Long-Range Spin Current Driven by Superconducting Phase Difference in a Josephson Junction with Double Layer Ferromagnets

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We theoretically study spin current through ferromagnet (F) in a Josephson junction composed of s-wave superconductors and two layers of ferromagnets. Using quasiclassical theory, we show that the long-range spin current can be driven by the superconducting phase difference without a voltage drop. The origin of this spin current is due to spin-triplet Cooper pairs (STCs) formed by electrons of equal spin, which are induced by the proximity effect inside the F. We find that the spin current carried by the STCs exhibits long-range propagation in the F even where the Josephson charge current is practically zero. We also show that this spin current persists over a remarkably longer distance than the ordinary spin current carried by spin polarized conduction electrons in the F. Our results thus indicate the promising potential of Josephson junctions based on multilayer ferromagnets for spintronics applications with long-range propagating spin current.

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Spin current, a flow of electron spin angular momenta, can be generated in various ferromagnetic materials and plays a key role in spintronics. Spintronics devices have the advantage over conventional electronics in data storage, nonvolatile memory, low power consumption, and high speed processing [1-3]. These spintronics devices are controlled by spin currents, and thus the well-defined spin current is of crucial importance. However, it is well known that the spin current carried by spin polarized electrons in ferromagnets can propagate only for a short distance. This is simply because the propagation distance of the spin current is determined by the spin diffusion length in ferromagnets, which is typically in a range of a few to 10 nm [4,5]. Therefore, the efficient generation of long-range propagating spin current is one of the primary issues in spintronics.

It is notable that the spintronics devices combined with superconductors have been rapidly developed for the last decade. The superconducting spintronics exhibits many fascinating phenomena which are not observed in the nonsuperconducting spintronics [6,7]. The most fundamental element of the superconducting spintronics involves an s-wave superconductor/ferromagnet (S/F) hybrid structure. In a S/F junction, due to the proximity effect, spin-singlet Cooper pairs (SSCs) penetrate into the F. Because of the exchange splitting of the electronic density of states for up and down electrons, the SSC in the F acquires the finite center-of-mass momentum, and the pair amplitude shows a damped oscillatory behavior with the thickness of the F [8]. For application purposes, the most interesting effect in the superconducting spintronics so far is the so-called π state in a S/F/S Josephson junction [8–11]. As opposed to the ordinary Josephson junction, i.e., S/normal metal/S, the π state has the minimum Josephson coupling energy at the superconducting phase difference of π . It has been proposed that the π state can be used for quantum computing [12].

One severe limitation in the superconducting spintronics devices based on the SSCs is, however, that the proximity effect in the S/F junction becomes negligibly small at a distance exceeding the magnetic coherence length ξ_F , which is typically shorter than a few dozen nanometers [10,11,13]. Therefore, the penetration length of the SSC into the F is very short. This implies that any device based on superconducting spintronics has to be smaller than nanometer size.

By contrast, the spin-triplet Cooper pairs (STCs) composed of electrons of equal spin with spin |S| = 1 are superior because of the very long penetration depth into the F in the S/F junction. It is known that not only the SSCs but also the STCs can be induced in the F of the S/Fjunction, for example, when the F contains a magnetic domain wall [14,15], the F has spiral magnetic structure (as in Ho) [16], the junction consists of multilayers of Fs[17,18], or the interface is spin active [19,20]. Although the pair amplitude monotonically decreases with the thickness of the F, in these S/F junctions the STC can propagate into the F over a distance of the order of normal metal coherence length ξ_N , which is typically about several hundred nanometers [21-26]. This is approximately 2 orders of magnitude larger than the propagation distance of the SSC ($\sim \xi_F$). Thus, the proximity effect of the STC is called the long-range proximity effect.

On the one hand, the charge transport of the STCs for these S/F junctions have been extensively studied.

For instance, the Josephson current carried by the STCs has been predicted theoretically [14,19] and confirmed experimentally [22–26]. On the other hand, only limited studies have been reported thus far for the spin transport of the STCs in rather complex S/F junctions containing a magnetic domain wall with spin active interfaces [27,28]. Understanding the spin transport of the STCs remains highly desirable because transport properties in S/F multilayer systems strongly depend on the geometry of the junction as well as the property of F. The main purpose of our study is to propose a simple S/F junction involving neither a magnetic domain wall nor spin active interfaces in which the proximity effect of the STC can induce the long-range propagating spin current.

