Resonant X-ray Diffraction Study of the Strongly Spin-Orbit-Coupled Mott Insulator CaIrO₃

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(Received 19 August 2011; revised manuscript received 23 March 2013; published 24 May 2013)

We performed resonant x-ray diffraction experiments at the L absorption edges for the post-perovskite-type compound $CaIrO_3$ with a $(t_{2g})^5$ electronic configuration. By observing the magnetic signals, we could clearly see that the magnetic structure was a striped ordering with an antiferromagnetic moment along the c axis and that the wave function of a t_{2g} hole is strongly spin-orbit entangled, the $J_{eff}=1/2$ state. The observed spin arrangement is consistent with theoretical work predicting a unique superexchange interaction in the $J_{eff}=1/2$ state and points to the universal importance of the spin-orbit coupling in Ir oxides, independent of the octahedral connectivity and lattice topology. We also propose that non-magnetic resonant scattering is a powerful tool for unraveling an orbital state even in a metallic iridate.

DOI: 10.1103/PhysRevLett.110.217212 PACS numbers: 75.25.Dk, 71.30.+h, 75.50.Ee, 78.70.Ck

There is a new trend toward exploring Mott physics in a system with a strong spin-orbit interaction [1–5]. Theoretical calculations on the Hubbard model revealed that the spin-orbit interaction drives a transition from a correlated metal to an insulator [3–5]. This novel Mott insulating state is actually realized in a layered-perovskite-type compound Sr_2IrO_4 , including Ir^{4+} ions with a $(t_{2g})^5$ electronic configuration [1,2]. In this compound, one hole among t_{2g} manifolds takes a complex wave function with the spin and orbital magnetic moments of 1/3 and 2/3 μ_B , respectively. This so-called $J_{\rm eff} = 1/2$ state is achieved by the superiority of the spin-orbit interaction over the tetragonal crystal field around the 5d transition element.

The superexchange interaction between two Ir⁴⁺ ions in the $J_{\rm eff} = 1/2$ state is theoretically shown to be unique [6]. Whereas an antiferromagnetic Heisenberg interaction $J_1S_i \cdot S_j$ (S_j being the spin at the jth Ir site) is dominant in a corner-shared IrO₆ bond (the Ir-O-Ir bond angle being 180°), it completely vanishes in the edge-shared IrO₆ bond (the Ir-O-Ir bond angle being 90°) owing to an interference effect. Instead, the magnetic interaction of the edge-shared bonds becomes a highly anisotropic and ferromagnetic one $-J_2S_i^zS_i^z$, where the z direction is perpendicular to the plane expanded by the two Ir atoms and two O atoms responsible for the edge-shared bond [see Fig. 1(a)]. This interaction, which is called the quantum compass model, is unique in the sense that the spin anisotropy is produced by the perturbation effect of the Hund's coupling (not the spin-orbit interaction). To test the validity of this theory, it is necessary to elucidate the magnetic structure of an Ir oxide with an edge-sharing octahedral network.

CaIrO₃ forms the post-perovskite structure shown in Fig. 1(a). It is composed of edge-shared (corner-shared) IrO_6 octahedra along the a(c) axis, where each octahedron is compressed along the corner-shared O direction (the z direction) with a bond length ratio of 0.97 [7]. This structure is in stark contrast to Sr₂IrO₄, where elongated IrO₆ octahedra with the bond length ratio 1.04 are connected solely by sharing corners. Hence, CaIrO₃ is an ideal platform for investigating the universal role of spin-orbit coupling in Ir oxides. The compound shows a Mott insulating behavior characterized by the charge gap \sim 0.17 eV and undergoes a transition to a possibly canted antiferromagnetic state at 115 K(= T_N) [8,9]. A deviation from the Curie-Weiss law above $T_{\rm N}$ as well as large coercive fields below T_N suggest an emergence of the spin-orbit interaction.

