## $\beta$ Decay of <sup>38</sup>Ca: Sensitive test of Isospin Symmetry-Breaking Corrections from Mirror Superallowed $0^+ \rightarrow 0^+$ Transitions

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We report the first branching-ratio measurement of the superallowed  $0^+ \rightarrow 0^+ \beta$  transition from <sup>38</sup>Ca. The result, 0.7728(16), leads to an *ft* value of 3062.3(68) s with a relative precision of ±0.2%. This makes possible a high-precision comparison of the *ft* values for the mirror superallowed transitions, <sup>38</sup>Ca  $\rightarrow$  <sup>38</sup>*m* K and <sup>38*m*</sup>K  $\rightarrow$  <sup>38</sup>Ar, which sensitively tests the isospin symmetry-breaking corrections required to extract  $V_{ud}$ , the up-down quark-mixing element of the Cabibbo-Kobayashi-Maskawa (CKM) matrix, from superallowed  $\beta$  decay. The result supports the corrections currently used and points the way to even tighter constraints on CKM unitarity.

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Superallowed  $0^+ \rightarrow 0^+\beta$  decay is the experimental source of the most precise value for  $V_{ud}$ , the up-down quark-mixing element of the Cabibbo-Kobayashi-Maskawa (CKM) matrix. According to the standard model, this matrix should be unitary, and currently the most exacting test of that expectation is the top-row sum,  $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2$ , which equals 1.00008(56) with the most recent data being used [1]. Thus, unitarity is satisfied with a small enough uncertainty (±0.06%) to place meaningful constraints on some proposed extensions to the standard model [2]. Any reduction in this uncertainty would tighten those constraints.

We have measured for the first time precise branching ratios for the  $\beta$  decay of <sup>38</sup>Ca (see Fig. 1), which includes a superallowed  $0^+ \rightarrow 0^+$  branch not previously characterized. Our result sets a new benchmark for such measurements:  $\pm 0.35\%$  systematic experimental uncertainty. With the corresponding  $Q_{EC}$  value [3] and half-life [4,5] already known, the transition's ft value can now be determined to  $\pm 0.2\%$ . This is the first addition to the set of well-known superallowed transitions [6] in nearly a decade and, being from a  $T_Z = -1$  parent nucleus, it provides the opportunity to make a high-precision comparison of the ft values from a pair of mirror superallowed decays,  ${}^{38}Ca \rightarrow {}^{38m}K$  and  ${}^{38m}$ K  $\rightarrow {}^{38}$ Ar. The ratio of mirror *ft* values is very sensitive to the model used to calculate the small isospin symmetrybreaking corrections that are required to extract  $V_{ud}$  from the data. Since the uncertainty in these corrections contributes significantly to the uncertainty both on  $V_{ud}$  and on the unitarity sum, experimental constraints imposed by mirror *ft*-value ratios can serve to reduce those uncertainties by up to 10%.

Because  $0^+ \rightarrow 0^+ \beta$  decay between T = 1 analog states depends exclusively on the vector part of the weak interaction, conservation of the vector current requires the experimental ft values to be related to a fundamental constant, the vector coupling constant  $G_V$ , which is the same for all such transitions. In practice, the expression for ft includes several small (~1%) correction terms. It is convenient to combine some of these terms with the ft value and define a "corrected"  $\mathcal{F}t$  value [6] as follows:

$$\mathcal{F}t \equiv ft(1+\delta_R')(1+\delta_{NS}-\delta_C) = \frac{K}{2G_V^2(1+\Delta_R^V)}, \quad (1)$$

where  $K/(\hbar c)^6 = 2\pi^3 \hbar \ln 2/(m_e c^2)^5 = 8120.2787(11) \times 10^{-10}$  GeV<sup>-4</sup> s and the isospin-symmetry-breaking correction is denoted by  $\delta_C$ . The transition-independent part of the radiative correction is  $\Delta_R^V$ , while the terms  $\delta_R'$  and  $\delta_{NS}$  comprise the transition-dependent part of the radiative correction, the former being a function only of the decay energy and the *Z* of the daughter nucleus, while the latter, like  $\delta_C$ , depends in its evaluation on the details of nuclear structure. From this equation, it can be seen that each



