

## High-Precision Predictions for the Light $CP$ -Even Higgs Boson Mass of the Minimal Supersymmetric Standard Model

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For the interpretation of the signal discovered in the Higgs searches at the LHC it will be crucial in particular to discriminate between the minimal Higgs sector realized in the standard model (SM) and its most commonly studied extension, the minimal supersymmetric standard model (MSSM). The measured mass value, having already reached the level of a precision observable with an experimental accuracy of about 500 MeV, plays an important role in this context. In the MSSM the mass of the light  $CP$ -even Higgs boson,  $M_h$ , can directly be predicted from the other parameters of the model. The accuracy of this prediction should at least match the one of the experimental result. The relatively high mass value of about 126 GeV has led to many investigations where the scalar top quarks are in the multi-TeV range. We improve the prediction for  $M_h$  in the MSSM by combining the existing fixed-order result, comprising the full one-loop and leading and subleading two-loop corrections, with a resummation of the leading and subleading logarithmic contributions from the scalar top sector to all orders. In this way for the first time a high-precision prediction for the mass of the light  $CP$ -even Higgs boson in the MSSM is possible all the way up to the multi-TeV region of the relevant supersymmetric particles. The results are included in the code FEYNHIGGS.

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*Introduction.*—After the spectacular discovery of a signal in the Higgs-boson searches at the LHC by ATLAS and CMS [1,2], the exploration of the properties of the observed particle is meanwhile in full swing. In particular, the observation in the  $\gamma\gamma$  and the  $ZZ^{(*)} \rightarrow 4\ell$  channels has made it possible to determine its mass with already a remarkable precision. Currently, the combined mass measurement from ATLAS is  $125.5 \pm 0.2 \pm 0.6$  GeV [3], and the one from CMS is  $125.7 \pm 0.3 \pm 0.3$  GeV [4]. The other properties that have been determined so far (with significantly lower accuracy) are compatible with the minimal realization of the Higgs sector within the standard model (SM) [5], but a large variety of other interpretations is possible as well, corresponding to very different underlying physics. While within the SM the Higgs-boson mass is just a free parameter, in theories beyond the standard model (BSM) the mass of the particle that is identified with the signal at about 126 GeV can often be directly predicted, providing an important test of the model. The most popular BSM model is the minimal supersymmetric standard model (MSSM) [6], whose Higgs sector consists of two scalar doublets accommodating five physical Higgs bosons. In lowest order these are the light and heavy  $CP$ -even  $h$  and  $H$ , the  $CP$ -odd  $A$ , and the charged Higgs bosons  $H^\pm$ .

The parameters characterizing the MSSM Higgs sector at lowest order are the gauge couplings, the mass of the  $CP$ -odd Higgs boson,  $M_A$ , and  $\tan\beta \equiv v_2/v_1$ , the ratio of the

two vacuum expectation values. Accordingly, all other masses and mixing angles can be predicted in terms of those parameters, leading to the famous tree-level upper bound for the mass of the light  $CP$ -even Higgs boson,  $M_h \leq M_Z$ , determined by the mass  $M_Z$  of the  $Z$  boson. This tree-level upper bound, which arises from the gauge sector, receives large corrections from the Yukawa sector of the theory, which can amount up to  $\mathcal{O}(50\%)$  (depending on the model parameters) upon incorporating the full one-loop and the dominant two-loop contributions [7]. The prediction for the light  $CP$ -even Higgs-boson mass in the MSSM is affected by two kinds of theoretical uncertainties, namely parametric uncertainties induced by the experimental errors of the input parameters, and intrinsic theoretical uncertainties that are due to unknown higher-order corrections. Concerning the SM input parameters, the dominant source of parametric uncertainty is the experimental error on the top-quark mass  $m_t$ . Very roughly, the impact of the experimental error on  $m_t$  on the prediction for  $M_h$  scales like  $\delta M_h^{\text{para},m_t}/\delta m_t^{\text{exp}} \sim 1$  [8]. As a consequence, high-precision top physics providing an accuracy on  $m_t$  much below the GeV level is a crucial ingredient for precision physics in the Higgs sector [8]. Concerning the intrinsic theoretical uncertainties caused by unknown higher-order corrections, an overall estimate of  $\delta M_h^{\text{intr}} \sim 3$  GeV has been given in Refs. [7,9] [the more recent inclusion of the leading  $\mathcal{O}(\alpha_t\alpha_s^2)$  three-loop corrections [10] has slightly