In this Letter, we investigate the magnetic and orbital structure of CaIrO₃ by using the resonant x-ray diffraction [10] at the L absorption edges. This technique is particularly powerful in compounds with 5d transition metals because the wavelength of the x-ray beam is comparable to the lattice parameters [2,11–13] and the scattering amplitude is enhanced due to a dipole-allowed nature. We also note that neutron scattering measurements are not so easy for the present system with a strong neutron-absorbing element Ir. We clarify that the magnetic structure of CaIrO₃ is a striped-type one and that the $J_{\rm eff}=1/2$ orbital state is realized also in a compressed octahedral

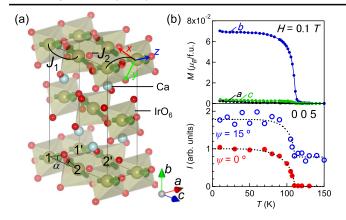


FIG. 1 (color online). (a) Crystal structure of the post-perovskite-type compound CaIrO₃. The solid lines indicate the conventional unit cell, which is twice as large as the primitive unit cell. The magnetic interaction, as well as the magnetic structure determined in this study, are also shown. (b) Temperature (T)dependence of the magnetization (M) at the magnetic field (H)of 0.1 T (see the Supplemental Material [14]) (upper), and the intensity (I) of the $(0\ 0\ 5)$ reflection at $\psi=0$ and $(15)^{\circ}$ (lower).

coordination. We then compare these results with theoretical predictions.

Single crystalline CaIrO₃ was grown by the flux method. CaCO₃, IrO₂, and CaCl₂ with a molar ratio of 1:1:16 was slowly cooled from 1200 °C to 1000 °C for 240 h. Resonant x-ray diffraction measurements were performed at the beam line BL19LXU at SPring-8 (see the Supplemental Material [14] and Ref. [15]). An incident beam was monochromated by a pair of Si (1 1 1) crystals and irradiated on the (0 0 1) surface of the sample, which was mounted in a ⁴He closed-cycle refrigerator installed on a four-circle diffractometer with a vertical scattering plane geometry. The intensities of incident and scattered beams were detected by an ionization chamber and a Si PIN photodiode, respectively. The polarization of the incident beam was perpendicular to the scattering plane (σ) and that of the scattered beam was analyzed by using the (0 0 8) reflection of pyrolytic graphite. The azimuthal angle ψ is defiled as $\psi = 0^{\circ}$ when $\sigma \parallel a$. We also performed similar experiments at the beam line BL02B1 at SPring-8, where we use an imaging plate as a detector [16].

Figure 2 displays the absorption spectra obtained by fluorescence measurements at room temperature (T) as well as the energy dependence of the scattered intensity of the $(0\ 0\ 5)$ reflection at $T=10\ K$ (see the Supplemental Material [14]). At $\psi=0^\circ$ [see Fig. 2(b)], we can observe a strong resonance peak at the L_3 edge $\sim 11.2\ keV$; the intensity is about 0.015% of the fundamental $(0\ 0\ 4)$ reflection. There are fine structures denoted by A and B with an integrated intensity ratio of 1:0.20, the origin of which will be addressed below. The space group of CaIrO₃ is Cmcm with orthorhombic symmetry, where $(0\ 0\ 2n+1)$ reflections are forbidden according to the c-glide reflection. The polarization analysis indicates the π' character of

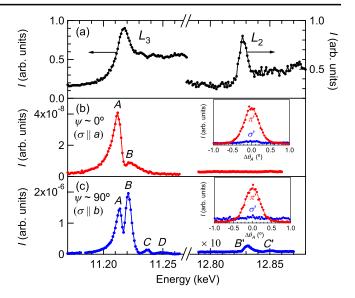


FIG. 2 (color online). (a) X-ray absorption spectra near the Ir L edge for CaIrO₃. (b) The energy dependence of the magnetic scattering intensity (I) of the (0 0 5) reflection at T=10 K and $\psi=0^{\circ}$. The inset shows the polarization analysis of the scattered light at the L_3 edge, where $\Delta\theta_A$ represents the analyzer angle. (c) Same data as (b) except for $\psi=90^{\circ}$. The ATS scattering is dominant in this geometry. Note that the data at the L_2 edge is magnified by 10 for clarity.

the scattered beam $I_{\sigma-\sigma'}/I_{\sigma-\pi'}=3\%$ [see the inset of Fig. 2(b)], which also rules out Thomson scattering as the origin. The T variation of the integrated intensity at 11.212 keV follows well that of the weak ferromagnetic moment [see Fig. 1(b)] (see the Supplemental Material [14]). Considering also that the anisotropic tensor of susceptibility (ATS) scattering is prohibited in this geometry as discussed below, we conclude that the observed reflection originates from a commensurate antiferromagnetic ordering. Importantly, the $(0\ 0\ 5)$ reflection cannot be detected within experimental accuracy at the L_2 edge ~ 12.82 keV, $I_{L_2}/I_{L_3} < 0.3\%$. At the L_3 edge, we also observed magnetic reflections at $(0\ 0\ l)$ with l=1,3,7, and 9.