FIG. 1. Beta-decay scheme of <sup>38</sup>Ca showing the most intense branches. For each level, its  $(J^{\pi}, T)$  is given as well as its energy expressed in keV relative to the <sup>38</sup>K ground state. Branching percentages come from this measurement.

measured transition establishes an individual value for  $G_V$ and, according to conservation of the vector current, all these values—and all the  $\mathcal{F}t$  values themselves—should be identical within uncertainties, regardless of the nuclei involved. This expectation is strongly supported by the data from all 13 well known  $0^+ \rightarrow 0^+$  transitions [6].

Accepting the constancy of  $\mathcal{F}t$ , we can use Eq. (1) to write the ratio of experimental ft values for a pair of mirror superallowed transitions as follows,

$$\frac{ft^a}{ft^b} = 1 + \left(\delta_R^{\prime b} - \delta_R^{\prime a}\right) + \left(\delta_{NS}^b - \delta_{NS}^a\right) - \left(\delta_C^b - \delta_C^a\right), \quad (2)$$

where superscript "a" denotes the decay of the  $T_Z = -1$ parent (<sup>38</sup>Ca  $\rightarrow$ <sup>38m</sup>K in the present case) and "b" denotes the decay of the  $T_Z = 0$  parent (<sup>38m</sup>K  $\rightarrow$  <sup>38</sup>Ar). The advantage offered by Eq. (2) is that the (theoretical) uncertainty on a difference term such as ( $\delta_C^p - \delta_C^a$ ) is significantly less than the uncertainties on  $\delta_C^p$  and  $\delta_C^a$ individually.

To understand this, one must first recognize how  $\delta_C$  and its quoted uncertainty were derived in the first place [7]. The term itself was broken down into two components,  $\delta_{C1}$ and  $\delta_{C2}$ , with the first corresponding to a finite-sized shellmodel calculation typically restricted to one major shell, while the second took account of configurations outside that model space via a calculation of the mismatch between the parent and daughter radial wave functions. The parameters used for the shell-model calculation were taken from the literature, where they had been based on a wide range of independent spectroscopic data from nearby nuclei. In all cases, more than one parameter set was available, so more than one calculated value was obtained for each correction term. The value adopted for  $\delta_{C1}$  was then the average of the results obtained from the different parameter sets, and the quoted "statistical" uncertainty reflected the scatter in those results. If the same approach is used to derive the mirror differences of correction terms  $(\delta_{C1}^b - \delta_{C1}^a)$ , the scatter among the results from different parameter sets is less than the scatter in either  $\delta_{C1}^b$  or  $\delta_{C1}^a$ .

For  $\delta_{C2}$  there is a further source of theoretical uncertainty that arises from the choice of potential used to obtain the parent and daughter radial wave functions. Both Woods-Saxon (WS) and Hartree-Fock (HF) eigenfunctions have been used but there is a consistent difference between their results. Consequently a "systematic" uncertainty corresponding to half the difference has been assigned to  $\delta_{C2}$ , which naturally increases the uncertainty on the derived  $V_{ud}$  and on the unitarity sum [6].

With the statistical (theoretical) uncertainty contribution from  $\delta_C$  reduced in the mirror *ft*-value ratio, Eq. (2) offers the opportunity to use experiment to distinguish cleanly between WS and HF radial wave functions. If one set of calculations were to be convincingly eliminated, then the systematic uncertainty on  $\delta_C$  could also be eliminated and the uncertainty in  $V_{ud}$  reduced.

