

Anionic Depolymerization Transition in IrTe₂

Yoon Seok Oh,¹ J. J. Yang,² Y. Horibe,¹ and S.-W. Cheong^{1,2}

¹Rutgers Center for Emergent Materials and Department of Physics and Astronomy, Piscataway, New Jersey 08854, USA

²Laboratory for Pohang Emergent Materials and Department of Physics, Pohang University of Science and Technology, Pohang 790-784, Korea

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Selenium substitution drastically increases the transition temperature of iridium ditelluride (IrTe₂) to a diamagnetic superstructure from 278 to 560 K. Transmission electron microscopy experiments revealed that this enhancement is accompanied by the evolution of nonsinusoidal structure modulations from $q = 1/5(10\bar{1})$ to $q = 1/6(10\bar{1})$ types. These comprehensive results are consistent with the concept of the destabilization of polymeric Te-Te bonds at the transition, the temperature of which is increased by chemical and hydrostatic pressure and by the substitution of Te with the more electronegative Se. This temperature-induced depolymerization transition in IrTe₂ is unique in crystalline inorganic solids.

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A polymer is a large molecule made up of repeating chemical units connected by covalent bonds [1]. Many polymers are thermally unstable and decompose at high temperatures (T). Other polymers undergo phase transitions upon changes in temperature. Rubbery or flexible thermoplastics can transform to glassy or crystalline states below specific temperatures without losing their polymeric nature. Depolymerization-polymerization transitions have also been observed in a number of polymeric materials. For example, rhombic sulfur with cyclic molecule rings (depolymerized S₈) undergoes a reversible depolymerization-polymerization transition to form polymerized sulfur chains above 140° C [2,3]. Fullerene (C₆₀) molecules [4] can be polymerized to orthorhombic one-dimensional chains [5] or rhombohedral two-dimensional lattices [6] under external pressure. In addition, ultraviolet light illumination induces the polymerization of C₆₀ molecules [7].

Layered chalcogenides, composed of stacking polyhedron layers with van der Waals (vdW) gaps, exhibit rich quasi-low-dimensional physical properties such as superconductivity [8,9], topological insulating behavior [10–12], and high mobility in field-effect-transistor structures [13,14]. Transition metal dichalcogenides [MX₂, such as 1T-TaS₂, 1T-TaSe₂, and 1T-TiSe₂, forming layered CdI₂ structures (space group $P\bar{3}m1$)] show charge-density-wave (CDW) states accompanied by structural modulations below their transition temperatures (T_C). For 1T-TaS₂ and 1T-TiSe₂, applied pressure and chemical doping suppress the CDW state and induce superconductivity [15,16], attributed to competition between CDW and superconductivity. IrTe₂ also crystallizes in the CdI₂ structure. A sudden increase in resistivity below ~260 K accompanying structural modulation and diamagnetism was interpreted in terms of CDW instability. Superconductivity in Pd-intercalated and doped IrTe₂ was also understood in terms of the competition between CDW and superconductivity [17]. However, a recent

optical spectroscopy study suggested that the electronic or structural transition in IrTe₂ is driven by a reduction in the kinetic energy of electrons due to Te 5*p* band splitting below T_C [17]. Studies using x-ray photoemission spectroscopy (XPS) [18] and angle-resolved photoemission spectroscopy [19] have indicated the importance of the orbital degeneracy of Ir 5*d* and/or Te 5*p* for the transition. Thus, the origin of the electronic or structural transition below ~260 K remains unclear.

This Letter provides evidence that the electronic or structural transition in IrTe₂ is a phase transition involving the depolymerization-polymerization of anionic Te bonds. Short Te-Te bonds between adjacent Te layers in the normal state of IrTe₂ have already been suggested to result in three-dimensional polymeric networks with multiple covalent Te-Te bonds [Fig. 1(a)] [20,21]. Formation of the

