Decoherence of a Single-Ion Qubit Immersed in a Spin-Polarized Atomic Bath

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(Received 22 January 2013; published 19 April 2013)

We report on the immersion of a spin qubit encoded in a single trapped ion into a spin-polarized neutral atom environment, which possesses both continuous (motional) and discrete (spin) degrees of freedom. The environment offers the possibility of a precise microscopic description, which allows us to understand dynamics and decoherence from first principles. We observe the spin dynamics of the qubit and measure the decoherence times $(T_1$ and $T_2)$, which are determined by the spin-exchange interaction as well as by an unexpectedly strong spin-nonconserving coupling mechanism.

DOI: [10.1103/PhysRevLett.110.160402](http://dx.doi.org/10.1103/PhysRevLett.110.160402) PACS numbers: 03.65.Yz, 03.67.Ac, 37.10.Ty

A spin- $1/2$ system represents the most fundamental quantum mechanical object. Its spin dynamics and decoherence when interacting with an environment determine its potential use as a qubit and are responsible for a multitude of impurity effects encountered in the solid state. While an extensive amount of theoretical work on this problem exists (for reviews see Refs. [[1](#page-3-0)[,2\]](#page-3-1)), experiments with well-controlled and adjustable environments are scarce. The necessary sensitivity to probe single spins, ideally with a single-shot readout, is often incompatible with the ability to adjust the properties of the environment. Among the few examples of controlled decoherence processes are the quantum measurement process [[3](#page-3-2)], the decoherence of motional quantum states of trapped ions by noisy classical electric fields [[4\]](#page-3-3), and the effects of spontaneous emission [[5](#page-3-4)[–7](#page-3-5)]. These are related to spin-boson physics, where the environment is formed by a set of harmonic oscillator modes [\[1](#page-3-0)]. On the contrary, the decoherence of a localized spin impurity inside an environment of other spins lies at the heart of the so-called central-spin problem [[2](#page-3-1)]. Here, the occurring decoherence mechanisms are different from spin-boson physics since the spectrum of the bath is discrete and spin-spin or spin-orbit interactions play a role. The central-spin model has been often applied as a simplified and approximate description of the interaction of semiconductor quantum dots [\[8\]](#page-3-6) and color centers in solids [\[9](#page-3-7)] with their environment.

Here we investigate the model system of a single localized spin $1/2$ coupled to a spin-polarized environment of tunable density. Specifically, we embed a trapped single Yb^+ ion, initially laser cooled to Doppler temperature, into a spin-polarized ultracold neutral bath of ⁸⁷Rb atoms and study the resulting decoherence of the ion's internal spin state. We observe an intricate decoherence mechanism, which is spin nonconserving and involves the coupling of the orbital degrees of freedom with the spin degrees of freedom. We measure the longitudinal (T_1) and the transverse (T_2) coherence times, also with respect to the energy separation, and identify the time scales for Zeeman- and hyperfine-state relaxation.

The interaction between an ion and a neutral atom is, to leading order, via a central potential $V_\sigma(r)$, where r is the internuclear separation. Asymptotically $(r \rightarrow \infty)$, the central potential is determined by the polarization interaction $-C_4/2r^4$ and is spin independent [\[10–](#page-3-8)[12\]](#page-3-9). For small r, collisions in the electronic singlet and triplet channels exhibit different potentials $V_S(r)$ and $V_T(r)$ giving rise to a spin-exchange interaction, which is spin conserving for the total spin of the atom and ion. Langevin collisions in the central potential, i.e., collisions with energies above the centrifugal barrier, occur at an energy-independent rate $\gamma_L = 2\pi\sqrt{C_4/\mu}n_a$, where μ is the reduced mass and n_a
is the neutral atom density. In our experiment we have is the neutral atom density. In our experiment we have $\gamma_L/n_a = 2.1 \times 10^{-15} \text{ m}^3/\text{s}$ and we use typical densities
of $n_a = 10^{18} \text{ m}^{-3}$ Even though the Langevin rate is sigof $n_a = 10^{18} \text{ m}^{-3}$. Even though the Langevin rate is significantly smaller than the total collision rate γ_c (see the Supplemental Material [[13\]](#page-3-10)), in previous experiments the Langevin process has dominated cold inelastic ion-atom collisions [\[14–](#page-3-11)[19](#page-3-12)]. For spin-dependent processes additionally the anisotropic magnetic dipole-dipole interaction and the second-order spin-orbit coupling can play important roles, the latter, in particular, for heavy atoms [[20](#page-3-13)]. They induce coupling between the spin and the orbital motion and break the conservation of the total electronic spin. In this work we determine which of these mechanisms lead to spin decoherence.

