Demonstration of a Strong Rydberg Blockade in Three-Atom Systems with Anisotropic Interactions

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We study the Rydberg blockade in a system of three atoms arranged in different two-dimensional geometries (linear and triangular configurations). In the strong blockade regime, we observe high-contrast, coherent collective oscillations of the single excitation probability and an almost perfect van der Waals blockade. Our data are consistent with a total population in doubly and triply excited states below 2%. In the partial blockade regime, we directly observe the anisotropy of the van der Waals interactions between $|nD\rangle$ Rydberg states in the triangular configuration. A simple model that only uses independently measured two-body van der Waals interactions fully reproduces the dynamics of the system without any adjustable parameter. These results are extremely promising for scalable quantum information processing and quantum simulation with neutral atoms.

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Engineering quantum many-body systems with a high degree of control and tunable interactions is an active field of research as it is a prerequisite for quantum information processing [1] and quantum simulation [2]. Recently, significant achievements have been obtained towards this goal, e.g., using trapped ions for simulating quantum magnetism [3–5]. Another platform considered for such tasks consists of systems of neutral Rydberg atoms interacting via the strong and controllable long-range dipoledipole interaction, which is responsible for the Rydberg blockade [6–9]. Through this mechanism, multiple excitations with a resonant narrow-band laser are inhibited within a blockade sphere by Rydberg-Rydberg interactions. The dipole blockade provides a way to realize fast quantum gates and to entangle particles, as demonstrated for two atoms [10,11]. This mechanism can in principle be extended to an ensemble of N atoms, with fascinating applications in quantum state engineering [12].

Although the picture of a blockade sphere has been remarkably successful at describing many recent experiments [13–22], some theoretical works question this simple approach. Even for the case of N = 3, some situations have been identified where nearly resonant dipole-dipole interactions [23], the nonadditivity of the van der Waals potentials [24], or the anisotropy of the interactions [25] lead to the breakdown or reduction of the blockade.

In this Letter, we show that, for experimentally relevant parameters, the Rydberg blockade is robust in ensembles of three atoms. In particular, we consider two different arrangements, namely, a line and an equilateral triangle. We observe an almost perfect van der Waals blockade and the coherent collective behavior of Rydberg excitations in both configurations. To go beyond this observation and understand the dynamics of the system in detail, we measure the angular dependence of the effective interaction energy V_{eff} between two single-atoms excited to $|r\rangle \equiv |nD_{3/2}, m_j = 3/2\rangle$ Rydberg states. Using the measured two-body interaction strength we demonstrate that it is possible to fully reproduce the three-atom excitation dynamics in both the full and partial blockade regimes, with a model based on a master equation with no adjustable parameters. With the degree of experimental control demonstrated here, many theoretical proposals envisioning quantum simulation using Rydberg atoms become realistic.

We consider three atoms, with ground $|g_i\rangle$ and Rydberg $|r_i\rangle$ states coupled with Rabi frequencies Ω_i , and interacting via pairwise interactions V_{ij} . The system is thus described by the Hamiltonian [26]

$$\hat{H} = \sum_{i=1}^{3} \frac{\hbar \Omega_{i}}{2} (\hat{\sigma}_{rg}^{(i)} + \hat{\sigma}_{gr}^{(i)}) + \sum_{i < j} V_{ij} \hat{\sigma}_{rr}^{(i)} \hat{\sigma}_{rr}^{(j)}, \qquad (1)$$

where $\hat{\sigma}_{rg}^{(i)} = |r_i\rangle\langle g_i|, \hat{\sigma}_{gr}^{(i)} = |g_i\rangle\langle r_i|$, and $\hat{\sigma}_{rr}^{(i)} = |r_i\rangle\langle r_i|$. All parameters of the Hamiltonian can be tuned by a proper choice of the experimental settings. In particular, choosing $|r\rangle = |nD_{3/2}\rangle$ gives an extra degree of freedom to tune V_{ij} due to the anisotropy of the interaction. In what follows all Rabi couplings $\Omega_i \equiv \Omega$ are equal within 5%.

