Effects of Three-Nucleon Forces and Two-Body Currents on Gamow-Teller Strengths

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We optimize chiral interactions at next-to-next-to leading order to observables in two- and three-nucleon systems and compute Gamow-Teller transitions in $\frac{14C}{12240}$ using consistent two-body currents. We compute spectra of the daughter nuclei ${}^{14}N$ and ${}^{22,24}F$ via an isospin-breaking coupled-cluster technique, with several predictions. The two-body currents reduce the Ikeda sum rule, corresponding to a quenching factor $q^2 \approx 0.84$ –0.92 of the axial-vector coupling. The half-life of ¹⁴C depends on the energy of the first excited 1^+ state, the three-nucleon force, and the two-body current.

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Introduction.— β decay is one of the most interesting processes and most useful tools in nuclear physics. On the one hand, searches for neutrinoless double- β decay probe physics beyond the standard model and basic properties of the neutrino; see Avignone *et al.* [\[1\]](#page-4-0) for a recent review. If neutrinoless double- β decay is observed, an accurate nuclear-physics matrix element is needed to extract neutrino masses from the lifetime. On the other hand, β decay of rare isotopes populates states in exotic nuclei and thereby serves as a spectroscopic tool [\[2,3\].](#page-4-1) The theoretical calculation of electroweak transition matrix elements in atomic nuclei is a challenging task because it requires an accurate description of the structure of the mother and daughter nuclei and an employment of a transition operator that is consistent with the Hamiltonian.

For the transition operator, the focus is on the role of two-body currents (2BCs) from chiral effective field theory (χEFT) [\[4\]](#page-4-2). Two-body currents are related to three-nucleon forces (3NFs) [\[5,6\]](#page-4-3) because the low energy constants (LECs) of the latter constrain the former within χ EFT. Consistency of Hamiltonians and currents is one of the hallmarks of an EFT [\[7\],](#page-4-4) and 2BCs are applied in electromagnetic processes of light nuclei; see Kölling et al. [\[8\]](#page-4-5), Grießhammer *et al.* [\[9\],](#page-4-6) and Pastore *et al.* [\[10\],](#page-4-7) and see Bacca and Pastore [\[11\]](#page-4-8) for a recent review. For weak decays, only the calculation of triton β decay [\[12,13\]](#page-4-9), the related μ decay on ³He and the deuteron [\[14\],](#page-4-10) and protonproton fusion [\[15\]](#page-4-11) exhibits the required consistency, while the very recent calculation of the neutral-current response in 12 C employs phenomenological 3NFs and 2BCs [\[16\].](#page-4-12)

The one-body operator $g_A \sum_{i=1}^A \sigma_i \tau_i^{\pm}$ induces Gamow-
ller transitions. Here quis the axial-vector coupling Teller transitions. Here, g_A is the axial-vector coupling, σ denotes the spin, and τ^{\pm} changes the isospin. Gamow-Teller strength functions [\[17,18\]](#page-4-13) are also of particular interest because of their astrophysical relevance [\[19\]](#page-4-14). Charge-exchange measurements on ⁹⁰Zr and other medium-mass nuclei have suggested that the total strength for β decay is quenched by a factor of $q^2 \approx 0.88 - 0.92$ [\[20](#page-4-15)–23] when compared to the Ikeda sum rule [\[24\]](#page-4-16). Similarly, shell-model calculations [\[25,26\]](#page-4-17) suggest that g_A needs to be quenched by a factor $q \approx 0.75$ to match data. It is not clear whether renormalizations (including 2BCs) of the employed Gamow-Teller operator, missing correlations in the nuclear wave functions, or model-space truncations are the cause of this quenching.

Recent calculations [\[27](#page-4-18)–29] show that chiral 2BCs yield an effective quenching of g_A . However, the Hamiltonians employed in these works are not consistent with the currents (and they contain no 3NFs) and/or the 2BCs are approximated by averaging the second nucleon over the Fermi sea of symmetric nuclear matter. The recent studies [\[30,31\]](#page-4-19) of electroweak transitions in light nuclei employ 3NFs but lack 2BCs. This gives urgency for a calculation of weak decays that employs 3NFs and consistent 2BCs.