First, we study spin relaxation of the Zeeman qubit of the isotope 174Yb^+ , which represents an ideal two-level system (see Fig. [1](#page-1-0)). We prepare the $|m_J = 1/2 \rangle \equiv |\uparrow\rangle$ or the $|m_J = -1/2 \rangle \equiv |\downarrow\rangle$ qubit state in an adjustable magnetic field inside the neutral atom cloud. During the interaction period, the ion undergoes binary collisions with the atoms, and we normalize interaction times by the Langevin time constant $t_L = 1/\gamma_L$. We detect the population of the oubit state by electronic shelving and determining the qubit state by electronic shelving and determining the probability of the ion being in a bright (p_{Bright}) or dark

FIG. 1 (color online). (a) Illustration of the trapped single ion spin coupled to a spin-polarized neutral atom cloud. (b) Level structure of the Yb^+ electronic ground state in a weak magnetic field. To implement the spin- $1/2$ system, we use either the Zeeman qubit $|m_J = \pm 1/2\rangle$ in the isotope ¹⁷⁴Yb⁺ or the magnetic field insensitive hyperfine qubit $|F = 0, m_F = 0\rangle$ and $|1, 0\rangle$ in the isotope 171Yb^+ . (c) The cloud of neutral 87Rb atoms is prepared in one of the four atomic spin states prepared in one of the four atomic $|F = 2, m_F = 2\rangle_a, |2, -2\rangle_a, |1, 1\rangle_a$ or $|1, -1\rangle_a$.

(p_{Dark}) state using light scattering on the $S_{1/2} - P_{1/2}$ transition (see Supplemental Material [\[13\]](#page-3-10)). Measurements of the T_1 time are performed for varying density and neutral atom spin composition. The data for the two different bath configurations $|F = 1, m_F = 1\rangle_a$ and $|2, 2\rangle_a$ are shown in Figs. $2(a)$ and $2(b)$, respectively. We find that the initially polarized ion spin relaxes into a mixed steady state within a few Langevin collision times. This result cannot be understood from spin-exchange collisions, for which, for example, the doubly spin-polarized combination $| \uparrow \rangle$ and $|2, 2\rangle$ _a is protected from spin-changing collisions due to spin conservation. From our steady-state population data for atoms in the $|2, 2\rangle_a$ state and the measured $T_1 =$ $(2.50 \pm 0.39)t_L$, we determine the spin-exchange and spin-relaxation rates to be $\gamma_{\text{LSE}} = (0.22 \pm 0.03)/T_1$ and $\gamma_{\text{LSE}} = \gamma_{\text{LSE}} = (0.39 \pm 0.02)/T_1$ (see Supplemental $\gamma_{\text{LSR}} = \gamma_{\text{LSR}} = (0.39 \pm 0.02)/T_1$ (see Supplemental
Material [13]) An analogous result holds for the $(2, -2)$ Material [\[13\]](#page-3-10)). An analogous result holds for the $|2, -2\rangle_a$ state. Notably, the measured spin-relaxing collision rate is

FIG. 2 (color online). Spin-relaxation in the 174Yb^+ Zeeman qubit. The probability p_{Bright} of the ion to occupy the bright $|\uparrow\rangle$ state after preparation in $| \uparrow \rangle$ (full symbols) or $| \downarrow \rangle$ (open symbols) in a bath of (a) $|1, 1\rangle_a$ or (b) $|2, 2\rangle_a$ atoms. Error bars denote 1 standard deviation uncertainty intervals resulting from approximately 3000 measurements per spin state. (c) The equilibrium spin states (corrected for detection efficiencies) for all four atomic bath configurations $|2, -2\rangle_a$, $|1, -1\rangle_a$, $|1, 1\rangle_a$, and $|2, 2\rangle_a$.

