## Effects of Lifshitz Transition on Charge Transport in Magnetic Phases of Fe-Based Superconductors

Y. Wang,<sup>1</sup> Maria N. Gastiasoro,<sup>2</sup> Brian M. Andersen,<sup>2</sup> M. Tomić,<sup>3</sup> Harald O. Jeschke,<sup>3</sup>

Roser Valentí,<sup>3</sup> Indranil Paul,<sup>4</sup> and P. J. Hirschfeld<sup>1</sup>

<sup>1</sup>Department of Physics, University of Florida, Gainesville, Florida 32611, USA

<sup>2</sup>Niels Bohr Institute, University of Copenhagen, Universitetsparken 5, DK-2100 Copenhagen, Denmark

<sup>3</sup>Institut für Theoretische Physik, Goethe-Universität Frankfurt, 60438 Frankfurt am Main, Germany

<sup>4</sup>Laboratoire Matériaux et Phénomènes Quantiques, Université Paris Diderot-Paris VII & CNRS, UMR 7162, 75205 Paris, France

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The unusual temperature dependence of the resistivity and its in-plane anisotropy observed in the Fe-based superconducting materials, particularly  $Ba(Fe_{1-x}Co_x)_2As_2$ , has been a long-standing puzzle. Here, we consider the effect of impurity scattering on the temperature dependence of the average resistivity within a simple two-band model of a dirty spin density wave metal. The sharp drop in resistivity below the Néel temperature  $T_N$  in the parent compound can only be understood in terms of a Lifshitz transition following Fermi surface reconstruction upon magnetic ordering. We show that the observed resistivity anisotropy in this phase, arising from nematic defect structures, is affected by the Lifshitz transition as well.

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Lifshitz transitions (LT) in metals [1], where Fermi surfaces change topology, have mostly been studied as zero temperature (T) phenomena driven by external parameters such as doping and pressure, etc. [2,3]. Temperature driven LT that can occur in spin or charge density wave phases of metals have received comparatively less attention. In this context, an interesting aspect of the Fe-based superconductors (FeSC) is their multiband nature with several hole and electron pockets. After band reconstruction in the spin density wave (SDW) phase, some of these pockets can disappear due to the increase of the SDW potential with lowering temperature. Recently, a combined study of electron Raman and Hall conductivity on SrFe<sub>2</sub>As<sub>2</sub> has reported signatures of such a transition [4]. This motivates us to study the effects of such transitions on the charge transport of the FeSC. Using a model where current relaxation is due to impurity scattering, we find remarkably strong signatures of such transitions in both the average resistivity  $\rho_{avg}$  and the resistivity anisotropy  $\rho_{ani}$ that are consistent with known experimental trends of these quantities.

The charge transport properties of the FeSC, particularly of BaFe<sub>2</sub>As<sub>2</sub>, are currently the subject of intense research. The *ab*-plane anisotropy of the resistivity  $\rho_{ani} \equiv \rho_a - \rho_b$  of the strain detwinned crystals below the structural transition temperature  $T_s$  has an intriguing sign with the shorter *b* axis being more resistive than the longer *a* axis [5–7]. The anisotropy weakens upon entering the SDW phase even though the magnetic order by itself breaks  $C_4$  symmetry. Furthermore, the anisotropy magnitude in the SDW phase typically increases upon light doping. Together with other measurements [8–16], substantial  $\rho_{ani}$  has been taken as strong evidence for intrinsic electronic nematic behavior [17–19]. The behavior of the average resistivity  $\rho_{avg}$ , which has received considerably less attention, is also highly unusual [20]. In the parent compounds and lightly doped systems,  $\rho_{avg}$  falls abruptly below the SDW transition at  $T_N$ , in dramatic contrast with conventional SDW systems such as Cr.

Several theoretical works have attempted to explain the origin of  $\rho_{ani}$  based on either anisotropic inelastic scattering with spin fluctuations giving rise to hot spot physics [21–23] or on an anisotropic Drude weight of the carriers 24,25]]. Note that, in the 122 systems, where the anisotropy has mostly been studied, the band structure poses an additional challenge, since the ellipticity of the electron pockets vary along the  $k_z$  axis; the ellipticity at  $k_z = 0$  and  $\pi$  planes have opposite signs [26]. Consequently, in theories where the sign of  $\rho_{ani}$  is determined by the ellipticity  $\xi_e$  of the electron pockets on each  $k_z$  plane, such as those involving spin fluctuation scattering, at least a partial cancelation is expected after the  $k_z$  average, and the total  $\rho_{ani}$  will depend on details of the band structure.

