New Short-Lived Isotope 221 U and the Mass Surface Near N=126

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Two short-lived isotopes 221 U and 222 U were produced as evaporation residues in the fusion reaction 50 Ti + 176 Yb at the gas-filled recoil separator TASCA. An α decay with an energy of $E_{\alpha}=9.31(5)$ MeV and half-life $T_{1/2}=4.7(7)$ μ s was attributed to 222 U. The new isotope 221 U was identified in α -decay chains starting with $E_{\alpha}=9.71(5)$ MeV and $T_{1/2}=0.66(14)$ μ s leading to known daughters. Synthesis and detection of these unstable heavy nuclei and their descendants were achieved thanks to a fast data readout system. The evolution of the N=126 shell closure and its influence on the stability of uranium isotopes are discussed within the framework of α -decay reduced width.

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The shell structure of the atomic nucleus is one of the fundamental pillars of nature. As one consequence, spherically shaped nuclei with fully-filled proton and neutron shells at Z, N = 2, 8, 20, 28, 50, 82,and N = 126 have enhanced stability against any type of ground-state radioactive decay (alpha, beta, fission etc.) [1,2]. Many theoretical models are able to successfully describe the properties of these shell closures, and have thus attempted to predict the next heaviest magic numbers [3–7]. However, in contrast to the lighter magic numbers their results do not agree on the location of the next spherical doubly magic nucleus. Models within the macroscopic-microscopic approach often refer to Z = 114 and N = 184 [3–5], while microscopic ones predict various combinations (e.g., Z = 120, N = 172 [7] or Z = 126, N = 184 [6]). Direct tracing of these potential nuclear shell closures is limited by minute production rates, approaching the atom-per-month level for heaviest known elements up to Z = 118 [8]. Moreover neutron number N = 184 is presently not accessible experientially. Obtaining information about the evolution of nuclear shell closures in the heavy-element region is thus a prerequisite for gaining an improved understanding of superheavy nuclei.

Our current understanding of shell structure is well established, particularly in the case of nuclei along the valley of stability, where the magicity of shell closures is found. The robustness of these shell closures when going to

extremes in the proton-to-neutron ratio is less well studied, but the fading of classical shell closures has been observed in lighter regions of the chart of nuclei [2]. The N=126 shell closure hosts the heaviest known stable doubly magic spherical nucleus, $^{208}_{82}\text{Pb}_{126}$, and is experimentally established up to protactinium (Z=91), above which its evolution is yet poorly examined.

The evidence for the presence of the N=126 shell closure above ^{208}Pb is based on systematic analyses of a limited amount of experimental data available to date like E_{α} and thus the deduced Q_{α} values, and half-life, $T_{1/2}$. More detailed information on nuclear structure can be obtained from the α -particle preformation probability inside the nucleus [9], which microscopically quantifies the stability against α decay. Different variables that are equivalent to the α -particle preformation probability in which both macroscopic observables Q_{α} and $T_{1/2}$ are simultaneously involved, can be deduced within different quantum-mechanical approaches [10,11]. Commonly, a reduced width for α decay, δ^2 [10], which takes into account the angular momentum of the emitted α particle, is used.

At and below N = 126, reduced widths of isotones of Po (Z = 84) to Pa are significantly lower than those of the N = 128-130 isotones located beyond the closed N = 126 shell [10–12]. This reflects the robustness of the N = 126 shell closure up to Pa and the effect of the semi-magic core with N = 126. The evolution of this closure towards higher

Z is yet unknown due to the absence of data on U isotopes with N=128-130. U isotopes with N=124-127 and $N \ge 131$ are known by their α decay [13–15]. For 222 U (N=130), only a half-life is known, $T_{1/2}=1.0^{+1.2}_{-0.4}$ μs, deduced from the observation of just three events [16]. The α -decay energies could not be measured as a result of the signals being summed (pileup) with those of the rapidly following α decays of the 218 Th daughter ($T_{1/2}=0.117(9)$ μs [13]). Fast electronics have been successfully applied in recent decades to resolve similar pileup events in the charged particle spectroscopy of shortlived nuclei in regions of lighter elements (Refs. [17,18] and references therein).

