Spatial Coherence and Stability in a Disordered Organic Polariton Condensate

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Although only a handful of organic materials have shown polariton condensation, their study is rapidly becoming more accessible. The spontaneous appearance of long-range spatial coherence is often recognized as a defining feature of such condensates. In this Letter, we study the emergence of spatial coherence in an organic microcavity and demonstrate a number of unique features stemming from the peculiarities of this material set. Despite its disordered nature, we find that correlations extend over the entire spot size, and we measure $g^{(1)}(r, r')$ values of nearly unity at short distances and of 50% for points
separated by nearly 10 μ m. We show that for large spots, strong shot to shot fluctuations emerge as varying separated by nearly 10 μ m. We show that for large spots, strong shot-to-shot fluctuations emerge as varying phase gradients and defects, including the spontaneous formation of vortices. These are consistent with the presence of modulation instabilities. Furthermore, we find that measurements with flat-top spots are significantly influenced by disorder and can, in some cases, lead to the formation of mutually incoherent localized condensates.

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In the last few years, a number of molecular systems that show room-temperature polariton condensation have emerged [1–[3\].](#page-3-1) Polaritons are hybrid exciton-photon quasiparticles that form in optical microcavities when dissipation is low as compared to the light-matter interaction. Like their fundamental constituents, they obey Bose statistics at low densities. They inherit an effective mass as low as 10^{-10} times that of a Rb⁸⁷ atom from their photonic component. Meanwhile, they collide with other polaritons and excitons due to an effective interaction stemming from their matter component. In inorganic microcavities, these features have been exploited to demonstrate rich phenomenology associated with Bose-Einstein condensation (BEC). The most well known of these effects is the macroscopic occupation of the ground state beyond a critical density n_c . A perhaps more important consequence of the phase transition is the sudden appearance of off-diagonal long-range order in coordinate space [\[4,5\].](#page-4-0) This manifests itself in the nonvanishing long-range behavior of the first-order spatial coherence $g^{(1)}(\mathbf{r}, \mathbf{r}')$. At the polariton condensation threshold a similar transition the polariton condensation threshold, a similar transition occurs, thus breaking U(1) symmetry, but also showing a number of distinct features resulting from the strongly nonequilibrium nature of the system [\[6\]](#page-4-1).

Several materials have been used to demonstrate polariton condensation. The majority of these have used CdTeand GaAs-based semiconductors whose operation is limited to low temperatures due to their small exciton binding energy. Recently, however, wide band gap semiconductors such as ZnO and GaN have emerged as viable materials for room-temperature applications [7–[10\]](#page-4-2). Organic semiconductors are especially attractive in this context due to their large exciton binding energy.

Molecular excitons are commonly of the Frenkel type where both the electron and hole are localized on a single molecule and exciton transport occurs incoherently between neighboring molecules. In microcavities, long-range coupling between molecules is provided by the photon field, and theoretical studies have shown that a phase transition can occur even in the absence of electronic coupling between molecular dipoles [\[11\]](#page-4-3). Organics offer the advantage of a broad spectral range beyond that covered by GaN and ZnO and can be easily fabricated without the need for epitaxial growth. As-grown films, however, tend to be highly disordered and to overcome possible localization effects [\[12](#page-4-4)–24]. To overcome possible localization effects, the first demonstration of organic polariton condensation used a single-crystalline organic semiconductor as the active material [\[1\]](#page-3-1). Two recent demonstrations, however, have shown that the same phenomenology can be extended to amorphous systems: one consisting of a spin-coated polymer [\[3\]](#page-4-5) and the other of a thermally evaporated oligomer [\[2\].](#page-3-2) By using interferograms, these reports have also evidenced the presence of long-range correlations in these systems. Here, we study in detail the onset of spatial and temporal coherence in an organic polariton condensate. We show that even in the presence of disorder, correlations can span the entire system size. Moreover, we highlight the important role of the pump and observe a number of unique features such as the spontaneous formation of vortices, which suggest the presence of modulation instabilities.