The observed magnetic reflections at $(0\ 0\ 2n+1)$ are well accounted for by considering an antiparallel arrangement of two Ir spins [labeled 1 and 2 in Fig. 1(a)] in a primitive unit cell. In principle, one can also determine the spin direction experimentally by the ψ dependence of the magnetic signal: $I_{\text{mag}} \propto \sin^2 \psi$, $\cos^2 \psi$, and 1 for the spin direction along the a, b, and c axes, respectively [17]. However, the needlelike crystal morphology along the a axis prevents us from performing such an analysis. We therefore employed the representation analysis, the results of which are summarized in Table I. We note that the crystallographic space group for the magnetic phase below $T_{\rm N}$ has been revealed to be Cmcm by oscillation photographs obtained at BL02B1. Considering the parasitic ferromagnetism along the b axis [see Fig. 1(b)] together

TABLE I. The magnetic structures of the irreducible representations (Γ_i) for the Cmcm space group. M denotes the magnetic point group, where $\underline{1}$ stands for the time-reversal operation. a, b, and c represent the spin directions. AF and F denote the antiferromagnetic and ferromagnetic arrangement of spins at two Ir sites in a unit cell.

Γ_i	М	Generators	а	b	с
Γ_{1g}	mmm	$2_x, 2_y, \bar{1}$	AF	•	
Γ_{2g}	m <u>mm</u>	$2_{x}, \underline{2}_{y}, \bar{1}$	F	•	•
Γ_{3g}	<u>m</u> m <u>m</u>	$\underline{2}_{x}, 2_{y}, \bar{1}$	•	F	AF
Γ_{4g}	<u>mm</u> m	$\underline{2}_x$, $\underline{2}_y$, $\overline{1}$	٠	AF	F

with the second order nature of the magnetic transition [18], we conclude that the Γ_{3g} representation with the antiferromagnetic moments along the c axis is realized. The obtained magnetic structure is schematically drawn in Fig. 1(a). It is a stripe-type order with a parallel alignment along the a axis and an antiparallel alignment along the c axis. This is in harmony with the prediction of the first-principle calculations [19,20]; however, it differs from the proposed ferromagnetic ordering [9]. Also, it markedly contrasts with the checkerboard spin arrangement on the rro_2 plane in rro_2 [2].

We move to the wave function of a t_{2g} hole. When the tetragonal crystal field Δ (> 0 for the compressed octahedron) and the spin-orbit coupling ζ are present, the sixfold degenerated t_{2g} orbitals are split into three doubly degenerated bands (see the Supplemental Material [14]). At the ground state, one hole occupies one of the highest energy orbitals $|\varphi,\pm\rangle=[1/(\sqrt{A^2+2})](A|xy,\pm\rangle\pm|yz,\mp\rangle+i|zx,\mp\rangle$), where $A=(-\zeta-6\Delta+\sqrt{3}\sqrt{3}\zeta^2+4\zeta\Delta+12\Delta^2)/2\zeta$ quantifies the role of the tetragonal crystal field: A=0 when $\Delta/\zeta=\infty$ and A=1 when $\Delta/\zeta=0$; the latter corresponds to the $J_{\rm eff}=1/2$ state. There has been a simple argument that the orbital character can be determined by the edge dependence of the magnetic scattering intensity [2]. We here discuss this issue in more detail on the basis of CaIrO₃ (see the Supplemental Material [14]).