A strong blockade is obtained if the interaction strengths V_{ij} between atom pairs are much greater than the atomlight coupling $\hbar\Omega$ [Fig. 1(a)]. In this regime, the states carrying double and triple Rydberg excitations are offresonant with the light field and the system can be described as a two-level model involving the collective states $|ggg\rangle$ and $|\Phi_{1r}\rangle = (|ggr\rangle + |grg\rangle + |rgg\rangle)/\sqrt{3}$, coupled by an effective Rabi frequency $\sqrt{3}\Omega$. Here, $|ijk\rangle \equiv |i_1\rangle|j_2\rangle|k_3\rangle$ stands



FIG. 1 (color online). (a) Relevant energy levels of a three-atom system with van der Waals interactions V_{ij} . In the blockade regime, the ground state $|ggg\rangle$ is resonantly coupled to the symmetric collective state $(|ggr\rangle + |grg\rangle + |rgg\rangle)/\sqrt{3}$. (b) Scheme of the experimental setup. Arbitrary geometries of two-dimensional arrays of dipole traps are obtained by imprinting a phase map φ with the SLM. (c) Trap geometry. Three single-atoms are trapped in microscopic optical tweezers separated by $R = 4 \mu m$ in a linear (top) and by $R = 8 \mu m$ in a triangular arrangement (bottom). The quantization axis \hat{z} is set by a 3G external magnetic field.

for products of the single-atom ground $|g\rangle$, and Rydberg $|r\rangle$ states for atoms 1, 2, and 3.

Our apparatus, shown schematically in Fig. 1(b), was previously described in detail [27]. Three single ⁸⁷Rb atoms are loaded from a magneto-optical trap into three 1 mK-deep microscopic optical traps [28], formed by focusing down a 850 nm Gaussian beam to a waist of 1 μ m (1/ e^2 radius) using a high numerical aperture lens under vacuum [29]. Arbitrary patterns of traps are obtained by imprinting a calculated phase pattern on the beam with a spatial light modulator (SLM) [30]. CCD images of the two trap configurations used in this work are displayed in Fig. 1(c). In the first arrangement (top), the three traps are collinear (parallel to the quantization axis \hat{z}) and separated by $R = 4 \mu$ m. In the second configuration (bottom), the traps form an equilateral triangle with 8 μ m sides.

The same aspheric lens is used to collect the atom fluorescence from each trap. We trigger the experimental sequence as soon as one atom is detected in each of the three traps. The atoms are then optically pumped into $|g\rangle = |5S_{1/2}, F = 2, m_F = 2\rangle$. The quantization axis \hat{z} is set by a 3G external magnetic field. For Rydberg excitation from $|g\rangle$ to $|nD_{3/2}, m_i = 3/2\rangle$, we use a two-photon process [31]: a π -polarized laser beam at 795 nm, detuned from the $|5P_{1/2}, F = 2, m_F = 2\rangle$ intermediate state by $2\pi \times 740$ MHz, and a σ^+ -polarized 474 nm laser beam. Both excitation lasers are frequency locked using an ultrastable cavity providing laser linewidths ~10 kHz. During the Rydberg excitation, the dipole traps are switched off to avoid light shifts. After excitation for a duration τ , we switch on again the dipole traps and we look for the fluorescence of the three atoms. Excitation of an atom to the Rydberg state is inferred from its loss from the corresponding trap (and thus the absence of fluorescence), as Rydberg states are not trapped. The eight different populations P_{ijk} of the three-atom states $|ijk\rangle$ are then reconstructed by repeating each sequence ~150 times [31].

