



Laser-Frequency Stabilization Based on Steady-State Spectral-Hole Burning in $\text{Eu}^{3+}:\text{Y}_2\text{SiO}_5$

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We present and analyze a method of laser-frequency stabilization via steady-state patterns of spectral holes in $\text{Eu}^{3+}:\text{Y}_2\text{SiO}_5$. Three regions of spectral holes are created, spaced in frequency by the ground-state hyperfine splittings of $^{151}\text{Eu}^{3+}$. The absorption pattern is shown not to degrade after days of laser-frequency stabilization. An optical frequency comparison of a laser locked to such a steady-state spectral-hole pattern with an independent cavity-stabilized laser and a Yb optical lattice clock demonstrates a spectral-hole fractional frequency instability of $1.0 \times 10^{-15} \tau^{-1/2}$ that averages to $8.5_{-1.8}^{+4.8} \times 10^{-17}$ at $\tau = 73$ s. Residual amplitude modulation at the frequency of the rf drive applied to the fiber-coupled electro-optic modulator is reduced to less than 1×10^{-6} fractional amplitude modulation at $\tau > 1$ s by an active servo. The contribution of residual amplitude modulation to the laser-frequency instability is further reduced by digital division of the transmission and incident photodetector signals to less than 1×10^{-16} at $\tau > 1$ s.

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Frequency stable laser local oscillators (LLOs) are key tools in the field of metrology. Applications of such LLOs include optical atomic clocks [1–3], tests of general relativity [4,5], searches for variation of fundamental constants [6,7], and relativistic geodesy [8,9]. The best stabilized lasers to date [10,11] are obtained by locking their frequencies to Fabry-Perot reference cavities, and their stability is intrinsically limited by thermomechanical length fluctuations of the cavity [12,13].

Higher stability might be possible by the method of spectral-hole burning (SHB) [14–16], where a narrow optical transition of rare-earth ions doped into a cryogenically cooled crystal is used as the frequency reference. Strains in the crystalline host inhomogeneously broaden the narrow absorption line by several gigahertz. For laser-frequency stabilization, narrow transparencies (spectral holes) are created within the absorption line by frequency selective optical pumping [17]. These narrow spectral holes can be used for laser-frequency stabilization by actively steering the frequency of the laser to maximize the transmission through the crystal.

Spectral holes in $\text{Eu}^{3+}:\text{Y}_2\text{SiO}_5$ [18] are particularly promising for laser-frequency stabilization. At 4 K, this material supports spectral holes at 580 nm with linewidths as narrow as 122 Hz [19] and lifetimes of 10^6 s [18]. The frequency shifts due to fluctuations in the ambient magnetic and electric fields, temperature, pressure, and acceleration are all small enough to allow laser-frequency instabilities at the 10^{-17} fractional frequency level [20,21]. However, prior laser-frequency stabilization experiments with $\text{Eu}^{3+}:\text{Y}_2\text{SiO}_5$ have been limited to run times of a few thousand seconds due to degradation of the spectral holes caused by noise and saturation of the probe laser [22].

In this work, we demonstrate frequency stabilization to a steady-state pattern of spectral holes in 1.0 at.% $\text{Eu}^{3+}:\text{Y}_2\text{SiO}_5$ crystals at temperatures near 4 K. This pattern consists of three regions of spectral holes spaced in frequency by 46.2 and 34.6 MHz (see Fig. 1), corresponding to the ground-state hyperfine splittings of $^{151}\text{Eu}^{3+}$ positioned at crystallographic site 1 [23,24]. The Eu^{3+} population reaches steady state as the spectral holes in the three regions are burned. Additional interleaved probing does not modify the absorption spectrum because, for a subset of the $^{151}\text{Eu}^{3+}$ ions with certain detunings within