In this Letter, we study the spin current through the F of a Josephson junction composed of s-wave superconductors and two layers of ferromagnets with no spin active interfaces (Fig. 1). Based on the quasiclassical Green's function theory, we show that the long-range spin current can be driven by the superconducting phase difference (θ) without a voltage drop. The origin of this spin current is due to the STCs in the F induced by the proximity effect. We find that the spin current carried by the STCs can propagate over a much longer distance inside the F, as compared with the ordinary spin current carried by spin polarized conduction electrons, even where the Josephson current is practically zero. Our result therefore indicates that the spin and charge degrees of freedom can in practice be separated in the present S/F junction.

As depicted in Fig. 1, we consider the S/F1/F2/S junction made of two layers of ferromagnets (F1 and F2) attached to s-wave superconducting electrodes. We assume that each layer has good electric contact with the same mean-free path and the same conductivity, and with no spin active interfaces. The spin current in the diffusive limit is evaluated by solving the linearized Usadel equation in each region [8.15,29],

$$i\hbar D\partial_x^2 \hat{f} - i2\hbar |\omega_n| \hat{f} + 2\hat{\Delta} - \operatorname{sgn}(\omega_n) [\vec{h}_{\text{ex}} \cdot \hat{\sigma}, \hat{f}] = \hat{0}, \quad (1)$$

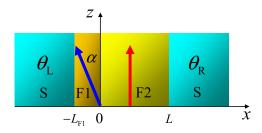


FIG. 1 (color online). Schematic illustration of the S/F1/F2/S junction studied. Two arrows indicate the direction of magnetizations in F1 and F2 layers with thickness L_{F1} and L, respectively. Here, the uniform magnetization is assumed in each F. α is the polar angle of the magnetization in the F1, while the magnetization direction in F2 is fixed along the z direction. The phase difference between two s-wave superconductors is $\theta = \theta_R - \theta_L$.

where D is the diffusion coefficient, ω_n is the fermion Matsubara frequency, $\operatorname{sgn}(A)$ represents the sign of A, and $\hat{\sigma}$ is the Pauli matrix [30]. The anomalous part \hat{f} of the (2×2) quasiclassical Green's function [19] is given by

$$\hat{f} = \begin{pmatrix} f_{\uparrow\uparrow} & f_{\uparrow\downarrow} \\ f_{\downarrow\uparrow} & f_{\downarrow\downarrow} \end{pmatrix} = \begin{pmatrix} -f_{tx} + if_{ty} & f_s + f_{tz} \\ -f_s + f_{tz} & f_{tx} + if_{ty} \end{pmatrix}, \quad (2)$$

where x dependence is implicitly assumed. The s-wave superconducting gap $\hat{\Delta}$ is finite only in the S and assumed to be constant, i.e.,

$$\hat{\Delta} = \begin{cases} \begin{pmatrix} 0 & -\Delta \\ \Delta & 0 \end{pmatrix}, & x < -L_{F1}, x > L \\ \hat{0}, & -L_{F1} < x < L \end{cases}$$
(3)

The exchange field $\vec{h}_{\rm ex}$ due to the ferromagnetic magnetizations in the Fs is described by

$$\vec{h}_{\text{ex}} = \begin{cases} 0, & x < -L_{F1} \\ h_{\text{ex}1}(-\sin\alpha\vec{e}_x + \cos\alpha\vec{e}_z), & -L_{F1} < x < 0 \\ h_{\text{ex}2}\vec{e}_z, & 0 < x < L \\ 0, & x > L \end{cases}$$
(4)

where α is the polar angle of the magnetization in the F1 and $\vec{e}_{x(z)}$ is the unit vector along the x(z) direction (see Fig. 1). Within the quasiclassical theory and the linearized approximation, the spin current polarized in the x spin quantization axis flowing along the x direction is given by

$$j_{S}^{\perp}(x) = \frac{ie\pi DN(0)}{2\beta} \sum_{i\omega_{n}} \text{tr}[\hat{\sigma}^{x}(\hat{f}\partial_{x}\hat{f}^{\dagger} - \hat{f}^{\dagger}\partial_{x}\hat{f})],$$

