

Successive Magnetic Phase Transitions and Multiferroicity in the Spin-One Triangular-Lattice Antiferromagnet $\text{Ba}_3\text{NiNb}_2\text{O}_9$

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We report the magnetic and electric properties of $\text{Ba}_3\text{NiNb}_2\text{O}_9$, which is a quasi-two-dimensional spin-one triangular-lattice antiferromagnet with trigonal structure. At low T and with increasing magnetic field, the system evolves from a 120 degree magnetic ordering phase (A phase) to an up-up-down (uud) phase (B phase) with a change of slope at $1/3$ of the saturation magnetization, and then to an “oblique” phase (C phase). Accordingly, the ferroelectricity switches on at each phase boundary with appearance of spontaneous polarization. Therefore, $\text{Ba}_3\text{NiNb}_2\text{O}_9$ is a unique triangular-lattice antiferromagnet exhibiting both uud phase and multiferroicity.

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The two dimensional (2D) triangular lattice antiferromagnet (TLAF) is one of the simplest possible geometrically frustrated spin systems [1]. When the value of the spin is small, $S = 1/2$ or 1, in addition to frustration, there are strong quantum spin fluctuations at low temperatures that lead to exotic ground states [2]. One celebrated example is the unusual spin up-up-down (uud) ground state. Theories have predicted that quantum fluctuations should stabilize the uud state in spin-1/2 TLAFs [3–5]. In this collinear state, the low temperature magnetization is constant over a finite range of the magnetic field and equal to $1/3$ of the saturation magnetization M_s . Experimentally, Cs_2CuBr_4 is a rare example of spin-1/2 TLAF, in which the uud state occurs [6,7]. Recently, the $1/3 M_s$ magnetization plateau has been observed for $\text{Ba}_3\text{CoSb}_2\text{O}_9$, another TLAF with effective spin-1/2 [8]. The only reported spin-one TLAF exhibiting $1/3 M_s$ is $\text{Ba}_3\text{NiSb}_2\text{O}_9$ [9]. Searching for new TLAFs with magnetization plateaus is still a very active topic in condensed matter physics.

Another interesting property of TLAFs is multiferroicity, in which the magnetic and electric degrees of freedom [10,11] are strongly coupled. The multiferroicity has been observed in TLAFs with a 120 degree magnetic ordering phase for classical spins, such as ACrO_2 ($\text{Cr}^{3+} S = 3/2$, $A = \text{Ag}$ and Cu) [12,13] and $\text{RbFe}(\text{MO}_4)_2$ ($\text{Fe}^{3+} S = 5/2$) [14]. The study on $\text{RbFe}(\text{MO}_4)_2$ also shows that the ferroelectricity disappears in the uud phase, which is stabilized by the thermal fluctuations. The theory for multiferroicity in TLAFs is still under development [15], since the well established theories, such as the spin current model or the inverse Dzyaloshinskii-Moriya model, do not predict ferroelectricity in TLAFs [16–18]. However, it has been predicted that a broad range of trigonal materials with the 120 degree spin structure could be multiferroic, since both ACrO_2 and $\text{RbFe}(\text{MO}_4)_2$ have trigonal structure.

So far, no other TLAFs with trigonal structure and 120 degree spin structure were found to be multiferroic to further confirm this prediction. Also, no TLAFs with quantum spins ($S = 1/2$ or 1) have been reported to show multiferroicity. Moreover, the coexistence of the uud phase and multiferroicity has not been reported in any TLAF. Here, we report detailed magnetic and electric property studies on new spin-one TLAF with trigonal structure, $\text{Ba}_3\text{NiNb}_2\text{O}_9$ (Ni^{2+} has $S = 1$). We observed successive magnetic phase transitions at $1/3$ and $\sqrt{3}/3$ of the saturation magnetization, which are also accompanied by spontaneous reversible polarization and dielectric anomalies. Although a distinctive magnetization plateau was not observed due to the polycrystallinity and the finite temperature, our results strongly suggest that the title compound is a rare example of TLAF with coexistence of collinear magnetic structure and multiferroicity.