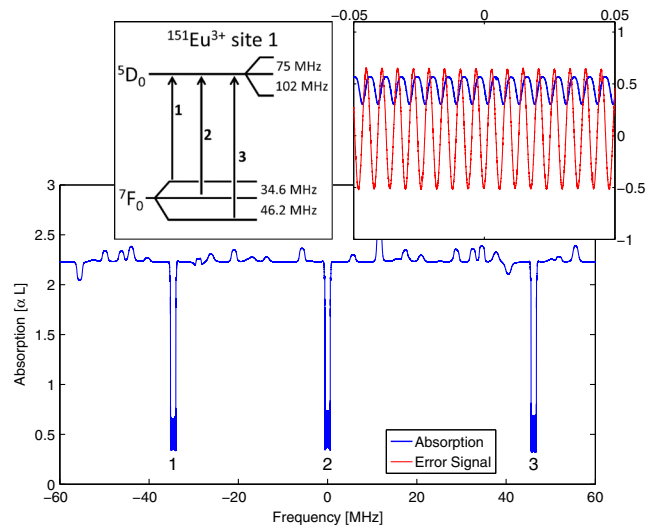


FIG. 1 (color online). Absorption of a steady-state spectral-hole pattern with three regions of spectral holes. The left-hand inset shows a level diagram of $^{151}\text{Eu}^{3+}$ positioned at crystallographic site 1. The right-hand inset shows the absorption (blue) and corresponding PDH error signal (red) of a subset of the center region.

the inhomogeneously broadened absorption line, all three of the hyperfine ground states are addressed by the laser as it probes spectral holes in the three regions. Absorption does not accumulate between the spectral holes because they are spaced by only a few times the minimum observed spectral-hole width. This persistent and self-regenerating pattern is achieved by utilizing probe pulses whose center frequency coincides with an absorption minimum. Weaker phase modulation sidebands are spaced to coincide with absorption maxima to yield a Pound-Drever-Hall (PDH-) type error signal. Using this spectral-hole pattern, laser-frequency stabilization experiments can be made to run indefinitely.

Our SHB LLO employs a two-stage laser-frequency stabilization scheme, as shown in Fig. 2 and similar to that described in Ref. [22]. A 1160 nm external cavity diode laser (ECDL) is frequency doubled to 580 nm and prestabilized to a Fabry-Perot cavity [25]. The prestabilized laser fractional frequency instability is 3×10^{-15} for $0.1 < \tau < 1$ s. This light is split into two beams that are sent through two independent frequency and intensity tunable acousto-optic modulators (AOMs) in order to burn and probe spectral holes in two $\text{Eu}^{3+}:\text{Y}_2\text{SiO}_5$ crystals. A laser intensity of $2 \mu\text{W}/\text{cm}^2$ incident on the crystals is used for both burning and probing for all of the experiments discussed in this Letter. Two fiber-coupled electro-optic modulators (FEOMs) apply sidebands to the beams at 15 kHz for crystal 1 and 21 kHz for crystal 2, for generation of a PDH error signal [17,26]. Detectors (DETs) I1 and I2 measure the power incident on the two crystals, which is stabilized by feedback to the rf power of the probe AOM drives. Detectors T1 and T2 measure the probe light transmitted through the crystals. For measurements of

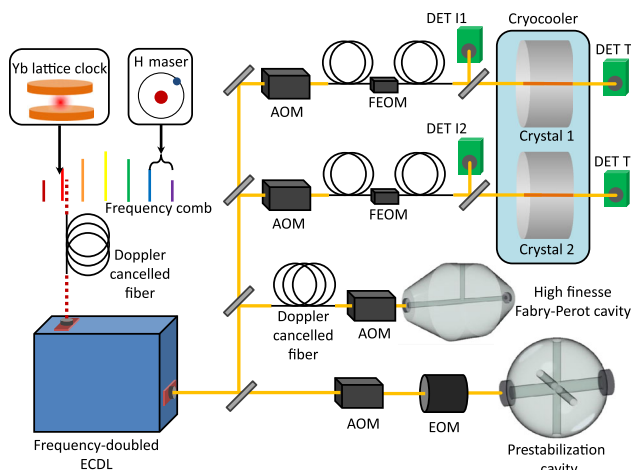


FIG. 2 (color online). Schematic diagram of the spectral-hole burning experiment. Solid yellow lines denote 580 nm laser propagation, and dashed red lines denote 1160 nm laser propagation. AOM, acousto-optic modulator; FEOM, fiber-coupled electro-optic modulator; DET, detector; ECDL, external cavity diode laser.

the laser-frequency stability, visible laser light is sent to an independent high-finesse Fabry-Perot reference cavity [27], and infrared laser light is sent to a frequency comb for comparison against other frequency references, each through a Doppler-cancelled optical fiber [28].

During a SHB laser-frequency stabilization run, several hundred spectral holes are created. A hole is then randomly selected, and the laser spends a few milliseconds probing the center of the spectral hole. Frequency corrections from the two crystals are averaged and applied to the prestabilization cavity AOM. In order to reduce laser-frequency degradation due to the Dick effect [29], probe pulses for the two crystals are interleaved with a 100% duty cycle, as shown in Fig. 3. To reduce frequency instability caused by error signal transients at the beginning of each probe pulse, the error signal generated during the first several hundred microseconds of each pulse is not used for frequency feedback.