In this Letter, we address the quenching of g_A and employ 3NFs together with consistent 2BCs for the computation of β decays and the Ikeda sum rule. We study the β decays of ¹⁴C and ^{22,24}O with interactions and currents from χEFT at next-to-next-to leading order (NNLO) for cutoffs $\Lambda_{\gamma} = 450, 500, 550$ MeV. For the states of the daughter nuclei, we generalize a coupledcluster technique and compute them as isospin-breaking excitations of the mother nuclei. We present predictions and spin assignments for the exotic isotopes 22.24 F and revisit the anomalously long half-life of ^{14}C [31–[33\].](#page-4-20)

Hamiltonian and model space.—The chiral nucleonnucleon (NN) interactions are optimized to the protonproton and the proton-neutron scattering data for laboratory

TABLE I. Pion-nucleon LECs c_i and partial-wave contact LECs (C, C) for the chiral NN interaction at NNLO using Λ_{γ} = 500 MeV and the spectral-function regulator cutoff $\Lambda_{\rm SFR} =$ 700 MeV [\[37\]](#page-4-28). The c_i , \tilde{C}_i , and C_i have units of GeV⁻¹, 10^4 GeV⁻², and 10^4 GeV⁻⁴, respectively.

LEC	Value	LEC	Value	LEC	Value
$\tilde{C}^{{p} {p}}_{^1S_0} \\ C^{{1}}_{{}^1S_0}$ $C_{^{1}P_{1}}$ $C_{^{3}S_{1}-^{3}D}$	-0.91940746 $-0.15136364 \tilde{C}_{1S_0}^{np}$ 2.404 312 35 C_3^{v} 0.414 829 08 $C_{^3P_0}$ $0.61855040 C_{3p}$	c_3	-3.88983848 $-0.15215263 \tilde{C}^{nn}_{1S_0}$ 0.927 937 12 $C_{\frac{3}{5}}$ -0.67347042	c_4	4.307 367 47 -0.15180482 -0.15848125 1.265 789 78 C_{3p_1} -0.77998484

scattering energies below 125 MeV and to deuteron observables. The χ^2 /datum varies between 1.33 for $\Lambda_{\gamma} = 450 \text{ MeV}$ and 1.18 for $\Lambda_{\gamma} = 550 \text{ MeV}$. The χ^2 optimization employs the algorithm POUNDERS [\[34\]](#page-4-21). Table [I](#page-1-0) shows the parameters of the NN interaction for the cutoff $\Lambda_{\gamma} = 500$ MeV; the parameters for the other cutoffs are in the Supplemental Material [\[35\].](#page-4-22) The parameters displayed in Table [I](#page-1-0) are close to those of the chiral interaction $NNLO_{opt}$ [\[36\],](#page-4-23) which were fit to phase shifts.

The 3NF is regularized with nonlocal cutoffs [\[38,39\]](#page-4-24) (to mitigate the convergence problems documented by Hagen et al. [\[40\]](#page-4-25) for local cutoffs). Following Gazit et al. [\[13\],](#page-4-26) we optimize the two LECs $(c_D \text{ and } c_E)$ of the 3NF to the ground-state energies of $A = 3$ nuclei and the triton lifetime. Figure [1](#page-1-1) shows the reduced transition matrix element $\langle E_1^A \rangle = \langle ^3\text{He} || E_1^A || ^3\text{H} \rangle$ as a function of c_D . Here, E_1^A is the $I = 1$ electric multipole of the weak axial-vector current at $J = 1$ electric multipole of the weak axial-vector current at NNLO [\[13\]](#page-4-26). The leading-order (LO) contribution to E_1^A is
proportional to the one-body Gamow-Teller operator proportional to the one-body Gamow-Teller operator $E_1|_{\text{LO}} = ig_A(\text{on})$ \rightarrow $\sum_{i=1}^{\infty} o_i \tau_i$. For the current, we use
the empirical value $g_A = 1.2695(29)$ [\[41\].](#page-4-27) The 2BCs enter
at NNI O and depend on the LECs can can confirmed the chiral $\frac{A}{1}$ [_{LO} = $ig_A(6\pi)^{-1/2} \sum_{i=1}^{A} \sigma_i \tau_i^{\pm}$. For the current, we use at NNLO and depend on the LECs c_D, c_3, c_4 of the chiral interaction [\[42,43\].](#page-5-0) The triton half-life yields an empirical value for $\langle E_1^A \rangle_{\text{emp}}$, which constrains c_D and c_E . For the sets of three different chiral cutoffs $\Lambda = 450, 500, 550$ the sets of three different chiral cutoffs $\Lambda_{\gamma} = 450, 500, 550$, the sets of

FIG. 1 (color online). The quantity related to the triton half-life (E_1^2) as a function c_D for chiral cutoffs $\Lambda_{\chi} = 450, 500, 550$ MeV (dash-dotted red, dashed blue, and dotted green lines, respec- $\langle E_1^A \rangle$ as a function c_D for chiral cutoffs $\Lambda_\gamma = 450, 500, 550$ MeV tively) with corresponding error bands. The different lines were determined by a fit of c_D and c_E to $A = 3$ binding energies.