Polycrystalline $\text{Ba}_3\text{NiNb}_2\text{O}_9$ samples were prepared by solid state reaction. Appropriate mixtures of BaCO_3 , NiO , and Nb_2O_5 were ground together, pressed into pellets, and then calcined in air at 1230°C for 24 hours. The room temperature powder x-ray diffraction (XRD) pattern [Fig. 1(a)] of the as-prepared sample can be indexed as a hexagonal $P-3m1$ structure with $a = b = 5.7550(5)$ Å and $c = 7.0656(2)$ Å as reported previously [19], which belongs to the trigonal space group. The 1:2 ordering of the B site ions ($-\text{Ni}-\text{Nb}-\text{Nb}-$) in this structure has been confirmed by two evidences: (i) the appearance of low intensity Bragg peaks in the XRD pattern related to the ordering structure [20], such as the (112) and (103) peaks [inset of Fig. 1(a)], and (ii) the high angle annular dark field Z -contrast image from scanning transmission electron microscopy (STEM) [Figs. 1(c) and 1(d)]. The intensity of the Nb and Ni atom columns in the image clearly shows the $-\text{Ni}-\text{Nb}-\text{Nb}-$ ordering viewed down the [010] direction

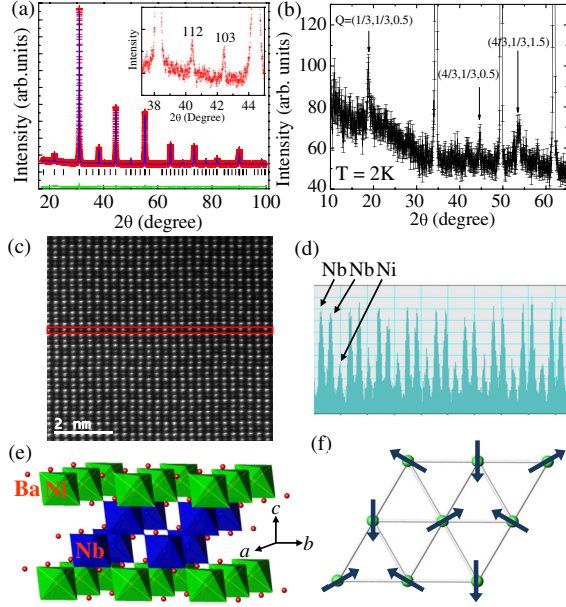


FIG. 1 (color online). (a) The room temperature XRD pattern (Cu $K_{\alpha 1}$ $\lambda = 1.54059$ Å) for $\text{Ba}_3\text{NiNb}_2\text{O}_9$ (plus marks). The solid curve is the best fit from the Rietveld refinement using FULLPROF. Inset: the (112) and (103) peaks from the XRD pattern. (b) The neutron diffraction pattern measured using the neutron powder diffractometer HB2A at ORNL showing several magnetic Bragg reflections at 2 K. (c) Atomic resolution STEM high angle annular dark field Z-contrast image looking down [010]. Ba, Nb, and Ni atoms show brightest, brighter, and weak contrast, respectively. (d) Line profile of the atomic columns indicated by the box in (c) showing the ordering sequence of -Ni-Nb-Nb-. (e) Schematic crystal structures for $\text{Ba}_3\text{NiNb}_2\text{O}_9$: the green octahedra represent Ni sites and the blue octahedra represent Nb sites. (f) Zero field magnetic structure below T_{N1} composed of Ni^{2+} ions and the arrows representing their spins.

due to their atomic number Z difference [21,22]. No defects are seen on the Ni or Nb sites. We noticed that with the annealing temperature above 1230 °C, the sample will turn out to be $\text{Ba}(\text{Ni}_{0.33}\text{Nb}_{0.67})\text{O}_3$ with B -site disorder and $Pm-3m$ cubic structure. With the $P-3m1$ structure, $\text{Ba}_3\text{NiNb}_2\text{O}_9$ can be represented as a framework consisting of corner-sharing NiO_6 and NbO_6 octahedra [Fig. 1(e)]. The Ni ions occupy the $1b$ Wyckoff sites, and this site forms the triangular lattice in the ab plane [Fig. 1(f)]. Therefore, the structure can be regarded as a pseudo-two-dimensional triangular magnet; i.e., the Ni magnetic triangular lattices are magnetically separated by the two nonmagnetic Nb layers.