A schematic diagram of the error signal generation and residual amplitude modulation (RAM) servo is shown in Fig. 4. The transmission detector signal is digitally divided by the incident detector signal on a field-programmable gate array (FPGA) in order to suppress laser intensity noise. This also provides some suppression of the RAM caused by the FEOM. After filtering, this signal is multiplied with the local oscillator to produce the PDH error signal. The incident detector signal is independently demodulated in order to control the RAM through a servo loop by applying a dc bias to the FEOM [30]. This suppresses the contribution of RAM, converted to fractional frequency instability of a laser locked to a steady-state hole pattern, to less than 1×10^{-16} at averaging times greater than 1 s, and to less than 1×10^{-17} at averaging times greater than 100 s.

To reduce frequency instability due to temperature fluctuations [21], the $\text{Eu}^{3+}:\text{Y}_2\text{SiO}_5$ crystals are housed in a sealed copper pillbox with a fixed amount of helium gas. The temperature of the cryocooler is servo controlled to keep the copper pillbox within 5 mK of the first-order insensitive temperature (3.941 K). The measured out-of-loop temperature instability, converted to fractional frequency instability, is less than 1×10^{-16} at averaging times

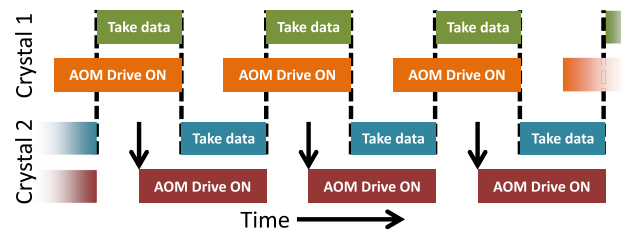


FIG. 3 (color online). Pulse sequence of the interleaved probe scheme for 100% duty cycle laser-frequency stabilization. Frequency feedback from the previous probe pulse on each crystal is applied to the prestabilization cavity AOM at the times indicated by vertical arrows.

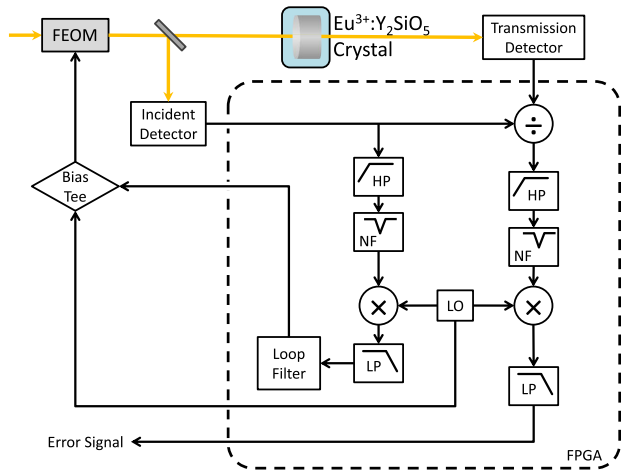


FIG. 4 (color online). Frequency feedback and residual amplitude modulation servo schematic diagram. Black arrows denote electronic signal propagation, and the dashed box denotes calculations performed digitally on a field-programmable gate array (FPGA). LP, low-pass filter; HP, high-pass filter; LO, local oscillator; NF, notch filter.

greater than 1 s, and less than 1×10^{-17} at averaging times between 100 and 10^4 s.

The time evolution of an unperturbed spectral hole at 3.941 K is shown in Fig. 5. The top plot of Fig. 5 shows a decrease in hole depth (in units of αL from maximum absorption of the crystal) and an increase in hole width. The bottom plot of Fig. 5 shows the time evolution of the normalized area of the spectral hole. The hole area is fit to a three-part exponential decay with empirically determined time constants of 2.7, 53.3, and 856.2 h. During a steady-state laser-frequency stabilization run, the entire spectral-hole pattern must be probed frequently enough to reburn all