In contrast, to the best of our knowledge, there is no theory of the characteristic drop in the average resistivity  $\rho_{avg} \equiv (\rho_a + \rho_b)/2$  immediately below  $T_N$ . Clearly, it is important to simultaneously account for this unusual feature of  $\rho_{avg}$  in addition to  $\rho_{ani}$ . A drop in the inverse Drude weight below  $T_N$  has been recovered in simulations [24] and *ab initio* calculations [34], but this quantity is distinct from the resistivity and includes no information about the scattering mechanism. Qualitatively, the sharp drop in  $\rho_{avg}$  below  $T_N$  can be understood in terms of a collapse in the scattering rate due to the decrease in phase space upon partial gapping of the Fermi surface, which then overcompensates the loss of carriers. However, since these

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two competing effects have the same physical origin, namely the growth of the SDW amplitude with decreasing T, the challenge here is to understand why the scattering rate collapse dominates the resistivity, at least in the undoped and lightly doped compounds, and whether this collapse is dominated by the elastic or inelastic scattering channel.

Our focus on impurity scattering can be appreciated from Fig. 1(a), where we fit the resistivity data of BaFe<sub>2</sub>As<sub>2</sub> from Ref. [35] in the high-*T* paramagnetic phase  $(T > T_N \approx 141 \text{ K})$  to  $\rho_{\text{avg}} = A + BT^2$ . We find excellent agreement up to  $T \approx 300 \text{ K}$ , which argues in favor of *conventional Fermi liquid* and *disorder scattering*, rather than bad-metal physics [36]. More importantly, we find that  $A \gg BT_N^2$  by an order of magnitude, implying that already at  $T_N$  the *elastic scattering* from impurities dominates over inelastic processes.

The relevance of impurity scattering to explain  $\rho_{ani}$  is currently being debated. Recently, Ishida *et al.* [35] reported that, upon annealing,  $\rho_{ani}$  of BaFe<sub>2</sub>As<sub>2</sub> nearly vanished, while significant anisotropy remained in Co-doped compounds. They argued that  $\rho_{ani}$  is due to "nematogens" or anisotropic scattering potentials induced by Fe vacancies and Co defects. Such spatially extended defects aligned preferentially along *a* direction have also been reported by scanning probe studies [37–44]. From the theoretical standpoint,  $C_4$  symmetry breaking defect structures around pointlike impurities driven by orbital [45] or spin [46,47] correlations have indeed been found in realistic models of the Fe-based materials. On the other hand, Kuo and Fisher [48], from a comparison of Co and Ni

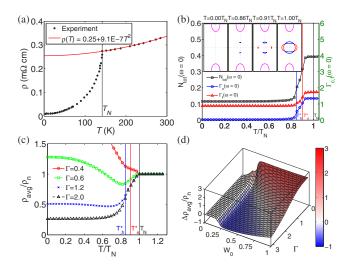


FIG. 1 (color online). (a) Fit (red line) of resistivity data (black dots) from Ref. [35] in the high-*T* paramagnetic phase with  $\rho_{\rm avg} = 2.5 \times 10^{-1} + 9.1 \times 10^{-7} T^2$ . (b) *T* evolution of the total density of states and the *c*- and *f*-electron scattering rates. Insets: Fermi surface evolution due to *T* dependence of SDW potential.  $T_N$ ,  $T_e^*$ ,  $T_h^*$  are defined in text. (c) *T* dependence of average resistivity for various total scattering rates  $\Gamma$ .  $\rho_n \equiv \rho_{\rm avg}(T = T_N)$ . (d)  $\Delta \rho_{\rm avg}$  (defined in text) dependence on  $W_0$  and  $\Gamma$ .

doped samples, have argued that the strain induced  $\rho_{ani}$  does not depend on impurity concentration and therefore is an intrinsic property of the carriers.