approximately 5 orders of magnitude higher than the charge-exchange collision rate $[16,21]$ $[16,21]$ $[16,21]$ $[16,21]$ $[16,21]$. All measurements were performed at an energy splitting of the ion Zeeman qubit of 37.5 MHz; however, the same behavior was found for different Zeeman splittings in the range from 0.39 to 139 MHz in a $|1, 1\rangle$ _a environment.

The observed spin dynamics of the Yb^+ ion in a spin polarized cloud of 87Rb atoms is inconsistent with the picture of dominant spin exchange and negligible spin relaxation, that has previously been reported in $He⁺$ + Cs collisions [[22](#page-3-16)], in neutral atom-atom collisions even at room temperature [\[23\]](#page-3-17), and in semiconductor quantum dots [[24](#page-3-18)]. Moreover, investigations in both ultracold gases [\[25\]](#page-3-19) and optically pumped vapor cells [[26\]](#page-3-20) have revealed that even for heavy alkali-metal collisions the hierarchy $\gamma_c \approx \gamma_{SE} \gg \gamma_{SR}$ is fulfilled. In such a situation, the domi-
nant spin exchange interaction leads to a steady state near a nant spin-exchange interaction leads to a steady state near a perfect polarization of spin and environment both when the environment is initially polarized but the spin is unpolarized and when the single spin is continuously pumped but the environment is initially unpolarized. The strong spin relaxation observed here could be aided by a level crossing of both the incoming singlet $A^1\Sigma^+$ and triplet $a^3\Sigma^+$ channels to a 3 H channel at short internuclear separation
[27.28] which notentially provides a mechanism for [\[27](#page-3-21)[,28\]](#page-3-22), which potentially provides a mechanism for spin-orbit coupling. A conceptually similar competition between spin-orbit induced relaxation and spin-conserving processes seems to play a role in the ultrafast relaxation of magnetization in ferromagnets [[29](#page-3-23)].

The dependence of the steady-state spin population of the ion on the atomic bath configuration has been determined for the $|2, -2\rangle_a$, $|1, -1\rangle_a$, $|1, 1\rangle_a$, and $|2, 2\rangle_a$ states and is shown in Fig. $2(c)$. The steady-state values for the $|1, -1\rangle_a$ and $|1, 1\rangle_a$ states can be qualitatively understood considering their projections into the electron singlet and triplet bases and taking into account that spin-exchange collisions leading to a transition of the atomic hyperfine state from the $|F = 1\rangle_a$ to the $|F = 2\rangle_a$ manifold are energetically suppressed.

Next, we study the spin relaxation of the magnetic field insensitive hyperfine qubit of the electronic ground state of 171Yb^+ 171Yb^+ (see Fig. 1 and the Supplemental Material [\[13](#page-3-10)]). The spin detection is performed by resonant light scattering on the $S_{1/2}|F = 1\rangle \rightarrow P_{1/2}|F = 0\rangle$ transition and measuring the probability $p_{\text{Bright}}(p_{\text{Dark}})$ of the ion being in a bright (dark) state $|F = 1\rangle$ ($|F = 0\rangle$). If the neutral atoms are prepared in the $|1, -1\rangle$ _a state [see Fig. [3\(a\)\]](#page-2-0), the ion relaxes towards the spin ground state, as expected for amplitude decoherence, and we observe an exponential decay with a time constant T_1 of a few Langevin collision times.

In contrast, if the neutral atoms are prepared in the $|2, 2\rangle_a$ state [Fig. [3\(b\)\]](#page-2-0), the steady-state probability to measure the ion spin in the $|F = 1\rangle$ manifold is 0.16(1). We interpret this nonzero steady-state value as resulting from the intake of hyperfine energy from the atoms.