With current capabilities for producing superallowed  $T_Z = 0$  parent nuclei in sufficient quantity for a highstatistics measurement, there are four mirror pairs that can be completed. These are listed in Table I, where it can be seen that the calculated differences between the WS and HF calculations range from 0.20(2)% for the mass-26 pair to 0.27(6)% for mass 42. Though small, these differences are large enough for experiment to be capable of selecting one calculation over the other.

We produced 444-ms <sup>38</sup>Ca using a 30A-MeV <sup>39</sup>K primary beam from the Texas A&M K500 superconducting cyclotron to initiate the  ${}^{1}H({}^{39}K, 2n){}^{38}Ca$  reaction on a LN<sub>2</sub>cooled hydrogen gas target. The fully stripped ejectiles were separated by their charge-to-mass ratio, q/m, in the MARS recoil separator [8], producing a <sup>38</sup>Ca beam at the focal plane, where the beam composition was monitored by the periodic insertion of a position-sensitive silicon detector. With the detector removed, the <sup>38</sup>Ca beam exited the vacuum system through a 50-µm-thick Kapton window, passed successively through a 0.3-mm-thick BC-404 scintillator and a stack of aluminum degraders, finally stopping in the 76- $\mu$ m-thick aluminized Mylar tape of a fast tapetransport system. The combination of q/m selectivity in MARS and range separation in the degraders provided implanted samples that were 99.7% pure <sup>38</sup>Ca, with the main surviving trace contaminants being <sup>34</sup>Ar, <sup>35</sup>Ar, and <sup>36</sup>K. Approximately 24,000 atoms/s of <sup>38</sup>Ca were implanted in the tape.

During the measurement, each <sup>38</sup>Ca sample was accumulated in the tape for 1.6 s, with its rate of accumulation being measured by the scintillation detector located ahead of the degrader stack. Then the beam was turned off and the tape moved the sample in 200 ms to a shielded counting location 90 cm away, where data were collected for 1.54 s, after which the cycle was repeated. This computer-controlled sequence was repeated continuously for nearly five days.

At the counting location, the sample was positioned precisely between a 1-mm-thick BC-404 scintillator to detect  $\beta^+$  particles, and our specially calibrated 70% HPGe

TABLE I. Calculated  $ft^a/ft^b$  ratios for four doublets with Woods-Saxon (WS) and Hartree-Fock (HF) radial wave functions used to calculate  $\delta_C$ . The uncertainties due to the differences in  $\delta'_R$ ,  $\delta_{NS}$ , and  $\delta_C$  are all incorporated, although the  $\delta_C$  uncertainty predominates.

	$ft^a$	$/ft^b$
Decay pairs, a;b	WS	HF
$^{26}$ Si $\rightarrow^{26m}$ Al; $^{26m}$ Al $\rightarrow^{26}$ Mg	1.00389(26)	1.00189(26)
$^{34}\text{Ar} \rightarrow ^{34}\text{Cl}; \ ^{34}\text{Cl} \rightarrow \ ^{34}\text{S}$	1.00171(26)	0.99971(43)
${}^{38}\text{Ca} \rightarrow {}^{38m}\text{K}; \; {}^{38m}K \rightarrow {}^{38}\text{Ar}$	1.00196(39)	0.99976(43)
$^{42}\text{Ti} \rightarrow ^{42}\text{Sc}; \ ^{42}\text{Sc} \rightarrow \ ^{42}\text{Ca}$	1.00566(65)	1.00296(42)

detector for  $\gamma$  rays. The former was located 3 mm from one side of the tape, while the latter was 15.1 cm away on the other side. We saved  $\beta$ - $\gamma$  coincidences event by event, recording the energy of each  $\beta$  and  $\gamma$  ray, the time difference between their arrival, and the time that the event itself occurred after the beginning of the counting period. For each cycle we also recorded the rate of accumulation of <sup>38</sup>Ca ions in the tape as a function of time, the total number of  $\beta$ - and  $\gamma$ -ray singles, and the output from a laser-ranging device that recorded the distance of the stopped tape from the HPGe detector. From cycle to cycle that distance could change by a few tenths of a millimeter, enough to require a small adjustment to the HPGe detector efficiency. Our recorded spectrum of  $\beta$ -coincident  $\gamma$  rays appears in Fig. 2.