Generally, the synthesis and detection of neutron-deficient isotopes of U (as well as heavier elements) in this region are challenging due to their low production rates and short half-lives [16,19]. An additional difficulty arises from the fusion reaction itself, as the compound nucleus fission and the evaporation of protons and/or α particles is by far dominant over neutron evaporation [19]. Thus, no new or improved data in this region of sub- μ s isotopes carrying information on the N=126 shell closure of elements above Pa have been measured in the last thirty years.

In this Letter, we report the first identification of the isotope ^{221}U and new data for ^{222}U . The known data on Po-U are discussed by means of α -decay systematics and thus help to shed light on the evolution of the N=126 shell closure in U.

The experiment was carried out at the GSI Helmholtzzentrum für Schwerionenforschung, Darmstadt, Germany. The isotopes ²²¹U and ²²²U were produced in the ⁵⁰Ti + ¹⁷⁶Yb reaction at the gas-filled TransActinide Separator and Chemistry Apparatus (TASCA) [20,21]. A pulsed (5 ms beam on and 15 ms beam off) ⁵⁰Ti¹²⁺ beam was accelerated by the UNIversal Linear ACcelerator (UNILAC) to energies in the range of 231-255 MeV in the center of the ¹⁷⁶YbF₃ targets. These correspond to excitation energies of 40-60 MeV in ²²⁶U* where the maxima of 4n (222U) and 5n (221U) evaporation channels are predicted to occur according to the statistical fusionevaporation code HIVAP [22]. Four target segments with average thicknesses of 0.45(5) mg/cm² (176Yb) were mounted on a wheel which rotates synchronously to the beam pulses [23]. The magnets of TASCA were set to guide the evaporation residues (ERs) ²²¹U and ²²²U with a magnetic rigidity of 1.66 Tm [24-26] to the center of the focal plane with an estimated efficiency of 50(5)%. The time of flight of the ^{221,222}U ERs through TASCA was estimated to be $0.53(6) \mu s$.

ERs that do not decay in flight (through TASCA) were implanted into a double-sided silicon strip "stop detector" with 144 vertical and 48 horizontal 1-mm wide strips. A multiwire proportional counter (MWPC) was mounted in front of the stop detector to distinguish the genuine radioactive decay of implanted ERs from beam-related events. A detailed description of the TASCA focal plane detector is given in Ref. [21].

Signals from all the detectors were processed in a combined analog and digital (CANDI) data acquisition system comprising analog and digital branches. The shapes of the preamplified signals from the 48 horizontal strips $(n^+ \text{ side})$ were recorded in 50 μ s-long traces by analog-todigital converters with 60 MHz sampling [27]. The trace length was selected to be longer than the dead time of the analog branch of $\approx 35 \mu s$. Energy resolutions (FWHM) of individual vertical strips of the stop detector coupled to the analog branch were about 30 keV for 8.7-MeV α particles. The amplitudes, i.e., energies of signals stored in traces were extracted by using different types of software algorithms depending on the multiplicity of the recorded signals [28]. The best resolutions, about 40 keV, were achieved for 8.7-MeV α particles that were registered as single events in the traces. The best energy resolutions of multiple α events stored in a single trace with time differences down to 1 μ s and 0.17 μ s were \approx 110 keV and \approx 180 keV, respectively.

Half-lives known for ^{222}U and its daughter ^{218}Th and predicted for ^{221}U are much shorter [13] than the 50 μs trace-length of CANDI. Thus, their radioactive decay signature is registered in digital traces of implantation signals (ER-like). The analysis procedure thus consists of two main steps.

