s-Wave Collisional Frequency Shift of a Fermion Clock

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We report an *s*-wave collisional frequency shift of an atomic clock based on fermions. In contrast to bosons, the fermion clock shift is insensitive to the population difference of the clock states, set by the first pulse area in Ramsey spectroscopy, θ_1 . The fermion shift instead depends strongly on the second pulse area θ_2 . It allows the shift to be canceled, nominally at $\theta_2 = \pi/2$, but correlations perturb the null to slightly larger θ_2 . The frequency shift is relevant for optical lattice clocks and increases with the spatial inhomogeneity of the clock excitation field, naturally larger at optical frequencies.

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At ultracold temperatures, atom-atom interactions can only occur through *s*-wave collisions. While *s*-wave collisions are allowed for bosons and are the most important limitation to the accuracy of clocks that establish international atomic time [1,2], they are forbidden for identical fermions by the Pauli exclusion principle. Even when dephasing made fermions distinguishable, collision shifts were absent [3]. Thus, ultracold fermions were thought to be immune to *s*-wave collisional frequency shifts (*s*CFS's) making them ideally suited for precision metrology [4–8] and quantum memories [9–12]. However, recent theoretical work predicted that fermions can have an *s*CFS because generally occurring inhomogeneities of excitation fields makes particles distinguishable [13–15].

Here we experimentally observe an s-wave collisional frequency shift of an atomic clock based on a thermal gas of ultracold fermions. Ramsey spectroscopy clearly distinguishes the novel behaviors of the sCFS, via specific dependences on the first and second Ramsey pulse areas, θ_1 and θ_2 . We demonstrate that the shift is insensitive to θ_1 and thereby the difference of the spin populations [13], in stark contrast with the shifts for bosons and the often-used mean-field expression. Instead, the fermion sCFS depends strongly on θ_2 , which reads out the interaction-induced phase shifts of each atom. The shift is canceled if the atoms' phases are detected, on average, with equal sensitivity [13]. Interestingly, we show that correlations in the sample perturb the null of the sCFS to θ_2 slightly greater than $\pi/2$. We explicitly see that the sCFS increases as expected with the inhomogeneity of the clock field, which we characterize independently. The fermion sCFS we observe in the resolved sideband regime is directly analogous to those of optical lattice clocks [6], for which the spatial field inhomogeneity is naturally large at optical frequencies. Recently, the fermion sCFS was simulated using an ⁸⁷Rb Bose gas [16]. They worked, in contrast, with unresolved trap sidebands to directly excite a spin wave and observed the predicted dependence on θ_2 , but an unexpected and unexplained dependence on θ_1 . They elegantly showed a direct link between spin waves and the



FIG. 1 (color online). (a) The *s*-wave scattering length $a_{||}$ in ⁶Li tunes linearly through zero at a bias field of 527.5 G, giving an unambiguous signature to the *s*-wave collisional frequency shift. (b) Rabi spectra in the resolved sideband limit for Raman beams centered on (solid curve) or offset from (dashed curve) the cloud center. (c) Two copropagating Raman beams, focused to a waist comparable to the size of the atomic cloud, provide a spatially inhomogeneous excitation. (d) Measured frequency shifts versus density for several $a_{||}$, demonstrating a sinusoidal dependence characteristic of spin waves. Inset: the dependence at low density gives the linear shift, shown for the four values of $a_{||}$ in (a). (e) Singlet and triplet states for two fermions in different trap states. A spatial inhomogeneity $\Delta\Omega$ couples triplet states to the singlet state, which has collisional interactions $g \propto a_{||}$.

fermion *s*CFS. Here we observe these predicted spin waves in the resolved sideband regime, demonstrating the dependence of the *s*CFS on the correlations of the inhomogeneities of the two Ramsey pulses. The *s*CFS is almost invariably smaller for fermions as compared to bosons, generally nonzero, and vanishes for a pulse area θ_2 near $\pi/2$, which maximizes the clock's stability.