The following are our main results. (i) We show that the characteristic drop in  $\rho_{avg}(T)$  in the SDW phase is a consequence of one or more temperature-driven LT. (ii) The result applies to a multiband system in a "dirty" limit, in which an effective elastic scattering rate  $\Gamma > W_0$ , where  $W_0$  is SDW potential at T = 0. In the opposite limit,  $\rho_{\text{avg}}(T)$  increases in the SDW phase. (iii) Consistent with our earlier study [47], we find that extended anisotropic impurity states aligned along a direction give rise to  $\rho_{ani}$  < 0 in the paramagnetic state. More importantly, we show that the anisotropy is independent of the ellipticity of the electron pockets provided the scattering is dominantly intraband. (iv) For parameters relevant for the parent compound, the LT produce a drop in  $\rho_{ani}(T)$  below  $T_N$ which is consistent with experiments. This feature is suppressed by reducing  $W_0$  sufficiently, which is in qualitative agreement with the measured doping dependence of  $\rho_{ani}(T \to 0)$ .

Model.-We consider the two-band model of Brydon et al. [49] along with a mean field description of the SDW state and introduce intraband impurity scattering. Since our goal is to study the effect of rapid change of density of states due to a T-driven LT, we do not expect orbital physics to affect the results qualitatively. The Hamiltonian is given by  $\mathcal{H} = \mathcal{H}_c + \mathcal{H}_f + \mathcal{H}_{SDW} + \mathcal{H}_{imp}$ . Here,  $\mathcal{H}_c =$  $\sum_{\mathbf{k},\sigma} \varepsilon_{\mathbf{k}}^{c} c_{\mathbf{k},\sigma}^{\dagger} c_{\mathbf{k},\sigma}$  and  $\mathcal{H}_{f} = \sum_{\mathbf{k},\sigma} \varepsilon_{\mathbf{k}}^{f} f_{\mathbf{k},\sigma}^{\dagger} f_{\mathbf{k},\sigma}$  describe *c*-hole and f-electron bands, with spin  $\sigma$ , centered around  $\Gamma$  and X/Y points of the 1 Fe/cell Brillouin zone (BZ) with dispersions  $\varepsilon_{\mathbf{k}}^{c} = \varepsilon_{c} + 2t_{c}(\cos k_{x} + \cos k_{y})$  and  $\varepsilon_{\mathbf{k}}^{f} = \varepsilon_{f} + t_{f1}\cos k_{x}\cos k_{y} - t_{f2}\xi_{e}(\cos k_{x} + \cos k_{y})$ , respectively.  $\mathcal{H}_{\text{SDW}} =$  $\sum_{\mathbf{k},\sigma} \sigma W c_{\mathbf{k},\sigma}^{\dagger} f_{\mathbf{k}+\mathbf{Q},\sigma} + \text{H.c., with } \mathbf{Q} = (\pi, 0).$  SDW potential  $W = W_0 \tanh(2\sqrt{T_N/T - 1})$  for  $T \le T_N$  and zero otherwise. We specify all energies in units of  $t_c$ , and we choose  $\varepsilon_c = -3.5$ ,  $\varepsilon_f = 3.0$ ,  $t_{f1} = 4.0$ ,  $t_{f2} = 1.0$ ,  $T_N = 0.04$ . Depending on the magnitude of  $W_0$ , there are either no LT ( $W_0 < W_e^*$ ), or one LT ( $W_h^* > W_0 > W_e^*$ ) where electron pockets disappear below  $T < T_e^*$ , or two transitions  $(W_0 > W_h^*)$  where, in addition, hole pockets disappear below  $T < T_h^* < T_e^*$ .  $(W_e^*, W_h^*, T_e^*, T_h^*)$  depend on the dispersion parameters.

The impurity potential  $\mathcal{H}_{imp} = \sum_{\mathbf{k},\mathbf{q},\sigma} V_{\mathbf{q}} c_{\mathbf{k},\sigma}^{\dagger} c_{\mathbf{k}+\mathbf{q},\sigma} + (c \rightarrow f)$ , with  $V_{\mathbf{q}} = V_0 + V_1(1 + 2\cos q_x)$ , describes scattering of electrons with both isotropic pointlike ( $V_0$  term) and anisotropic extended impurity ( $V_1$  term) potentials. The latter is modeled by three pointlike scatterers aligned along the long or antiferromagnetic *a* direction (*x* axis), and constitutes *T*-independent analogs of the emergent nematogens reported in Ref. [47]. In the BaFe<sub>2</sub>As<sub>2</sub> system,  $V_0$  might represent weak out of plane disorder not capable of generating nematogens [46,47], and  $V_1$  strong in-plane scatterers like Fe vacancies.

