Role of Valence Fluctuations in the Superconductivity of Ce122 Compounds

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Pressure dependence of the Ce valence in CeCu₂Ge₂ has been measured up to 24 GPa at 300 K and to 17 GPa at 18–20 K using x-ray absorption spectroscopy in the partial fluorescence yield. A smooth increase of the Ce valence with pressure is observed across the two superconducting (SC) regions without any noticeable irregularity. The chemical pressure dependence of the Ce valence was also measured in $Ce(Cu_{1-x}Ni_x)_2Si_2$ at 20 K. A very weak, monotonic increase of the valence with x was observed, without any significant change in the two SC regions. Within experimental uncertainties, our results show no evidence for the valence transition with an abrupt change in the valence state near the SC II region, challenging the valence-fluctuation mediated superconductivity model in these compounds at high pressure and low temperature.

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The study of heavy-fermion superconductivity has been motivated by the discovery of superconductivity in CeCu₂Si₂ [1]. The BCS theory predicts the suppression of superconductivity by a small amount of magnetic impurities. Therefore, Ce-based heavy-fermion superconductors have been considered to be unconventional superconductors because their valences are close to the magnetic Ce^{3+} state. Superconductivity in these compounds is widely believed to be mediated by antiferromagnetic spin fluctuations. Furthermore, in the Ce-based heavy-fermion systems which exhibit superconductivity under pressure, the superconducting (SC) transition often occurs in the vicinity of the quantum critical point (QCP), leading to scenarios which attribute superconductivity to the occurrence of the spin fluctuations around the QCP. As illustrated in Fig. 1 (in SC I and SC II [2-4]), the SC phase diagrams of $CeCu_2Si_2$ and $CeCu_2Ge_2$, where T_C is the SC critical temperature, show two dome-shaped SC regions. Both SC dome structures of CeCu₂Si₂ and CeCu₂Ge₂ appear to be identical after pressure scaling. Similar anomalies in transport properties of these compounds have been reported [5,6].

The phase diagram of the CeCu₂Ge₂ shows an overlap between SC I and antiferromagnetism (AFM), suggesting a possible antiferromagnetic spin fluctuation mediated pairing interaction. On the other hand, the separation between the onset of the second region SC II, which corresponds to the sharp increase in T_C around 12 GPa, and the disappearance of the AFM order around 8 GPa indicates to a different mechanism for the emergence of the SC II phase. Based on the expanded periodic Anderson model with the slave-boson mean-field theory, valence fluctuations (VF) were proposed as a possible pairing mechanism for the appearance of the SC II region [5,8-10]. A theoretical orbital transition between two different levels has also been suggested as a mechanism for the occurrence of the superconductivity in the SC II region that is far away from the AFM QCP [11,12].

Transport properties of CeCu2Ge2 such as T-linear resistivity can be explained by the theory of the critical valence fluctuation scenario for the superconductivity in the SC II region (VF mediated superconductivity) [5]. The pressure dependence of the unit-cell volume also showed an anomalous contraction around the maximum T_{C} $(T_{C \times max})$, suggesting a valence instability and providing further evidence for a pairing mechanism mediated by VF [13]. However, recently, results from detailed measurements of the unit cell volume at 12 K were unable to confirm the occurrence of the anomalous volume contraction [14]. This calls for a direct measurement of the pressure dependence of the Ce valence in CeCu₂Ge₂.

It has been recently observed that Ni substitution for Cu sites in CeCu₂Si₂ also generates two similar SC domes, although the second SC region shows filamentary superconductivity (SC II') [7]. Ni substitution for Cu in CeCu₂Si₂ induces chemical pressure, which results in a



FIG. 1 (color online). (a) Schematic view of pressure-temperature phase diagram of CeCu₂Ge₂ and CeCu₂Si₂ [3]. The pressure for CeCu₂Si₂ is shifted by 10 GPa (upper horizontal axis) to be consistent with that of CeCu₂Ge₂. The superconducting region consists of SC I and SC II. Antiferromagnetic (AFM) order is only observed in CeCu₂Ge₂. (b) The pressure-temperature phase diagram of Ce(Cu_{1-x}Ni_x)₂Si₂ as a function of x [7]. Kondo temperature (T_K) is also shown for comparison.