The microcavity is identical to that of Ref. [\[2\].](#page-3-2) It uses nine dielectric mirror pairs on opposite sides of a layer of 2,7-bis[9,9-di(4-methylphenyl)-fluoren-2-yl]- 9,9-di(4-methylphenyl)fluorene (TDAF) and was impulsively pumped high above the polariton energy (i.e., nonresonantly). To highlight the presence of disorder, realspace photoluminescence (PL) using a Gaussian pump is shown in Fig. [1.](#page-1-0) In the linear regime, given in Fig. [1\(a\),](#page-1-0) we find that the PL is independent of sample location. Above threshold, however, in-plane potential energy fluctuations cause strong variations as a function of sample location, as shown in Figs. $1(b)-1(d)$ $1(b)-1(d)$. Although elastic scattering due to disorder has previously been observed for organic polaritons in the linear regime [\[25\],](#page-4-6) the local intensity fluctuations seen here only appear beyond the condensation threshold. These bear striking similarities to those observed in disordered inorganic microcavities [\[16,23,26,27\].](#page-4-7)

Although a number of other criteria exist, the spontaneous onset of long-range spatial coherence is often recognized as a defining feature for condensation. This was first reported for a CdTe microcavity in the seminal work of Kasprzak et al. using a Michelson interferometer with one arm replaced by a retroreflector [\[27\]](#page-4-8). Soon after, the spatial coherence of a GaAs microcavity was measured using a Young's double slit experiment and found to reach 30% at distances of 8 μ m [\[28\]](#page-4-9). Theoretical predictions regarding the asymptotic behavior of $g^{(1)}(\mathbf{r}, \mathbf{r}')$ have shown
that it can be used to shed light on the nature of the phase that it can be used to shed light on the nature of the phase transition [\[29\]](#page-4-10), and experiments with a low noise floor have observed a power-law decay and attributed this to a Berezinskii-Kosterlitz-Thouless (BKT) phase transition [\[30\]](#page-4-11). Recent theoretical work has, however, suggested that this decay may be the result of a crossover phenomenon at intermediate length scales and that correlations should instead fall off exponentially [\[31\]](#page-4-12). Interferometric techniques have also been used to identify excitations such as vortices and vortex-antivortex pairs and to probe quantum fluidic effects in polaritonic systems [\[32](#page-4-13)–34].

In this Letter, we use the retroreflector configuration from Ref. [\[27\].](#page-4-8) A typical interferogram measured at the location of Fig. [1\(d\)](#page-1-0) is shown in Fig. [1\(e\).](#page-1-0) Despite the nonuniform intensity, parallel fringes indicate a flat phase over the entire condensate area. Similar results are observed for all sample locations. The visibility and phase offset are extracted by scanning a delay mirror (DM) over a phase of 6π and fitting the resulting pattern at each pixel as shown in Fig. [1\(f\).](#page-1-0) The offset is shown in Fig. [1\(g\)](#page-1-0) and is due to the small angle difference between the two interferometer arms. For a circular spot, one expects ballistic propagation of polaritons away from the center accompanied by a radially increasing local wave vector for the condensate [\[35\]](#page-4-14). An upper limit for this propagation length can be calculated using $l_p \lesssim \hbar k_c/\gamma_c m^* = 2 \mu m$, where $k_c =$
2.1 μ m⁻¹ is the largest condensate wave vector supported 2.1 μ m⁻¹ is the largest condensate wave vector supported by the dispersion, $m^* = 2.1 \times 10^{-5} m_e$ is the effective mass,
and $\gamma = 6 \text{ ns}^{-1}$ is the polariton decay rate. For small and $\gamma_c = 6 \text{ ps}^{-1}$ is the polariton decay rate. For small enough pump spots, this leads to an annular condensate density as shown in the Supplemental Material [\[36\]](#page-4-15).

Figure [2](#page-2-0) shows the spatial dependence of $g^{(1)}(-\mathbf{r}, \mathbf{r})$ for three values of pump fluence. The spatial coherence

FIG. 1 (color online). (a-d) Real-space images of the timeintegrated PL below (a) and above threshold at different locations (b–d) using an elliptical Gaussian pump. The linear image (a) remains identical regardless of the sample location. (e) Interferogram from location (d) averaged over 15 laser shots. (f) Typical intensity versus phase delay. For every pixel, a cosine fit is used to extract both $g^{(1)}(-\mathbf{r}, \mathbf{r})$ and the phase offset. (g) Phase extracted from the fit. The scale bar is 5 μ m from the fit. The scale bar is 5 μ m.