 (c_D, c_E) that reproduce the triton half-life and the $A = 3$ binding energies are (0.0004;−0.4231), (0.0431;−0.5013), (0.1488;−0.7475), respectively. The vertical bands in Fig. [1](#page-1-1) give the range of c_D that reproduces $\langle E_1^A \rangle_{\text{emp}}$ within the experimental uncertainty the experimental uncertainty.

We employ an $N = 12$ model space consisting of $N + 1$ oscillator shells with frequency $\hbar\Omega = 22$ MeV. The 3NFs use an energy cutoff of $E_{3\text{ max}} = N\hbar\Omega$; i.e., the sum of the excitation energies of three nucleons does not exceed $E_{3\text{ max}}$. We employ the intrinsic Hamiltonian $H = T - T_{c.m.} +$ $V_{NN} + V_{3NF}$ to mitigate any spurious center-of-mass exci-tations [\[44,45\]](#page-5-1). Here, T and $T_{c.m.}$ are the kinetic energy and the kinetic energy of the center of mass, while V_{NN} and V_{3NF} are the chiral NN interaction and 3NF, respectively.

We perform a Hartree-Fock (HF) calculation and compute the normal-ordered Hamiltonian H_N with respect to the reference state $|HF\rangle$. We truncate H_N at the normalordered two-body level. This approximation is accurate in light- and medium-mass nuclei [\[46,47\].](#page-5-2)

Formalism.—We compute the closed-subshell mother nuclei ¹⁴C and ²²;²⁴O with the coupled-cluster method [\[48](#page-5-3)–55]. The similarity-transformed Hamiltonian \bar{H} ≡ $e^{-T}H_Ne^T$ employs the cluster amplitudes

$$
T = \sum_{ia} t_i^a N_a^{\dagger} N_i + \frac{1}{4} \sum_{ijab} t_{ij}^{ab} N_a^{\dagger} N_b^{\dagger} N_j N_i \tag{1}
$$

that create one-particle–one-hole $(1p-1h)$ and two-particle– two-hole $(2p-2h)$ excitations with amplitudes t_i^a and t_i^{ab} ,
respectively Here *i i* denote occupied orbitals of the HF respectively. Here, i , j denote occupied orbitals of the HF reference while a, b denote orbitals of the valence space. The operators N_q^{\dagger} and N_q create and annihilate a nucleon in orbital a respectively. It is understood that the cluster orbital q, respectively. It is understood that the cluster amplitudes T do not change the number of protons and neutrons; i.e., they conserve the z component T_z of isospin. We note that $|HF\rangle$ is the right ground state of the non-Hermitian Hamiltonian \bar{H} . Its left ground state is $\langle \Lambda | = \langle HF | (1 + \Lambda)$, with Λ being a linear combination of $1p-1h$ and $2p-2h$ deexcitation operators [\[54,55\]](#page-5-4).

The daughter nuclei ^{14}N and $^{22,24}F$ are computed via a novel generalization of the coupled-cluster equation-ofmotion approach [\[56](#page-5-5)–58]. We view the states of the daughter nuclei as isospin-breaking excitations $|R\rangle \equiv$ $R|HF\rangle$ of the coupled-cluster ground state, with

$$
R \equiv \sum_{ia} r_i^a p_a^\dagger n_i + \frac{1}{4} \sum_{ijab} r_{ij}^{ab} p_a^\dagger N_b^\dagger N_j n_i. \tag{2}
$$

Here, p_q^{\dagger} and p_q (n_q^{\dagger} and n_q) create and annihilate a proton (neutron) in orbital q with annihilate r_q^q . The combination (neutron) in orbital q with amplitude r_i^a . The combination
 $N^{\dagger} N$ either involves poutrons $N^{\dagger} N$ = $r^{\dagger} r$ or protons $N_q^{\dagger} N_s$ either involves neutrons $N_q^{\dagger} N_s = n_q^{\dagger} n_s$ or protons $N_{\perp}^{\dagger} N_s = n_q^{\dagger} n_s$ and goes with the existence evaluated x^{ab} $N_q^{\dagger} N_s = p_q^{\dagger} p_s$ and goes with the excitation amplitude r_{ij}^{ab} .
We note that *P* lowers the isosnin component *T* of the UE We note that R lowers the isospin component T_z of the HF reference by one unit and keeps the mass number unchanged.