$$= \frac{2e\pi DN(0)}{\beta} \sum_{i\omega_{n}} \text{Im}(f_{tx}\partial_{x}f_{s}^{*} - f_{s}\partial_{x}f_{tx}^{*}$$

$$+ if_{tz}\partial_{x}f_{ty}^{*} - if_{ty}\partial_{x}f_{tz}^{*}), \tag{5}$$

where N(0) is the density of states (DOS) per unit volume and per electron spin at the Fermi energy [31], $\beta = 1/k_{\rm B}T$, and T is the temperature. In the following, we calculate the spin current flowing through the F2 using the above equation.

The Usadel equation given in Eq. (1) can be solved by imposing appropriate boundary conditions [17,29]. Here, we assume that the superconducting electrodes are much larger than the ferromagnetic layers. Then, obviously, the anomalous Green's function in the right (left) S for $x \to +\infty$ $(-\infty)$ is given by $f_s = |\Delta| e^{i\theta_{\rm R(L)}}/\hbar|\omega_n|$, and $f_{tx} = f_{ty} = 0$, i.e., the solution of the Usadel equation in a bulk S. Solving Eq. (1) with these boundary conditions, the anomalous Green's function \hat{f}^{F2} in the F2 is given by

$$f_s^{F2} = -i \frac{\Delta_R \kappa_{F2} \Phi_{\omega_n}^s}{\hbar |\omega_n| k} \Pi(x) - i \frac{\Delta_L \kappa_{F2} \Phi_{\omega_n}^s}{\hbar |\omega_n| k} \Xi(x), \quad (6)$$

and

$$f_{tx}^{F2} = \frac{\Delta_{R}}{\hbar |\omega_{n}|} \frac{\operatorname{sgn}(\omega_{n}) h_{\text{ex}1}^{x} \kappa_{F1}^{2} \kappa_{F2} L_{F1} \Phi_{\omega_{n}}^{s}}{\hbar D k^{2} (\kappa_{F1} - k) (\kappa_{F1} + k)} e^{-kx} + \frac{\Delta_{L}}{\hbar |\omega_{n}|} \frac{\operatorname{sgn}(\omega_{n}) h_{\text{ex}1}^{x} \kappa_{F1}^{2} \kappa_{F2} L_{F1} \Phi_{\omega_{n}}^{s}}{\hbar D k^{2} (\kappa_{F1} - k) (\kappa_{F1} + k)} \Pi(L) e^{-kx}, \quad (7)$$

where $\Delta_{R(L)} = |\Delta| e^{i\theta_{R(L)}}$

$$\Phi_{\omega_n}^s = \left\{ 2 \frac{\kappa_{F2}}{k} \cosh(\kappa_{F2} L) + \left[1 + \left(\frac{\kappa_{F2}}{k} \right)^2 \right] \sinh(\kappa_{F2} L) \right\}^{-1},$$

and

$$\frac{\Pi(x)}{\Xi(x+L)} = \cosh(\kappa_{F2}x) \pm \frac{k}{\kappa_{F2}} \sinh(\kappa_{F2}x)$$

with $\kappa_{F1(F2)} = \sqrt{\frac{2\hbar|\omega_n| - i2\operatorname{sgn}(\omega_n)h_{\mathrm{ex1}}\cos\alpha(h_{\mathrm{ex2}})}{\hbar D}}$, $k = \sqrt{2|\omega_n|/D}$, and $h_{\mathrm{ex1}}^x = -h_{\mathrm{ex1}}\sin\alpha$. Notice that k^{-1} with n = 0

corresponds to the normal metal coherence length $\xi_{\rm N}=$

 $\sqrt{\frac{\hbar D}{2\pi k_{\rm B}T}}$. It should be noted that $f_{ty}=0$ since the exchange field in the F1 does not have the y component. Equations (6) and (7) are obtained assuming $\kappa_{F1(F2)}L_{F1}$, $kL_{F1}\ll 1$ [32]. Inserting Eqs. (6) and (7) into Eq. (5) and L into x, we obtain the spin current $j_{\rm SC}^{\perp}(L,\theta)=j_{\rm SC}^{\perp}(L)\sin\theta$, flowing through the F2. Here, $j_{\rm SC}^{\perp}(L)=j_{\rm SC1}^{\perp}(L)+j_{\rm SC2}^{\perp}(L)$ is the θ independent part, and $j_{\rm SC1}^{\perp}(L)$ and $j_{\rm SC2}^{\perp}(L)$ are given by