changeover from a heavy-fermion state to an intermediate valence regime via an increase in the Kondo temperature (T_K) . Ce $(Cu_{1-x}Ni_x)_2Si_2$ in the paramagnetic region shows similar anomalies in resistivity such as *T*-linear behavior in CeCu₂Si₂. Therefore, the SC II' region in Ce $(Cu_{1-x}Ni_x)_2Si_2$ possibly has the same origin as that in the parent compounds of CeCu₂Si₂ and CeCu₂Ge₂.

In this Letter we report the first direct measurement of the Ce valence in $CeCu_2Ge_2$ as a function of pressure, using x-ray absorption spectroscopy (PFY-XAS) in the high-resolution partial fluorescence yield mode [15–17]. The measured high-resolution x-ray absorption spectroscopy permits reliable derivations of small changes in the Ce valence which cannot be otherwise detected using the normal XAS [18]. The PFY-XAS is a photon-in and photon-out spectroscopic technique that was conducted through the Be gasket of the high-pressure diamond anvil cell. To avoid the destruction of the brittle Be gasket at low temperatures, the maximum pressure achieved was limited to less than 17 GPa. We also measured the temperature dependence of the Ce valence for both CeCu2Ge2 and $CeCu_2Si_2$, as well as the dependence as a function of x in $Ce(Cu_{1-x}Ni_x)_2Si_2$ up to $x \sim 0.2$. Our results show a smooth increase of the Ce valence as a function of hydrostatic pressure for CeCu₂Ge₂ and chemical pressure (Ni concentration) for the Ni-doped CeCu₂Si₂.

The temperature dependence of the PFY-XAS spectra is shown in Figs. 2(a) for CeCu₂Ge₂ and 2(b) for CeCu₂Si₂. Examples of the fits are shown in Fig. 2(c). The spectra of these compounds mainly consist of the $4f^1$ (Ce³⁺) component with small fractions of $4f^0$ (Ce⁴⁺) and $4f^2$ (Ce²⁺). The intensity of $4f^0$ is stronger in CeCu₂Si₂ than that in CeCu₂Ge₂. These results agree with a previous photoemission study [19]. In Fig. 2(d) the estimated spectral weight ratios (w_R) are shown as a function of temperature. We define this ratio as $w_R = 3 + \{I(f^0) - I(f^2)\}/\{I(f^0) +$ $I(f^1) + I(f^2)$, where $I(f^n)$ is the intensity of the f^n component in the PFY-XAS spectra. The absolute value of w_R is not strictly equivalent to the Ce valence in the ground state because the $4f^2$ component can partly stem from the core-hole effect in the final state of the PFY-XAS process [20,21]. Because no variation in the intensity of $4f^2$ is found as a function of temperature and pressure, the changes of the w_R and ground-state valence can be considered nearly identical. The experimental errors mainly



FIG. 2 (color online). Temperature dependences of PFY-XAS for (a) $CeCu_2Ge_2$ and (b) $CeCu_2Si_2$. (c) Examples of the fits for $CeCu_2Ge_2$ and $CeCu_2Si_2$. (d) Derived ratios for the PFY-XAS spectral weight of the compounds as a function of temperature.

originate from the statistics of the data and spectral fitting. In the Ni-doped systems the spectral uncertainty is the main contributor. However, since we systematically fitted the spectra, relative errors in the pressure dependence as well as the x dependence should be small.