The states of the daughter nucleus result from solving the eigenvalue problem $\overline{H}R_{\alpha}|\text{HF}\rangle = \omega_{\alpha}R_{\alpha}|\text{HF}\rangle$. Here, ω_{α} is the excitation energy with respect to the HF reference and R_{α} denotes a set of amplitudes $R_{\alpha} = (r_i^a(\alpha), r_{ij}^{ab}(\alpha))$. We also introduce the left-acting deexcitation operator introduce the left-acting deexcitation operator

$$
L \equiv \sum_{ia} l_a^i n_i^\dagger p_a + \frac{1}{4} \sum_{ijab} l_{ab}^{ij} n_i^\dagger N_j^\dagger N_b p_a \tag{3}
$$

and solve the left eigenvalue problem $\langle HF|L_{\beta}\bar{H}$ = ω_{β} (HF|L_β. Here, l_a^i and l_b^{ij} are the corresponding 1p-1h
and $2n$, $2b$ description applitudes. The left and right and $2p-2h$ deexcitation amplitudes. The left and right eigenvectors are biorthogonal, i.e., $\langle HF|L_aR_\beta|HF \rangle =$ $\sum_{ia} I_a^i(\alpha) r_i^a(\beta) + \frac{1}{4} \sum_{ijab} I_{ab}^{ij}(\alpha) r_i^{ab}(\beta) = \delta_{\alpha\beta}$.
The energies B and I in Eqs. (2) and (3)

The operators R and L in Eqs. [\(2\)](#page-1-2) and [\(3\)](#page-2-0) excite states in the daughter nucleus that results from β^- decay. If instead we were interested in β^+ decay, we would employ R^{\dagger} and L^{\dagger} and solve the corresponding eigenvalue problems. Our approach allows us to compute excited states in the daughter nucleus that are dominated by isospin-breaking $1p-1h$ excitations of the closed-shell reference $|HF\rangle$ (with ²p-2h excitations being smaller corrections).

Results.—The spectra for ¹⁴N and ^{22,24}F are shown in Fig. [2](#page-2-1) for $\Lambda_{\gamma} = 500 \text{ MeV}$ and compared to data. The sensitivity of our results on the chiral cutoff Λ_{χ} is shown as bands for selected states. The odd-odd daughter nuclei 14 N and $22,24$ F exhibit a higher level density than their mother nuclei. Overall, 3NFs increase the level densities slightly and yield a slightly improved comparison to experiment. For 22.24 F, we make several predictions and spin assignments. In these isotopes, our spectra also compare well to shell-model calculations by Brown and Richter [\[59\].](#page-5-6) Low-lying excitation energies changed by less

FIG. 2 (color online). Spectra of the odd-odd daughter nuclei ¹⁴N and ^{22,24}F resulting from the *NN* interaction with chiral cutoff $\Lambda_{\gamma} = 500$ MeV (blue lines) and the NN interaction and 3NF at NNLO with chiral cutoff $\Lambda_{\gamma} = 500$ MeV (red lines), compared to experiment (black lines). Bands from variation of the chiral cutoff $\Lambda_{\chi} = 450-550$ MeV are shown for the $0^+, 2^+, 1^+$ and the 2^+ , 1^+ excited states in ¹⁴N and ²⁴F, respectively. The band with diagonal gray lines in ^{14}N is for the 1^+ excited state. Parentheses indicate tentative spin-parity assignments.

than 5% when going to $E_{3\text{max}} = 14\hbar\Omega$, and 15% is an error estimate including the error from truncating at the coupledcluster ²p-2h level.