reduced this estimated uncertainty by few  $\mathcal{O}(100 \text{ MeV})$ , while it was pointed out that a more detailed estimate needs to take into account the dependence on the considered parameter region of the model. In particular, the uncertainty of this fixed-order prediction is expected to be much larger for scalar top masses in the multi-TeV range. This region of the parameter space has received considerable attention recently, partly because of the relatively high value of  $M_h \approx 126 \text{ GeV}$ , which generically requires either large top squark masses or large mixing in the scalar top sector, and partly because of the limits from searches for supersymmetric (SUSY) particles at the LHC. While within the general MSSM the lighter scalar superpartner of the top quark is allowed to be relatively light (down to values even as low as  $m_t$ ), both with respect to the direct searches and with respect to the prediction for  $M_h$  (see, e.g., Ref. [11]), the situation is different in more constrained models. For instance, global fits in the constrained minimal supersymmetric standard model (CMSSM) prefer scalar top masses in the multi-TeV range [12,13].

Here we present a significantly improved prediction for the mass of the light  $CP$ -even Higgs boson in the MSSM, which is expected to have an important impact on the phenomenology in the region of large squark masses and on its confrontation with the experimental results.

*Improved prediction for  $M_h$ .*—In the MSSM with real parameters (we restrict to this case for simplicity; for the treatment of complex parameters see Refs. [14,15] and references therein), using the Feynman diagrammatic (FD) approach, the higher-order corrected  $CP$ -even Higgs boson masses are derived by finding the poles of the  $(h, H)$ -propagator matrix. The inverse of this matrix is given by  $-i \times$

$$\begin{pmatrix} p^2 - m_{h,\text{tr}}^2 + \hat{\Sigma}_{hh}(p^2) & \hat{\Sigma}_{hH}(p^2) \\ \hat{\Sigma}_{hH}(p^2) & p^2 - m_{H,\text{tr}}^2 + \hat{\Sigma}_{HH}(p^2) \end{pmatrix}, \quad (1)$$

where  $m_{h,H,\text{tr}}$  denote the tree-level masses, and  $\hat{\Sigma}_{hh,HH,hH}(p^2)$  are the renormalized Higgs boson self-energies evaluated at the squared external momentum  $p^2$  [for the computation of the leading contributions to those self-energies it is convenient to use the basis of the fields  $\phi_1, \phi_2$ , which are related to  $h, H$  via the (tree-level) mixing angle  $\alpha$ :  $h = -\sin \alpha \phi_1 + \cos \alpha \phi_2$ ,  $H = \cos \alpha \phi_1 + \sin \alpha \phi_2$ ]. The status of higher-order corrections to these self-energies is quite advanced. The complete one-loop result within the MSSM is known [16,17]. The by far dominant one-loop contribution is the  $\mathcal{O}(\alpha_t)$  term due to top quark and top squark loops ( $\alpha_t \equiv h_t^2/(4\pi)$ ,  $h_t$  being the top-quark Yukawa coupling). The computation of the two-loop corrections has meanwhile reached a stage where all the presumably (sub)dominant contributions are available, see Ref. [7] and references therein. The public code FEYNHIGGS [7,14,18,19] includes all of the above corrections, where the on-shell (OS) scheme for the

renormalization of the scalar quark sector has been used (another public code, based on the renormalization group (RG) improved effective potential, is CPSUPERH [20]). A full two-loop effective potential calculation (supplemented by the momentum dependence for the leading pieces and the leading three-loop corrections) has been published [21]. However, no computer code is publicly available. Most recently another leading three-loop calculation at  $\mathcal{O}(\alpha_t \alpha_s^2)$  became available (based on a  $\overline{\text{DR}}$  or a “hybrid” renormalization scheme for the scalar top sector), where the numerical evaluation depends on the various SUSY mass hierarchies [10], resulting in the code H3M (which adds the three-loop corrections to the FEYNHIGGS result).

We report here on an improved prediction for  $M_h$  where we combine the fixed-order result obtained in the OS scheme with an all-order resummation of the leading and subleading contributions from the scalar top sector. We have obtained the latter from an analysis of the renormalization group equations (RGEs) at the two-loop level [22]. Assuming a common mass scale  $M_S = \sqrt{m_{\tilde{t}_1} m_{\tilde{t}_2}}$  ( $m_{\tilde{t}_{1,2}}$  denote the two scalar top masses, and  $M_S \gg M_Z$ ) for all relevant SUSY mass parameters, the quartic Higgs coupling  $\lambda$  can be evolved via SM RGEs from  $M_S$  to the scale  $Q$  (we choose  $Q = m_t$  in the following) where  $M_h^2$  is to be evaluated (see, for instance, Ref. [23] and references therein)