(i) A correlation analysis of the analog data, searching for ER- α chains requiring that both the ER-like and the α -like events (7–18 MeV) occurred in the same pixel of the stop detector within 20 s. The results of the correlation analysis are shown in Fig. 1. The implantation of 214 Ra, 215 Ra, 217 Th, and 214 Fr was identified by their known

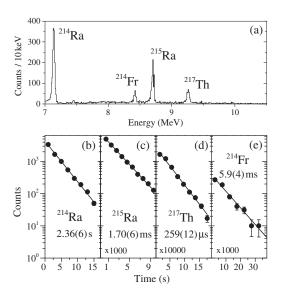


FIG. 1. Results from a correlation analysis of the type ER- α within 20 s: (a) Spectrum of correlated α particles registered at a bombarding energy of 239 MeV and (b)–(d) total decay curves of the implanted nuclei. (e) Decay curve of 214 Fr identified in the correlation analysis of type ER- α (7–18 MeV)- α (214 Fr).

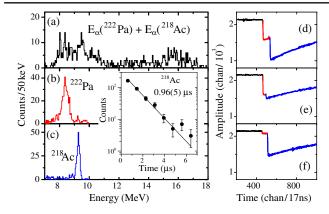


FIG. 2 (color online). Identification spectra for the separation of pileup events originating from the decay chains ER- α (7 – 18 MeV)- α (214 Fr). (a) Energy spectrum from the analog part of the data. (b),(c) Energy spectra of events deduced from the digital traces. Examples of some pileup traces: (d) two α particles with full energies, (e) and (f) for traces where the second and first α particle, respectively, escaped in the backward direction and deposited only partial energy in the stop detector.

 α -decay properties [13], and the corresponding ERs were assigned for each event.

(ii) Traces of all ERs correlated to a subsequent α decay of 214 Ra and 217 Th, which are members of the α -decay chains originating from 222 U and 221 U, respectively, were checked event by event for the presence of multiple signals.

In the cases of ²¹⁷Th and ²¹⁴Fr, an additional ER- α - α correlation analysis was performed to reconstruct the full pattern of the α -decay chain. As an example, 214 Fr was found to be the last member of the ER- α (7-18 MeV)- α (²¹⁴Fr) chain with $T_{1/2} = 5.9(4)$ ms (see Fig. 1). An energy spectrum (analog branch) of the second member with $T_{1/2} =$ 3.5(1) ms is shown in Fig. 2(a). To resolve apparent pileup events, the digital traces were analyzed in the second step. Different examples of such events are presented in Figs. 2(d)-2(f). The energy spectra of the two signals allowed the separate peaks to be clearly resolved, which correspond to known α -decay energies of ²²²Pa and ²¹⁸Ac [13]. Time differences between those signals yield $T_{1/2} = 0.96(5) \mu s$, which agrees well with the literature data of 218 Ac [13]. Thus, the origin of the α decay of 214 Fr was attributed to the implantation of ²²²Pa produced as an ER via the p3n deexcitation channel from the compound nucleus ²²⁶U*. The same digital-trace analysis was used for the extraction of α -decay properties of all other short-lived nuclei.

Significant amounts of ER traces correlated to $\alpha(^{215}\text{Ra})$ were stored with double signals. A resolved energy spectrum of the second signal and the decay curve extracted from the time difference of these signals (shown in Fig. 3) is in good agreement with the literature data for ^{219}Th [13]. No triple signals, which would correspond to the implantation of ^{223}U ($T_{1/2}=55(10)~\mu\text{s}$ [13]) from the 3n channel, were detected.

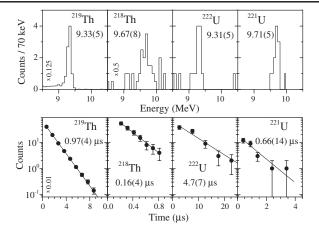


FIG. 3. Energy spectra and decay curves of α particles emitted from 219 Th, 218 Th, 222 U, and 221 U. The data were extracted from the digital data branch. In the case of 218 Th both double and triple-signaled traces from ER- α (214 Ra) were used. All traces with time differences down to 100 ns between the preceding signal and α decay were used.

