

Self-Guided Propagation of Ultrashort Laser Pulses in the Anomalous Dispersion Region of Transparent Solids: A New Regime of Filamentation

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We report measurements concerning the propagation of femtosecond laser pulses in fused silica with a wavelength at $1.9\ \mu\text{m}$ falling in the negative group velocity dispersion region. Under sub-GW excitation power, stable filaments are observed over several cm showing the emergence of nonspreading pulses both in space and time. At higher excitation powers, one observes first multiple pulse splitting followed by the emergence of the quasispatiotemporal solitary filament. These results are well reproduced by numerical simulations.

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The propagation of an intense ultrashort laser pulse in a transparent medium, despite the apparent simplicity of the problem, is a complex process. The nonlinear propagation is first dominated by the optical Kerr response of the medium. The light-induced change of refractive index leads to beam self-focusing [1], pulse spectral broadening [2], and beam profile reshaping [3,4]. For a pulse peak power above a critical value $P_{\text{cr}} = 3.77\lambda_0^2/8\pi n_0 n_2$, where λ_0 is the laser wavelength in vacuum, n_0 the corresponding refractive index and n_2 the nonlinear Kerr index, diffraction is unable to arrest the beam self-focusing effect. The intensity grows to the point that strong field ionization of the medium occurs. This prevents beam collapse because the generated plasma consumes laser energy and induces a defocusing of the beam. The further evolution of the pulse is ruled by a competition between diffraction, group velocity dispersion, the increase of the refractive index from the optical Kerr effect, multiphoton absorption, and the reduction of refractive index due to plasma formation. The combination of these effects leads to filamentation, a process where the pulse maintains a narrow diameter and high peak intensity over impressive distances that can reach several km in atmosphere [5,6]. Most experiments on filamentation so far have concentrated on situations where the laser wavelength corresponds to a region of normal group velocity dispersion (GVD). Filamentary behavior has been observed as a generic trend in transparent gases, solids, and liquids. However, this universal trend masks a complex underlying situation. The filament length and plasma density depend critically on the initial pulse intensity, initial pulse duration, and beam convergence [7]. Plasma and GVD induced pulse splitting lead to pulse self-shortening with a single compressed pulse component emerging fortuitously at some distance, followed by a rapid deterioration [8]. As a consequence, it is hard to achieve a

controlled and stable filamentation regime with preserved laser pulse features over extended distances.

A simpler behavior is expected when the laser wavelength falls in the anomalous dispersion region. New red (blue) frequencies generated by self-phase modulation on the ascending (descending) slopes of the pulse are now swept back to the peak of the pulse, instead of being dispersed as in the normal case. As a consequence, a simultaneous time and space compression occurs, which favors a new type of filamentation where the self-guided pulses do not spread in time and space over long distances [9]. Several authors have started to investigate this regime, both experimentally and theoretically. On the theoretical front, Shim *et al.* [10] have simulated filamentation in air at $3.1\ \mu\text{m}$, a region of negative GVD. The authors conclude that this medium is unfavorable for a clear demonstration of temporal solitons because pulse self-compression is restricted by a limited range of negative dispersion (approximately 200 nm around $3.1\ \mu\text{m}$). The situation is more favorable in condensed media such as fused silica (SiO_2), where a broad spectral bandwidth of negative GVD extending over more than 2000 nm beyond $1.26\ \mu\text{m}$ is available. Several authors have performed numerical simulations of the propagation of IR laser pulses in fused silica [11–13]. On the experimental side, measurements in fused silica have shown that the critical threshold for filamentation is reduced [12] and that a broad conical continuum emission is produced [14,15], suggesting efficient pulse self-compression. However, to the best of our knowledge, there is no report yet on the free propagation of a stable, self-compressed pulse over long distances.