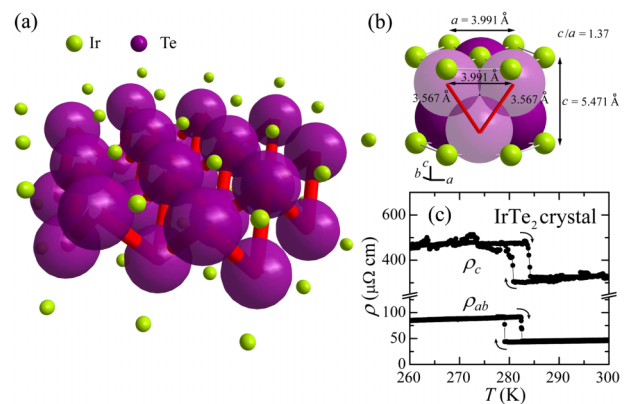


FIG. 1 (color online). (a) Schematic perspective view of the polymeric network of Te-Te bonds. (b) Crystal structure of IrTe₂ showing Te-Te bond lengths and the relative sizes of the Ir⁴⁺ and Te²⁻ ions (the radii of the Ir⁴⁺ and Te²⁻ ions with 6 coordination sites are 0.62 and 2.2 Å, respectively). (c) Temperature dependence of the resistivity $\rho(T)$ of an IrTe₂ single crystal along the c axis (ρ_c) and in the ab plane (ρ_{ab}).

polymeric Te-bond networks is associated with a fractional ionic character of Te ($\text{Te}^{1.5-}$) and with the destabilization of the highly oxidized state of Ir, resulting in effective Ir^{3+} valence states [22]. Consistently, the Te-Te distance (3.567 Å) between neighboring Te-Te layers is $\sim 10\%$ shorter than that in each Te layer [21] [Fig. 1(b)]. As a result, IrTe_2 has a c/a ratio of 1.37, significantly smaller than the c/a ratio of 1.6–1.8 for the typical hexagonal close-packed CdI_2 structure with vdW gaps [23]. For example, in HfTe_2 ($1T\text{-TiSe}_2$), where Hf (Ti) ions are in a stable, highly oxidized state of 4+, vdW gaps are allowed between the Te-Te (Se-Se) layers, and thus HfTe_2 ($1T\text{-TiSe}_2$) exhibits a large c/a ratio of 1.68 (1.70) [22,23]. Combined with the results of an earlier XPS [18], our comprehensive experimental results on IrTe_2 with Se substitution and hydrostatic pressure (P) strongly suggest that below ~ 260 K the covalent Te-Te bonds weaken and the polymeric Te-bond network becomes depolymerized. This depolymerization of Te-Te bonds is associated with an increase in the ionic character of $\text{Te}^{1.5-\delta/2-}$ and a mixed valence state of $\text{Ir}^{3+\delta+}$ in the diamagnetic superstructure, where δ indicates the change in the Ir valence state.

$\text{IrTe}_{2-x}\text{Se}_x$ specimens were prepared in polycrystalline and single crystalline forms. For polycrystalline $\text{IrTe}_{2-x}\text{Se}_x$, Ir, Te, and Se elements were mixed stoichiometrically, ground, pelletized, and synthesized in vacuum-sealed quartz ampules. XRD experiments were performed using a Rigaku D/Max-RB x-ray diffractometer with $\text{Cu } K_\alpha$ radiation. Single crystalline samples were grown from the Te flux. The Se compositions of $\text{IrTe}_{2-x}\text{Se}_x$ single crystals were estimated by comparing their T_C 's with those of polycrystalline $\text{IrTe}_{2-x}\text{Se}_x$. Magnetization and electrical resistivity were measured up to 400 K using the Quantum Design MPMS-XL7 and PPMS-9. High- T transport properties were measured in a tube furnace using a DS340 function generator and an SR510 lock-in amplifier, and P experiments were performed using EASYPACK PCELL30. Samples for TEM studies were prepared by cleaving and Ar ion milling. TEM experiments were carried out with JEOL-2010F and JEOL-2000FX transmission electron microscopes equipped with a low- T sample stage and a room- T double-tilt sample stage.

