} and different 3*N* contact structures: The blue band corresponds to $V_{E\tau}$, the red band to V_{E1} , and the green band to V_{EP} . The green band coincides with the *NN* + 2 π -exchange-only result because both V_D and V_E vanish in this case. The bands are calculated as described in the text.

AFDMC method described in Refs. [3,34]. We show the energies for $R_0 = 1.0$ fm for the *NN* and full 3*N* interactions. We use V_{D2} and the three different V_E structures: $V_{E\tau}$ (blue band), V_{E1} (red band), and $V_{E\mathcal{P}}$ (green band). The error bands are determined as in the light nuclei case. The $V_{E\mathcal{P}}$ interaction fits A = 4,5 with a vanishing c_D ; hence, this choice of V_E leads to an equation of state identical to the equation of state with $NN + V_C$, as in Ref. [24] (the projector \mathcal{P} is zero for pure neutron systems), and qualitatively similar to previous results using chiral interactions at N²LO [35] and next-to-next-to-leading order [36].

As discussed, the contributions of V_D and V_E are only regulator effects for neutrons. However, they are sizable and result in a larger error band. At saturation density $n_0 \sim 0.16 \text{ fm}^{-3}$, the difference of the central value of the energy per neutron after inclusion of the 3N contacts V_{E1} or $V_{E\tau}$ is ~2 MeV, leading to a total error band with a range of ~6.5 MeV when considering different V_E structures. This relatively large uncertainty can be qualitatively explained when considering the following effects. Because the expectation value $\langle 1 \rangle$ in ⁴He, c_E will also have opposite signs in the two cases to fit the binding energy. However, in neutron matter both operators are the same, spreading the uncertainty band. A similar argument was made in Ref. [37].

With the regulators used here, the Fierz-rearrangement invariance valid at infinite cutoff is only approximate at finite cutoff, and hence the different choices of V_D and V_E can lead to different results. The different local structures can lead to finite relative *P*-wave contributions. These can be eliminated by choosing $V_{E\mathcal{P}}$, which has a projection onto even-parity waves (predominantly *S* waves). The usual nonlocal regulator in momentum space does not couple *S* and *P* waves.

In conclusion, we find for the first time that chiral interactions can simultaneously fit light nuclei and low-energy *P*-wave n- α scattering and provide reasonable estimates for the neutron matter equation of state. Other commonly used phenomenological 3N models do not provide this capability. These chiral forces should be tested in light *p*-shell nuclei, medium-mass nuclei, and isospin-symmetric nuclear matter to gauge their ability to describe global properties of nuclear systems.

We also find that the ambiguities associated with contact-operator choices can be significant when moving from light nuclei to neutron matter and possibly to medium-mass nuclei, where the $T = \frac{3}{2}$ triples play a more significant role. The reason for the sizable impact may be the regulators used here, which break the Fierz-rearrangement invariance, making further investigations of regulator choices a priority. The impact of these ambiguities in the contact operators can contribute to the uncertainties and needs to be studied further. We thank G. Hale for useful discussions and for providing us with the *R*-matrix analysis of the *n*- α phase shifts. We also thank A. Dyhdalo, E. Epelbaum, R. J. Furnstahl, K. Hebeler, and A. Lovato for useful discussions. This work was supported by the NUCLEI SciDAC program, the U.S. DOE under Contract No. DE-AC52-06NA25396, ERC Grant No. 307986 STRONGINT, the Natural Sciences and Engineering Research Council of Canada, the LANL LDRD program, and the NSF under Grant No. PHY-1404405. Computational resources have been provided by Los Alamos Open Supercomputing and the Jülich Supercomputing Center. We also used resources provided by NERSC, which is supported by the U.S. DOE under Contract No. DE-AC02-05CH11231.

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