For a better assessment of systematic uncertainties, we compared the results at LO, NLO, and NNLO for Λ_{γ} = 500 MeV. For the ground-state energy of ¹⁴C, we find -60.5 , -93.2 , and -74.4 MeV, respectively, hinting at a slow convergence with respect to the chiral power counting and a significant underbinding with respect to the experimental value of −105.3 MeV. Similar results are obtained for ²²;²⁴O. The convergence is faster for the excited states. The excited $J^{\pi} = 0^+$ ($J^{\pi} = 1^+$) [$J^{\pi} = 2^+$] state in ¹⁴N is at 2.1, 2.8, 2.1 MeV (1.7, 5.6, 4.4 MeV) [0.7, 4.9, 4.4 MeV] in LO, NLO, NNLO, respectively. We also note that the ground-state energies of the daughter nuclei ¹⁴N, ^{22,24}F are 0.54, −2.62, and −6.55 MeV with respect to their corresponding mother nuclei, in fair agreement with experiment. Thus, the systematic uncertainty due to the Hamiltonian is significant for ground states but less of a concern for the excited states discussed in this Letter. The underbinding of the present Hamiltonian suggests that the role of 3NFs and/or higher-order EFT corrections might be more complicated than proposed by Ekström et al. [\[36\]](#page-4-23).

Within the coupled-cluster framework, we compute the total strengths

$$
S_{+} = \langle \Lambda | \overline{\hat{O}_{GT}} \overline{\hat{O}_{GT}^{\dagger}} | HF \rangle, \qquad S_{-} = \langle \Lambda | \overline{\hat{O}_{GT}^{\dagger}} \overline{\hat{O}_{GT}} | HF \rangle
$$

for β^{\pm} decays. Here, $\overline{\hat{O}_{GT}}$ is the similarity-transformed Gamow-Teller operator Gamow-Teller operator

$$
\hat{O}_{GT} \equiv \hat{O}_{GT}^{(1)} + \hat{O}_{GT}^{(2)} \equiv g_A^{-1} \sqrt{3\pi} E_1^A.
$$
 (4)

The one-body operator is $\hat{O}_{GT}^{(1)} = g_A^{-1}$
two-body operator $\hat{O}_{GT}^{(2)}$ is from the 2E $\sqrt{3\pi}E_1^A|_{\text{LO}}$, and the two-body operator $\hat{O}_{GT}^{(2)}$ is from the 2BC at NNLO, with a local regulator and with the same cutoff as the interaclocal regulator and with the same cutoff as the interaction [\[42,43\]](#page-5-0).

The Ikeda sum rule is $S_ - - S_ + = 3(N - Z)$ for $\hat{O}_{GT} = \hat{O}_{GT}^{(1)}$. This identity served as a check of our calculations. Our interest of course is in the contribution calculations. Our interest, of course, is in the contribution of the 2BC operator $\hat{O}_{GT}^{(2)}$ to the total β decay strengths S_{\pm} .
We considered two approximations of this two-body We considered two approximations of this two-body operator. In the normal-ordered one-body approximation (NO1B), the second fermion of the 2BC is summed over the occupied states of the HF reference. In the second approximation, we add the two-body operator $\hat{O}_{GT}^{(2)} \approx \hat{O}_{GT}^{(2)}$
to the NO1B contribution. This is the LO coupled-cluster to the NO1B contribution. This is the LO coupled-cluster contribution of $\hat{O}_{GT}^{(2)}$, and it is a smaller correction to the NO1B contribution for the nuclei we study NO1B contribution for the nuclei we study.

Figure [3](#page-3-0) shows the quenching factor $q^2 = (S_ - - S_+)/$ $[3(N-Z)]$ for ¹⁴C and ^{22,24}O. For the cutoff $\Lambda_{\gamma} =$ 500 MeV, we vary c_D between −0.9 and 0.9 and fix c_E such that the binding energies of the $A = 3$ nuclei are

FIG. 3 (color online). The quenching factor q^2 for ¹⁴C (solid black line), 22 O (dashed red line), and 24 O (dash-dotted blue line) for different c_D values. The calculations used NN and 3NF with consistent 2BCs. The gray area marks the region of c_D that yields the triton half-life and shows the cutoff dependence. The dotted lines show the NO1B results.

reproduced. The ground-state energies and excited states in 14 C and 22.24 F are insensitive to this variation. Thus, the dependence of $(S_ - - S_+)/[3(N - Z)]$ on c_D is due to 2BCs. The NO1B approximation (shown as dotted lines) yields a major part of the quenching. The sensitivity of our results to the chiral cutoffs (Λ_{χ} = 450, 500, 550 MeV) is shown as the gray band for values of c_D and c_E that reproduce the triton half-life. The quenching factor depends on the nucleus, with $q^2 \approx 0.84 - 0.92$ due to 2BCs for the studied nuclei, consistent with Ref. [\[28\]](#page-4-29). We recall that $q^2 \approx 0.88 - 0.92$, extracted from experiments on ⁹⁰Zr [\[21](#page-4-30)–23], are within our error band. We also computed the low-lying strengths for β^- decay and found that only 70%–80% of the total strength S_{\pm} is exhausted below
10 MeV of excitation energy 10 MeV of excitation energy.