We treat the impurity scattering in the Born approximation, and calculate the c and f-scattering rates  $\Gamma_{\mathbf{k}}^{c}(\omega) = -\text{Im}[n_{i}\sum_{\mathbf{k}'}|V_{\mathbf{k}-\mathbf{k}'}|^{2}G_{\mathbf{k}'\mathbf{k}'}^{cc}(\omega)], \text{ where } n_{i} \text{ is the}$ impurity concentration, and similarly  $\Gamma^f_{\mathbf{k}}(\omega)$ , respectively. We parameterize the two impurity potentials by defining the scattering rates  $\Gamma \equiv n_0 V_0^2 N_{\text{tot}}$  and  $\Gamma_1 \equiv n_1 V_1^2 N_{\text{tot}}$ , where  $(n_0, n_1)$  are the concentrations of pointlike and extended impurities, respectively, and  $N_{tot}$  is the total density of states at the chemical potential. Note that, due to c-f mixing in the SDW phase, the Green's functions acquire double indices. Here,  $G^{cc}$ ,  $G^{ff}$ , etc., denote retarded Green's functions in the absence of disorder. In other words, we do not calculate the scattering rates selfconsistently, but we checked that doing so does not change the results significantly. We ignore the real parts of these diagonal (in c-f basis) self energies since our aim is only to extract lifetime effects from the impurity scattering. Similarly, we do not intend to study how impurity scattering affects the SDW potential, and consequently, we ignore impurity induced off diagonal self energies. We calculate the conductivity in units of  $e^2/\hbar$ 

$$\begin{aligned} \sigma_{ii} &= -2 \sum_{\mathbf{k} \in \mathrm{BZ}} \int_{-\infty}^{\infty} \frac{d\omega}{\pi} \frac{\partial n_{\mathrm{F}}(\omega)}{\partial \omega} \{ [2v_{\mathbf{k},i}^{c} \mathrm{Im} \bar{G}_{\mathbf{kk}}^{cc}(\omega)]^{2} \\ &+ [v_{\mathbf{k},i}^{f} \mathrm{Im} \bar{G}_{\mathbf{kk}}^{ff}(\omega)]^{2} + 4 v_{\mathbf{k},i}^{c} v_{\mathbf{k+Q},i}^{f} [\mathrm{Im} \bar{G}_{\mathbf{kk+Q}}^{cf}(\omega)]^{2} \}, \end{aligned}$$

$$(1)$$

where  $\bar{G}$  represent the impurity dressed Green's functions,  $v_{\mathbf{k}}^{c,f}$  the velocity vectors, and *i* is the (a, b) component of the conductivity tensor  $\stackrel{\leftrightarrow}{\sigma}$  (which is diagonal by symmetry). The factor 2 before  $v_{\mathbf{k}}^c$  in the brackets accounts for two hole pockets at  $\Gamma$ .

Note that  $\rho_{avg}(T)$  and  $\rho_{ani}(T)$  are *T* independent in the paramagnetic phase of this model, while the main *T* dependence in the SDW phase is due to that of the potential W(T). By contrast, in experiment  $\rho_{ani}$  is peaked near  $T_N$  [35]. In Ref. [47], we argued that this *T*-dependent anisotropy is intimately related to the unusual nature of the nematogens, whereby they grow in size as the system approaches  $T_N$ . In the current Letter of the effects of LT, we ignore this *T* dependence for simplicity.

Average resistivity.—We compute first  $\rho_{avg}(T)$  by considering only pointlike impurities  $(V_1 = 0)$ . In this case, changing the sign of the ellipticity  $\xi_e \rightarrow -\xi_e$  is approximately equivalent to  $\rho_a \leftrightarrow \rho_b$  so  $\rho_{avg}(T)$  is unchanged (see below). Thus, we compute it reliably for a given ellipticity, which we fix to  $\xi_e = 2$ . In Figs. 1(b)–1(c) we take  $W_0 = 0.32$  with  $W_0/T_N = 8$  (consistent with optical measurements [50,51]), such that  $W_0 > W_h^*$ . The Fermi surface reconstructions associated with the two LT as a function of T are shown in the inset of Fig. 1(b). The main panel of (b) shows rapid drops in  $N_{tot}(\omega = 0)$  and in the scattering rates  $\Gamma_{c,f}(\omega = 0)$ , which is expected from the loss of Fermi