No temperature dependence of the valence is observed for either compound, contrary to the predicted temperature dependence of the Ce valence derived from the temperature dependence of the lattice parameters [22]. The magnitude of the crystal electric field (CEF) is 191 K for CeCu₂Ge₂ (Ref. [23]), and 140 and 364 K for CeCu₂Si₂ (Ref. [24]), while the Kondo temperature is 6 K for CeCu₂Ge₂ and 4.5–10 K for CeCu₂Si₂. A much smaller T_K than the CEF may explain the absence of the temperature dependence in both compounds [25]. Another clear feature in our study is that w_R is always higher in CeCu₂Si₂ than in CeCu₂Ge₂, indicating a strong c-f hybridization in CeCu₂Si₂. The mean w_R , averaged over the measured temperature range, is estimated to be 2.99 ± 0.01 for CeCu₂Ge₂ and 3.02 ± 0.01 for CeCu₂Si₂, which is confirmed by the analyses of the resonant x-ray emission spectra as a function of the incident photon energy [17]. The weaker hybridization in CeCu₂Ge₂ is consistent with the larger atomic radius of Ge compared to Si; the substitution resulted in larger lattice constants for CeCu₂Ge₂ [14,22].

We note that the Ce valence normally increases with pressure because of the increase of c-f hybridization. In other words, volume contraction may increase the hybridization, resulting in the increase of the Ce valence. In CeCu₂Si₂ a volume contraction of about 13% occurs with pressure up to 9 GPa, while in CeCu₂Ge₂ the volume contraction of about 11% requires a pressure increase of approximately 20 GPa [14]. Thus, the compressibility of CeCu₂Si₂ is much larger than that of CeCu₂Ge₂, indicating larger monotonic valence changes with pressure. Therefore, it is difficult to find a sudden Ce valence crossover hidden in a larger background of the monotonic pressure-induced valence change if the sudden change in volume at the valence crossover point is relatively small. Studying both $CeCu_2Ge_2$ and $Ce(Cu_{1-x}Ni_x)_2Si_2$ has an advantage in that the amplitude of the external and chemical pressureinduced volume changes is much smaller than that of CeCu₂Si₂. An anomalous small jump in the valence would therefore be easier to detect.

In Fig. 3 we show the pressure dependence of the PFY-XAS spectra measured at (a) 300 and (b) 16–18 K. With increasing pressure, the intensity of $4f^1$ decreases, while the intensity of $4f^0$ increases, showing a monotonic increase of the Ce valence. The Ce valence at low temperature is slightly higher than at 300 K, reflecting the increase of hybridization at low temperatures. The theory of the VF-mediated superconductivity predicts a change in the valence greater than an order of 0.01 at the critical valence crossover pressure just after $T_{C\times max}$ [26]. Here we construe the valence without a



FIG. 3 (color online). PFY-XAS spectra of $CeCu_2Ge_2$ as a function of pressure at (a) 300 and (b) 16–18 K. (c) Estimated spectral weight ratio from the fit to the PFY-XAS spectra as a function of pressure at 300 K (closed circle) and 16–18 K (open circle) with a schematic figure of two superconducting regions.

first-order transition. However, within experimental errors, we only observe a smooth increase of the Ce valence with pressure without any noticeable changes in spectral features across the two SC regions at both room and low temperatures. Another distinct feature is the significantly smaller pressure dependence of the Ce valence in CeCu₂Ge₂ than in CeCu₂Si₂ [27]. This may correspond to the smaller compressibility of CeCu₂Ge₂ [14].

We also measured the Ce valence as a function of the Ni concentration x in Ce(Cu_{1-x}Ni_x)₂Si₂. Increasing x results in a monotonic decrease of the volume at room temperature [7]. A specific heat measurement revealed that low-lying antiferromagnetic quantum fluctuations around the AFM QCP are notably suppressed by the Ni substitution, and that the Fermi liquid state recovers in the Ni-rich region at approximately x > 0.12 [7]. A *T*-linear dependence of the resistivity was observed at $x \approx 0.1$ together with an indication of superconductivity, which is similar to the SC II region of CeCu₂Si₂ in Fig. 1(b). Figure 4(a) shows representative PFY-XAS spectra of Ce(Cu_{1-x}Ni_x)₂Si₂ at 20 K. Chemical composition dependence of the spectra is very small although the Kondo temperature increases