The sCFS of a Fermi gas behaves distinctly differently than that of a Bose gas. The boson sCFS depends on the population difference of the two clocks states, often ascribed to the difference of mean-field energies. Thus, in Ramsey spectroscopy, the boson shift generally depends strongly on the area of the first pulse, which sets the populations for collisions that occur before the second Ramsey pulse. The boson sCFS is insensitive to the area of the second Ramsey pulse. For the fermion sCFS, the often-used mean-field expression does not apply since the shift is in fact insensitive to θ_1 [13]. It instead hinges on the atoms being excited differently so that they are distinguishable. Equally important is that the excitation inhomogeneity of the second Ramsey pulse is correlated with that of the first. The atoms in each colliding pair experience opposite frequency shifts, which cancel on average if the second pulse is uncorrelated with the first. Additionally, even for correlated pulses, if the second pulse reads out the phase shifts of both atoms with the same sensitivity (e.g. $\theta_2 \approx \pi/2$), the sCFS again vanishes [13].

These dependences on θ_1 and θ_2 were not observed in initial reports of Sr and Yb fermion *s*CFS's in optical lattice clocks [17–21]. The Yb shifts were actually *p* wave and not *s* wave [22], apparent because they depended strongly on θ_1 and not θ_2 , an explanation consistent with the Sr observations [18–21]. Here, we additionally tune the *s*-wave scattering length through zero near a Feshbach resonance [23,24] [Fig. 1(a)] to further and conclusively demonstrate that the shifts we detect are *s* wave and not *p* wave.

We use the two lowest-energy hyperfine states of ⁶Li atoms as clock states, denoted as $|\downarrow\rangle$ and $|\uparrow\rangle$. At a bias field near 528 G the interstate s-wave scattering length $a_{1\uparrow} \simeq 0$ [Fig. 1(a)] [23,24]. The gas of $\sim 8 \times 10^4$ atoms has a temperature of 45 μ K, $\approx 1.7 \times$ the Fermi temperature and is confined in an optical dipole trap with trap frequencies $(\nu_x, \nu_y, \nu_z) = (3.8, 7.2, 11.0)$ kHz [Fig. 1(b)]. We drive a two-photon Raman transition between $|\downarrow\rangle$ and $|\uparrow\rangle$ using copropagating laser fields, which are focused to $w_0 \simeq$ 10 μ m, comparable to the thermal cloud radius $w_{\rm th} \simeq$ 6.5 μ m [Fig. 1(c)]. The Rabi frequency is inhomogeneous, giving different trap states different Rabi frequencies $\Omega_{\alpha} \propto$ $\langle \psi_{\alpha} | e^{-2r^2/w_0^2} | \psi_{\alpha} \rangle$. The mean Rabi frequency for the ensemble, $\Omega \simeq 2\pi \times 500$ Hz, is sufficiently below the trapping frequencies ν_{y} and ν_{z} . A smooth turn-on and turn-off of the pulses further suppresses sideband excitations [25].

To measure the *s*CFS, we record Ramsey fringes by shifting the phase of the second pulse with different pulse areas and densities. Figure 1(d) shows the *s*CFS $\Delta \nu$ as a

function of density for $\theta_1 = \frac{\pi}{2}$, $\theta_2 = \frac{3\pi}{4}$, and several $a_{|\uparrow|}$. The apparent pulse areas θ_1 and θ_2 are defined as $\theta_1 = \theta_2 = \pi/2$ giving maximum Ramsey fringe contrast. The mean total density, $\rho = \rho_1 + \rho_1$, is normalized to our canonical maximum of the mean density, $\rho_0 = 8 \times 10^{12} \text{ cm}^{-3}$. With a large $a_{|\uparrow|}$, the density dependence of $\Delta \nu$ is nonlinear at high density (see below). To extract the *s*CFS for a weakly interacting Fermi gas, we vary θ_1 and θ_2 while at low density and small $a_{|\uparrow|}$ [Fig. 1(d) inset], where $\Delta \nu$ is linear in $a_{|\uparrow|}$ and ρ [26].