It can be seen from Fig. 1 that all  $\beta$  transitions from <sup>38</sup>Ca populate prompt- $\gamma$ -emitting levels in <sup>38</sup>K, except for the superallowed branch. To obtain the superallowed branching ratio, our approach is first to determine the number of 1568-keV  $\gamma$  rays relative to the total number of positrons emitted from <sup>38</sup>Ca. This establishes the  $\beta$ -branching ratio to the 1<sup>+</sup> state in <sup>38</sup>K at 1698 keV. Next, from the relative intensities of all the other (weaker) observed  $\gamma$ -ray peaks, we determine the total Gamow-Teller  $\beta$ -branching to all 1<sup>+</sup> states. Finally, by subtracting this total from 100%, we arrive at the branching ratio for the superallowed transition.

More specifically, if the  $\gamma$  ray deexciting state *i* in <sup>38</sup>K is denoted by  $\gamma_i$ , then the  $\beta$ -branching ratio,  $R_i$ , for the  $\beta$  transition populating that state can be written

$$R_{i} = \frac{N_{\beta\gamma_{i}}}{N_{\beta}\varepsilon_{\gamma_{i}}}\frac{\varepsilon_{\beta}}{\varepsilon_{\beta_{i}}},\tag{3}$$

where  $N_{\beta\gamma_i}$  is the total number of  $\beta$ - $\gamma$  coincidences in the  $\gamma_i$  peak;  $N_\beta$  is the total number of beta singles corresponding



FIG. 2 (color online). Spectrum of  $\gamma$  rays observed in prompt coincidence with positrons from the decay of <sup>38</sup>Ca. The small peak labeled "511+171" is caused by positron annihilation, from which one 511-keV  $\gamma$  ray sums with a backscattered  $\gamma$  ray from the second 511-keV  $\gamma$  ray. The "511+1568" peak is the result of coincidence summing between a 1568-keV  $\gamma$  ray and annihilation radiation from the positron decay that preceded it.

to <sup>38</sup>Ca  $\beta$  decay;  $\varepsilon_{\gamma_i}$  is the efficiency of the HPGe detector for detecting  $\gamma_i$ ;  $\varepsilon_{\beta_i}$  is the efficiency of the plastic scintillator for detecting the betas that populate state *i*; and  $\varepsilon_{\beta}$  is the average efficiency for detecting the betas from all <sup>38</sup>Ca transitions.

Efficiency calibration.—Equation (3) highlights the importance of having a precise absolute efficiency calibration for the  $\gamma$ -ray detector and a reasonable knowledge of relative efficiencies in the  $\beta$  detector. Our HPGe detector's efficiency has been meticulously calibrated with source measurements and Monte Carlo calculations to  $\pm 0.2\%$ absolute ( $\pm 0.15\%$  relative) between 50 and 1400 keV [9], to  $\pm 0.4\%$  above that, up to 3500 keV [10], and to  $\pm 1.0\%$ up to 5000 keV [11]. For the 1568-keV  $\gamma$  ray, the peak efficiency is  $\varepsilon_{\gamma_i} = 0.1777(4)\%$ . The relative efficiency of the plastic scintillator has been determined as a function of  $\beta$  energy by Monte Carlo calculations, which have been checked by comparison with measurements on sources that emit both betas and conversion electrons [12]. For the  $\beta$  transition feeding the 1568-keV  $\gamma$  ray, the ratio is  $\epsilon_{\beta}/\epsilon_{\beta_i} = 1.0038(4)$ .

