## **Understanding and Revisiting Properties of EuTiO<sub>3</sub> Bulk Material** and Films from First Principles

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Ab initio computations are performed to investigate properties of bulk material and epitaxial films made of EuTiO<sub>3</sub> (ETO). A whole family of nanoscale twinned phases, that present complex oxygen octahedra tilting (OOT) and unusual antiferroelectricity, is found to be degenerate in energy with simpler phases (all possessing typical OOT) in *bulk* ETO. Such degeneracy provides a successful explanation of recently observed anomalous phenomena. The calculations also lead to revisiting the (rich) phase diagram of ETO films.

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The search for novel multiferroics [1] constitutes an important research direction, which explains why EuTiO<sub>3</sub> (ETO) systems have been recently investigated [2–14]. One interesting finding in these materials is that, while bulk ETO is not multiferroic [it exhibits a G-type antiferromagnetic (AFM) ordering below 5.3 K [15] but is paraelectric down to 0 K [16,17]], epitaxial ETO films become both ferroelectric (FE) and ferromagnetic (FM) for large enough misfit strain [2,13]. A recent experiment [6] suggested that, in contrast to what was previously believed, the ground state of bulk ETO is not cubic, paraelectric  $Pm\bar{3}m$  but rather is tetragonal I4/mcm, and therefore exhibits oxygen octahedra tilting (OOT). This same work [6] pointed out an unusual difference between shortrange and average crystallographic structures. For instance, Rietveld experiments yield a value of  $\simeq 3.5^{\circ}$  for the angle associated with OOT, while pair distribution function analysis gave a value more than two times bigger. Firstprinciple calculations [5] confirmed the importance of OOT in bulk ETO, but did not address the enigma about difference in local and average structures. Another measurement [7] determined that the OOT further adopts an unusual modulation that not only extends over several unit cells but also for which the corresponding diffraction peaks change in intensity, position, and broadness over a long time period. The reason behind such change is unknown. Anomalous antiferroelectric patterns were further found to coexist with these modulated OOT [7]. One would like to know what is the real ground state of bulk ETO and better understand this puzzling modulated OOT structure and its associated antiferroelectricity. Furthermore, previous experimental and theoretical studies on ETO films have neglected OOT. As a result, their phase diagrams may need to be revisited.

This Letter resolves the aforementioned issues by conducting first-principles calculations. It explains the puzzling observations made in bulk ETO, based on a presently discovered degeneracy between "simple" OOT phases and a whole family of nanoscale twinned phases. This Letter also reports the existence of several novel equilibrium phases in ETO films.

Computations on EuTiO<sub>3</sub> systems are performed within density-functional theory (with an energy cutoff of 550 eV), as implemented in the Vienna *ab initio* simulation package (VASP) [18,19]. Supercells containing 10, 20, 40, 60, or 80 atoms are used, with different  $\Gamma$ -centered k-point meshes (varying between  $6 \times 6 \times 6$  and  $6 \times 6 \times 1$ ), depending on the investigated phase. Both G-type AFM and FM orders are considered. More details about the method are given in the Supplemental Material [20–27].

Let us first focus on bulk ETO, by allowing the cell shape and volume of the supercells mimicking different phases to fully relax. We investigated the following states with different OOT patterns (indicated by Glazer's notations [28]): cubic  $Pm\bar{3}m$  ( $a^0a^0a^0$ ), tetragonal P4/mbm $(a^0a^0c^+)$ , orthorhombic *Pnma*  $(a^-a^-c^+)$ , tetragonal I4/mcm ( $a^0a^0c^-$ ), orthorhombic Imma ( $a^-a^-c^0$ ), rhombohedral  $R\bar{3}c$  ( $a^-a^-a^-$ ) and monoclinic C/2c ( $a^-a^-c^-$ ). A 20-atom supercell is used for all these states. A G-type antiferromagnetism is adopted, since we found it to be of lower energy than FM order. Out of these phases, four of them are energetically much more stable than  $Pm\bar{3}m$ : the I4/mcm, Imma, Pnma, and C2/c states are lower in energy by 37, 36, 36, and 35 meV per 5 atom, respectively. Such results are consistent with those of Ref. [5], and therefore emphasize the need of incorporating OOT (also, termed antiferrodistortive, AFD, motions) to properly describe ETO systems [29]. They also further confirm that different "simple" states have very similar energy and that I4/mcm is the lowest of them by a minute amount—as also in agreement with Ref. [5].