The predicted sCFS of a weakly interacting, many-body Fermi gas emerges when just two atoms are considered [13]. The singlet-triplet basis for the two-atom wave function [Fig. 1(e)] is helpful because only the singlet state has a collisional interaction g, proportional to $a_{\downarrow\uparrow}$ [27]. The triplet (singlet) states are the product of a symmetric (antisymmetric) spin wave function and an antisymmetric (symmetric) combination of spatial wave functions, trap-eigenstates ψ_{α} and ψ_{β} [Fig. 1(e)]. We initially prepare the atoms in the same internal state, \downarrow , and illuminate them with two spatially inhomogeneous Ramsey pulses [Fig. 1(c)], giving different Rabi frequencies, Ω_{α} and Ω_{β} . Because the atoms in the different trap states have different Rabi frequencies, they become distinguishable, populate a pairwise singlet state, and interact during the interrogation time T between the two Ramsey pulses [28]. For weak interactions, $g_{\alpha\beta}T \ll 1$, the *s*CFS for two or more atoms is [13]

$$\Delta \nu = \frac{\sum_{\text{pairs}} g_{\alpha\beta} T \sin(2\Delta\theta_1) \sin(\Delta\theta_2) \cos(\bar{\theta}_2)}{\pi T \mathcal{A}}, \quad (1)$$

where the sum is over all atom pairs. Here, $\Delta \theta_i = \Delta \Omega \tau_i$ and $\bar{\theta}_i = \bar{\Omega} \tau_i$, where $\tau_{1(2)}$ denotes the first (second) pulse duration, $\bar{\Omega} \equiv (\Omega_{\alpha} + \Omega_{\beta})/2 \gg g_{\alpha\beta}$, and $\Delta \Omega \equiv (\Omega_{\alpha} - \Omega_{\beta})/2$. For weak interactions, the Ramsey fringe amplitude \mathcal{A} is given by $\sin(\theta_1)\sin(\theta_2)$ summed over all atoms.

In Fig. 2(a) we plot the prediction from Eq. (1) for a thermal gas along with the observed linear shift $\Delta\nu$ at $\rho_0 = 8 \times 10^{12}$ cm⁻³, $a_{\downarrow\uparrow} = 4a_0$, and $\Delta\Omega/\Omega = 0.20$ [29]. Two independent methods determine $\Delta\Omega$ and are described below. Fitting the amplitude of the prediction to the observed shifts determines $a_{\downarrow\uparrow}$. Versus *B*, with an absolute atom number uncertainty $\approx 25\%$, $\Delta\nu$ gives $a_{\downarrow\uparrow} = [3.5(9)a_0/\text{G}]$ [*B* – 527.61(7)\text{G}] [Fig. 1(a)], in agreement with Refs. [23,24].

The *s*CFS given by Eq. (1) vanishes if either $\Delta\theta_1$ or $\Delta\theta_2$ is zero. Physically, $\Delta\theta_1$ must be nonzero to make the atoms distinguishable and populate the singlet state. During the interrogation time *T*, the singlet state acquires a collisional phase shift exp $[2ig_{\alpha\beta}T]$ and the second pulse must also be inhomogeneous so that this phase shift is read out. For $\bar{\theta}_2 = \pi/2$ [Figs. 2(a)–2(c) and 2(e)], $\cos(\bar{\theta}_2)$ goes to 0 so