with x. However, a small increase of $4f^1$ and a decrease of $4f^0$ are clearly observed due to the high statistics of the spectra. The x dependence of the Ce valence is shown in Fig. 4(b) for x < 0.12. Our results indicate a very weak and progressive x dependence of the Ce valence without any discontinuous change. The small amplitude of the change in the valence can be explained by the fact that the volume change between x = 0 and 0.2 is only ~1% [7]. The pressure dependence of the valence for the x = 0.05 sample is actually remarkably small as well, as shown in Fig. 4(c), compared with previous results for CeCu₂Si₂, suggesting the possibility that a small amount of Ni substitution results in a decrease in the compressibility. We note that the sample containing x = 0.05 has a reduced critical pressure of \sim 2.8 GPa for the *T*-linear resistivity as compared with that of ~4 GPa for CeCu₂Si₂. The result shown in Fig. 4(c)is surprising because 5% Ni substitution can greatly affect the pressure dependence of the Ce valence.

In the theory of the VF mediated superconductivity, the Coulomb repulsion U_{fc} between f and conduction (c) electrons was included, causing a valence transition with pressure [8,9], where the first-order valence transition which terminates the *d*-wave superconductivity was found to be enhanced. This can be seen as a d-wave pairing mechanism generated by the Coulomb repulsion. Experimentally, one would expect to observe a valence transition with an abrupt valence-change just after $T_{C \times max}$. In CeCu₂Si₂, a smooth valence increase was observed under pressure across the SC domes at both low [27] and room [28] temperatures. Rueff et al. concluded a possible valence fluctuation mediated superconductivity based on these results. However, such a gradual valence increase is actually consistent with what is normally observed in compressed Ce compounds [29], in which the valence fluctuation mediated superconductivity is not theoretically expected. In these Ce compounds, a pressure-induced transition occurs from Kondo to valence fluctuation regions, resulting in a gradual increase of the Ce valence as well as an increase of the Kondo temperature. Theoretically, the mechanism for the appearance of the superconductivity in the SC II region of CeCu₂Ge₂ is the same as that in CeCu₂Si₂. We note that the pressureinduced change in the Ce valence is very different in two Ce compounds; the change in the Ce valence for CeCu₂Ge₂ is much less than that in CeCu₂Si₂. The theory of the VFmediated superconductivity showed that a larger change in the Ce valence induces a larger $T_{C \times \text{max}}$. Thus, if the large pressure-induced background change in the Ce valence results in the valence fluctuation mediated superconductivity, $T_{C \times \text{max}}$ of CeCu₂Si₂ should be much larger than that of CeCu₂Ge₂. However, $T_{C \times max}$ of both compounds is the same order as shown in Fig. 1(a).

To verify the theory based on the valence fluctuation scenario, we should find an abrupt change in the valence on the background of the gradual change in the Ce valence. In



FIG. 4 (color online). (a) PFY-XAS spectra of $Ce(Cu_{1-x}Ni_x)_2Si_2$ as a function of x at 20 K. (b) Ce valence (spectral weight ratio) estimated from the fit to the PFY-XAS spectra with a schematic figure of two superconducting regions. (c) Pressure-induced change in the Ce valence for $Ce(Cu_{0.95}Ni_{0.05})_2Si_2$ with the data of $CeCu_2Si_2$ from the literature [27,28].

CeCu₂Si₂ pressure-induced change in the Ce valence was large primarily due to the larger compressibility described above, inducing a large background of monotonic increase in the Ce valence. In $Ce(Cu_{1-x}Ni_x)_2Si_2$, even a small substitution of Ni for the Cu site would strongly affect the pressure-induced change in the Ce valence. Thus, our Ce122 systems may serve as better candidates for observations of the small valence crossover. Within experimental uncertainties at both room and low temperatures, our results also show a smooth increase of the Ce valence as a function of pressure for $CeCu_2Ge_2$ and as a function of x for $Ce(Cu_{1-x}Ni_x)_2Si_2$, without any anomalous jump just after $T_{C \times \text{max}}$. Since $\text{Ce}(\text{Cu}_{1-x}\text{Ni}_x)_2\text{Si}_2$ has been observed to show the filamentary superconductivity, the relationship between the bulk superconductivity and the Ce valence at high pressures and low temperatures remains to be further investigated in the future.