surface sheets associated with the LT. These two competing trends define a crossover in the T dependence of  $\rho_{avg}(T)$ which is shown in Fig. 1(c). For small  $\Gamma \ll W_0$  (clean limit), the loss of carriers dominates and the resistivity increases with lowering T. But for large  $\Gamma \gg W_0$  (dirty limit), the decrease in the scattering rates dominates, and results in a drop in  $\rho_{avg}(T)$  whose magnitude for  $\Gamma = 2$  is comparable to that of the parent compounds. Note that this scenario of enhanced conductivity due to increased lifetime, as opposed to that due to enhanced Drude weight [24], is consistent with optical measurements [50,51]. Furthermore, at T = 0, we get  $\Gamma_c(\omega = 0) \ll W_0$  [see Fig. 1(b)], which agrees with optical conductivity measuring the Drude peak and the spectral weight depletion due to SDW as well-separated features in frequency [50,51], while the remaining  $\Gamma_f(\omega = 0)$  contributes to a broad background.

Next, we define the net change in average resistivity  $\Delta \rho_{\text{avg}} \equiv \rho_{\text{avg}}(T=0) - \rho_{\text{avg}}(T=T_N)$  and show how it varies with  $\Gamma$  and  $W_0$  in Fig. 1(d). For  $W_0 < W_e^*$ , there is no LT and the change is negligible. For  $W_0 > W_e^*$ , such that the system undergoes at least one LT, we see clearly the dirty (where  $\Delta \rho_{\text{avg}} < 0$ ) to clean (where  $\Delta \rho_{\text{avg}} > 0$ ) cross-over as  $\Gamma$  is changed for fixed  $W_0$ . This implies that  $\rho_{\text{avg}}(T)$  of undoped or lightly doped compounds can be explained by a LT provided  $W_e^* < W_0 < \Gamma$ .

*Resistivity anisotropy.*—We model the Fermi surface of the 122 systems by calculating the contributions to the conductivity from the planes  $k_z = \pi(0)$  with their dispersions differing only in the *f*-band ellipticities  $\xi_e = 2(-2)$ . We calculate the resistivity anisotropy of the planes  $\rho_{\text{ani},\xi_e} \equiv \rho_{a,\xi_e} - \rho_{b,\xi_e}$  separately, and then the experimentally relevant net anisotropy  $\rho_{ani} = \bar{\rho}_a - \bar{\rho}_b$  from the average of the conductivities of the two planes, i.e.,  $\bar{\rho}_i = \langle \sigma_i(k_z) \rangle_{k_z}^{-1} \simeq 2/(\rho_{i,\xi_e}^{-1} + \rho_{i,-\xi_e}^{-1})$ , where  $\langle \rangle_{k_z}$  is the exact integral over  $k_z$ , which we have approximated by the average of the contributions at  $k_z = 0$  and  $\pi$ . As noted earlier for  $\Gamma_1 = 0$ , since  $\xi_e \rightarrow -\xi_e$  leads approximately to  $\rho_a \leftrightarrow \rho_b$ , the net anisotropy  $\rho_{ani} \simeq 0$  for  $T < T_N$ , as seen in experiments on annealed samples [35], even though the SDW state itself breaks  $C_4$  symmetry (see Fig. 2 bottom inset). The real BaFe<sub>2</sub>As<sub>2</sub> Fermi surface is considerably more complicated, and there is no exact cancellation between the contributions of  $k_z = 0$  and  $\pi$  to  $\rho_{ani}$ , but the true  $\rho_{ani}$  will nevertheless be considerably reduced due to  $k_{\tau}$  averaging.

We now consider nematogen scattering by setting  $\Gamma_1 = 0.5\Gamma$ , and calculate the anisotropies both in the paramagnetic and the SDW phases. Figure 2 shows  $\rho_{ani,\xi_e}$  and  $\rho_{ani}$  at  $T = T_N$  and 0 for a wide range of  $W_0$ . We note that both  $\rho_{ani}(T_N) < 0$  and  $\rho_{ani}(0) < 0$ , consistent with experiments. The physical implication of the negative sign is that the nematogens, being aligned along the *a* direction, scatter more carriers moving along *b* than those

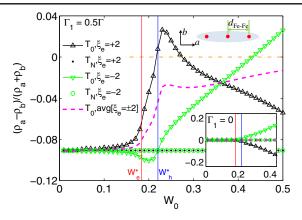


FIG. 2 (color online). Main panel:  $\rho_{ani}$  vs. SDW gap  $W_0$  for  $\Gamma_1 = 0.5\Gamma$ . Curves for ellipticity  $\xi_e = \pm 2$  at  $T = T_0 = 0$  (upward or downward triangles, respectively) and at  $T = T_N$  (dots or circles, respectively), and for the average of two-plane model (dashed line). The dash-dotted line indicates  $\rho_{ani} = 0$ .  $W_e^*$ ,  $W_h^*$  are defined in text. Bottom inset: same quantities for  $\Gamma_1 = 0$ . Top inset: cartoon of extended impurity potential aligned along antiferromagnetic axis *a*.