The susceptibility χ measured at $H = 0.1$ T [Fig. 2(a)] shows a peak around 4.9 K related to the long range magnetic ordering. The linear Curie-Weiss fit of $1/\chi$ at high temperature (not shown here) gives a $\theta_{\text{CW}} = -16.4$ K, showing the antiferromagnetic nature of the exchange interactions and an effective moment $\mu_{\text{eff}} = 3.15 \mu_{\text{B}}/\text{Ni}$, which corresponds to a Landé g factor of $g = 2.23$ and is

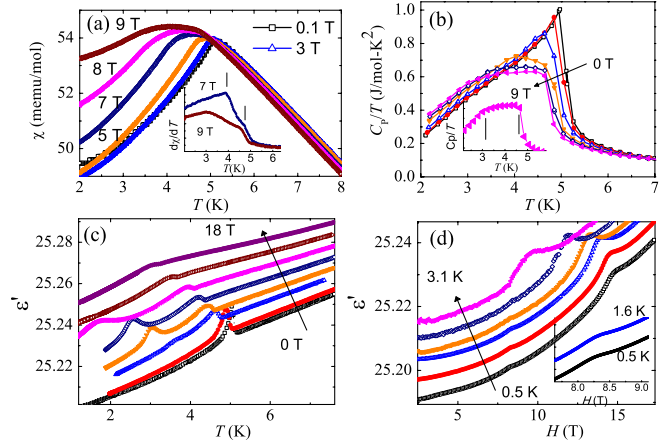


FIG. 2 (color online). (a) Temperature dependence of χ for $\text{Ba}_3\text{NiNb}_2\text{O}_9$ at different fields. Inset: $d\chi/dT$ vs T for $H = 7$ and 9 T. (b) Temperature dependence of C_p/T at 0, 3, 5, 7, 8, and 9 T. Inset: Expansion of the 9 T data. (c) Temperature dependence of ϵ' at 0, 4, 8, 10, 12, 14, 16, and 18 T, and (d) magnetic field dependence of ϵ' at 0.5, 0.9, 1.6, 2, 2.6, and 3.1 K. Inset: Expansion around $H = 8$ T for 0.5 and 1.6 K (data is offset for clarity). The vertical lines in (a) and (b) indicate T_{N1} (higher T) and T_{N2} (lower T).

typical for Ni^{2+} ions [23]. Assuming that each Ni^{2+} spin only interacts via exchange J with the $z = 6$ nearest neighbor spins on the triangular lattice, the Heisenberg Hamiltonian is $J\sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j$. In mean-field theory, this leads to a Curie-Weiss law with $\theta_{\text{CW}} = -zJS(S+1)/3k_{\text{B}}$. For $\text{Ba}_3\text{NiNb}_2\text{O}_9$, $S = 1$ and $J/k_{\text{B}} = -1/(4\theta_{\text{CW}}) = 4.1$ K. The neutron diffraction pattern measured at 2 K [Fig. 1(b)] shows magnetic Bragg peaks at $Q = (n_1 + 1/3, 1/3, n_2 + 1/2)$ (n_i : integer). Accordingly, its refinement (not shown here) reveals a magnetic structure with collinear antiferromagnetic (AFM) spins between the nearest neighbor layers and the 120 degree AFM ordering within the triangular lattice with an ordered moment of $1.8 \mu_{\text{B}}$ for each Ni^{2+} ion. This refinement also shows a B site ordered $P-3m1$ lattice structure at 2 K, which means there is no obvious structural distortion below 4.9 K.

For $H > 5$ T, the peak of the susceptibility χ becomes broader [Fig. 2(a)] and the related $d\chi/dT$ vs T curves display two peaks [inset of Fig. 2(a)]. We define T_{N1} and T_{N2} by the locations of the higher and lower temperature peaks, respectively. Below 9 T, both T_{N1} and T_{N2} decrease with increasing field. The zero field specific heat data [Fig. 2(b)] show a single peak around T_{N1} . For $H > 5$ T, this peak becomes broader and could be regarded as two peaks as indicated by lines in Fig. 2(b) for 9 T. Their locations are consistent with those of T_{N1} and T_{N2} defined from $d\chi/dT$.