Let us now determine if states with higher complexity can also be of low energy in bulk ETO. We have in mind to consider complex oxygen octahedra tilting about the [001] pseudocubic direction. Examples include mmpp, mmpppp, ppppmmmm patterns that repeat themselves periodically along a line being parallel to [001] and joining neighboring Ti atoms. Here, p (respectively, m) denotes an O<sub>6</sub> oxygen octahedron rotating clockwise (respectively, counterclockwise) about [001]. Such nanoscale twinned phases have been proposed in bulk EuTiO<sub>3</sub> [7], based on x-ray data. We investigated several phases for which the tilting patterns can be described in a modified Glazer notation [28] by  $a^0a^0c^m$  and  $a^-a^-c^m$ , where  $c^m$  corresponds to the aforementioned complex tilting about [001] (with a possible periodic length of 4, 6, and 8 unit cells), and where  $a^0$  and  $a^-$  denote no tilting and antiphase tilting, respectively, about the [100] and [010] pseudocubic directions, respectively. Table I of the Supplemental Material [20] provides the total energy of such complex phases and compares them with that of the simple tilted I4/mcmand C2/c phases (indicated in the first row of that table). One can see that several different  $a^-a^-c^m$  phases (e.g., mmpppp, mmmppp, ppppmmm, pppppmmm, and ppppppmm) have energies that are nearly identical to that of the simpler I4/mcm state. In other words, there is a whole family of nanoscale twinned phases whose energies are basically degenerate with that of the recently assumed 14/mcm ground state [5,6] of bulk ETO [30]. Such degeneracy likely implies that nanodomains formed by different phases can coexist in bulk EuTiO<sub>3</sub>, with the size of these domains (and resulting macrosocopic properties) having the possibility to evolve with time—as in nonergodic systems [31]. Such degeneracy therefore provides a successful explanation for some striking phenomena observed in Refs. [6,7], such as the change in intensity, position and broadness of diffractions peaks over a long time period, or the mismatch between short-range and average crystallographic structures. For instance, it is remarkable that (i) the tilt angle of  $\simeq 3.5^{\circ}$  measured from Rietveld measurement in Ref. [6] nearly coincides with our prediction that the amplitude of the different oxygen octahedral tilts about [001] in all these low-energy nanoscale twinned phases are of the order of 3° [32]; and (ii) that the same experimental study [6] extracted a much larger tilt angle of 8° from (short-range) pair distribution function analysis, while we numerically found that the antiphase tilting angle about [001] in the more simple I4/mcm state is indeed around 8°. Items (i) and (ii) suggest that nanodomains made of I4/mcm and of the more complex twinned AFD phases are both present in bulk ETO. The nanoscale twinned phases are also found to have unusual antiferroelectricity. For instance, the state possessing a mmmppp tilting pattern about [001] and antiphase octahedral tiling about [110] exhibits antiferroelectric displacements for the Eu ions of the type -+0-+0 when moving along adjacent (001) planes and where - and + represent displacement along  $[\bar{1}\ \bar{1}\ 0]$  and [110], respectively, while 0 represents zero displacement. Such antiferroelectricity is therefore associated with a k vector that lies in-between the  $\Gamma$  and X points of the cubic first Brillouin zone. Strikingly, Ref. [7] also invoked unusual antiferroelectric displacements that are consistent with such kind of k point to explain weak intensities in the x-ray spectra of nanoscale twinned tilting phases of bulk ETO. However, antiferroelectricity in Ref. [7] was assumed to be caused by Ti atoms moving along [001] or [001] directions rather than by Eu atoms moving along  $[\bar{1}\ \bar{1}\ 0]$  and [110]. Our prediction of A-driven antiferroelectric, in-plane motions being coupled to out-ofplane complex oxygen octahedra tilt is fully consistent with what is documented in BiFeO<sub>3</sub> systems [33] and with symmetry [34]. We also report, in parentheses in Table I of the Supplemental Material [20], the energies of the simple  $a^-a^-c^-$  (C2/c) and  $a^-a^-c^+$  (Pnma) states as well as the complex  $a^-a^-c^m$  with  $c^m$  corresponding to the mmmppp pattern, when the antiferroelectric displacements of Eu atoms are prevented from occurring (symmetry implies that antiferroelectric motions can exist in the last two phases, but not in the  $a^-a^-c^-$  state [33]). These energies as well as the relaxed ones for these three phases indicate that (1) a pure antiphase tilting about [001]  $(a^-a^-c^-)$  state) is intrinsically of lower energy than a pure in-phase tilting about this direction  $(a^-a^-c^+)$  state), but by a relatively small amount, of the order of 0.9 meV, when Eu antiferroelectric motions are annihilated; (2) the complex tilting pattern has an intermediate energy between those of  $a^-a^-c^-$  and  $a^-a^-c^+$  when Eu antiferroelectric displacements are not incorporated; and (3) phases having in-phase tilting (such as  $a^-a^-c^+$  and  $a^-a^-c^m$ ) can even further decrease their energies via the occurrence of Eu antiferroelectric displacements. Items (1)–(3) therefore explain why nanoscale twinned phases can be of low energy in ETO.