In this Letter we report measurements concerning the propagation of femtosecond laser pulses in fused silica with a central wavelength falling in the negative GVD region. Impressive stability of self-guided pulses is observed in the time and space domain, showing the emergence of a

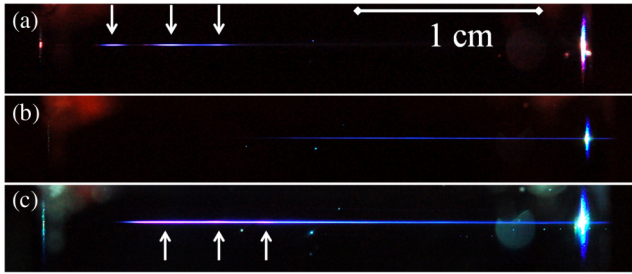


FIG. 1 (color online). Side view photography of the blue fluorescence of SiO_2 induced by a self-guided laser pulse at (a) 800 nm with $P = 18 P_{\text{cr}}$, (b) $1.9 \mu\text{m}$ with $P = 13 P_{\text{cr}}$ and (c) $1.9 \mu\text{m}$ with $P = 30 P_{\text{cr}}$. The laser pulse is focused on a $70 \mu\text{m}$ spot (FWHM) at the left surface of the 3 cm thick sample. Vertical arrows indicate the position of focusing-defocusing cycles.

quasispaciotemporal soliton. Our results are well reproduced by numerical simulations.

Infrared laser pulses at $1.9 \mu\text{m}$ of 40 fs duration and energy between 8 and $20 \mu\text{J}$ were weakly focused close to the front surface of a 3 cm thick block of fused silica (beam numerical aperture $\text{NA} = 0.015$). Side images recorded with a CCD camera of the blue luminescence of SiO_2 reveal a thin filamentary track extending over a large part of the sample (see Fig. 1). The blue luminescence induced by multiphoton absorption of the propagating laser pulse becomes apparent at laser pulse intensities $I > 10^{12} \text{ W/cm}^2$. In Fig. 1, we compare the filaments obtained for a similar ratio $P/P_{\text{cr}} \sim 15$ for a laser pump wavelength at $0.8 \mu\text{m}$ [normal dispersion, $P_{\text{cr}} = 3 \text{ MW}$, Fig. 1(a)] and $1.9 \mu\text{m}$ [anomalous dispersion region, $P_{\text{cr}} = 16 \text{ MW}$, Fig. 1(b)]. Propagation with positive GVD generates a significantly shorter filament with multiple refocusing cycles. Figure 1(c) also shows the filament at $1.9 \mu\text{m}$ obtained at higher input powers $P > 25 P_{\text{cr}}$. In this case, multiple focusing-defocusing cycles appear first, followed by a continuous and uniform filament similar to that seen in Fig. 1(b).

We have measured the diameter of the infrared filament obtained with light at $1.9 \mu\text{m}$ with $P \sim 18 P_{\text{cr}}$. The spatial profile of the laser pulse emerging from the back surface of the sample was imaged by a silica lens with a focal distance of 10 cm onto a camera. The filament length at which the diameter was measured was varied by displacing the focus of the converging beam toward the interior of the sample, effectively bringing the filament closer to the sample rear surface. A circular beam with a constant diameter (FWHM) of $20 \mu\text{m}$ is obtained [Fig. 2(a)]. By comparison, the beam profile recorded at an equivalent distance in the absence of sample shows a larger asymmetric pattern [see Fig. 2(b)]. Spatial self-compression and self-cleaning of the laser beam profile is telltale of filamentation [4].

A single-shot, self-referenced spectral interferometry technique called Wizzler [16] operating in the near infrared region was chosen to characterize the duration of the

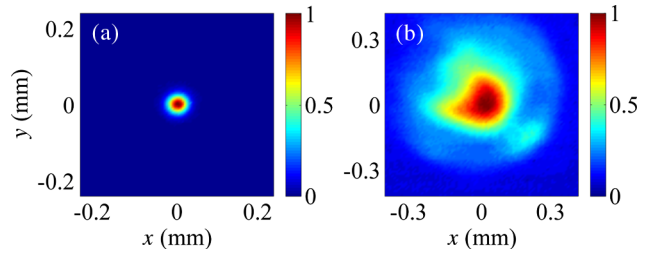


FIG. 2 (color online). Beam profile of the laser pulse at $1.9 \mu\text{m}$ (a) with filamentation (b) without filamentation. Intensity scale is normalized.