Figure 2(a) exhibits the Se substitution effect on $\chi_{\text{DC}}(T)$ of polycrystalline $\text{IrTe}_{2-x}\text{Se}_x$. As Se concentration increases, T_C to the low- T diamagnetic state increases significantly from 278 K ($x = 0.05$) to 288 K ($x = 0.1$) and 370 K ($x = 0.3$). At $x = 0.7$, it only shows diamagnetic susceptibility up to 400 K. This T_C enhancement is more evident in Fig. 2(b), which shows the T dependence of electric resistivity [$\rho(T)$] of polycrystalline specimens up to $x = 1.1$. A maximum T_C of ~ 560 K was observed for $\text{IrTe}_{0.9}\text{Se}_{1.1}$, corresponding to the chemical solubility limit of Se. A single crystal of IrTe_2 undergoes its transition at 283 K (279 K) upon warming (cooling), as shown

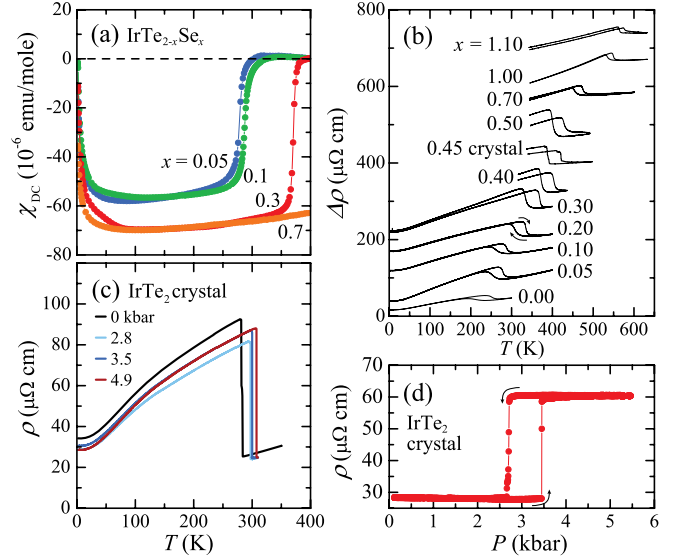


FIG. 2 (color online). Temperature dependence of (a) the magnetic susceptibility of polycrystalline $\text{IrTe}_{2-x}\text{Se}_x$ in $\mu_0 H = 1$ T upon warming, and (b) the resistivity of polycrystalline $\text{IrTe}_{2-x}\text{Se}_x$ and a single crystal. $\rho(T)$ curves for $x \neq 0$ are shifted by arbitrary constants for clarity. (c) $\rho(T)$ of an IrTe_2 single crystal upon warming under various hydrostatic pressures. (d) Pressure dependence of the resistivity of an IrTe_2 single crystal at 300 K.

in Fig. 1(c). As shown in Fig. 2(c), applying P to an IrTe_2 single crystal also increases T_C . The sharp transition in ambient pressure increases monotonically with increasing P . At 300 K, P consistently induces the transition at 3.5 Kbar (2.7 Kbar) upon increasing (decreasing) pressure.

Note that diamagnetic susceptibility suddenly increases from approximately -60×10^{-6} emu/mole ($x = 0.0$ [24], 0.05, and 0.1) to -70×10^{-6} emu/mole ($x = 0.3$ and 0.7). The estimated core diamagnetism is approximately -170×10^{-6} emu/mole, and the difference between the core diamagnetism and the observed diamagnetic signals corresponds to the contribution of Pauli paramagnetism from itinerant electrons. This sudden change in Pauli paramagnetism reflects an abrupt change in the electronic structure of $\text{IrTe}_{2-x}\text{Se}_x$ with respect to Se doping. Indeed, TEM below T_C reveals two distinct modulated structures, characterized by two distinct superlattice peaks. Figures 3(a)–3(f) show electron diffraction patterns around the $\bar{1}20$ and $02\bar{1}$ fundamental spots for $x = 0.0, 0.15, 0.2, 0.3, 0.5,$ and 1.0 , respectively. The $1/5(10\bar{1})$ -type superlattice spots observed at $x = 0.0$ [Fig. 3(a)] remain intact for $x = 0.15$ and 0.2 [Figs. 3(b) and 3(c)] but change suddenly to the $1/6(10\bar{1})$ type at $x \geq 0.3$ [Figs. 3(d) and 3(f)]. The $1/5(10\bar{1})$ and $1/6(10\bar{1})$ superlattice peaks correspond to 1.4 and 1.7 nm spacings in real space, respectively. In both cases, we have frequently observed fine antiphase boundaries (APB) within a large strain-relieving twin domain in dark-field images obtained using a $02\bar{1}$ fundamental spot, as shown in Fig. 3(g) ($x = 0.0$ at ~ 85 K) and Fig. 3(h)