We first consider a one-dimensional array of three individual atoms aligned along the quantization axis [see Fig. 1(c) top] and separated by 4 μ m. To obtain the singleatom Rabi frequencies Ω_i we measure the probability P_r to excite atom *i* to the Rydberg state, with the other two traps switched off, as a function of the excitation pulse area. We observe well-contrasted Rabi oscillations [Fig. 2(a)]. A fit of the data (solid line) gives the same Rabi frequencies $\Omega_i \simeq 2\pi \times 0.8$ MHz for the three atoms (within 5%), as well as small damping rates $\gamma_i \simeq 0.3 \ \mu s^{-1}$ (see below). In Fig. 2(b) a single atom is loaded in each of the three traps. In this configuration we expect full blockade, as the singleatom Rabi frequencies are much smaller than van der Waals interactions: even for the $R = 8 \ \mu m$ distance between the outermost atoms, extrapolation of the measurement of Ref. [27] gives $V_{13} \simeq h \times 32$ MHz. The three atoms are excited to the collective state $|\Phi_{1r}\rangle$ [Fig. 1(a)], and the single excitation probability $P_{1r} \equiv P_{rgg} + P_{grg} + P_{ggr}$ shows oscillations with a frequency of $(1.72 \pm 0.02)\Omega$, compatible with the expected $\sqrt{3}\Omega$. Clear blockade of multiple Rydberg



FIG. 2 (color online). (a) Representative single-atom Rabi flopping to the $|82D_{3/2}\rangle$ state for the central atom in the linear arrangement. Single-atom Rabi frequencies $\Omega \simeq 2\pi \times 0.8$ MHz, and damping rates $\gamma \simeq 0.3 \ \mu s^{-1}$ for all three atoms are obtained from fits (solid lines) to the solution of the OBEs for a single twolevel atom. (b) Probability of single (blue circles), double (red triangles), and triple (green squares) Rydberg excitation as a function of the excitation pulse area in the linear arrangement. The collective enhancement of the Rabi frequency by $\sqrt{3}$ clearly appears in the data. Solid lines are the result of the model described in the text without any adjustable parameter. (c) Same as (b) but for the triangular geometry.

excitations is observed in the data, as the populations $P_{2r} = P_{rrg} + P_{rgr} + P_{grr}$ ($P_{3r} = P_{rrr}$) of doubly (triply) excited states are almost totally suppressed in the system, with P_{2r} (P_{3r}) never exceeding 9% (1%).

We now show that the actual blockade is even better than suggested by these values. Indeed, each atom has a small probability ε to be lost during the sequence, independently of its internal state [32]. An independent measurement of the loss probability gives $\varepsilon = (5 \pm 1)\%$. Since in our detection scheme an atom loss is interpreted as an excitation to the Rydberg state, the *observed* double excitation P_{2r} differs from the *actual* one \tilde{P}_{2r} and, to first order in ε , it reads [32]

$$P_{2r} = (1 - \varepsilon)\tilde{P}_{2r} + 2\varepsilon\tilde{P}_{1r}.$$
(2)

If the blockade were perfect, one would have $\tilde{P}_{2r} = 0$, and the measured P_{2r} would thus oscillate between 0 and 2ε , in phase with P_{1r} . From the data on Fig. 2(b) we can extract an upper bound of ~2% on \tilde{P}_{2r} [32].

To gain more insight into the quality of the blockade for our experimental parameters, we simulate the dynamics of the system with Hamiltonian (1). A sum of independent single atom dissipators,

$$L[\rho] = \sum_{i} \frac{\gamma_i}{2} \left(2\hat{\sigma}_{gr}^{(i)} \rho \hat{\sigma}_{rg}^{(i)} - \hat{\sigma}_{rr}^{(i)} \rho - \rho \hat{\sigma}_{rr}^{(i)} \right), \tag{3}$$

is used to account for a small experimental damping γ_i of the oscillations (mainly due to off-resonant spontaneous emission through the intermediate state $|5P_{1/2}\rangle$; all the γ_i are equal within 10%). The results of the simulation, with no adjustable parameter, are represented by solid lines in Fig. 2(b), where the loss-error correction (2) is included. The very good agreement with the data further supports the quality of the blockade. Our results are compatible with the prediction of the model of double excitation probability $\tilde{P}_{2r}^{(\text{theo.})} \sim 10^{-3}$ for the same experimental parameters. Although proving experimentally that the double excitation is that low would require a more detailed study of systematic effects, this figure is very encouraging for high-fidelity generation of three-atom $|W\rangle$ states.