Let us finally turn to the β^- decay of ¹⁴C. The long halflife of this decay, about $5700a$, is used in carbon dating of organic material. This half-life is anomalously long in the sense that it exceeds the half-lives of neighboring β unstable nuclei by many orders of magnitude. Recently, several studies attributed the long half-life of ¹⁴C to 3NFs [\[31](#page-4-20)–33], while the experiment points to a complicated strength function [\[60\]](#page-5-7). What do 2BCs contribute to this picture? To address this question, we compute the matrix element $\langle E_1^A \rangle = \langle {}^{14}N|E_1^A| {}^{14}C \rangle$ that governs the β^- decay of ${}^{14}C$ to the ground state of ${}^{14}N$ with c_0 and c_0 from the ¹⁴C to the ground state of ¹⁴N, with c_D and c_E from the triton lifetime. Figure [4](#page-3-1) shows the various contributions to the matrix element. In agreement with Maris et al. [\[31\]](#page-4-20) and Holt *et al.* [\[33\],](#page-4-31) 3NFs reduce the matrix element significantly in size, and our result is similar in magnitude to that reported by Maris et al. [\[31\]](#page-4-20). However, 2BCs counter this reduction to some extent, with the NO1B approximation and the LO approximation both giving significant contributions. Our results for $\langle E_1^A \rangle$ from 2BCs and 3NFs are heaven 5×10^{-3} and 2×10^{-2} This is more than an order between 5×10^{-3} and 2×10^{-2} . This is more than an order

FIG. 4 (color online). The squared transition matrix element for β ⁻ decay of ¹⁴C from increasingly sophisticated calculations (from left to right). NN, 1BC: NN interactions and one-body currents (1BCs) only; $NN + 3NF$, 1BC: addition of 3NF; $NN + 3NF$, $1BC + 2BC_{NO1B}$: addition of 2BC in the NO1B approximation; and $NN + 3NF$, $1BC + 2BC_{LO}$: addition of leading-order 2BC.

of magnitude larger than the empirical value $\langle E_1^A \rangle_{\text{emp}} \approx$
6 × 10⁻⁴ extracted from the 5700*a* half-life of ¹⁴C. In *6*⁻¹ 6×10^{-4} extracted from the 5700*a* half-life of ¹⁴C. In β ⁻¹ decay of ¹⁴C. 2BCs increase the strength of the transition to decay of ¹⁴C, 2BCs increase the strength of the transition to the $14N$ ground state, while they yield an overall quenching (of the sum rule) when all transitions are considered.

We also find that the matrix element $\langle E_1^4 \rangle$ depends on the energy of the first excited 1^+ state in 1^4 N. For the three energy of the first excited 1^+ state in 14 N. For the three different cutoffs $\Lambda_{\gamma} = 450, 500, 550$ MeV, this excited 1^{+} state is at 5.69, 4.41, 3.35 MeV, respectively (compared to 3.95 MeV from experiment). As the value of $\langle E_1^A \rangle$ decreases
strongly, with decreasing excitation energy a correct strongly with decreasing excitation energy, a correct description of this state is important for the half-life in ¹⁴C.

Summary.—We studied β^- decays of ¹⁴C and ^{22,24}O. Because of 2BCs, we found a quenching factor $q^2 \approx$ 0.84–0.92 from the difference in total β decay strengths $S_$ – S₊ when compared to the Ikeda sum rule value $3(N - Z)$. To carry out this study, we optimized interactions from χ EFT at NNLO to scattering observables for chiral cutoffs $\Lambda_{\gamma} = 450$, 500, 550 MeV. We developed a novel coupled-cluster technique for the computation of spectra in the daughter nuclei and made several predictions and spin assignments in the exotic neutron-rich isotopes of fluorine. We find that 3NFs increase the level density in the daughter nuclei and thereby improve the comparison to data. The anomalously long half-life for the β^- decay of ¹⁴C depends in a complicated way on 3NFs and 2BCs. While the former increase the theoretical half-life, the latter somewhat counter this effect. Taken together, the inclusion of 3NFs and 2BCs yields an increase in the computed half-life.

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