Another proposed scenario for the origin of the SC II region is the orbital fluctuation mediated pairing mechanism [11,12]. In the theoretical model by Hattori [11] two localized f orbitals were assumed and their occupancy changed discontinuously with pressure, resulting in the increase of the orbital fluctuations at a critical end point.

However, the orbital fluctuations coupled with charge fluctuations, resulting in a valence transition coinciding with the orbital crossover. Thus, this scenario contrasts with our results. Pourovskii et al. suggested that the change of orbital occupancy of the two levels, split by the crystal field as a function of temperature or pressure, affects the 4fdensity of states in the vicinity of the Fermi level [12]. This theory based on the orbital fluctuations showed a possible change in the nonresonant inelastic scattering spectra due to the orbital fluctuation and direct observations of the orbital fluctuation remains to be investigated in the future. Finally, we emphasize in our clear experimental findings that there is no apparent sign of the valence crossover within our experimental errors. Our results here call for a reconsideration of the valence fluctuation scenario to account for the unconventional superconductivity in $Ce(Cu, Si)_2Ge_2$ heavy fermion compounds.

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- F. J. Steglich, J. Aarts, C. D. Bredl, W. Lieke, D. Meschede, W. Franz, and H. Schäfer, Phys. Rev. Lett. 43, 1892 (1979).
- [2] B. Bellarbi, A. Benoit, D. Jaccard, J. M. Mignot, and H. F. Braun, Phys. Rev. B 30, 1182 (1984).
- [3] D. Jaccard, H, Wilhelm, K, Alami-Yadri, and E. Vargoz, Physica (Amsterdam) 259–261B, 1 (1999).
- [4] H. Q. Yuan, F. M. Grosche, M. Deppe, C. Geibel, G. Sparn, and F. Steglich, Science 302, 2104 (2003).
- [5] A. T. Holms, D. Jaccard, and K. Miyake, J. Phys. Soc. Jpn. 76, 051002 (2007).
- [6] Y. Kitaoka, H. Tou, G.-q. Zheng, K. Ishida, K. Asayama, T. C. Kobayashi, A. Kohda, N. Takeshita, K. Amaya, Y. Ōnuki, G. Geibel, C. Schank, and F. Steglich, Physica (Amsterdam) 206–207B, 55 (1995).
- [7] Y. Ikeda, S. Araki, T. C. Kobayashi, Y. Shimizu, T. Yanagisawa, and H. Amitsuka, J. Phys. Soc. Jpn. 81, 083701 (2012).
- [8] Y. Onishi and K. Miyake, J. Phys. Soc. Jpn. 69, 3955 (2000).
- [9] K. Miyake, J. Phys. Condens. Matter 19, 125201 (2007).
- [10] S. Watanabe and K. Miyake, J. Phys. Condens. Matter 23, 094217 (2011).
- [11] K. Hattori, J. Phys. Soc. Jpn. 79, 114717 (2010).
- [12] L. V. Pourovskii, P. Hansmann, M. Ferrero, and A. Georges, Phys. Rev. Lett. **112**, 106407 (2014).