Let us now shift our attention to ETO films that are epitaxially grown along [001]. Mimicking such films consists of imposing that (001) planes all have a square-basis lattice of parameter  $a_{IP}$ , with  $a_{IP}$  having the possibility to vary in order to model the growth of ETO films on different substrates. The misfit strain is defined as  $\eta = \frac{a_{IP} - a_0}{a_0}$ , where  $a_0 = 3.87$  Å is the in-plane lattice constant found for the equilibrium I4/mcm phase of bulk ETO.

Figure 1(a) shows the total energy of "simple" states of (001) ETO film for misfit strain ranging between -8% and 8% (note that the largest investigated strains are likely not achievable in experiments, but their associated structural phases may be found at smaller strains at finite temperature). Using FM or G-type AFM ordering provides similar curve for each of these phases in Fig. 1(a) because of the

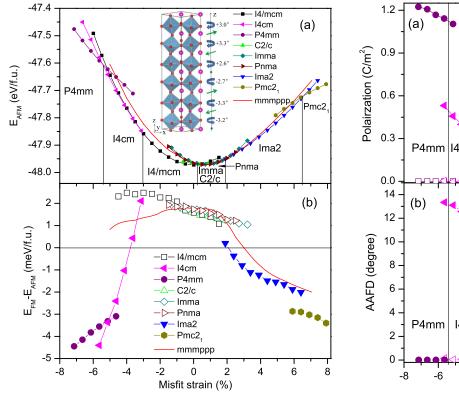


FIG. 1 (color online). Predicted total energy of the G-type AFM state [panel (a)] and energy difference between the G-type AFM and FM states [panel (b)] versus the misfit strain for low-in-energy phases in epitaxial (001) ETO films. The inset of panel (a) displays a schematic of the  $a^-a^-c^m$ -type nanoscale twinned phases possessing the mmmppp tilting pattern. In this inset, the curled and straight arrows represent oxygen octahedra tilting about [001] or  $[00\bar{1}]$  and antiferroelectric Eu displacements, respectively. The different tilting angles about [001] are also provided here.

scale of this figure. To resolve this issue, the energy difference between FM and AFM for each of these crystallographic states is displayed in Fig. 1(b) as a function of misfit strain. Figures 2(a) and 2(b) show Cartesian components of the polarization (as calculated from the modern theory of polarization [35]) and of the antiphase antiferrodistortive (AAFD) vector, respectively, for some of these simple states—while the inset of Fig. 2(b) displays Cartesian components of the in-phase antiferrodistortive (IAFD) vector. Note that the AAFD (respectively, IAFD) vector is defined such that its axis provides the direction about which oxygen octahedra tilt in antiphase (respectively, in-phase), whereas its magnitude provides the angle of such tilting [36]. The x, y, and z axis are along the pseudocubic [100], [010], and [001] directions, respectively. Figures 1(a) and 1(b) also report the strain dependence of the total energy and of the difference in energy between FM and G-type FM states for a particular nanoscale twinned phase. This phase is the one shown in the inset of Fig. 1(a), which possesses a periodic mmmppp tilting pattern along

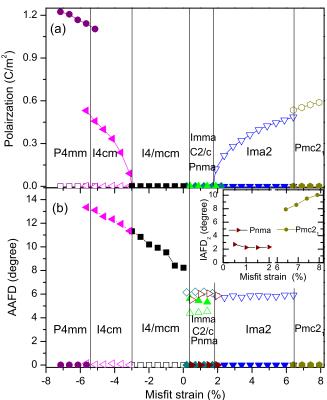


FIG. 2 (color online). Evolution of the polarization [panel (a)] and AAFD vector [panel (b)] with strain for equilibrium phases. The inset of Fig. 2(b) shows the IAFD vector of the Pnma and  $Pmc2_1$  state. Open symbols display the x component (which is identical to the y component) while solid symbols show the z component. For strain ranging between 0.25% and 1.9%, the rhombus, inverted triangles, and triangles correspond to Imma, Pnma, and C2/c states, respectively, in panel (b).

[001] as well as "regular" antiphase octahedral tiling about [110].