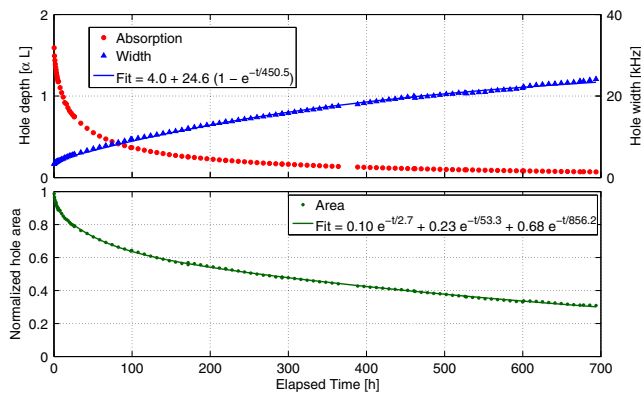


FIG. 5 (color online). Time evolution of a spectral hole in the absence of degradation due to probing. The top plot shows a decrease in the absorption depth (red circles, left axis) and an increase in the FWHM (blue triangles, right axis) with a fit of the width to a function $A + B(1 - e^{-t/\tau})$. The bottom plot shows the area of the spectral hole normalized to the initial area. The data are fit to a three-part exponential decay.

of the spectral holes before they decay. Spectral diffusion [31,32] causes the spectral holes to broaden, limiting the minimum frequency spacing of holes within the steady-state pattern.

The absorption pattern of the three-region steady-state spectral-hole pattern after 3 h of laser-frequency stabilization run time is shown in Fig. 1. Each of the three regions has 201 holes spaced by 6 kHz. As the pattern reaches steady state, the spectral holes increase from an initial 1.7 kHz FWHM to their steady-state FWHM of 3.3 kHz after 10 h of run time.

In contrast, a subset of the single-region spectral-hole pattern used in previous work [22] is shown in Fig. 6, after 3 h of run time. The 603 holes of this pattern are spaced by 270 kHz. Starting from an initial width similar to that of the three-region pattern, the spectral holes have broadened to 5.6 kHz after 3 h of run time. The spectral holes continue to broaden indefinitely, which degrades the frequency stability of the laser locked to this single-region spectral-hole pattern.

Interspersed periodically between probe pulses used for laser-frequency stabilization are scan pulses of individual spectral holes, which allow for the hole shape and error signal slope to be monitored as a run progresses. The top plot of Fig. 7 shows a comparison between the slope of the error signal of a single-region pattern and a three-region steady-state pattern, as a function of the duration of time that the pattern has been used for laser-frequency stabilization. These values are an average of the error signal slope at the center of each spectral hole within the pattern. For both patterns, the error signal slope reaches a maximum as the absorption at the center of the holes approaches zero, then decreases as the holes start to broaden. The three-region steady-state pattern asymptotically approaches a nonzero error signal slope, with a time constant that indicates how long it takes the pattern to reach steady state. The single-region pattern error signal slope decreases until the lock can no longer be maintained after approximately 70 h of run time. The bottom plot of Fig. 7 shows the 1 s averaging time Allan deviation of the differential

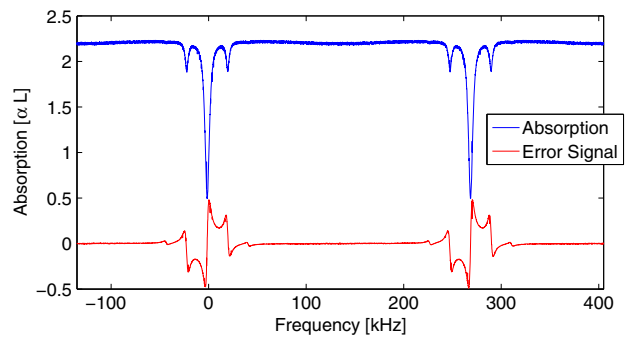


FIG. 6 (color online). Absorption (blue line) and corresponding PDH error signal (red line) of two out of a total of 603 spectral holes in a single-region spectral-hole pattern.

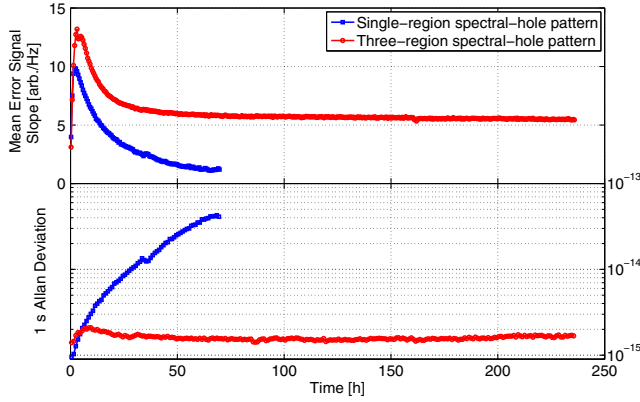


FIG. 7 (color online). Comparison of a single-region pattern (blue squares) versus a three-region steady-state spectral-hole pattern (red circles). The top plot shows the error signal slope averaged over all of the holes in the pattern, and the bottom is the 1 s crystal versus crystal Allan deviation with linear frequency drift removed. Both are plotted with respect to the run time of the laser-frequency stabilization.

frequency noise of the two laser beam lines independently locked to the two crystals, after linear drift has been removed. The Allan deviation values have been divided by $\sqrt{2}$, which is an upper bound on the crystal with better spectral-hole frequency stability. After the three-region pattern has reached steady state, the 1 s differential fractional frequency instability never rises above 2×10^{-15} , out to a run time of almost 10 days. The differential frequency instability of the single-region pattern steadily increases, rising above 1×10^{-14} at 33 h of run time.