$$M_h^2 = 2\lambda(m_t)v^2. \quad (2)$$

Here  $v \sim 174 \text{ GeV}$  denotes the vacuum expectation value of the SM. Three coupled RGEs are relevant for this evolution, the ones for  $\lambda, h_t$ , and  $g_s$  [the strong coupling constant,  $\alpha_s = g_s^2/(4\pi)$ ]. Since SM RGEs are used, the relevant parameters are given in the  $\overline{\text{MS}}$  scheme. We incorporate the one-loop threshold corrections to  $\lambda(M_S)$  as given in Ref. [23], with  $x_t = X_t/M_S$ ,  $h_t = h_t(M_S)$ ,

$$\lambda(M_S) = (3h_t^4)/(8\pi^2)x_t^2[1 - 1/12x_t^2], \quad (3)$$

where as mentioned above  $X_t$  is an  $\overline{\text{MS}}$  parameter. Equation (3) ensures that Eq. (2) consists of the “pure loop correction” that will be denoted  $(\Delta M_h^2)^{\text{RGE}}$  below. Using RGEs at two-loop order [22], including fermionic contributions from the top sector only, leads to a prediction for the corrections to  $M_h^2$  including leading and subleading logarithmic contributions  $L^n$  and  $L^{(n-1)}$  at  $n$ -loop order [ $L \equiv \ln(M_S/m_t)$ ], originating from the top quark and top squark sector of the MSSM. We have obtained both analytic solutions of the RGEs up to the seven-loop level as well as a numerical solution incorporating the leading and subleading logarithmic contributions up to all orders. In a similar way in Ref. [24] the leading logarithms at three- and four-loop order have been evaluated analytically.

Concerning the combination of the higher-order logarithmic contributions obtained from solving the RGEs with

the fixed-order FD result implemented in FEYNHIGGS comprising corrections up to the two-loop level in the OS scheme, we have used the parametrization of the FD result in terms of the running top-quark mass at the scale  $m_t$ ,  $\bar{m}_t = m_t^{\text{pole}}/[1 + 4/(3\pi)\alpha_s(m_t^{\text{pole}}) - 1/(2\pi)\alpha_t(m_t^{\text{pole}})]$ , where  $m_t^{\text{pole}}$  denotes the top-quark pole mass. Avoiding double counting of the logarithmic contributions up to the two-loop level and consistently taking into account the different schemes employed in the FD and the RGE approach, the correction  $\Delta M_h^2$  takes the form

$$\Delta M_h^2 = (\Delta M_h^2)^{\text{RGE}}(X_t^{\text{MS}}) - (\Delta M_h^2)^{\text{FD,LL1,LL2}}(X_t^{\text{OS}}),$$

$$M_h^2 = (M_h^2)^{\text{FD}} + \Delta M_h^2. \quad (4)$$

Here  $(M_h^2)^{\text{FD}}$  denotes the fixed-order FD result,  $(\Delta M_h^2)^{\text{FD,LL1,LL2}}$  are the logarithmic contributions up to the two-loop level obtained with the FD approach in the OS scheme, while  $(\Delta M_h^2)^{\text{RGE}}$  are the leading and subleading logarithmic contributions (either up to a certain loop order or summed to all orders) obtained in the RGE approach, as evaluated via Eq. (2). In all terms of Eq. (4) the top-quark mass is parametrized in terms of  $\bar{m}_t$ ; the relation between  $X_t^{\text{MS}}$  and  $X_t^{\text{OS}}$  is given by

$$X_t^{\text{MS}} = X_t^{\text{OS}}[1 + 2L(\alpha_s/\pi - (3\alpha_t)/(16\pi))] \quad (5)$$

up to nonlogarithmic terms, and there are no logarithmic contributions in the relation between  $M_S^{\text{MS}}$  and  $M_S^{\text{OS}}$ .

Since the higher-order corrections beyond two-loop order have been derived under the assumption  $M_A \gg M_Z$ , to a good approximation these corrections can be incorporated as a shift in the prediction for the  $\phi_2\phi_2$  self-energy (where  $\Delta M_h^2$  enters with a coefficient  $1/\sin^2\beta$ ). In this way the new higher-order contributions enter not only the prediction for  $M_h$ , but also all other Higgs sector observables that are evaluated in FEYNHIGGS. The latest version of the code, FEYNHIGGS 2.10.0, which is available at FEYNHIGGS.DE, contains those improved predictions as well as a refined estimate of the theoretical uncertainties from unknown higher-order corrections. Taking into account the leading and subleading logarithmic contributions in higher orders reduces the uncertainty of the remaining unknown higher-order corrections. Accordingly, the estimate of the uncertainties arising from corrections beyond two-loop order in the top quark or top squark sector is adjusted such that the impact of replacing the running top-quark mass by the pole mass (see Ref. [7]) is evaluated only for the nonlogarithmic corrections rather than for the full two-loop contributions implemented in FEYNHIGGS. Further refinements of the RGE resummed result are possible, in particular extending the result to the case of a large splitting between the left- and right-handed soft SUSY-breaking terms in the scalar top sector [25] and to the region of small values of  $M_A$  (close to  $M_Z$ ) as well as including the corresponding

contributions from the (s)bottom sector. We leave those refinements for future work.