$$j_{\text{SC1(2)}}^{\perp}(L) = -\frac{2e\pi N(0)h_{\text{ex1}}^{x}}{\hbar\beta} \sum_{i\omega_{n}} \text{Im} \left[\frac{|\Delta \kappa_{F2}|^{2}}{\hbar|\omega_{n}|} \frac{\text{sgn}(\omega_{n})}{k} \right] \times |\Phi_{\omega_{n}}^{s}|^{2} \Phi_{1(2)}(L,\omega_{n}) e^{-kL} .$$
(8)

The *L*-dependent functions $\Phi_{1(2)}(L, \omega_n)$ in Eq. (8) are defined by

$$\begin{split} \Phi_{1}(L,\,\omega_{n}) &= \frac{\kappa_{F1}}{k} \frac{\kappa_{F1}L_{F1}}{(\kappa_{F1}-k)(\kappa_{F1}+k)} \bigg[1 + \frac{1}{2} \bigg(1 + \frac{\kappa_{F2}^{*}}{\kappa_{F2}} \bigg) \cosh(2k_{1}^{F2}L) + \frac{1}{2} \bigg(\frac{\kappa_{F2}^{*}}{k} + \frac{k}{\kappa_{F2}} \bigg) \sinh(2k_{1}^{F2}L) \bigg] \\ &- \frac{\kappa_{F1}^{*}}{k} \frac{\kappa_{F1}^{*}L_{F1}}{(\kappa_{F1}^{*}-k)(\kappa_{F1}^{*}+k)} \bigg\{ 1 - \frac{1}{2} \bigg[1 + \bigg(\frac{k}{|\kappa_{F2}|} \bigg)^{2} \bigg] \cosh(2k_{1}^{F2}L) - \text{Re}\bigg(\frac{k}{\kappa_{F2}} \bigg) \sinh(2k_{1}^{F2}L) \bigg\} \end{split} \tag{9}$$

and

$$\Phi_{2}(L, \omega_{n}) = \frac{\kappa_{F1}}{k} \frac{\kappa_{F1}L_{F1}}{2(\kappa_{F1} - k)(\kappa_{F1} + k)} \left[\left(1 - \frac{\kappa_{F2}^{*}}{\kappa_{F2}} \right) \cos(2k_{2}^{F2}L) + i \operatorname{sgn}(\omega_{n}) \left(\frac{\kappa_{F2}^{*}}{k} - \frac{k}{\kappa_{F2}} \right) \sin(2k_{2}^{F2}L) \right] \\
+ \frac{\kappa_{F1}^{*}}{k} \frac{\kappa_{F1}^{*}L_{F1}}{2(\kappa_{F1}^{*} - k)(\kappa_{F1}^{*} + k)} \left[\left[1 - \left(\frac{k}{|\kappa_{F2}|} \right)^{2} \right] \cos(2k_{2}^{F2}L) + 2 \operatorname{sgn}(\omega_{n}) \operatorname{Im}\left(\frac{k}{\kappa_{F2}} \right) \sin(2k_{2}^{F2}L) \right] \tag{10}$$

with

$$k_{1(2)}^{F2} = \sqrt{\frac{\sqrt{(\hbar|\omega_n|)^2 + (h_{\rm ex2})^2} + (-)\hbar|\omega_n|}{\hbar D}}.$$

It should be readily noticed in Eqs. (8)–(10) that $j_{SC1}^{\perp}(L)$ decreases monotonically with L, whereas $j_{SC2}^{\perp}(L)$ shows damped oscillatory behavior. Although Eq. (8) is obtained by products of f_{tx} and f_s [see Eq. (5)], this observation indicates that the main contribution to $j_{SC1}^{\perp}(L)$ [$j_{SC2}^{\perp}(L)$] is the STC (SSC). This is also supported by the fact that $j_{SC1}^{\perp}(L)$ [$j_{SC2}^{\perp}(L)$] is insensitive (sensitive) to h_{ex2} .