Beta singles.—The presence of  $N_{\beta}$  in Eq. (3) makes clear how essential it is to deposit a nearly pure <sup>38</sup>Ca source and to know quantitatively the weak impurities that remain. We identified weak contaminant beams at the MARS focal plane, then calculated their energy loss in the degraders, and thus derived the amount of each that stopped in our tape. From that, we determined that all impurities contributed only 0.6(3)% to the total number of betas recorded. Much more significant is the contribution from the decay of  $^{38m}$ K, the daughter of  $^{38}$ Ca. This nuclide is not present in the beam, but it naturally grows in the collected sample as the <sup>38</sup>Ca decays. Since the half-lives of <sup>38</sup>Ca and <sup>38m</sup>K are well known [4–6], the ratio of their activities could be accurately calculated, based on the measured time dependence of the <sup>38</sup>Ca deposit rate. We determined that the betas from <sup>38</sup>Ca constituted 35.10(2)% of the combined betas from <sup>38</sup>Ca and <sup>38m</sup>K. Finally, a Monte Carlo-calculated correction factor of 0.99957(4) was applied to account for <sup>38</sup>Ca  $\gamma$  rays being detected in the thin  $\beta$  detector.

Beta-coincident 1568-keV gamma rays.— To obtain the  $\beta$ -coincident  $\gamma$ -ray spectrum in Fig. 2, we gated on the prompt peak in the  $\beta$ - $\gamma$  time-difference spectrum and subtracted the random-coincidence background. Our procedure for extracting  $\gamma$ -peak areas was then to use a modified version of GF3, the least-squares peak-fitting program in the RADWARE series [13]. In doing so, we were using the same fitting procedure as was used in the original detector-efficiency calibration [9–11]. To determine  $N_{\beta\gamma_i}$  for the 1568-keV transition, coincident summing with 511-keV annihilation radiation also had to be accounted for. Although the sum peak at 2079 keV could be seen and its area determined, the summing loss from the 1568-keV peak area depends on the total 511-keV response function: peak plus Compton distribution. This response function is,

in principle, displayed in the first 511 keV of the spectrum in Fig. 2 but, in practice, it is distorted by the response to the 328-keV  $\gamma$  ray. We therefore used an off-line source of <sup>22</sup>Na—a positron emitter with no  $\gamma$  ray below 511 keV—to help establish the required response function. The final summing correction factor for the 1568-keV  $\gamma$  ray (including an adjustment for annihilation in flight) is 1.0263(26).

Correction for dead time and pile-up.— Dead time in the  $\beta$ -counting system is small, and affects equally both the numerator and denominator in Eq. (3), so it does not influence our result. However, dead time and pileup do affect the much slower signals from the HPGe detector, and they depend not only on the rate of coincident  $\gamma$  rays, which averaged 94 counts/s, but also on the singles  $\gamma$  rate, which averaged 430 counts/s. Furthermore, the rate during each cycle also decreased with time. Taking account of these effects we arrived at a dead-time/pileup correction factor of 1.01366(11).

Combining these results into Eq. (3), we found the branching ratio for the  $\beta$  transition to the 1698-keV state in  $^{38}$ K to be 0.1949(13). Then, by analyzing the full  $\gamma$ -ray spectrum of Fig. 2, and making provision for weak  $1^+ \rightarrow$  $1^+ \gamma$  transitions, we obtained the total of all Gamow-Teller branches relative to this transition. In this process, account had to be taken of the small electron-capture competition with  $\beta^+$  decay, since the former would not have led to a coincidence in our spectrum. This only has a slight impact on the two lowest-energy (and weakest)  $\beta$  transitions. Our final result for the total Gamow-Teller branching from <sup>38</sup>Ca is 0.2272(16), and this leads to a superallowed branching ratio of  $0.7728 \pm 0.0014_{\text{stat}} \pm 0.0009_{\text{syst}}$  or, with the uncertainties combined in quadrature,  $0.7728 \pm 0.0016$ . The full details of this experiment and its analysis will appear in a subsequent publication [14].