When one electron is virtually excited from the 2p orbitals in a resonant process, the t_{2g} bands are fully occupied; this simplicity enables us to calculate the atomic scattering tensor straightforwardly. By combining contributions of two Ir sites in a striped-ordered state, we obtain the tensor structure amplitude \hat{F} for the $(0\ 0\ 2n+1)$ reflection. Nonzero components in \hat{F} are $F_{ab}=-F_{ba}\equiv iF_{mag}$ and $F_{bc}=F_{cb}\equiv F_{ATS}$ (see the Supplemental Material [14] and Ref. [21]). The F_{mag} term changes its sign by applying the time-reversal operation, and represents the magnetic scattering of the magnetic dipole origin [22]. The F_{ATS} term corresponds to the ATS scattering of the nonmagnetic quadrupole origin. The local principal axes towards the corner-shared O, z, of two Ir sites in a primitive

unit cell are alternately tilted by an angle $\pm \alpha (\sim 23^{\circ})$ from the c axis [see Fig. 1(a)]. This difference in the local anisotropy revives $(0\ 0\ 2n+1)$ reflections, which are pronounced in a resonant condition. The scattering intensity shows the polarization and azimuthal dependence as follows: $I_{\sigma-\sigma'} = 0$ and $I_{\sigma-\pi'} = |\cos\theta\sin\psi F_{ATS} + i\sin\theta F_{mag}|^2$, where θ is the Bragg angle (see the Supplemental Material [14]). These results are totally consistent with those of Lovesey et al. [22]. The scattering intensity also shows a large difference between the L_2 and L_3 edges. We can quantitatively estimate this by referring to calculated results: $F_{\text{mag}} = \pm (\cos \alpha/3) f(A^2 - 2A - 2)/(A^2 + 2)$ and $F_{\text{ATS}} = -(\sin 2\alpha/3) f(A^2 + A - 2)/(A^2 + 2)$ for the L_3 edge; and $F_{\text{mag}} = \mp (\cos \alpha/3) f(A-1)^2/(A^2+2)$ and $F_{ATS} = -(\sin 2\alpha/6) f(A-1)^2/(A^2+2)$ for the L_2 edge (f being a constant value) (see the Supplemental Material [14]). The intensity ratio of the L_2 to L_3 edges are plotted in Fig. 3. One can see that both the magnetic and ATS scattering intensity ratio steeply decrease upon approaching the $J_{\text{eff}} = 1/2$ state (A = 1) and that particularly the ATS scattering ratio with a larger value is more useful to determine the orbital character in a large A region than the magnetic scattering ratio.

We now focus on the spectra at $\psi=90^\circ$ [see Fig. 2(c)], where the ATS scattering becomes largest. In this geometry, the ψ -independent magnetic scattering is overlapping. In order to divide the two contributions, we measured the T dependence of $I_{\sigma-\pi'}$ at $\psi=15^\circ$ for the L_3 edge [see Fig. 1(b)]. Since the ATS scattering is expected to be T independent and the magnetic scattering gradually evolves below $T_{\rm N}$, we can estimate $I_{\rm ATS}/I_{\rm mag}=0.78$ at T=10 K and $\psi=15^\circ$. Combining the knowledge that $I_{\rm ATS}$ is proportional to $\sin^2\psi$, we can deduce $I_{\rm ATS}/I_{\rm mag}=11.6$ at T=10 K and $\psi=90^\circ$, indicating the dominant contribution

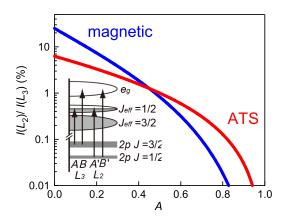


FIG. 3 (color online). The calculated intensity ratio in the magnetic and ATS scattering of the L_2 to L_3 edges as a function of the A coefficient. A=1 corresponds to the $J_{\rm eff}=1/2$ state. Note that the ordinate is scaled logarithmically. The inset shows the energy scheme of the virtual excitations in resonant processes.

from the ATS scattering in this experimental geometry [see Fig. 2(c)]. We also confirmed the π' character of the scattered beam $I_{\sigma-\sigma'}/I_{\sigma-\pi'}=3.9\%$ [see the inset of Fig. 2(c)].