The Josephson current flowing through the F2 is similarly calculated. Based on the quasiclassical Green's function theory and the linearized approximation, the Josephson current is given by

$$j_{J}(x) = \frac{i\pi eDN(0)}{2\beta} \sum_{i\omega} tr(\hat{f}\partial_{x}\hat{f}^{\dagger} - \hat{f}^{\dagger}\partial_{x}\hat{f}).$$
 (11)

Substituting into Eq. (11) the solutions of Eq. (1) with the appropriate boundary conditions, we obtain the Josephson current $j_{\rm J}(L,\theta)=j_{\rm c}(L)\sin\theta$ with

$$j_{c}(L) = \frac{2\pi e DN(0)}{\beta} \sum_{i\omega_{n}} \left(\frac{|\Delta \kappa_{F2}|}{\hbar |\omega_{n}|}\right)^{2} \frac{1}{k} \operatorname{Im} \left\{ i \cosh(\kappa_{F2}L) \right\}$$

$$\times \left[1 + \frac{k}{\kappa_{F2}} \tanh(\kappa_{F2}L) \right] + i \cosh(\kappa_{F2}^{*}L)$$

$$\times \left[1 + \frac{\kappa_{F2}^{*}}{k} \tanh(\kappa_{F2}^{*}L) \right] \left\{ |\Phi_{\omega_{n}}^{s}|^{2}.$$

$$(12)$$

Here, $\kappa_{F1(F2)}L_{F1}$, $kL_{F1} \ll 1$ is assumed as in the derivation of the spin current. It should be noted that in the present system the Josephson current is carried solely by the SSCs but not by the STCs. This is because the spin-triplet contribution $\text{Im}(f_{tx}^{F2}\partial_x f_{tx}^{F2^*})$ is exactly zero in Eq. (7). In order for the STCs to contribute the nonzero Josephson current, a Josephson junction with trilayer ferromagnets, for example, is necessary, as pointed out in Ref. [17].

Let us now evaluate numerically the spin current in the F2. For this purpose, the temperature dependence on Δ is assumed to be $\Delta = \Delta_0 \tanh(1.74\sqrt{T_{\rm C}/T}-1)$, where Δ_0 and $T_{\rm C}$ are the superconducting gap at zero temperature and the superconducting transition temperature, respectively [33]. Figure 2 shows a typical result of the spin

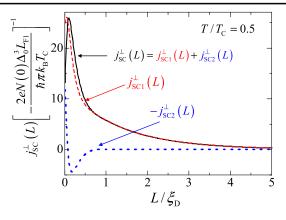


FIG. 2 (color online). Spin current $j_{\rm SC}^{\perp}(L)$ flowing through the F2 as a function of thickness L of the F2. Here, $\xi_{\rm D}$ is the normal metal coherence length $\xi_{\rm N}$ at $T=T_{\rm C}$ and N(0) is the DOS for the F2. The parameters used are $h_{\rm ex1}/\Delta_0=30$, $h_{\rm ex2}/\Delta_0=20$, $\alpha=-\pi/3$, and $T/T_{\rm C}=0.5$. For comparison, $j_{\rm SC1}^{\perp}(L)$ and $j_{\rm SC2}^{\perp}(L)$ [Eq. (8)] are also plotted separately.

current as a function of thickness L of the F2 normalized by the normal metal coherent length ξ_N at $T=T_C$ (denoted by ξ_D). We find in Fig. 2 that the spin current $j_{SC}^{\perp}(L)=j_{SC1}^{\perp}(L)+j_{SC2}^{\perp}(L)$ decreases monotonically with L for $L>\xi_D$ but can propagate over a much longer distance than the Josephson current for the same system (as will be shown below). It is also clear in Fig. 2 that the long-range propagating spin current $j_{SC}^{\perp}(L)$ is originated mostly from $j_{SC1}^{\perp}(L)$, which is carried by the STCs. Instead, the other component $j_{SC2}^{\perp}(L)$ of the spin current shows strongly damped oscillatory behavior with L. This is easily understood because $j_{SC2}^{\perp}(L)$ is carried by the SSCs, which are strongly destroyed in the F by the exchange field. Therefore, the origin of the long-range propagating spin current found here is attributed to the long-range proximity effect of the STC [34].