- [13] A. Onodera, S. Tsuduki, Y. Ohishi, T. Watanuki, K. Ishida, Y. Kitaoka, and Y. Ōnuki, Solid State Commun. 123, 113 (2002).
- [14] T. C. Kobayashi, K. Fujiwara, K. Takeda, H. Harima, Y. Ikeda, T. Adachi, Y. Ohishi, C. Geibel, and F. Steglich, J. Phys. Soc. Jpn. 82, 114701 (2013).
- [15] I. Jarrige, J.-P. Rueff, S. R. Shieh, M. Taguchi, Y. Ohishi, T. Matsumura, C. P. Wang, H. Ishii, N. Hiraoka, and Y. Q. Cai, Phys. Rev. Lett. **101**, 127401 (2008).
- [16] H. Yamaoka, I. Jarrige, N. Tsujii, J.-F. Lin, T. Ikeno, Y. Isikawa, K. Nishimura, R. Higashinaka, H. Sato, N. Hiraoka, H. Ishii, and K.-D. Tsuei, Phys. Rev. Lett. 107, 177203 (2011).
- [17] See Supplemental Material at http://link.aps.org/ supplemental/10.1103/PhysRevLett.113.086403 for the experiment, the physical parameters of CeCu₂Ge₂ and CeCu₂Si₂, and the resonant x-ray emission spectra, which includes Refs. [30–53].
- [18] M. A. Edwards, S. Horn, and R. D. Parks, Solid State Commun. 61, 65 (1987).
- [19] D. Ehm, S. Hüffner, F. Reinert, J. Kroha, P. Wölfe, O. Stockert, C. Geibel, and H. v. Löhneysen, Phys. Rev. B 76, 045117 (2007).
- [20] H. Yamaoka, A. Kotani, Y. Kubozono, A. M. Vlaicu, H. Oohashi, T. Tochio, Y. Ito, and H. Yoshikawa, J. Phys. Soc. Jpn. 80, 014702 (2011).
- [21] H. Yamaoka, Y. Zekko, A. Kotani, I. Jarrige, N. Tsujii, J.-F. Lin, J. Mizuki, H. Abe, H. Kitazawa, N. Hiraoka, H. Ishii, and K.-D. Tsuei, Phys. Rev. B 86, 235131 (2012).
- [22] G. Neumann, J. Langen, H. Zahel, D. Plumacher, Z. Kletowski, W. Schlabitz, and D. Wohlleben, Z. Phys. B 59, 133 (1985).
- [23] G. Knopp, A. Loidl, K. Knorr, L. Pawlak, M. Duczmal, R. Caspary, U. Gottwick, H. Spille, F. Steglich, and A. P. Murani, Z. Phys. B 77, 95 (1989).
- [24] S. Horn, E. Holland-Moritz, M. Loewenhaupt, F. Steglich, H. Scheuer, A. Benoit, and J. Flouquet, Phys. Rev. B 23, 3171 (1981).
- [25] P. Bonville, J. A. Hodges, P. Imbert, D. Jaccard, J. Sierro, M. J. Besnus, and A. Meyer, Physica (Amsterdam) 163B, 347 (1990); P. Bonville, J. Hammann, J. A. Hodges, G. Imbert, P. Jéhanno, M. J. Besnus, and A. Meyeribid, *ibid*. 171B, 171 (1991).
- [26] S. Watanabe, A. Tsuruta, K. Miyake, and J. Flouquet, J. Phys. Soc. Jpn. 78, 104706 (2009).
- [27] J. P. Rueff, S. Raymond, M. Taguchi, M. Sikora, J.-P. Itié, F. Baudelet, D. Braithwaite, G. Knebel, and D. Jaccard, Phys. Rev. Lett. **106**, 186405 (2011).
- [28] J. Röhler, J. Klug, and K. Keulerz, J. Magn. Magn. Mater. 76–77, 340 (1988).
- [29] H. Yamaoka, I. Jarrige, A. Ikeda-Ohno, S. Tsutsui, J.-F. Lin, N. Takeshita, K. Miyazawa, A. Iyo, H. Kito, H. Eisaki, N. Hiraoka, H. Ishii, and K. D. Tsuei, Phys. Rev. B 82, 125123 (2010).
- [30] A. Loidl, K. Knorr, G. Knopp, A. Krimmel, R. Caspary, A. Böhm, G. Sparn, C. Geibel, F. Steglich, and A. P. Murani, Phys. Rev. B 46, 9341 (1992).
- [31] E. Lengyel, G. Sparn, M. Nicklas, H. S. Jeevan, C. Geibel, and F. Steglich, Physica (Amsterdam) 378–380B, 415 (2006).