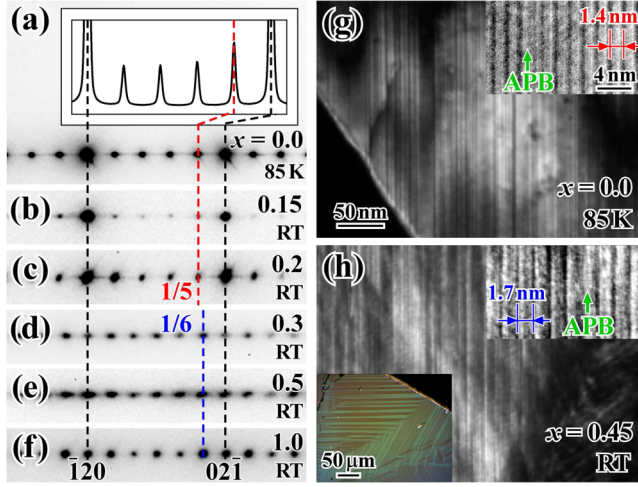


FIG. 3 (color online). (a)–(f) Electron diffraction patterns between the $\bar{1}20$ and $02\bar{1}$ fundamental spots for $\text{IrTe}_{2-x}\text{Se}_x$. The corresponding intensity profile of $x = 0.0$ is shown in the inset. Dark-field images of (g) $x = 0.0$ at ~ 85 K and (h) $x = 0.45$ at room temperature (RT). High-resolution TEM images are shown in the upper right-hand insets of (g) and (h), displaying the superlattice modulations with periodicities of 1.4 and 1.7 nm associated with the $1/5(10\bar{1})$ and $1/6(10\bar{1})$ superlattice peaks, respectively, as well as antiphase boundaries (APB) due to phase shifts of the superlattice modulations. The lower left-hand inset of (h) displays a polarized optical microscope image of twin domains of $x = 0.45$.

($x = 0.45$ at room T), respectively. Fine APB perpendicular to the superlattice modulation wave vectors are clearly visible in both Figs. 3(g) and 3(h). The typical spacing between APB is approximately 10 nm in both cases. High-resolution TEM images in the insets of Figs. 3(g) and 3(h) clearly indicate that these APB are associated with phase shifts of the superlattice modulation waves across the boundaries. The intensity profile between the $\bar{1}20$ and $02\bar{1}$ fundamental peaks of $x = 0.0$ [inset of Fig. 3(a)] reveals that all four $1/5(10\bar{1})$ -type superlattice peaks exhibit similar intensities. A similar trend can be observed for the superlattice peaks of other compositions. The presence of high harmonics with strong intensities indicates that the superstructure modulations are highly nonsinusoidal and rather rectangular. This highly nonsinusoidal modulation is different from the typical sinusoidal modulation in CDW states, for example, in $1T\text{-TaSe}_2$ and $1T\text{-TaS}_2$ [25]. In addition, most CDW transitions in MX_2 are associated with three q modulations, but the modulation in IrTe_2 occurs together with a “single q and three domains.” Indeed, the three domains (or twins), corresponding to three q values with a relative 120° in-plane angle, are visible in polarized optical microscope images [lower left-hand inset in Fig. 3(h)] as well as in TEM images (see Fig. S1 in Ref. [26]).

Figure 4(a) presents the T versus x phase diagram of $\text{IrTe}_{2-x}\text{Se}_x$, where the phase boundaries are determined from the results of TEM and $\rho(T)$ experiments with