moving along *a*. Consequently, we expect this feature to hold even in the presence of interband impurity scattering. Next, we note that  $\rho_{\operatorname{ani},\xi_e}(T_N)$  is independent of the sign of  $\xi_e$ , which can be understood as follows. In the paramagnetic phase, assuming intraband-only scattering, the *c*-and *f*-bands decouple. Consequently, shifting only the *f* band by  $(\pi, \pi)$ , keeping the *c* band unshifted, is an allowed unitary transformation.  $\rho_{\operatorname{ani},\xi_e}(T \ge T_N)$  is invariant under this transformation mapping  $\xi_e \to -\xi_e$  and is thus independent of the sign of  $\xi_e$ .

Strictly speaking, this argument is invalid in the SDW phase due to c-f mixing. Nevertheless for  $W_0 \ll W_e^*$ (relevant for sufficiently doped systems), i.e., without any LT, the Fermi surface reconstruction is rather weak, and we find that  $\rho_{ani,\xi_e}(0)$  is practically independent of the sign of  $\xi_e$ , and, moreover,  $\rho_{\text{ani},\xi_e}(0) \approx \rho_{\text{ani}}(0) \approx \rho_{\text{ani}}(T_N)$ . However, for  $W_0 > W_e^*$ , the Fermi surface reconstruction due to the LT is significant, and  $\rho_{ani,2}(0)$  and  $\rho_{ani,-2}(0)$  are generally different. On the other hand, the magnitude of the net anisotropy is always less than that in the paramagnetic state, i.e.,  $|\rho_{ani}(0)| < |\rho_{ani}(T_N)|$ . This is due to loss of  $N_{\rm tot}(\omega=0)$  accompanying the LT (presumably, the associated gain in carrier lifetime does not affect  $\rho_{ani}$ ). Thus, the LT scenario is able to explain why the resistivity anisotropy of the undoped and lightly doped systems decrease as one goes below  $T_N$  in the SDW phase even though the SDW itself breaks  $C_4$  symmetry. Furthermore, for  $W_0 < W_h^*$ ,  $|\rho_{ani}(0)|$  increases with decreasing  $W_0$ , which is consistent with the observation that the resistivity anisotropy in the SDW phase increases with sufficient doping [52]. Finally, in Fig. 3 we show the T dependence of  $\rho_{\operatorname{ani},\xi_e}(T)$ and  $\rho_{ani}(T)$  for  $W_0 = 0.2$  (intermediate doping) with  $W_0/T_N = 8.$ 

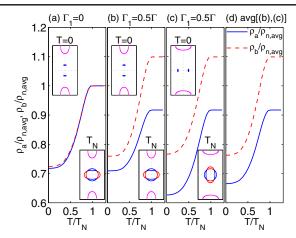


FIG. 3 (color online). (a) Resistivity  $\rho_{a,b}$  at  $k_z = \pi$  for a twoplane model with isotropic scatterers. (b)–(c) Same at  $k_z = \pi, 0$ , respectively, for a two-plane model with anisotropic scatterers. (d) Average of (b) and (c).

Conclusions.—We studied how T-driven Lifshitz transitions, where Fermi pockets disappear due to an increasing SDW potential, affect the average resistivity  $\rho_{avg}$  and its anisotropy  $\rho_{ani}$  of FeSC in the magnetic phase. By fitting experimental data, we argued that the dominant current relaxation mechanism in these materials is impurity scattering. We considered both pointlike and extended impurity (nematogen) potentials, and showed that the characteristic drop in  $\rho_{avg}(T)$  is due to Lifshitz transitions in a dirty SDW metal. Next, we showed that the nematogen generated  $\rho_{\rm ani}$ has the correct sign, namely the direction with longer lattice constant is less resistive. Within this model, the anisotropy in the paramagnetic phase is independent of the sign of the ellipticity of the electron pockets. In the SDW phase, the above holds approximately when the SDW potential is weak enough. The qualitative physics discussed here is general enough to be of potential interest for transport in other multiband systems showing density wave instabilities.

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