- [32] M. Ishikawa, N. Takeda, M. Koeda, M. Hedo, and Y. Uwatoko, Phys. Rev. B 68, 024522 (2003).
- [33] C. D. Bredl, S. Horn, F. Steglich, B. Lüthi, and R. M. Martin, Phys. Rev. Lett. 52, 1982 (1984).
- [34] P. Gegenwart, M. Lohmann, M. Lang, R. Helfrich, C. Langhammer, M. Köppen, C. Geibel, F. Steglich, and W. Assmus, Physica (Amsterdam) 230–232B, 572 (1997).
- [35] P. Gegenwart, C. Langhammer, C. Geibel, R. Helfrich, M. Lang, G. Sparn, F. Steglich, R. Horn, L. Donnevert, A. Link, and W. Assmus, Phys. Rev. Lett. 81, 1501 (1998).
- [36] P. Gegenwart, M. Lang, A. Link, G. Sparn, C. Geibel, F. Steglich, and W. Assmus, Physica (Amsterdam) 259–261B, 403 (1999).
- [37] G. Knebel, C. Eggert, D. Engelmann, R. Viana, A. Krimmel, M. Dressel, and A. Loidl, Phys. Rev. B 53, 11586 (1996).
- [38] A. Krimmel, A. Loidl, H. Schober, and P. C. Canfield, Phys. Rev. B 55, 6416 (1997).
- [39] B. C. Sales and R. Viswanathan, J. Low Temp. Phys. 23, 449 (1976).
- [40] T. Tayama, M. Lang, T. Lühmann, F. Steglich, and W. Assmus, Phys. Rev. B 67, 214504 (2003).
- [41] G. Liang, R. Barber, Y. Tang, M. Croft, J. L. Cobb, and J. T. Markert, Phys. Rev. B 51, 214 (1995).
- [42] D. Jaccard, K. Behnia, and J. Sierro, Phys. Lett. A 163, 475 (1992).
- [43] F. Thomas, C. Ayache, I. A. Fomine, J. Thomasson, and C. Geibel, J. Phys. Condens. Matter 8, L51 (1996).

- [44] R. A. Fisher, J. P. Emerson, R. Caspary, N. E. Philipps, and F. Steglich, Physica (Amsterdam) 194–196B, 459 (1994).
- [45] U. Lieke, U. Rauchschwalbe, C. B. Bredl, and F. Steglich, J. Appl. Phys. 53, 2111 (1982).
- [46] M. Loewenhaupt, E. Faulhaber, A. Schneidewind, M. Deppe, and K. Hradil, J. Appl. Phys. 111, 07E124 (2012).
- [47] E. A. Goremychkin and R. Osborn, Phys. Rev. B 47, 14280 (1993).
- [48] H. Yamaoka, I. Jarrige, N. Tsujii, N. Hiraoka, H. Ishii, and K.-D. Tsuei, Phys. Rev. B 80, 035120 (2009).
- [49] H. Yamaoka, I. Jarrige, N. Tsujii, M. Imai, J.-F. Lin, M. Matsunami, R. Eguchi, M. Arita, K. Shimada, H. Namatame, M. Taniguchi, M. Taguchi, Y. Senba, H. Ohashi, N. Hiraoka, H. Ishii, and K.-D. Tsuei, Phys. Rev. B 83, 104525 (2011).
- [50] O. Gunnarsson and K. Schönhammer, Phys. Rev. B 28, 4315 (1983).
- [51] H. Yamaoka, H. Sugiyama, Y. Kubozono, A. Kotani, R. Nouchi, A. M. Vlaicu, H. Oohashi, T. Tochio, Y. Ito, and H. Yoshikawa, Phys. Rev. B 80, 205403 (2009).
- [52] H. Yamaoka, I. Jarrige, N. Tsujii, A. Kotani, J.-F. Lin, F. Honda, R. Settai, Y. Ōnuki, N. Hiraoka, H. Ishii, and K.-D. Tsuei, J. Phys. Soc. Jpn. 80, 124701 (2011).
- [53] M. Yano, A. Sekiyama, H. Fujiwara, Y. Amano, S. Imada, T. Muro, M. Yabashi, K. Tamasaku, A. Higashiya, T. Ishikawa, Y. Ōnuki, and S. Suga, Phys. Rev. B 77, 035118 (2008).