self-guided pulse emerging from the sample. It is free from the coherence artifact due to shot-to-shot instability that can arise with multishot characterization techniques [17]. As the signal-to-noise ratio on the spectrometer was low, the measurements were integrated over ten shots. Pulse duration of 20 fs was retrieved, corresponding to a self-compression factor of 2 (see Fig. 3). Considering the small number of averaged shots and the reproducibility of the 20 fs pulse duration measurement, we can conclude that free propagation of an ultrashort laser pulse in the negative group velocity dispersion region of a transparent medium can lead to the formation of a stable self-guided pulse holding the attributes of a temporal solitary wave within a range of incident laser powers $P_{\text{cr}} < P < 25 P_{\text{cr}}$. However, it is necessary to stress that these self-guided pulses are intrinsically lossy and therefore cannot qualify *stricto sensu* as genuine solitons. Indeed, energy is consumed by multiphoton ionization at every step of the pulse progression. Recent papers have described such stationary

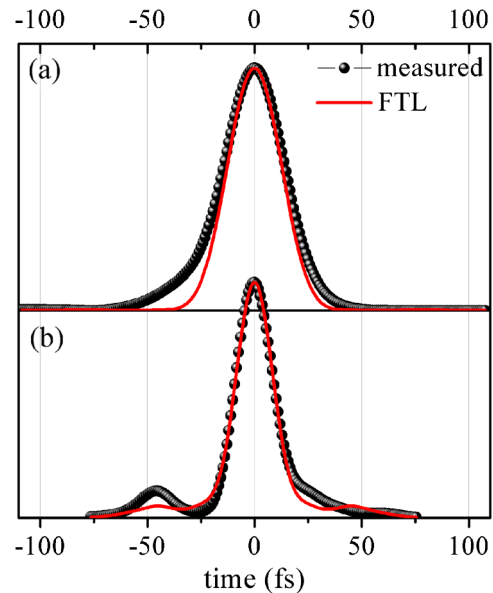


FIG. 3 (color online). Temporal pulse shape measured with the Wizzler for the initial pulse (40 fs FWHM) (a) and for filament lengths of 0.5 cm (20 fs FWHM) (b). Also shown in red is the Fourier Transform Limited (FTL) pulse.

and lossy optical pulses by the terms of *O-waves* or *dissipative light bullets* acting as attractors for the nonlinear pulse propagation in a Kerr medium with anomalous dispersion [18,19]. We also note that at high excitation $P > 30 P_{cr}$, the laser pulse experiences a spectral broadening with bluer components reaching the normal dispersion region. A detailed study of this broadening will be published elsewhere.

We have performed simulations of pulse propagation in the anomalous dispersion region of fused silica under conditions close to the experiments. The electric field is written as a complex envelope $E_{\omega_0}(\vec{r}, t, z)$ and a carrier at frequency ω_0 :

$$E = E_{\omega_0} \exp[i(k_{\omega_0} z - \omega_0 t)] \quad (1)$$

with $k_{\omega_0} \equiv k(\omega_0)$, where $k(\omega)$ denotes the dispersion relation in fused silica [20]. The propagation equation for the complex envelope $\hat{E}_{\omega_0}(k_{\perp}, \omega, z)$ in the Fourier domain takes the form of a canonical propagation equation [21]:

$$\frac{\partial \hat{E}_{\omega_0}}{\partial z} = iK_{\omega_0}(\omega, k_{\perp})\hat{E}_{\omega_0} + iQ_{\omega_0}(\omega)\left(\frac{\hat{P}_{\omega_0}}{\epsilon_0} + \frac{i\hat{J}_{\omega_0}}{\omega\epsilon_0}\right). \quad (2)$$