reaches peak values of $g^{(1)}(-\mathbf{r}, \mathbf{r}) > 0.8$ for points separated by up to 5 μ m. Vertical cuts through the center of rated by up to 5 μ m. Vertical cuts through the center of Figs. 2(a)–[2\(c\),](#page-2-0) are shown in Figs. [2\(d\)](#page-2-0)–2(f). A vertical profile was chosen to avoid artifacts resulting from the small collapse along the horizontal direction. These occur due to the small difference in the arrival time of the 50° pump pulse along this axis. The noise remains significant near the condensate edge, which prevents a clear statement regarding the functional dependence of the asymptotic behavior of $g^{(1)}(-\mathbf{r}, \mathbf{r})$. In analogy to the thermal case,
we simply show a Gaussian fit which shows a reasonable we simply show a Gaussian fit, which shows a reasonable agreement and allows us to extract a coherence length agreement and allows us to extract a coherence length $\lambda_c = 2\sqrt{2\pi}\sigma$, where σ is the standard deviation of the Gaussian fit. We obtain a coherence length of un to Gaussian fit. We obtain a coherence length of up to $\lambda_c = 38 \mu$ m, which is ultimately limited by the pump size. A typical power dependence of $g^{(1)}(-y, y)$ is shown in
Fig. 3(a) In all cases an increase in $g^{(1)}(-y, y)$ is observed Fig. [3\(a\)](#page-2-1). In all cases, an increase in $g^{(1)}(-y, y)$ is observed,
followed by a plateau near 1.5P. followed by a plateau near $1.5P_{th}$.

As previously reported, the effective polariton-polariton and polariton-exciton nonlinearities in state-of-the-art organic microcavities are dominated by exciton saturation. The resulting change in refractive index causes antiguiding in analogy to gain-guided, index antiguided conventional lasers. Moreover, the resulting nonlinearities are much weaker than in inorganics, which are dominated by the Coulomb exchange term between carriers[\[37\]](#page-4-16). From the blueshift in the region where the reservoir occupation is clamped (see Supplemental Material [\[36\]\)](#page-4-15), we can extract a polaritonpolariton interaction coefficient $g = 10^{-6}$ meV μ m². This allows us to estimate a typical healing length, calculated at allows us to estimate a typical healing length, calculated at $1.5P_{th}$, $\xi = \hbar / \sqrt{m^* g |\Psi|^2} = 2 \mu m$, where $|\Psi|^2$ is the

FIG. 2 (color online). (a-c) Contour maps of $g^{(1)}(-\mathbf{r}, \mathbf{r})$ for increasing pump fluence. The color-bar maximum corresponds to the peak
value of $g^{(1)}(\mathbf{r}, -\mathbf{r})$ in the panel (d-f) Vertical cuts through the (a-c) value of $g^{(1)}(\mathbf{r}, -\mathbf{r})$ in the panel. (d-f) Vertical cuts through the (a-c) color maps used to extract $g^{(1)}(-y, y)$. These are averaged over eight horizontal nivels, with the standard deviation shown as error hars. horizontal pixels, with the standard deviation shown as error bars. The resulting coherence length is labeled λ_c , and the fit residual is shown. Scale bars are 5 μ m.

condensate density. This sets the scale for density fluctuations and is in reasonable agreement with our observations. Although the effect of disorder is apparent in the intensity patterns, the long coherence length and high degree of firstorder coherence suggests the presence of a single condensate with a large condensate fraction [\[35\]](#page-4-14).

For an equilibrium condensate, increasing density typically leads to a screening of the disorder potential. Thunert et al. [\[22\]](#page-4-17) have recently reported on the important role of dissipation in nonequlibrium polariton condensates. They show that the competition between gain and dissipation can prevent screening of the disorder expected when the polariton interaction dominates over the potential fluctuations. Similarly in this Letter, we do not observe a screening of potential fluctuations up to a blueshift of $\mu \sim 8$ meV.

The same interferometry setup was used to measure the first-order temporal coherence of the polariton condensate. Here, the decrease in fringe contrast is measured over long time delays for two points spatially separated by 3 μ m. The temporal coherence, shown in Fig. [3\(b\)](#page-2-1), exhibits a Gaussian profile with a coherence time $\tau_c = 0.8$ ps. Due to the impulsive pump, this value is not dominated by fluctuations but instead agrees well with our calculation of the condensate survival time. From the emission linewidth, we find a condensate decay time of 1 ps, which is in good agreement with the measured temporal coherence.

One of the most startling features occurs for larger spot sizes. We find that for powers greater than \sim 1.5 P_{th} , phase gradients (density currents) and dislocations are commonly observed. These change from shot to shot, and the overall interference pattern becomes washed out. This is shown in Fig. [4](#page-3-3) where few-shot images were taken at the same location with small and large Gaussian pumps at $1.8P_{th}$. Identical parallel fringes are observed for the small spot, but strong shot-to-shot variations occur for the larger pump. For a small fraction of the laser shots, centrosymmetric fork dislocations due to singly charged vortices such as those shown in Fig. [4\(c\)](#page-3-3) can be observed. These form spontaneously at different locations within the spot from shot to shot. Real-space profiles for a large pump also show density fluctuations, while occasional regions of vanishing density can be attributed to vortex cores (see Supplemental Material [\[36\]\)](#page-4-15).