*Numerical analysis.*—In this section we briefly analyze the phenomenological implications of the improved  $M_h$  prediction for large top squark mass scales, as evaluated with FEYNHIGGS 2.10.0. The upper plot of Fig. 1 shows  $M_h$  as a function of  $M_S$  for  $X_t = 0$  and  $X_t/M_S = 2$  (which corresponds to the minimum and the maximum value of  $M_h$  as a function of  $X_t/M_S$ , respectively; here and in the following  $X_t$  denotes  $X_t^{\text{OS}}$ ). The other parameters are  $M_A = M_2 = \mu = 1000$  GeV,  $m_{\tilde{g}} = 1600$  GeV [ $M_2$  is the SU(2) gaugino mass term,  $\mu$  the Higgsino mass parameter, and  $m_{\tilde{g}}$  the gluino mass], and  $\tan\beta = 10$ . The plot shows for the two values of  $X_t/M_S$  the fixed-order FD result containing corrections up to the two-loop level (labeled as “FH295,” which refers to the previous version of the code FEYNHIGGS) as well as the latter result supplemented with the analytic solution of the RGEs up to the three-loop, . . . , seven-loop level (labeled as “3-loop,” . . . , “7-loop”). The curve labeled as “LL + NLL” represents our full result where the FD contribution is supplemented by the leading

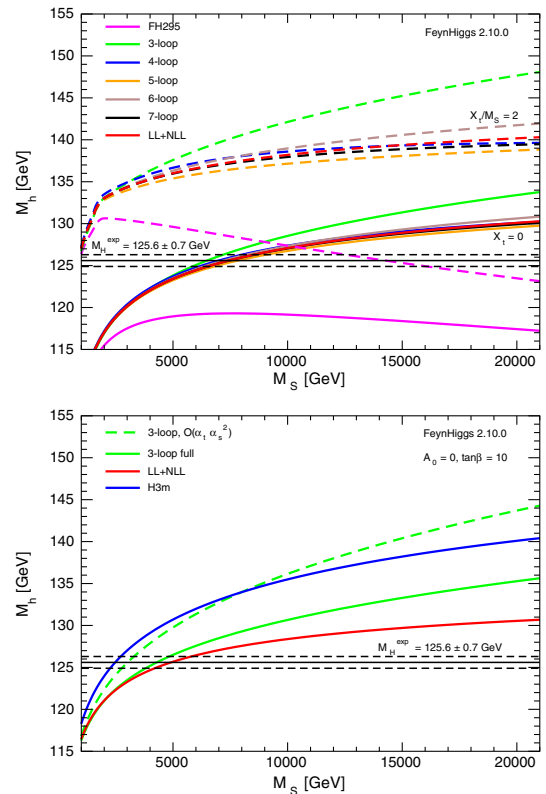


FIG. 1 (color online). Upper plot:  $M_h$  as a function of  $M_S$  for  $X_t = 0$  (solid) and  $X_t/M_S = 2$  (dashed). The full result (“LL + NLL”) is compared with results containing the logarithmic contributions up to the three-loop, . . . , seven-loop level and with the fixed-order FD result (“FH295”). Lower plot: comparison of FEYNHIGGS (red) with H3M (blue). In green we show the FEYNHIGGS three-loop result at  $\mathcal{O}(\alpha_t\alpha_s^2)$  (full) as dashed (solid) line.