FIG. 2 (color online). The *s*-wave collisional frequency shift of ⁶Li fermions versus Ramsey pulse areas θ_1 and θ_2 . (a) For $a_{||} = 4a_0$ (B = 528.7 G), the measured linear shift $\Delta \nu$ at $\rho_0 = 8 \times 10^{12}$ cm⁻³ is plotted along with Eq. (1) for a thermal gas with $\Delta \Omega / \Omega = 0.2$, determined independently. Two surface cuts, green (red) solid curve and points, show the predicted and measured shift as θ_1 (θ_2) is varied with $\theta_2(\theta_1) = \frac{\pi}{2}$. The blue solid curve and points for $\theta_1 = \theta_2$ shows the usual case of equal pulse areas. (b) and (c) are as in (a) with $a_{||} \approx 0$ (B = 527.5 G) and $a_{||} = -7a_0$ (B = 525.5 G). The shift does vary strongly with θ_2 , going to 0 near $\theta_2 = \pi/2$. (d)–(g) The collisional frequency shift for $a_{||} = -7a_0$ for the indicated surface cuts in (c). Also shown are fits to the model for just two atoms (dotted curve), the model for many atoms (dashed curve), and the numerically integrated model for many atoms (solid curve), which includes the pulse shapes and Raman light shifts. The shift is not proportional to the difference of partial densities, which would imply a strong dependence on θ_1 (gray dot-dashed mean-field curves).

that the *s*CFS vanishes, even for inhomogeneous clock fields, because the opposite phase shifts of each atom are read out with equal sensitivities [13].

It is remarkable that $\Delta \nu$ in Eq. (1) is insensitive to $\bar{\theta}_1$ [Figs. 2(a), 2(c), and 2(d)]. The amplitude in the singlet state (which acquires the collisional phase shift) depends only on $\Delta \theta_1$ and not on $\bar{\theta}_1$. The *s*CFS is in general nonzero for $\bar{\theta}_1 = \pi/2$, for which the population difference $N_{\uparrow} - N_{\downarrow} = -2N \cos(\bar{\theta}_1) = 0$ during the interrogation time *T*. This is in stark contrast with the widely used mean-field expression [gray dot-dashed curves in Figs. 2(d)-2(g)] [17–20,30], where the *s*CFS $\Delta \nu$ vanishes at $N_{\uparrow} - N_{\downarrow} = 0$ and disagrees with an interpretation of Rabi spectroscopy of a Fermi gas [14]. A key result of this work is the experimental measurement of the fermion *s*CFS, including an insensitivity of the *s*CFS to $\bar{\theta}_1$.

Tuning a_{\parallel} to 0 in Fig. 2(b) gives no *s*CFS as expected. With $a_{\parallel \uparrow} = -7a_0$, the *s*CFS in Figs. 2(c)–2(g) has the opposite sign of Fig. 2(a). The fit to Eq. (1) [dashed curves in Figs. 2(d)–2(g)] for an ensemble with $a_{\parallel \uparrow} = -7a_0$ is also shown, along with the model for just two atoms (dotted curves) with an effective g chosen to give the same $\Delta \nu$ for $\theta_{1,2} \rightarrow 0$. Equation (1) uses a short-pulse approximation where only interactions during the interrogation time are considered. In the experiment, the atoms also acquire a phase shift due to interactions during the pulses. Further, the Raman beams produce a small time-dependent light shift [31] of the transition during each pulse. We include these effects and the pulse shapes in a numerically integrated Monte Carlo simulation [solid curves in Figs. 2(d)-2(g)]. All of these give small corrections, and the interactions during the pulses are the largest of these.

We highlight that correlations between $g_{\alpha\beta}$ and $\theta_{\alpha,\beta}$ shift the pulse area where $\Delta \nu = 0$ from $\theta_2 = \pi/2$ to $\theta_2 =$ 0.51π in Fig. 2(e). Here, the average of $\cos\bar{\theta}_2$ crosses zero at $\theta_2 = 0.56\pi$ because the Ramsey fringe contrast has bigger contributions from large θ_{α} . However, atoms in low vibrational states have large $\bar{\theta}_2$ and also large $g_{\alpha\beta}$ since they reside in the high density region of the trap. This pushes the zero crossing of $\langle g_{\alpha\beta} \cos\bar{\theta}_2 \rangle$ to smaller θ_2 . Finally, because trap states that have a large overlap with each other have similar overlaps with the clock field, $\Delta\theta_1 \Delta\theta_2$ and $g_{\alpha\beta}$ are anticorrelated and this pushes the zero crossing to larger θ_2 . These perturbations are quite general, for both amplitude variations and wave front tilts, and in detail depend on the excitation inhomogeneity and trap geometry.