Here the first (linear) term on the right hand side represents diffraction, dispersion, and space-time coupling: $K_{\omega_0}(\omega, k_{\perp}) \equiv \frac{1}{2}(k_{\omega_0} + k'_{\omega_0}(\omega - \omega_0))^{-1}[k^2(\omega) - (k_{\omega_0} + k'_{\omega_0}(\omega - \omega_0))^2 - k_{\perp}^2]$, where the dispersive properties of the medium are described by a Sellmeier-like relation $k(\omega)$, and $k_{\omega_0} \equiv k(\omega_0), k'_{\omega_0} \equiv dk/d\omega|_{\omega_0}$. The nonlinear dispersion function reads $Q_{\omega_0}(\omega) \equiv \frac{1}{2}(k_{\omega_0} + k'_{\omega_0}(\omega - \omega_0))^{-1}(\omega^2/c^2)$. These frequency dependent operators in Eq. (2) generalize the standard nonlinear Schrödinger equation so as to properly describe nonlinear propagation of pulses with broad spectra, as short as a single cycle. The derivation is explained in details in Ref. [21]. In the temporal domain, pulse propagation is described in the moving frame $\tau = t - k'_{\omega_0} z$, where t denotes time in the laboratory frame. The nonlinear terms in Eq. (2) are all included in the nonlinear polarization envelope $\hat{P}_{\omega_0}(k_{\perp}, \omega, z)$ and current envelope $\hat{J}_{\omega_0}(k_{\perp}, \omega, z)$, acting as source terms for the propagation. The nonlinear polarization describes the optical Kerr effect:

$$\frac{P_{\omega_0}}{\epsilon_0} = 2n_{\omega_0}n_2|E_{\omega_0}|^2E_{\omega_0}. \quad (3)$$

The current describes plasma absorption and plasma defocusing in the framework of the Drude model, with collision time τ_c :

$$\frac{J_{\omega_0}}{\epsilon_0} = c\sigma_{\omega_0}(1 + i\omega_0\tau_c)\rho E_{\omega_0} + cn_{\omega_0}\beta_K|E_{\omega_0}|^{2K-2}E_{\omega_0}. \quad (4)$$

The various parameters in Eqs. (3) and (4) are the linear refractive index $n_{\omega_0} \approx 1.43$, the cross section for inverse bremsstrahlung $\sigma_{\omega_0} = 4.7 \times 10^{-21} \text{ cm}^2$ calculated from

the Drude model with the collision time $\tau_c = 3 \text{ fs}$ in fused silica, the cross section for multiphoton absorption $\beta_K = 3.1 \times 10^{-164} \text{ W}^{-13} \text{ cm}^{25}$, the number of photons $K = 14$ involved in the process at 1900 nm. Multiphoton absorption coefficients are estimated from the Keldysh model for dielectrics [22,23]. The nonlinear index coefficient $n_2 = 2.3 \times 10^{-16} \text{ cm}^2/\text{W}$ is slightly lower than the value $n_2 = 2.45 \times 10^{-16} \text{ cm}^2/\text{W}$ measured at 804 nm [24] due to a small effect of dispersion from 800 to 1900 nm. The role of the retarded Kerr effect was neglected as no significant Raman shift appeared in the measured spectra.

Ionization of fused silica is described by a single rate equation for the generation of free electrons with density ρ including source terms corresponding to multiphoton ionization, avalanche, and recombination processes:

$$\frac{\partial \rho}{\partial t} = \sigma_K|E_{\omega_0}|^{2K}(\rho_{nt} - \rho) + \sigma_{\omega_0}|E_{\omega_0}|^2\frac{\rho}{U_i} - \frac{\rho}{\tau_r}, \quad (5)$$

where $\sigma_K = 1.0 \times 10^{-168} \text{ cm}^{28} \text{ W}^{-14} \text{ s}^{-1}$ denotes the cross section for multiphoton ionization at 1900 nm, $\rho_{nt} \approx 2.1 \times 10^{22} \text{ cm}^{-3}$ denotes the density of neutral molecules, $U_i = 9 \text{ eV}$ denotes the ionization potential of fused silica, and $\tau_r = 150 \text{ fs}$ denotes a characteristic time for recombination [25].