Next, we compare the L dependence on the spin and Josephson currents for different exchange field $h_{\rm ex2}$ in Fig. 3. These results in Fig. 3 clearly reveal the long-range propagation characteristics of the spin current $j_{SC}^{\perp}(L)$ as compared with the Josephson current $j_c(L)$. Moreover, we find that the spin current $j_{SC}^{\perp}(L)$ is insensitive to the exchange field h_{ex2} . This is because most of the spin current is carried by the STCs (see Fig. 2), which are not destroyed by the exchange field. Instead, as seen in Fig. 3, the Josephson current $j_c(L)$ strongly decreases with increasing h_{ex2} . This strong decrease of $j_c(L)$ with h_{ex2} is due to the pair breaking effect of the SSC by the exchange field. It should be also emphasized in Fig. 3 that the spin current can propagate over a long distance even where the Josephson current is negligibly small for $L/\xi_{\rm D}\gg 1$. This result thus indicates that the spin and charge degrees of freedom can in practice be separated in this system, which is in sharp contrast to the previous studies in Refs. [27,28].

Let us now approximately estimate the propagating distance and the amplitude of the spin current inside the

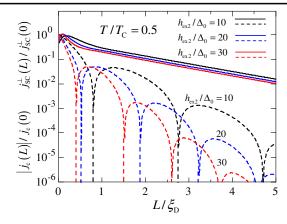


FIG. 3 (color online). Spin current $j_{\rm SC}^{\perp}(L)$ (solid lines) and Josephson current $j_{\rm c}(L)$ (dashed lines) flowing through the F2 as a function of thickness L of the F2 for different $h_{\rm ex2}/\Delta_0$ indicated in the figure. It is apparent that the spin current is insensitive to $h_{\rm ex2}$ in the F2. Here, $\xi_{\rm D}$ is the normal metal coherence length $\xi_{\rm N}$ at $T=T_{\rm C}$. The other parameters used are $h_{\rm ex1}/\Delta_0=30$, $\alpha=-\pi/3$, and $T/T_{\rm C}=0.5$. Note that the oscillatory behavior of the Josephson current is due to the sign change.

F2. In the case of dirty metal, ξ_D is in a range of several dozen to several hundred nanometers [21–26]. As shown in Fig. 3, the spin current can flow inside the F2 up to this length scale. This already implies that this spin current, which is carried mostly by the STCs, can flow much longer than the ordinary spin current carried by spin polarized conduction electrons in the F because the latter disappears at a distance of the spin diffusion length which is about a few nanometers [4,5]. We thus predict that the long-range spin current carried by the STCs can propagate about 10–100 times longer than the ordinary spin current. The amplitude A_{SC} of the long-range spin current is estimated to be of order $2eN(0)\Delta_0^3L_{F1}/(\hbar\pi k_{\rm B}T_{\rm C})$ (see Fig. 2). When we use a typical set of parameters [35], the amplitude $A_{\rm SC}$ is approximately 10^9 A/m², which should be large enough to be observed experimentally.

Finally, we shall comment on how to experimentally detect the spin current in our system. Among several currently available experimental methods, the spin Hall effect (SHE) is the most likely candidate to observe the spin current in the *F*. Indeed, recently, the SHE in a nonmagnetic Josephson junction has been theoretically predicted [36]. Similarly, the SHE is expected in our magnetic Josephson junction. Therefore, we expect that SHE devices [37] using the conventional experimental method [38] can detect and take out the spin current because Cooper pairs are generally scattered by spindependent interactions [36]. The detailed calculations of the SHE will be reported in the future.

In summary, we have theoretically studied the spin current through the *F* in the Josephson junction composed of *s*-wave superconductors and two layers of ferromagnets.

Based on the quasiclassical Green's function theory in the diffusive transport region, we have found that the long-range spin current can be driven by the superconducting phase difference without a voltage drop. The origin of this spin current is due to the STCs induced by the proximity effect in the ferromagnet. We have shown that this spin current can propagate in the ferromagnet over a distance about 10–100 times longer than the ordinary spin current carried by spin polarized electrons, even where the Josephson current is practically zero. Our results clearly demonstrated that Josephson junctions based on multilayer ferromagnets can provide the new spin-dependent transport and suggested the promising potential of these junctions for spintronics applications.

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