To emphasize the crucial role of the pump shape, we have performed similar experiments using a refractive

FIG. 3 (color online). (a) The spatial coherence for increasing pump fluence. We find a sharp increase in $g^{(1)}(r, -r)$, followed
by a plateau near $P = 1.5P$. Additional details are provided by a plateau near $P = 1.5P_{th}$. Additional details are provided in Ref. [\[36\]](#page-4-15). (b) First-order temporal coherence, $g^{(1)}(\tau)$, for $P = 1.7P$, measured for two points separated by 3 um Values $P = 1.7P_{th}$, measured for two points separated by 3 μ m. Values of $g^{(1)}(\tau)$ are shown as solid black circles, and the error bars
indicate the standard deviation for each point. The temporal indicate the standard deviation for each point. The temporal coherence of the condensate obtained from a Gaussian fit (red dashed line) is indicated as τ_c .

FIG. 4 (color online). (a-b) Interferograms using a small $(27 \times 25 \mu m)$ Gaussian pump taken at the same sample location and power integrated over four laser shots. (c–d) Interferograms using a large ($97 \times 60 \ \mu m$) Gaussian pump integrated over two laser shots. Yellow circles indicate a fork dislocation. The scale bar is 5 μ m.

beam shaper to control the pump beam profile. In this case, the excitation spot was made significantly larger and with a flat-top intensity. Figure [5](#page-3-4) shows the below threshold (a) and above threshold (b-d) real-space images from three different sample locations. Below threshold, the intensity is nearly flat over the entire pumped region, albeit with some small fluctuations. Above threshold, the appearance of multiple bright regions is observed. In some cases, these regions are separated by as much as ten microns. The resulting interferograms tend to be highly distorted, often showing a mixture of dislocations, phase gradients, and incoherent regions with strong shot-to-shot fluctuations. We have, in addition, verified that in cases with a significant separation between condensates, mutual coherence is lost (see Supplemental Material [\[36\]\)](#page-4-15).

Our experiments with various pump sizes and shapes point to two distinct causes for these distorted patterns. First, a greater sampling of the disorder for large spots can lead to condensation in regions further away from the center. In this case, our interferometric geometry which inverts about the origin will sample regions that can be uncorrelated or possess additional phase shifts due to their different positions. The latter is seen in Figs. $5(e)$ and $5(f)$ where the fringe orientation changes despite the identical geometry. Note also the presence of smaller cross fringes in both cases. These features are never seen for Gaussian pumping. Second, small Gaussian pumping has been theoretically predicted to be beneficial in reducing the region in reciprocal space where modulation instabilities can occur [\[6,38](#page-4-1)–40]. The criteria for such instabilities to occur is nearly always satisfied in organic cavities, which possess a typical cavity decay rate $> 10^2$ times those of reservoir excitons. In our case, for a homogeneous spot,

FIG. 5 (color online). Real-space emission for a flat-top pump spot below (a) and above threshold (b-d). Panels (c) and (d) are intensity patterns that were recorded from different sample locations. (e-f) Interference patterns recorded at the same pump power $(1.5P_{th})$, representing the sample locations (b) and (c), respectively. Note the change in fringe orientation, cross fringes, and poor contrast. The scale bar is $15 \mu m$.

these instabilities exist over a broad range of wave vectors for pump powers up to $10^4 P_{th}$. The short survival time of our condensate helps prevent their significant growth.

In conclusion, we find that organic polariton condensates bear similarities to disordered inorganic microcavities, but with some distinct features. For smaller spots, we always observe a single condensate showing good phase correlation and a coherence length ultimately limited by the pump size. In contrast, for large Gaussian pumps, phase gradients and defects emerge, with strong shot-to-shot fluctuations. Although masked in the linear regime, the role of disorder becomes evident beyond the condensation threshold. For homogeneous spots, the interferograms become highly distorted as a result of both disorder and fluctuations. The size and profile dependence are consistent with current predictions and suggest that the fluctuations may be due to modulation instabilities. Another interesting possibility, however, is that these may be remnants from a Kibble-Zurek-like mechanism [\[40\]](#page-4-18). The ease of fabrication of TDAF—it can be spin coated or thermally evaporated makes it a useful platform for further investigations of these effects.

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