In the results discussed so far, we only considered a onedimensional configuration. For scalability to a large number of atoms, however, two-dimensional arrays of traps are preferable. In this case, some atom pairs necessarily have an internuclear axis not aligned along the quantization axis and the anisotropy of the interaction comes into play, which might eventually prevent a perfect blockade [23–25]. To investigate this effect we study the blockade in an equilateral triangle configuration. Here, the anisotropic character of the *D*-state orbital plays a role and the interaction energies between atom pairs $V_{12} \approx V_{23}$ are weaker than V_{13} , although the atoms are equally separated. Despite this, Fig. 2(c) shows that the strength of the blockade is not reduced in the triangular geometry. Double and triple excitation probabilities are inhibited and the single excitation probability oscillates at $\sim \sqrt{3}\Omega$. This result opens encouraging prospects for achieving strong blockade over two-dimensional arrays of atoms.

In order to observe directly the anisotropy of the interaction [33] we measured the interaction energy between atom pairs separated by $R = 12 \ \mu m$ as a function of the angle θ between the internuclear axis and the quantization axis \hat{z} . The procedure to extract the effective interaction energy $V_{\rm eff}$ is similar to the one introduced in Ref. [27]. Working in the partial blockade regime ($\hbar \Omega \sim V_{eff}$), we model the excitation dynamics through the solution of the optical Bloch equations (OBE) involving two-level atoms. Strictly speaking, to model two atoms in the $|nD_{3/2}\rangle$ state and $\theta \neq 0$, one would need to consider all 49 Zeeman sublevels with their different van der Waals couplings [34]. So as to keep the model tractable, even for large number of atoms, we model the system in the simplest nontrivial way, retaining only one single doubly excited state $|rr\rangle$ with an effective energy shift $V_{\rm eff}(\theta)$. All input parameters are obtained from single-atom Rabi oscillation experiments. The measured dynamics of the two-atom system are then fitted with the solution of the OBEs with $V_{\rm eff}$ as the only fitting parameter. A more detailed study of the angular dependence of the van der Waals interaction, taking into account the full Zeeman structure of the atom pair, is beyond the scope of this Letter and will be the subject of future work.

The result of this approach is shown in Fig. 3 for the $|82D_{3/2}\rangle$ state. The anisotropy of the effective interaction is evident. The energy shift shows a maximum around $\theta = 0$



FIG. 3 (color online). Angular dependence of the effective interaction energy V_{eff} for two atoms in $|82D_{3/2}\rangle$ at $R = 12 \,\mu\text{m}$, with θ the angle between the internuclear axis and the quantization axis \hat{z} . Red squares indicate the measured energy shifts V_{13} , V_{23} , and V_{12} used for the simulation of three-atom dynamics in the partial blockade regime (see Fig. 4). In the inset, the angular dependence of the interaction for the spherically symmetric $|82S_{1/2}\rangle$ state is shown for comparison. Error bars represent one standard deviation confidence intervals in the fits.

and decreases for larger angles. A relative change of interaction strength by a factor ~3 is measured when θ varies from $\theta = 0$ to $\theta = 60^{\circ}$. In contrast, for a spherically symmetric *S*-Rydberg state, the interaction energy is isotropic (see inset of Fig. 3) [35]. For the *D* state, we observe an unexpected, slight asymmetry in the angular dependence of V_{eff} , probably due to small systematic effects [36].