We have measured the frequency stability of a laser locked to a three-region steady-state pattern of spectral holes in $\text{Eu}^{3+}:\text{Y}_2\text{SiO}_5$ using a three-cornered hat method [33]. The stability is measured relative to an independent Fabry-Perot reference cavity [27] and a Yb optical lattice clock with a stability of $3.2 \times 10^{-16} \tau^{-1/2}$ [34]. The fractional frequency instability of the laser stabilized to the spectral holes is $1.0 \times 10^{-15} \tau^{-1/2}$ for $0.01 < \tau < 20$ s, and reaches $8.5^{+4.8}_{-1.8} \times 10^{-17}$ at $\tau = 73$ s, as shown in Fig. 8. The duration of this measurement was limited by the duration of time the frequency comb remained mode locked. The crystal versus crystal fractional frequency instability averages to $4.6^{+1.4}_{-0.7} \times 10^{-17}$ at $\tau = 2000$ s with a 0.5 mHz/s linear drift removed. This Allan deviation of the frequency difference between the two crystals has been divided by $\sqrt{2}$ to put an upper bound on the frequency stability of the better of the two crystals. Figure 8 also shows the estimated contribution of temperature instability, Doppler shifts, RAM, and detection noise to the frequency instability of the SHB LLO. Temperature instability is measured using an out-of-loop sensor and converted to frequency instability assuming operation at 5 mK away from the first-order insensitive temperature. Doppler shifts introduced by the motion of the cryostat are measured interferometrically by

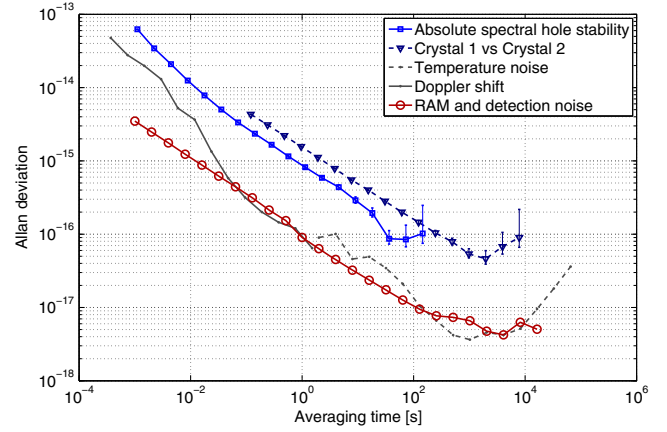


FIG. 8 (color online). Fractional frequency instability of a laser locked to a steady-state pattern of spectral holes in $\text{Eu}^{3+}:\text{Y}_2\text{SiO}_5$. Absolute laser-frequency instability from a three-cornered hat measurement is shown (blue squares), as well as the differential instability of a crystal versus crystal frequency comparison (triangles) where much of the technical noise is common mode. The instability of the crystal versus crystal measurement is worse at small averaging times because the duty cycle is 50%, while the absolute spectral-hole stability measurement uses feedback from both crystals to achieve 100% duty cycle. The expected frequency noise due to temperature fluctuations (dashed gray line), Doppler shifts due to motion of the pillbox (solid gray line), as well as RAM and detection noise (open red circles) are also shown.

retroreflecting a laser off of a mirror mounted on the copper pillbox. These sources of laser-frequency instability are shown not to limit the present performance of this spectral-hole burning experiment.

We have demonstrated steady-state SHB laser-frequency stabilization with a short-term fractional frequency instability of $1.0 \times 10^{-15} \tau^{-1/2}$ that averages down to $8.5^{+4.8}_{-1.8} \times 10^{-17}$ at $\tau = 73$ s. The steady-state spectral-hole pattern successfully prevents degradation of the laser-frequency stability out to run times of many days. RAM is suppressed to less than 1×10^{-6} fractionally at 1 s averaging time using an active servo, and the digital division of transmitted and incident photodetector signals further suppresses laser-frequency instability due to RAM.

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