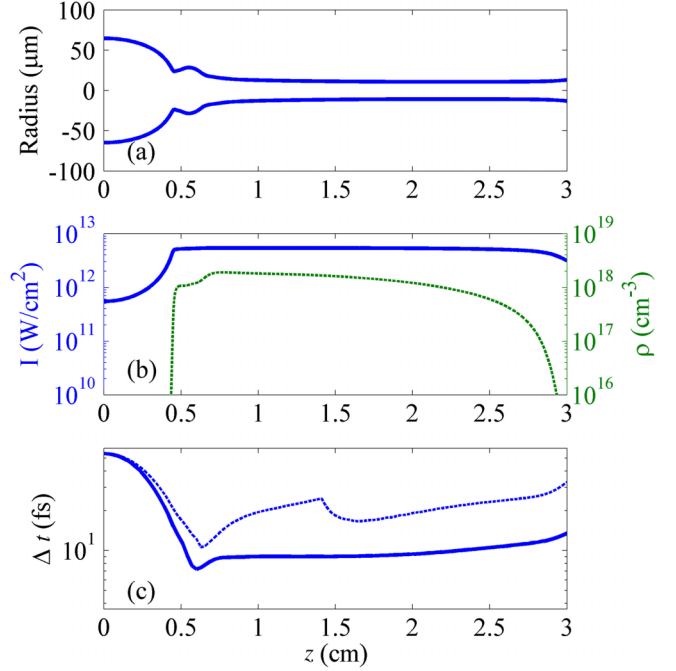


FIG. 4 (color online). Calculated results of the propagation through fused silica of an optical pulse at $1.9 \mu\text{m}$ of $110 \mu\text{m}$ diameter (FWHM) and $5 \times 10^{11} \text{ W}/\text{cm}^2$ intensity collimated on the front sample surface. (a) Beam radius as a function of distance z . (b) Intensity (full line) and free electron density (dotted green line) as a function of z . (c) Pulse duration as a function of z . The blue line corresponds to the duration within the filament core of $25 \mu\text{m}$ diameter, the dotted line corresponds to the duration obtained when averaging over a filament diameter of $50 \mu\text{m}$.

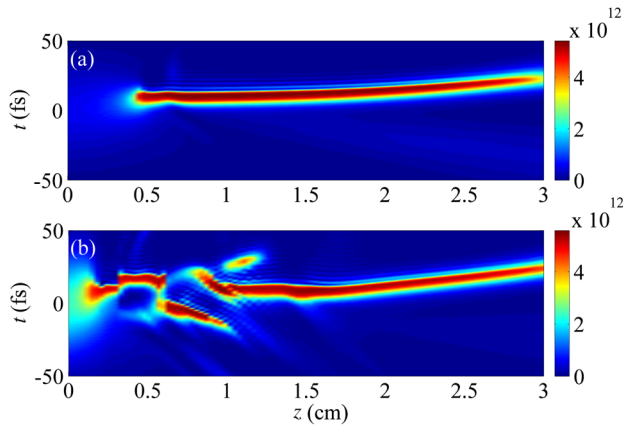


FIG. 5 (color online). Calculated time-space profile of the laser pulse for a laser pulse energy of $6\ \mu\text{J}$ (a) and $26\ \mu\text{J}$ (b) corresponding respectively to 7 and $30\ P_{\text{cr}}$.

For input powers close to P_{cr} , the numerical simulation reproduces well the observed features of Fig. 1(b). Simulations reveal the formation of a self-guided pulse with a fluence diameter of $20\ \mu\text{m}$ (FWHM), which starts after 0.5 cm of propagation and persists over the remaining sample length [Figs. 4(a), 4(b), and 5(a)]. The calculated pulse duration (FWHM) is 8 fs showing that the filament pulse reaches basically the single optical cycle limit [Fig. 4(c)]. Our measurements show a longer duration because of the limited time resolution of the Wizzler system and because no provision was taken during the measurement to remove the laser energy reservoir surrounding the filament, of longer duration [26]. By performing a spatially integrated calculation over a larger beam diameter, one obtains a duration of 20 fs, in agreement with the measurement [see Fig. 4(c)]. Simulations at incident laser power exceeding $10\ P_{\text{cr}}$ show a more complex situation at the initial stage of filamentation. The pulse undergoes first rapid variations of size and duration before a stationary pulse is formed [see Figs. 1(c) and 5(b)].

We believe that quasispatiotemporal solitons emerging from filamentation can be found in many other transparent media with a broad region of negative group velocity dispersion. We stress, however, that such quasisolitons are formed within a range of input power filamentation close to the critical power. Filamentation in the anomalous dispersion region of transparent solids should provide a simple method to produce ultrashort laser pulses with clean beam profile and well-defined intensity in the range of terawatt/cm². Such optical pulses can be useful in many applications where an intense ultrashort laser pulse of known characteristics is required.

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