The angular dependence of $V_{\rm eff}$ manifests itself in the interaction dynamics of the three atoms in the triangular configuration. By increasing the sides of the triangle to $R = 12 \ \mu m$, the effective interaction energies become $(V_{12}, V_{23}, V_{13}) \simeq h \times (0.9, 1.1, 2.6)$ MHz (see red squares in Fig. 3), and the blockade is only partial for our chosen Rabi frequency Ω . In Fig. 4 we show the populations of doubly $(P_{rrg}, P_{rgr}, P_{grr})$ and triply (P_{rrr}) excited states for two different Rabi frequencies. In the first data set [Fig. 4(a)], $\Omega = 2\pi \times 0.8$ MHz and the anisotropy in the binary interaction $(V_{12} \neq V_{13})$ is directly observed in the dynamics: the probability P_{rgr} to detect double excitation of atoms 1 and 3 is almost totally suppressed, while it is appreciable for P_{rrg} and P_{grr} . Those two curves show almost the same dynamics, as expected. Triple excitations are totally blocked in this regime. For comparison, we show also the dynamics when a slightly higher Rabi frequency $\Omega = 2\pi \times 1.6$ MHz is used [Fig. 4(b)]. This corresponds to a partial blockade regime where $V_{13} > \hbar\Omega > V_{12}$. In this case, even triple excitations are not completely blockaded. P_{rrq} and P_{qrr} also exhibit similar behavior, while P_{rqr} shows different dynamics. The populations of states carrying only single excitations also show the anisotropy [32].

Many-body effects have largely been recognized to play a key role in the modeling of systems in physics and



FIG. 4 (color online). Probabilities of detection of double Rydberg excitation P_{rrg} , P_{rgr} , P_{grr} , and triple excitation P_{rrr} versus excitation pulse area $\Omega \tau$ for driving Rabi frequencies $\Omega = 2\pi \times 0.8$ MHz (a), and $\Omega = 2\pi \times 1.6$ MHz (b) in the triangular configuration. The distance between the traps is $R = 12 \ \mu$ m. The ratio between effective pairwise interaction energies is $V_{13}/V_{12} \sim 3$ for $\theta = 60^{\circ}$. Solid lines are the solution of the OBEs without any adjustable parameter.

chemistry [37]. In the case of Rydberg atoms they have been invoked to explain anomalous broadenings of Förster resonances [38,39]. To understand the evolution of the population of the states during excitation and to investigate to what extent few-atom many-body physics can be described from pairwise interactions we perform again a simulation using the OBEs for the three-atom system. In the model, with no adjustable parameters, the measured interaction energies at $\theta = 0$ and $\theta = 60^{\circ}$ (red squares in Fig. 3) are introduced. As shown by the solid lines in Fig. 4, the simulation (where atom loss correction is included) fully reproduces the experimental data. The fact that the simulation can accurately describe the evolution of the triply excited state P_{rrr} suggests that, for our choice of parameters, the pairwise addition of van der Waals level shifts $V_{123} = V_{12} + V_{13} + V_{23}$ is valid to a very good approximation. However, this additivity of the potential may not hold in the case of resonant dipole-dipole interactions. There, quantum interference between different many-body interaction channels can influence the dynamics [23]. All these processes can be studied for Rydberg atoms close to Förster resonance and will be the subject of future work. Another interesting line of research will consist in studying the recently predicted Borromean trimers bound by the dipole-dipole interaction [40].

In summary, we have investigated the dynamics of a system of three Rydberg atoms in both full and partial blockade regimes. We observe a strong van der Waals blockade of the excitations and coherent Rabi oscillations for two different spatial configurations. For the same experimental parameters in the equilateral triangle arrangement, the anisotropy of the interaction potential between $|nD\rangle$ states does not prevent the observation of a strong van der Waals blockade, which is a prerequisite for the scalability of quantum information processing proposals using twodimensional arrays of dipole traps. The strong blockade achieved and the small damping of the oscillations pave the way for the generation of many-atom entanglement with high fidelity through the Rydberg blockade [12]. In the partial blockade regime, the angular dependence of the interaction energy shift between two atoms has been measured for the $|82D_{3/2}\rangle$ and $|82S_{1/2}\rangle$ Rydberg states. Furthermore, we have shown that with the measured effective energy shifts it is possible to reproduce the three-atom dynamics with high accuracy. This result demonstrates that one can confidently scale those studies for two-dimensional arrays of more than a few atoms, enabling the quantum simulation of large-size, long-range interacting spin systems.

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