Let us first focus on compressive strains. Figures 1(a) and 1(b) indicate that, for  $\eta$  ranging between 0 and -3%, ETO films adopt a tetragonal I4/mcm state, with a G-type AFM ordering between Eu atoms, as its ground state. Such state is paraelectric. On the other hand, this I4/mcm phase possesses a nonvanishing z component of its AAFD vector that increases from  $\sim 8^{\circ}$  to  $\sim 11^{\circ}$  when strengthening the strain from 0 to -3% [see Fig. 2(b)]. At  $\eta = -3\%$ , the epitaxial (001) ETO film then undergoes a second-order phase transition from this I4/mcm phase to a *I4cm* state, which is characterized by the appearance of an out-of-plane component of polarization in addition to the preexisting out-of-plane component of the AAFD vector. Both of these out-of-plane components increase as the magnitude of compressive strain increases from 3% to 5.4%. Strikingly, the I4cm phase adopts an AFM ordering for  $\eta$  ranging between -3% to -3.8%, while it is FM for larger-in-magnitude compressive strain. The magnetic transition therefore occurs at around -3.8%

within the same phase (namely, I4cm). Moreover, at  $\eta = -5.4\%$ , a first-order strain-driven phase transition from this tetragonal FM I4cm phase to a tetragonal FM P4mm phase occurs. In this P4mm state, the AAFD vector is annihilated while the z component of the polarization is large and further increases when the magnitude of compressive strain increases from 5.4% to  $\approx 7\%$ . Some of our results qualitatively agree with those of Ref. [13], namely that (001) ETO films are paraelectric and AFM at small compressive strains while being FE and FM at larger compressive strain.

Let us now turn our attention to (001) ETO films under tensile strain. Figures 1(a) and 1(b) reveal that, when  $0.25\% < \eta < 1.9\%$ , the "simple" orthorhombic *Imma*, *Pnma*, and monoclinic C2/c phases, as well as the mmmppp twinned phase (1) have total energies that are not only lower than that of I4/mcm but are also basically equal to each other; and (2) all adopt a G-type AFM order. The Imma state possesses a significant in-plane, strainindependent AAFD vector, for which the x and y components are equal to each other and are  $\approx 6.2^{\circ}$ . The "simple" C2/c state has both in-plane and out-of-plane components of the AAFD vector. The x and y components of this vector are identical and equal to 4.5° at 0.25% tensile strain, and slightly increases with  $\eta$ . On the other hand, the out-ofplane component of the AAFD vector is about 5.5° and decreases with the tensile strain. Moreover, the *Pnma* state possesses in-plane components of the AAFD vector of about 6° and an out-of-plane component of the IAFD vector of 2.5° in this strain region. We also numerically found (not shown here) that, in the mmmppp nanoscale twinned phase, the antiphase octahedral tiling about [110] are quantitatively unchanged, while the local angle in the complex tilting pattern about [001] decreases from  $\sim$ 3° to  $\sim 2^{\circ}$  and the antiferroelectric displacements grow when increasing the tensile strain from 0.25% to 1.9%.

For  $\eta$  ranging between 1.9% and 6.5%, the ground state of (001) epitaxial ETO films becomes orthorhombic Ima2 and is now FM. It exhibits a polarization aligned along the in-plane [110] direction that increases in magnitude as the strain increases from +1.9% to +6.5%. Our calculations thus reproduce previous results [2] that a large-enough tensile strain can induce a phase that is FE and FM while (001) ETO films under very small strain are paraelectric and AFM [37].

At the tensile strain of 6.5%, (001) ETO films undergo a first-order phase transition from Ima2 to a state of  $Pmc2_1$  symmetry. Such a state has also been found in BiFeO<sub>3</sub> and PbTiO<sub>3</sub> films [38]. As in Ima2, it possesses an in-plane polarization along [110] and is FM. However, unlike Ima2, the  $Pmc2_1$  state has a vanishing AAFD vector while exhibiting OOT being in-phase about the z axis. The resulting tilting angle has a magnitude of  $\approx$  8° near the transition, that further increases with the tensile strain. We also found (not shown here) that  $Pmc2_1$  has in-plane, zigzag pattern

for the Eu (or Ti) atoms belonging to any (001) plane [38], and exhibits orbital ordering between the f electron of Eu atoms.

In summary, this Letter provides a successful explanation for observed anomalies in bulk ETO (via the existence of a family of degenerate, nanoscale twinned phases), and revisits the phase diagram of epitaxial ETO films. Interestingly, nanoscale twinned phases have been observed in NaNbO<sub>3</sub> [39–42], AgNbO<sub>3</sub> [43], and (Ca, Sr)TiO<sub>3</sub> [44], and have also been predicted in BiFeO<sub>3</sub>-based systems [33]. It is also likely plausible that they can explain unusual phenomena that have been reported in the (Na, Bi)TiO<sub>3</sub> and (Na, Bi)TiO<sub>3</sub>-BaTiO<sub>3</sub> lead-free materials [45]. These complex twinned phases may thus constitute a general but typically overlooked feature of perovskites.

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Note added in proof.—We recently became aware of an article discussing OOT in ETO [46]. Some results of Ref. [46] (e.g., the strain dependency of the energy of the *I4/mcm* and *Imma* phases) are consistent with our findings.

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