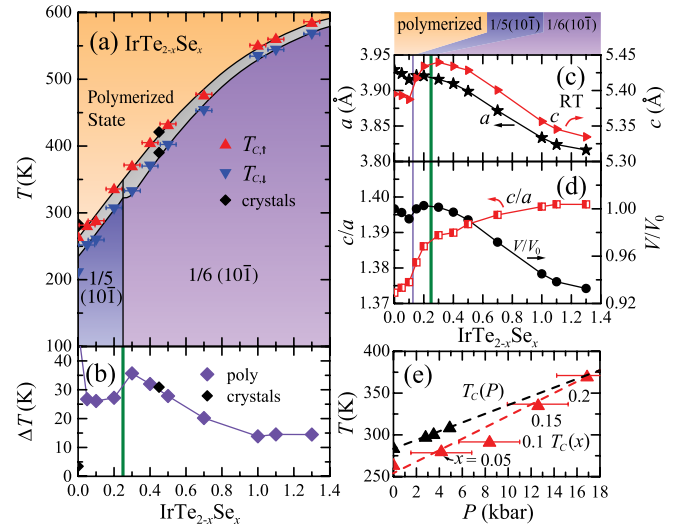


FIG. 4 (color online). (a) Temperature (T) versus Se concentration (x) phase diagram of $\text{IrTe}_{2-x}\text{Se}_x$ constructed with T_C values obtained from $\rho(T)$ measurements under warming (triangle) and cooling (inverted triangle). The diamond symbols indicate the T_C values of $\text{IrTe}_{2-x}\text{Se}_x$ single crystals ($x = 0$ and 0.45). (b) Width of the thermal hysteresis (ΔT) as a function of x in $\text{IrTe}_{2-x}\text{Se}_x$. The vertical green guide line depicts the phase boundary between the $1/5(10\bar{1})$ and $1/6(10\bar{1})$ superstructures. Se-doping dependence of (c) the a - and c -axis lattice constants and (d) the c/a ratio and the normalized volume determined from XRD results. The thin purple and thick green vertical lines indicate the phase boundaries of the paramagnetic to $1/5(10\bar{1})$ transition and the $1/5(10\bar{1})$ to $1/6(10\bar{1})$ transitions, respectively. (e) Hydrostatic pressure and calculated chemical pressure dependence of T_C of IrTe_2 .

warming and cooling. The thermal hysteresis (ΔT) of T_C , estimated from warming and cooling $\rho(T)$ curves as a function of x [see Fig. 4(b)], exhibits a sudden jump at $x = 0.2$ – 0.3 , coinciding with the abrupt change of superstructure from the $1/5(10\bar{1})$ to the $1/6(10\bar{1})$ type. Thus, although T_C appears to increase monotonically as a function of x across the phase boundary of the $1/5(10\bar{1})$ and $1/6(10\bar{1})$ superstructures, ΔT accurately reflects the presence of the phase boundary.

XRD experiments at room T are highly informative regarding the physical nature of the transition. As shown in Fig. 4(c), the a - and c -axis lattice constants for $x \leq 0.1$ decrease linearly with increasing x (i.e., following Vegard’s law), consistent with the fact that Se ions are smaller than Te ions. However, a sudden increase in “ c ” (along with a smaller increase in “ a ”) occurs at $x = 0.1$ – 0.15 , corresponding to the phase boundary (thin purple vertical line) between the high- T polymerized state and the $1/5(10\bar{1})$ superstructure. This dominant structural effect of the c increase at T_C reflects the sudden weakening of interlayer coupling. The increase of a and c gradually lessens beyond the phase boundary (thick green vertical line) between the $1/5(10\bar{1})$ and $1/6(10\bar{1})$ superstructures. The structural evolution over x seems better reflected in a

plot of the c/a ratio versus x . The c/a ratio increases drastically at the phase boundary between the high- T polymerized state and the diamagnetic $1/5(10\bar{1})$ superstructure, suggesting a weakening of the polymerized Te bonds through the first-order phase transition. As the c/a ratio (1.39–1.4) is still significantly smaller than that (1.6–1.8) of the true vdW systems, the depolymerization in the diamagnetic superstructure is still partial. In fact, the modulated superstructure may result from an ordered arrangement of polymerized and depolymerized Te bonds. We emphasize that the most drastic observation is the large increase in T_C resulting from the substitution of Se ions, which not only have a smaller ionic radius but are also more electronegative than Te ions. These electronegative Se ions should destabilize covalent anionic bonding, thus leading to the drastic increase in T_C .

Furthermore, the increase in the number of depolymerized Te bonds with increasing Se substitution is also consistent with the decrease in the magnitude of the modulating wave vector from a $1/5$ to $1/6$ type. This scenario is consistent with the weakening of anionic polymeric Te-Te bonds with Se doping observed in $\text{Pt}(\text{Te}, \text{Se})_2$ [27]. Depolymerization reorganizes the ionic characteristics of Te anions, and reorganized $\text{Te}^{1.5-\delta/2-}$ ions lead to a mixed valence state of Ir cations such as $\text{Ir}^{3+\delta+}$. In fact, evidence of mixed valence Ir ions in the low- T diamagnetic superstructure was observed in a previous study using XPS [18]. Note that the nonsinusoidal structural modulations in the TEM experiments here appear to be consistent with the charge ordering of the mixed valence states of Ir ions.