FIG. 3 (color online). Hyperfine spin relaxation in $^{171}Yb^+$. (a) The probability p_{Bright} after preparation in the $|1, 0\rangle$ (full symbols) or the $|0, 0\rangle$ (open symbols) state vs the interaction time for atoms in the $|1, -1\rangle$ _a state. Error bars denote 1 standard deviation uncertainty intervals resulting from a total of 5000 measurements. The fit values at $t = 0$ are limited by detection errors. (b) Similar data for collisions with $87Rb$ atoms in the $|2, 2\rangle$ _a state and a total of 19 000 measurements. (c)–(e) Zeemanresolved detection within the $F = 1$ manifold after preparation in $|1, 0\rangle$ (atoms in $|2, 2\rangle$ _a) with 1200 measurements per Zeeman state. The measurements are performed by applying resonant π pulses, exchanging the population of the dark state $|0, 0\rangle$ with $|1, -1\rangle$, $|1, 0\rangle$ or $|1, 1\rangle$ immediately before the detection of the probability of the ion being in the dark state p_{Dark} .

In order to quantitatively assess this effect, we assign the steady-state distribution of the ion's hyperfine spin state a "spin temperature" T_s by $\frac{p_1}{p_0} = 3 \exp(-\frac{E^{\mu rs}}{k_B T_s})$ resulting in $T_s = 200$ mK. Here, $p_1 = \sum_m p_{11,m}$ is the probabil-
ity p_1 is corrected for detection efficiencies (see ity p_{Bright} corrected for detection efficiencies (see Supplemental Material [[13](#page-3-10)]) and $E^{HFS} = h \times 12.6 \text{ GHz}$
is the hyperfine energy of the ion. In comparison, we is the hyperfine energy of the ion. In comparison, we estimate the kinetic energy E_{kin} from the balance of elastic and inelastic processes, assuming to be not dominated by micromotion heating effects at these temperatures [\[30\]](#page-4-0). The average kinetic energy intake of the ion per Langevin collision due to a hyperfine flip in the neutral atom is $\delta E_{\text{heat}} = \epsilon E_a^{HFS} \frac{m_a}{m_a + m_i}$. Here, m_a is the mass of the atom, m_i the mass of the ion, $0 \le \epsilon \le 1$ describes the probability that an atomic hyperfine flip occurs during a Langevin collision, and $E_d^{HFS} = h \times 6.8$ GHz is the internal hyperfine energy of the atom. The average ion internal hyperfine energy of the atom. The average ion energy loss by elastic ion-atom momentum transfer is $\delta E_{\text{cool}} = -\frac{2m_a m_i}{(m_a + m_i)^2} E_{\text{kin}}$ per Langevin collision. As a result, the steady-state average kinetic energy of the ion is

 $\langle E_{\text{kin}} \rangle = \epsilon E_a^{HFS} \frac{m_a + m_i}{2m_i} = \epsilon k_B \times 240 \text{ mK}$. For ϵ near unity, we hence obtain $\langle E_{\text{kin}} \rangle \approx k_B T_s$, which signals an equidistribution of energy between kinetic and spin degrees of freedom. In contrast, if the atomic bath is prepared in its hyperfine ground state $|F = 1\rangle_a$, no energy-releasing hyperfine changes can occur and the temperature of ion is expected to be limited by micromotion heating, which is on the order of 20 mK [\[22](#page-3-16)[,30\]](#page-4-0).

As an additional degree of freedom in the case of ¹⁷¹Yb⁺, we study the spin transfer within the $|F = 1\rangle$ manifold of 171Yb^+ when starting from $|1, 0\rangle$. The data are shown in Figs. $3(c)-3(e)$, together with the results of a four-level rate equation model, which involves spin transfer within the $|F = 1\rangle$ manifold as well as decay into the $|F = 0\rangle$ state. Most strikingly, the decay out of the initially prepared $|1, 0\rangle$ state exhibits two different time constants [see Fig. $3(d)$]. The fast initial decay is associated with the population of the $|1, \pm 1\rangle$ states, where the occupation correspondingly rises [see Figs. $3(c)$ and $3(e)$]. Eventually, the $|F = 1\rangle$ states decay to their steady-state populations. The significant buildup of population in the $|1, -1\rangle$ state and the relaxation from $|1, 1\rangle \rightarrow |0, 0\rangle$ are both forbidden by spin conservation; however, as for the Zeeman qubit we observe a strong spin-nonconserving process.