With a large $a_{\downarrow\uparrow}$, the density dependence of $\Delta\nu$ is nonlinear at high density [Fig. 1(d)] and reverses sign once the acquired phase shift during the interrogation time *T* exceeds π . For just two atoms, Eq. (1) has a sinusoidal dependence $\sin(2gT)$, instead of a linear dependence on gT, and this gives the observed sinusoidal dependence on density, where the effective *g* for many atoms is proportional to density [13,16]. As in Ref. [16], but here in the resolved-sideband limit, the sinusoidal dependence is a



FIG. 3 (color online). (a) The measured *s*CFS grows with increasing inhomogeneity $\Delta\Omega$, independently measured with Rabi oscillations (triangles) as in (b) and the frequency shift of the $|\uparrow\rangle \rightarrow |3\rangle$ rf transition (diamonds) as in (c). The scattering length $a_{|\uparrow}$ is $-7a_0$ and the dashed curve shows the expected quadratic dependence. (b) Decay of Rabi oscillations for Raman beams with waists comparable to the radius of the thermal cloud. A fit of the Rabi oscillations of a trapped thermal gas determines $\Delta\Omega$. (c) We use the collisional frequency shift of the $|\uparrow\rangle \rightarrow |3\rangle$ transition, with a spatially homogeneous rf Rabi pulse, to measure the singlet state populated by driving $|\downarrow\rangle \rightarrow |\uparrow\rangle$. The shift increases as expected with the inhomogeneity of the $|\downarrow\rangle \rightarrow |\uparrow\rangle$ Raman field and, via a model, also yields $\Delta\Omega$.

manifestation of a spin wave, although we do not spatially resolve the oscillating spin populations.

Figure 3(a) shows that the sCFS increases quadratically with the spatial inhomogeneity. Here, we vary the Raman beam waist, measuring the sCFS versus $\theta_{1,2}$ with $a_{\downarrow\uparrow} =$ $-7a_0$. The fitted surface, in the limit of small $\theta_{1,2}$, gives $\Delta \nu$, which is plotted versus $\Delta \Omega / \Omega$. We experimentally determine $\Delta \Omega$ in two independent ways. First, we drive the Raman transition and fit the decaying Rabi oscillations between $|\downarrow\rangle$ and $|\uparrow\rangle$ [Fig. 3(b)]. The circles, squares, and diamonds show the Rabi oscillations for increasing beam waists. We model the Rabi oscillations of a thermal distribution of trap states ψ_{α} with different Rabi frequencies Ω_{α} . Second, we probe the interactions with rf spectroscopy to a third internal state $|3\rangle$ [3,5,32]. A Raman pulse of area θ_1 is first applied to a sample prepared in $|\downarrow\rangle$ to populate pairwise singlet states, producing an interaction shift. This shift is observed with Rabi spectroscopy on the $|\uparrow\rangle \rightarrow |3\rangle$ transition. The interaction shift $\Delta
u_{\uparrow 3}$ is proportional to $\sum_{\alpha \neq \beta} (g_{\alpha\beta,\downarrow\uparrow} - g_{\alpha\beta,\uparrow3}) \sin^2 \Delta \theta_{1,\alpha\beta}.$ It increases with the singlet state population, $\sin^2 \Delta \theta_{1,\alpha\beta}$, which increases as $\Delta \Omega$ increases. The circles, squares, and diamonds in Fig. 3(c)show the measured shift versus θ_1 , normalized to the shift of a fully decohered gas. The fully decohered gas is prepared by optical pumping to create an equal $\downarrow\uparrow$ mixture. The curves are single-parameter fits of $\Delta\Omega/\Omega$. The dashed curve in Fig. 3(a) shows the expected quadratic dependence of $\Delta\nu$ on $\Delta\Omega$.