Samples with rectangular shape with typical dimensions of $5.0 \times 4.0 \times 0.15 \text{ mm}^3$ were cut from the pressed pellet to measure the dielectric constant and the pyroelectric current using the techniques found elsewhere [24]. The real part of the dielectric constant (ϵ') measured at zero

field [Fig. 2(c)] shows a sharp peak at T_{N1} . With increasing field, this peak shifts to lower temperatures and becomes broader. For $H > 8$ T, a second peak well separated from the first peak appears at lower temperatures. The field dependence of ϵ' measured at 0.5 K shows two peaks around 8 and 15 T, respectively [Fig. 2(b)]. With increasing temperature, the peak around 8 T does not move significantly while the peak around 15 T moves to lower fields. The two peaks tend to merge at about 3 K.

The pyroelectric current was measured on warming after poling the crystal in an electric field while cooling down from above T_{N1} with magnetic field (FC) or without magnetic field (ZFC). The spontaneous polarization was obtained by integrating the pyroelectric current with respect to time. At zero magnetic field, the pyroelectric current, and accordingly the spontaneous electric polarization, begin to develop below T_{N1} [Fig. 3(a)]. With opposite poling electric field, the pyroelectric current direction can be reversed [Fig. 3(c)]. This indicates the ferroelectric (FE) nature of the ground state, which is clearly coupled with the 120 degree magnetic ordering. The obtained polarization is around $1.1 \mu\text{C}/\text{m}^2$ at 0 T. The polarization overall decreases and shifts to lower temperatures with increasing magnetic field [Fig. 3(b)], which is consistent with the behavior observed for the higher temperature peak in ϵ' . For the polarization emerging at T_{N1} , there is no difference between the ZFC and FC measurements.

For $H \geq 8$ T another peak of the pyroelectric current (or another steplike increase of the polarization) is found at the same temperature where the lower temperature peak of ϵ' is observed. Note that this low temperature polarization increase is observed only when the sample is cooled under the presence of *both*, magnetic and electric, fields, i.e., after

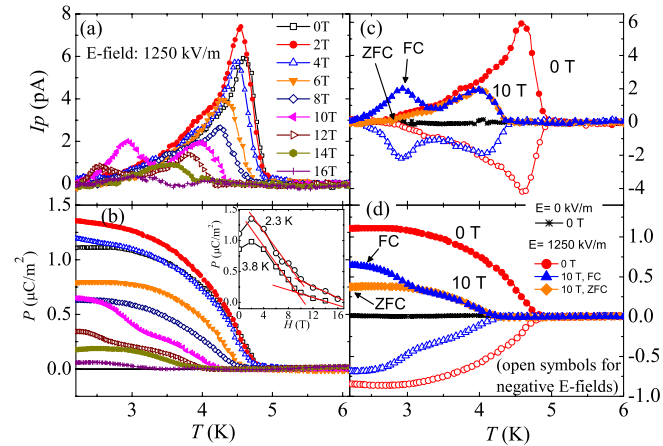


FIG. 3 (color online). Pyroelectric current (I_p) (a) and polarization (b) as a function of temperature at different magnetic fields under positive electric poling field and FC conditions. The inset of (b) shows polarization vs magnetic field at 2.3 and 3.8 K under ZFC conditions. I_p (c) and polarization (d) at $H = 0$ and 10 T under positive (solid symbols) and negative (open symbols) poling fields and ZFC and FC conditions.

magnetoelastic (ME) annealing. For example, the lower temperature peak for the pyroelectric current disappears for the ZFC measurement, as seen in Fig. 3(c) for the 10 T data. For some ME systems, the reversible pyroelectric peak is also observed under ME annealing without invoking a ferroelectric transition as a consequence of the combined effects of magnetic domains and the ME effect [24–26]. Therefore, the additional increase of the polarization and the low temperature ϵ' anomaly are more likely to arise from a magnetoelastic mechanism, rather than from another FE transition with a different order parameter.