Quantum mechanically, an isolated spin $1/2$ can exist in superposition states of spin-up and spin-down that are not describable by classical physics. Coupling to an environment affects the quantum mechanical superposition and, eventually, leads to decoherence as the information of the quantum correlations gets lost and the quantum mechanical superpositions transform into probability distributions of occupation numbers. In the problem discussed here, it is important to understand whether this decoherence results from inelastic spin-relaxation processes, i.e., amplitude decoherence, or whether also elastic (forward) scattering contributes to additional phase decoherence of superposition states. In the hydrogen maser [\[31\]](#page-4-1) spin-exchange processes have been identified as a leading source of both line shifts and broadening.

We characterize the influence of ion-atom collisions on the hyperfine clock transition in 171Yb^+ by measuring its coherence time and line shift using the Ramsey technique. To this end, we prepare the ion in the $|0, 0\rangle$ hyperfine ground state and apply a $\pi/2$ pulse on the 12.6-GHz clock transition, creating a superposition state $(0, 0)$ + $i|1,0\rangle/\sqrt{2}$. After a waiting time of 27 ms we apply a
second $\pi/2$ pulse followed by a readout of the $|F=1\rangle$ second $\pi/2$ pulse, followed by a readout of the $|F = 1\rangle$
spin state. Figure 4 displays our results. In panels (a)–(d) spin state. Figure [4](#page-3-24) displays our results. In panels (a)–(d) we show sample traces of our Ramsey fringes as a function of the detuning of the microwave pulse from the clock transition with increasing density of neutral atoms during the interaction time. Even without neutral atoms, the visibility of the Ramsey fringes is limited to $(55 \pm 2)\%$ owing to magnetic field fluctuations of the bias field. We find that

FIG. 4 (color online). Spin coherence of the hyperfine clock transition $|0, 0\rangle \leftrightarrow |1, 0\rangle$ in ¹⁷¹Yb⁺. (a)–(d) Ramsey fringes recorded for increasing atomic density. (e) Ramsey contrast as a function of t/t_L displays an exponential decay with a time constant of $T_2 = (1.4 \pm 0.2)t_L$. (f) No frequency shift of the clock transition is observed within the experimental errors. Error bars denote 1 standard deviation uncertainty intervals.

the spin coherence decays within $T_2 = (1.4 \pm 0.2)t_L$ [see Fig. $4(e)$]. This is on the time scale of the population relaxation of the $|1, 0\rangle$ state, which is driven by the spinexchange and spin-orbit interaction. The measurement hence identifies spin relaxation as the leading mechanism of spin decoherence in our system with a nondetectable contribution from elastic (forward) scattering. Finally, we note that the frequency shift $\Delta \nu$ of the clock transition is below the resolution set by the spin relaxation rate and is $\Delta \nu \leq 4 \times 10^{-11} E_i^{HFS}/h$ for our densities
[see Fig. 4(f)] [see Fig. $4(f)$].

Our measurements realize a novel spin bath with additional continuous degrees of freedom in which we have observed an unexpectedly strong coupling between internal (spin) and external (orbital) degrees of freedom. Future experiments with a driven impurity could reveal whether this coupling mechanism could lead to similar quantum phase transitions as predicted for the spin-boson model [[1](#page-3-0)], and how the physics of the single ion in the spinpolarized bath relates to the physics of polarons [\[32–](#page-4-2)[35\]](#page-4-3).

We thank A. Imamoglu and C. Kollath for discussions. The work has been supported by EPSRC (EP/H005676/1), ERC (Grant No. 240335), the Leverhulme Trust (C.S.), the Royal Society, and the Wolfson Foundation.

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