At the L_3 edge, we can discern four fine structures centered at 11.214, 11.221, 11.237, and 11.249 keV with an integrated intensity ratio of 1:0.95:0.06:0.04 [see Fig. 2(c)]. The first and second peaks, the energies of which coincide with inflection points of the absorption spectrum, are also observed at $\psi = 0^{\circ}$ and can be ascribed to the virtual excitation from the 2p J = 3/2 orbitals to the t_{2g} and e_g orbitals, respectively (see the inset of Fig. 3). However, the energy difference of these two peaks 7 eV is unreasonably large in light of conventional knowledge of the crystal field splitting due to the octahedral crystal field; we therefore need further studies to identify the origin. The higher energy structures denoted by C and D are likely related to the 6s and 6p bands.

At the L_2 edge, as in the case of $\psi = 0^{\circ}$, we could not observe any signal at the energy related to t_{2g} orbitals as an intermediate state [see Fig. 2(c)]. We note that a peak structure centered at 12.832 keV corresponds to an inflection point of the absorption spectrum at the higher energy side; hence, the intermediate state is \boldsymbol{e}_{g} orbitals. The intensity ratio at the t_{2g} related energy is estimated to be $I_{L_2}/I_{L_3} < 0.03\%$ by evaluating the variance of the noise at the L_2 edge. Comparing this observation with calculated results shown in Fig. 3 imposes a restriction of A > 0.89. On the other hands, the finite ATS signal at the L_3 edge indicates A < 1. We thus conclude that a t_{2g} hole has a slightly modified $J_{\rm eff}=1/2$ state. We here point out that the ATS scattering intensity is a quite sensitive probe of the wave function. It should be interesting to apply this probe to metallic iridates with no magnetic order [8,23,24], where various exotic quantum states are anticipated [4,25].

Our result that the $J_{\text{eff}} = 1/2$ state is realized in CaIrO₃ enables us to argue the magnetic structure in the framework of the theory by Jackeli and Khaliullin unambiguously [6]. We recall that the theory predicts an antiferromagnetic (ferromagnetic) interaction through the corner-shared (edge-shared) bonds, being consistent with our spin arrangements. Moreover, the weak ferromagnetism along the b axis can be successfully explained by the theory. There are two mechanisms which induce the spin canting. One is that the anisotropic axis z in the quantum compass model is distinguishable between the Ir(1)-Ir(1')and Ir(2)-Ir(2') bonds [see Fig. 1(a)]. Another is the Dzyaloshinskii-Moriya (DM) interaction at the Ir(1)-Ir(2) bond with the DM vector $\mathbf{D}_{1,2} = (D, 0, 0)$ (the site symmetry at the midpoint of the bond being m2m). A mean field treatment of the Hamiltonian including J_1 and J_2 terms, and the DM interaction gives as the most stable spin arrangement the experimentally observed stripe-type order with the spin canted angle equal to the tilting angle of IrO_6 octahedra α . On the other hand, when we assume the antiferromagnetic magnetic moment of $1\mu_B/Ir$, which is the expected value for the completely localized $J_{\rm eff}=1/2$ state, the observed uniform magnetic moment $0.07\mu_{\rm B}/{\rm Ir}$ indicates the canted angle \sim 4°. This is much smaller than α (\sim 23°). The reason for this discrepancy between the theory and experiment is likely related to a reduced spin moment due to quantum fluctuations, a slight deviation from the $J_{\rm eff}=1/2$ state, or the effect of the direct interaction which is not considered in the present analysis.

To summarize, we have investigated the spin and orbital state of the post-perovskite-type compound CaIrO₃ by resonant x-ray diffraction. The orbital of a t_{2g} hole is the $J_{\rm eff}=1/2$ state. This strongly spin-orbit coupled state stabilizes a striped-type magnetic order. We also propose the anisotropic tensor of susceptibility scattering as a tool to investigate the orbital character in a metallic iridate.

We thank Y. Ueda for the use of a single crystalline x-ray diffractometer. The synchrotron radiation experiments were performed at BL19LXU and BL02B1 in SPring-8 with the approval of RIKEN (Proposal No. 20090064) and the Japan Synchrotron Radiation Research Institute (JASRI) (Proposal No. 2009B1200), respectively. This work was supported by Special Coordination Funds for Promoting Science and Technology, Promotion of Environmental Improvement for Independence of Young Researchers; Grant-in-Aid for Scientific Research (B) (No. 20740211); the Grant Program of the Sumitomo Foundation; and the Grant Program of the Murata Science Foundation.

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