Combining all the values for the transition temperatures and critical magnetic fields observed from the various techniques described above, the low temperature H - T phase diagram for $\text{Ba}_3\text{NiNb}_2\text{O}_9$ shown in Fig. 4(c) is obtained. Below 4.9 K and with increasing magnetic field, at least three magnetic phases [labeled as A, B, and C in Fig. 4(c)] are consistently observed. In the A phase, the spins form the 120 degree coplanar AFM ordering at zero field. Under small external magnetic fields, the order in the A phase is expected to gradually deviate from the 120 deg structure while maintaining a similar degree of continuous degeneracy [27]. At higher fields, as the theories predict [3–5], for an AFM triangular lattice, the quantum fluctuations for small spins can lift the classical degeneracy in the A phase to select the B phase. We tentatively assign the uud state with a $1/3 M_s$ magnetization plateau stabilized in a finite magnetic field range to the B phase [3–5].

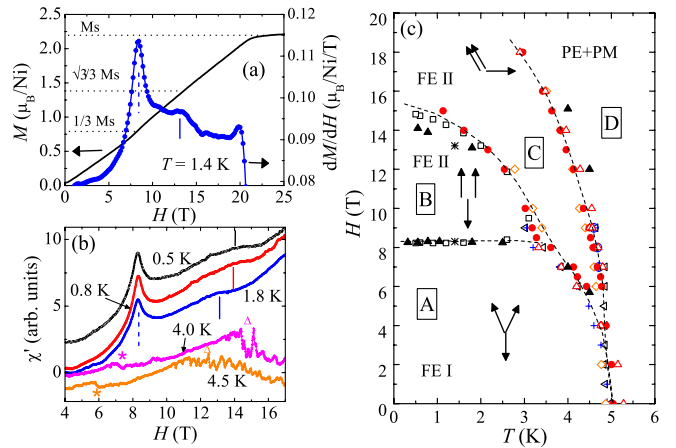


FIG. 4 (color online). (a) dc magnetization (M) and its derivative (dM/dH) for $T = 1.4$ K. (b) ac susceptibility as a function of magnetic field H for four temperatures. The asterisks and the triangles indicate A-C and C-D phase boundary respectively. (c) H - T phase diagram for $\text{Ba}_3\text{NiNb}_2\text{O}_9$. Different symbols denote phase boundaries obtained from different techniques. \square : ϵ' H -sweep, \bullet : ϵ' T -sweep, \diamond : polarization, \triangleleft : C_p , \blacktriangle : ac susceptibility H -sweep, \triangle : ac susceptibility T -sweep, \oplus : dc susceptibility T_{N1} , $+$: dc susceptibility T_{N2} , $*$: dc magnetization. The arrows indicate spin structures. The dashed (solid) vertical lines in (a) and (b) indicate the transition fields to uud (oblique) phases. The dashed lines in (c) are guides to the eyes.

In order to examine the possibility of the magnetization plateau in the B phase, the dc magnetization and ac susceptibility (χ') were measured. As seen in Fig. 4(a), the dc magnetization saturates around 23 T with $M_s = 2.2 \mu_B$. A slope change of M vs H around 8 T is observed, at which the magnetization is $0.77 \mu_B \approx 1/3 M_s$. Experimentally, the dM/dH curve shows a distinctive feature characterized by a broad valley in the magnetization plateau region and a sharp peak and a broad shoulder, respectively, on entering and exiting the putative plateau region [8,9,28]. In $\text{Ba}_3\text{NiNb}_2\text{O}_9$, the most distinctive feature (valley) is not apparent in the dM/dH curve as a consequence of the lack of the plateaulike magnetization. On the other hand, the χ' measurement, being a technique to probe dM/dH directly, revealed all the features as shown in Fig. 4(b): a dominant peak at 8 T followed by a broad valley at 9 T and a broad shoulderlike peak at around 14 T. However, the χ' at the valley is not the smallest as the overall χ' increases with the field. There are two possible reasons why the magnetization plateau was not clearly observed: (a) the polycrystalline nature of our sample and (b) that even in a single crystal, the plateau is manifested only in certain directions of the field with respect to the crystalline axes.