and next-to-leading logarithms summed to all orders. One can see that the impact of the higher-order logarithmic contributions is relatively small for  $M_S = \mathcal{O}(1 \text{ TeV})$ , while large differences between the fixed-order result and the improved results occur for large values of  $M_S$ . The three-loop logarithmic contribution is found to have the largest impact in this context, but for  $M_S \gtrsim 2500(6000) \text{ GeV}$  for  $X_t/M_S = 2(0)$  also contributions beyond three-loop are important. A convergence of the higher-order logarithmic contributions towards the full resummed result is visible. At  $M_S = 20 \text{ TeV}$  the difference between the seven-loop result and the full resummed result is around  $900(200) \text{ MeV}$  for  $X_t/M_S = 2(0)$ . The corresponding deviations stay below  $100 \text{ MeV}$  for  $M_S \lesssim 10 \text{ TeV}$ . The plot furthermore shows that for  $M_S \approx 10 \text{ TeV}$  (and the value of  $\tan\beta = 10$  chosen here) a predicted value of  $M_h$  of about  $126 \text{ GeV}$  is obtained even for the case of vanishing mixing in the scalar top sector ( $X_t = 0$ ). Since the predicted value of  $M_h$  grows further with increasing  $M_S$  it becomes apparent that the measured mass of the observed signal, when interpreted as  $M_h$ , can be used (within the current experimental and theoretical uncertainties) to derive an upper bound [very roughly of  $\mathcal{O}(1000 \text{ TeV})$ ] on the mass scale  $M_S$  in the scalar top sector, see also Ref. [26].

In the lower plot of Fig. 1 we compare our result with the one based on the code H3M [10] using a CMSSM scenario with  $m_0 = m_{1/2} = 200 \cdots 15000 \text{ GeV}$ ,  $A_0 = 0$ ,  $\tan\beta = 10$ , and  $\mu > 0$ . The spectra were generated with SOFTSUSY 3.3.10 [27]. The H3M result (blue line) is based on the FEYNHIGGS result up to the two-loop order and incorporates the  $\mathcal{O}(\alpha_t\alpha_s^2)$  corrections containing also nonlogarithmic contributions. Besides our result where FEYNHIGGS is supplemented by the leading and subleading logarithmic corrections to all orders (red line) we also show the expansion of our result up to the three-loop level (green solid line), containing at this level the  $L^3$  and  $L^2$  terms, and the result restricting the contributions at the three-loop level to the ones of  $\mathcal{O}(\alpha_t\alpha_s^2)$  (green dashed). We find that the latter result agrees rather well with H3M, with maximal deviations of  $\mathcal{O}(1 \text{ GeV})$  for  $M_S \lesssim 10 \text{ TeV}$ . The observed deviations can be attributed to the  $L^1$  and  $L^0$  terms contained in H3M, to the various SUSY mass hierarchies taken into account in H3M, and to the different renormalization schemes employed. However, one can see that the three-loop contributions beyond the  $\mathcal{O}(\alpha_t\alpha_s^2)$  terms, i.e., corrections of  $\mathcal{O}(\alpha_t^2\alpha_s, \alpha_t^3)$  that are not contained in H3M, have a sizable effect giving rise to a (downward) shift in  $M_h$  by  $\sim 5 \text{ GeV}$  for  $M_S = 10 \text{ TeV}$ . The corrections beyond the three-loop order yield an additional shift of about  $2 \text{ GeV}$  for  $M_S = 10 \text{ TeV}$ , in accordance with our analysis above. Larger changes are found for  $M_S > 10 \text{ TeV}$ . Also shown is the current experimental value of the Higgs boson mass, demonstrating the relevance of the new corrections with respect to a determination of  $M_S$ .

In summary, we have obtained an improved prediction for the light  $CP$ -even Higgs boson mass in the MSSM by combining the FD result at the one- and two-loop level with an all-order resummation of the leading and subleading logarithmic contributions from the top quark or top squark sector obtained from solving the two-loop RGEs. Particular care has been taken to consistently match these two different types of corrections. The result, providing the most precise prediction for  $M_h$  in the presence of large masses of the scalar partners of the top quark, has been implemented into the public code FEYNHIGGS. We have found a sizable effect of the higher-order logarithmic contributions for  $M_S \equiv \sqrt{m_{\tilde{t}_1} m_{\tilde{t}_2}} \gtrsim 2 \text{ TeV}$ , which grows with increasing  $M_S$ . In comparison with H3M, which contains the  $\mathcal{O}(\alpha_t\alpha_s^2)$  corrections to  $M_h$ , we find that additional three-loop corrections of  $\mathcal{O}(\alpha_t^2\alpha_s, \alpha_t^3)$  and also higher-loop corrections are both important for a precise  $M_h$  prediction, amounting to effects of  $\sim 7 \text{ GeV}$  for  $M_S = 10 \text{ TeV}$  in our example. Finally, we have shown that for sufficiently high  $M_S$  the predicted values of  $M_h$  reach about  $126 \text{ GeV}$  even for vanishing mixing in the scalar top sector. As a consequence, even higher  $M_S$  values are disfavoured by the measured mass value of the Higgs signal.

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