The half-life of <sup>38</sup>Ca is 443.77(35) ms [4,5] and the  $Q_{EC}$  value for its superallowed branch is 6612.12(7) keV [3]. Taking these results with our new value for the branching ratio and correcting for electron capture, we arrive at an ft value for the <sup>38</sup>Ca superallowed branch of  $ft^a = 3062.3(68)$  s. The ft value for the mirror transition from <sup>38m</sup>K is  $ft^b = 3051.5(9)$  s, a value that comes from the 2009 survey [6] updated for a more recent  $Q_{EC}$  measurement reported by Eronen *et al.* [15]. The ratio of the two,  $ft^a/ft^b = 1.0036(22)$ , appears in Fig. 3, where it can be compared with the calculated results from Table I.

Although our experimental result favors the WS calculation, it is not yet definitive. Nevertheless, it clearly points the way to a potential reduction of the uncertainty on  $V_{ud}$ through the elimination of alternatives to the WS-calculated corrections currently used. The lack of precise branchingratio measurements has so far prevented the  $T_Z = -1$ decays of <sup>26</sup>Si, <sup>34</sup>Ar, <sup>38</sup>Ca, and <sup>42</sup>Ti from being fully characterized with high precision. Now that we have demonstrated the capability to make such a measurement on <sup>38</sup>Ca, the other three cases should not be far behind.



FIG. 3. Mirror-pair  $ft^a/ft^b$  values for A = 26, 34, 38 and 42, the four cases currently accessible to high-precision experiment. The black and grey bands connect calculated results that utilize Woods-Saxon (WS) and Hartree-Fock (HF) radial wave functions, respectively (see Table I). Our measured result for the A = 38 mirror pair is shown as the open circle with error bars.

Together, if all four convey a consistent message, they can have a major impact by sensitively discriminating among the models used to calculate the isospin-symmetry-breaking corrections.

The precision that could be quoted here for the superallowed transition benefitted from the fact that the branching ratios actually measured were significantly smaller than the superallowed one, which was derived by subtraction of the measured values from 1. This had a very salutary effect on the relative uncertainty for the superallowed branch, reducing it by a multiplicative factor of 0.3 (= 0.227/0.773)compared to the measured Gamow-Teller branches. As to the other three mirror cases: <sup>42</sup>Ti has no such reduction effect, but for <sup>26</sup>Si the reduction factor is again 0.3, and for <sup>34</sup>Ar it is an impressive 0.06. Currently, there is a 40-yearold measurement [16] of the total Gamow-Teller branches from <sup>34</sup>Ar, which has a relative uncertainty of 4.5%, far higher than we have demonstrated possible today. Even with the reduction factor, the  $ft^a/ft^b$  ratio it provides for A = 34 has a larger uncertainty than our A = 38 result and is not useful for the Fig. 3 comparison with theory. However, with a new branching-ratio measurement employing the techniques described here, a very tight uncertainty should be anticipated for the A = 34 ft-value ratio: With comparable statistics to the <sup>38</sup>Ca measurement reported here, the *ft*-value ratio for the mass-34 mirror pair should have an uncertainty of  $\pm 0.0007$ , three times smaller than the mass-38 uncertainty. We are currently well advanced in making such a measurement.

It may also be noted that the result presented here was limited to a relative uncertainty of 0.21% by the counting statistics acquired during less than five days of accelerator beam time. Ultimately, with additional running time the overall relative uncertainty for this A = 38 case could be reduced towards the limit of 0.12% set by systematic effects.

As a final remark, we point out that results such as these, which are at the limits of experimental precision, benefit enormously from repetition by independent groups. The robustness of the current data set for  $0^+ \rightarrow 0^+$  superallowed  $\beta$  decay can be attributed to the multiple measurements that contribute to each input datum. These branching ratios for the  $T_Z = -1$  parent nuclei should not stand as lingering exceptions.

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