Our experiment elucidates the novel behaviors of the collisional frequency shifts of clocks based on fermions. For both Ramsey and Rabi spectroscopy, the spatial inhomogeneities of the clock field make fermions distinguishable, producing a shift if the inhomogeneities of the excitation and the readout of the phases of the clock coherences are correlated. Optical lattice clocks are naturally susceptible to these shifts since optical-frequency clock fields have fast spatial variations. Wave front curvatures or small tilts of the clock-field phase fronts lead to different Rabi frequencies in a gas. When the *p*-wave collisions are not frozen out and the scattering lengths are favorable, both the *p*- and *s*-wave collisional frequency shifts can be independently canceled by adjusting θ_1 and θ_2 around $\pi/2$. We note that correlations in the sample generally perturb the zero crossing of the s-wave collisional frequency shift to a θ_2 slightly different from $\pi/2$. The shifts for fermions are naturally much smaller than those for clocks based on bosons, demonstrating that ultracold fermions are excellent candidates for a variety of precision experiments.

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- [25] For each θ_1 , θ_2 , we adjust the interrogation time *T* to keep a constant Ramsey fringe linewidth, with an effective interrogation time of 2.7 ms. The Raman $\pi/2$ pulse duration is 450 μ s. To always resolve the trap sidebands, we change the pulse area for $\theta > \pi/2$ ($\theta < \pi/2$) by increasing (decreasing) the duration (amplitude) of the Raman beam pulse and use a smooth turn-on and turnoff, which are 37.5 μ s long. For $\theta < \pi/2$, the total optical intensity is maintained by adding an optical field offresonant with the two-photon Raman transition.
- [26] To vary the density without changing the temperature, we vary the rf pulse area of $|\downarrow\rangle \rightarrow |\uparrow\rangle$, perform an adiabatic passage of $|\uparrow\rangle \rightarrow |3\rangle$, and clear $|3\rangle$ with a laser pulse. We do this at 568.8 G where $a_{\downarrow3} \approx 0$ and end with a $|3\rangle \rightarrow |\uparrow\rangle$ adiabatic passage so no atoms are left in $|3\rangle$.
- [27] We consider a contact interaction $V(\mathbf{r}_1, \mathbf{r}_2) = \frac{4\pi\hbar^2 a_{||}}{m} \delta(\mathbf{r}_1 \mathbf{r}_2)$. Here, $g_{\alpha\beta} = \frac{2\hbar a_{||}}{m} \int \psi_{\alpha}^2(\mathbf{r}) \psi_{\beta}^2(\mathbf{r}) dV$. [28] We use scattering lengths much smaller than the deBroglie
- [28] We use scattering lengths much smaller than the deBroglie wavelength, $2000a_0$, so that trap state changing (lateral) collisions can be neglected.
- [29] We define $\Delta\Omega^2 \equiv \langle g_{\alpha\beta}\Delta\Omega^2_{\alpha\beta}\rangle/\langle g_{\alpha\beta}\rangle$, where $\langle \rangle$ denotes an ensemble average over all dom pairs in states ψ_{α} and ψ_{β} . Then, for small $\Delta\Omega$ and Ω , $\Delta\nu$ is $(g/\pi)(\Delta\Omega/\Omega)^2$ for two atoms and $[(N-1)\langle g_{\alpha\beta}\rangle/\pi](\Delta\Omega/\Omega)^2$ for N atoms. Here, Ω is the average Rabi frequency. In the context of the Rabi flopping in Fig. 3(b), a reasonable definition of $\Delta\Omega^2$ is simply $\langle\Delta\Omega^2_{\alpha\beta}\rangle$, but this neglects important correlations between $\Delta\Omega^2_{\alpha\beta}$ and $g_{\alpha\beta}$.
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