Traces with two and three signals were detected for ERs followed by $\alpha(^{214}\text{Ra})$. Traces with two signals and with very short time differences leading to $T_{1/2}=0.16(4)~\mu\text{s}$ (see Fig. 3) between the signals were assigned to the implantation and α decay of $^{218}\text{Th}~(T_{1/2}=0.117(9)~\mu\text{s}$ [13]) produced in the $\alpha 4n$ channel.

Eighty-one ER traces containing three signals were unambiguously attributed to the implantation of 222 U followed by α decays of 222 U and 218 Th. One such trace is shown in Fig. 4. A half-life of $4.7(7)~\mu s$ and an energy of 9.31(5) MeV were deduced for the α decay of 222 U (see Fig. 3).

Twenty-six ER traces followed by subsequent α decays of 217 Th and 213 Ra were stored with double signals and are attributed to the implantation and α decay of the hitherto unknown 221 U (see Fig. 4). A half-life of $0.66(14)~\mu s$ and an α -particle energy of 9.71(5) MeV were deduced (see Fig. 3) for this isotope.

The most favored α transitions in nuclei with N=129 proceed through the same $\nu 2g_{9/2}$ orbital in the mother and

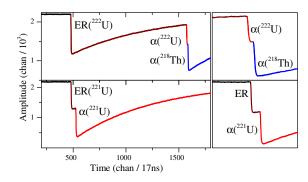


FIG. 4 (color online). Examples of traces where ²²²U and ²²¹U were registered. Right panel: Enlarged figures of rapidly correlated signals.

daughter nuclei. Thus, the observed α decay in $^{221}\mathrm{U}$ is attributed to such a transition. The $(9/2^+)$ state is tentatively assigned to the ground state of $^{221}\mathrm{U}$ based on systematics [13,14]. Alpha decays of both $^{221}\mathrm{U}$ and $^{222}\mathrm{U}$ are in good agreement with Q_{α} [29] and $T_{1/2}$ systematics [14]. The new α -decay data on $^{221}\mathrm{U}$ and $^{222}\mathrm{U}$ together with

literature values for Po-Th ([13,15]) allow us to construct the tendencies of δ^2 in the N = 129, 130 isotones up to U, where the $\pi(1h_{9/2})$ orbital is fully filled. The deduced δ^2 values for the N = 124, 126-130 isotones are shown in Fig. 5. In the case of the N=129 isotones, only α transitions populating the same single-neutron states in the daughter nuclei were taken. For the cases at N = 127, the α transition proceeds between different initial $\nu(2g_{9/2})^1$ and final $\nu(3p_{1/2})^{-1}$ configurations. Thus we use $\Delta \ell = 0$ for N = 129 and $\Delta \ell = 5$ for N = 127. Up to Th (Z = 90), the δ^2 values for the N=124,128-130 isotones are larger than the N = 126, 127 ones, which clearly shows a strong effect of the N=126 shell closure. At the same time, the δ^2 values for the N = 126, 127 isotones, which are known up to U, smoothly rise with increasing Z, indicating a weakening of the semi-magic core with N = 126. For the N = 129, 130 isotones, where our new data allow extending the systematics up to U, the δ^2 values decrease in contrast to the trend seen in the N = 126, 127 isotones. The sudden increase of δ^2 values when crossing the N=126shell closure seen in lighter elements with even A is no longer present at Z = 92. In odd-A nuclei, the gap is still

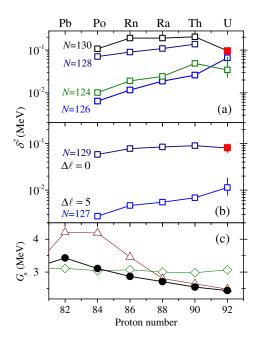


FIG. 5 (color online). Reduced α -decay widths (δ^2 , [10]) of even-A (a) and odd-A (b) isotopes, and (c) neutron-shell gaps (G_n , [2]) of Po-U as a function of the Z. Errors originating solely from half-lives are given for U. (c) Experimental data (full dots) [29] are compared to FRDM95 (open diamonds) [4] and HFB26 (open triangles) [30] calculations. See text for details.

persisting at Z=92, in contrast to the even-A case. Essentially, α decay of the even-even nuclei, where all nucleons are paired, provides better information on their structure compared to odd-A ones, where α decay is strongly influenced by their unpaired nucleon.