The increase in T_C with increasing P is summarized in Fig. 4(e). P also destabilizes the polymerized state, which seems to be counterintuitive. However, the application of P to PtTe_2 [28] with anionic polymeric Te-Te bonds increases the ratio of interlayer to intralayer Te-Te distance. Thus, this increase in the interlayer/intralayer ratio with P likely stabilizes the low- T depolymerized state, leading to the increase in T_C . The magnitude of the chemical pressure resulting from Se doping has been estimated using the initial slope of $a(x)$ and $c(x)$ for $0 \leq x \leq 0.1$ and the bulk modulus [29,30]. Figure 4(e) compares the effect of mechanical P with the effect of Se chemical pressure on T_C . This qualitative agreement indicates that the effect of Se substitution also fits the role of an archetypal chemical pressure effect. However, the positive slope with respect to chemical pressure, $\partial T_C/\partial P = +6.8$ K/kbar, is larger than that in response to P , $\partial T_C/\partial P = +5.4$ K/kbar, suggesting that the depolymerization of the polymeric Te bond is further enhanced by the electronegative character of Se ions. Note that the increase in T_C in IrTe_2 with increasing chemical or hydrostatic pressure is in contrast with the effect of chemical or hydrostatic pressure on MX_2 (such as $1T\text{-TaS}_2$ [15], $1T\text{-TiSe}_2$ [16], and $1T\text{-TiSe}_{2-x}\text{S}_x$ [31]), in which the CDW state is suppressed by pressure.

A number of our findings from the chemical or hydrostatic pressure, TEM, and XRD experiments are distinct from the typical behavior of CDW systems. A peak near $1/5(10\bar{1})$ in the charge susceptibility of IrTe_2 was interpreted as an indication for the presence of a nesting vector of Fermi surface and CDW instability [24], but the charge susceptibility exhibited other features. Our results, first, reveal that the superlattice modulations are associated with a single q and three domains and are highly nonsinusoidal, uncommon characteristics of typical CDW systems. Second, the drastic increase in T_C up to 560 K with the application of chemical and hydrostatic pressure has never been observed in any other CDW systems, which tend to have modest T_C values due to the small energy scale associated with Fermi surface instability. In addition, the sudden increase in the c/a ratio below T_C is also unique compared with the behavior of CDW systems. These empirical observations, combined with the earlier proposal of charge modulations based on XPS experiments [18], are consistent with our proposed scenario of a depolymerization-polymerization transition at T_C associated with the charge ordering of $\text{Ir}^{3+}/\text{Ir}^{4+}$ ions. We emphasize that the earlier study of fermiology [24] did not take into account the lattice contributions such as phonon contribution, and we cannot rule out that the Fermi surface instability contributes to the depolymerization-polymerization transition in a secondary manner. Full theoretical investigation of the intriguing transition including the lattice contributions will be necessary to unveil the microscopic origin of the transition.

In conclusion, this study has explored the unique nature of the first-order phase transition at ~ 260 K in IrTe_2 , leading to diamagnetism, an increase in resistivity, and nonsinusoidal superlattice modulations of the $1/5(10\bar{1})$ type. The weak ionic nature of Te and the stability of Ir^{3+} lead to a polymerized state with anionic polymeric networks of covalent Te-Te bonds in adjacent Te layers. The effective valence of Te in this polymerized state is $1.5 -$. Below ~ 260 K, the covalence of Te-Te bonds is partially lost, and the Te-Te networks are depolymerized. This leads to a reduced metallic character and the appearance of a superstructure. The effective valences of Ir and Te in the low- T depolymerized state are $(3 + \delta)+$ and $(1.5 + \delta/2) -$, respectively. This depolymerized state is found to be drastically stabilized by chemical pressure and hydrostatic pressure, as evidenced by increases in the c/a ratio and T_C with hydrostatic pressure and Se substitution. Substitution of Te with Se increases T_C up to 560 K and leads to a distinct transformation of the superstructure from $1/5(10\bar{1})$ to $1/6(10\bar{1})$. This reversible depolymerization-polymerization transition appears to be unique among crystalline inorganic solids. These findings provide a new facet in the research of layered chalcogenides, materials that have continuously drawn the attention of the condensed matter physics community over the past several decades.

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