The above observed feature for even-A nuclei indicates a weakening of the N=126 shell stabilization effect for U, which can be inferred even in the absence of data on 220 U (N=128). In addition, δ^2 values for the N=124 isotones show again a notable discrepancy in U. The smallest δ^2 value is found in 216 U (N=124), which can be argued as having a more stabilized core than the semi-magic 218 U (N=126).

A weakening of the N=126 shell closure can also be seen in the reduction of the neutron-shell gap in elements above Pb (Z=82). The neutron-shell gap, G_n , between the last-occupied and first-valence orbitals around N=126 can be calculated as

$$G_n(Z, 126) = 2B(Z, 126) - B(Z, 125) - B(Z, 127)$$
 (1)

using the known (except 217 U) binding energies, B [2,29]. These gaps are shown in Fig. 5 (bottom panel) where we compare experimental data ([29]) with those obtained using two different theoretical models (FRDM95 [4], HFB26 [30]). A reduction of G_n as a function of Z for heavier elements is observed in the experimental data, supporting the above discussed weakening of the shell closure inferred on the basis of the trends of δ^2 values. G_n values are significantly reduced when crossing Z=82, which can be attributed to the loss of the magic Z=82 partner, which leads to less stable semi-magic nuclei with 218 U being the most unstable N=126 isotone known to date.

Two theoretical models, FRDM95 and HFB26, were selected as representatives of the macroscopic-microscopic and microscopic approaches, respectively. The macroscopic-microscopic approach is based on corrections of calculated liquid-droplet masses to the shell structure, while the microscopic ones take into account the interactions between the nucleons with differently parametrized effective forces for the solution of the many-body quantum equations within particular approximations such as Hartree-Fock-Bogoliubov with Skyrme force (HFB26). The Finite-Range Droplet Model (FRDM95) predicts well the G_n values around the doubly magic ²⁰⁸Pb, but fails to describe the decreasing trend for heavier elements. On the other hand, the HFB26 model does not perform as well around 208 Pb, but predicts the reduction of G_n towards heavier elements better. This shows the importance of interactions between the valence nucleons for the evolution of the shell closure.

The anomalous behavior observed in U thus may hint at significant changes in its structure due to nucleon-nucleon interactions, for instance the presence of non-negligible deformation as discussed theoretically in Ref. [31]. To date, no experimental data on deformations of

N = 124-130 isotones are available for Po-U, except for 218 Ra (N = 130), where the quadrupole deformation is 0.091(4) [13].

In conclusion, we report the discovery of the isotope ²²¹U as well as unambiguous identification of ²²²U. Halflives of 4.7(7) μ s and 0.66(14) μ s and α -particle energies of 9.31(5) MeV and 9.71(5) MeV were measured for ²²²U and ²²¹U, respectively. These were produced in the fusionevaporation reaction 50Ti+176Yb with maximum cross sections of a few nanobarns at 47 and 54 MeV excitation energies of ²²⁶U* [28]. The comparative analysis of the reduced widths and neutron-shell gaps of the Po-U isotopes shows a significant weakening of the influence of the N = 126 shell closure in U. Our findings motivate further investigations of the N = 126 shell closure by synthesizing hitherto unknown nuclei, and by detailed studies of U. The experimental technique applied in the present work allows the identification of short-lived activities in a wide range of the nuclear chart and particularly for the still unobserved ²²⁰U for which, though, the predicted half-life is only several tens of ns [14] and hence too short for surviving the flight time through TASCA. A preferable way to synthesize this isotope would be via its significantly longer lived [32] α -decay precursor ²²⁴Pu.

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