The 14 T feature is also seen in dM/dH as a broad peak, where the magnetization is approximately $\sqrt{3}/3 M_s$ [Fig. 4(a)]. This suggests the 14 T feature is due to the transition from the uud to a coplanar 2:1 canted oblique phase (C phase) with one spin in the A phase rotated to be parallel with another spin, which gives $\sqrt{3}/3 M_s$. We emphasize here that our spin structure model in the oblique phase is based on the magnetization data and more rigorous experiments like neutron diffraction should be performed to confirm the structure. In general, the spin structure in the oblique phase, a generic term for a spin structure with two parallel spins tilted with respect to the third, is unique to each TLAF system depending on the magnitude of the spin and hence on the order of the fluctuations. It is noteworthy that our suggested 2:1 canted spin structure is the same as that of $\text{RbFe}(\text{MO}_4)_2$ under a 10 T in-plane magnetic field, which was confirmed by neutron experiments [see Fig. 1(d) of Ref. [14]]. At higher temperatures, the χ' data also show features [indicated as asterisks and triangles in Fig. 4(b)] at the phase A - C and C - D (paramagnetic phase) phase boundaries. These experimental observations clearly suggest that $\text{Ba}_3\text{NiNb}_2\text{O}_9$ evolves through successive magnetic phase transitions from the A phase to uud (B) phase and then to oblique (C) phase with the increasing magnetic field. Whether a magnetization plateau should exist in the B phase is still an open question. Experiments performed on single crystal samples with in-plane magnetic fields at lower temperatures are expected to reveal the existence of the magnetization plateau more clearly.

For TLAFs with classical spins, thermal fluctuations stabilize the uud phase at finite temperatures showing a plateaulike magnetization; hence, the magnetic field range

of the uud phase decreases with decreasing temperature. In $\text{Ba}_3\text{NiNb}_2\text{O}_9$, the uud phase has a range of about 8 T even at 0.5 K ($\ll T_{\text{Ni}}$) and the width of the uud phase increases with decreasing temperature. This suggests that the uud phase has a quantum mechanical origin due to the small spin $S = 1$ for Ni^{2+} . This makes $\text{Ba}_3\text{NiNb}_2\text{O}_9$ a rare $S = 1$ TLAF showing a uud phase driven by quantum fluctuations. Another noteworthy feature in the phase diagram of $\text{Ba}_3\text{NiNb}_2\text{O}_9$ is that within a narrow temperature window, $3.5 \text{ K} < T < 4.5 \text{ K}$, with increasing field the spin configuration goes from the A phase to the C phase directly without passing through the B phase (see online Supplemental Material for details [29]). This is significantly different from the other TLAF systems with an uud phase mentioned in the introduction, either for classical or quantum spins. For those systems, in order to reach the C phase from the A phase with increasing field, it is always necessary to pass through the B phase. To our knowledge, so far no theory predicts this feature and we leave the explanation for it as an open question for future investigations.

More interestingly, as the polarization measurements show, all these three magnetic phases have a FE ground state. Studies of multiferroic properties of TLAFs have so far been limited to systems with classical spins. Two celebrated examples are (i) ACrO_2 ($A = \text{Cu}$ and Ag) with trigonal $R\bar{3}m$ structure, and (ii) $\text{RbFe}(\text{MO}_4)_2$ with trigonal $P\bar{3}m$ structure. It has been proposed that the ferroelectricity in ACrO_2 is driven by the helical spin-spiral order of the Cr^{3+} ($S = 3/2$) spins among the stacked Cr layers [15]. The zero field magnetic structure of $\text{RbFe}(\text{MO}_4)_2$ has AFM spins between the nearest neighbor layers and a 120 degree AFM ordering within the triangular layers. A phenomenological model based on symmetry arguments (the broken inversion symmetry and the absence of a mirror plane perpendicular to the c axis) was proposed to explain the ferroelectricity in the A phase for $\text{RbFe}(\text{MO}_4)_2$ [14]. A similar situation could lead to the ferroelectricity in the A phase for $\text{Ba}_3\text{NiNb}_2\text{O}_9$, since the two Nb layers between the adjacent Ni layers lead to the absence of a mirror plane perpendicular to the c axis [Fig. 1(e)]. Although a smaller polarization, $P = 1.1 \mu\text{C}/\text{m}^2$, was observed due to the polycrystalline nature of $\text{Ba}_3\text{NiNb}_2\text{O}_9$, its value is still comparable to that of $\text{RbFe}(\text{MO}_4)_2$ obtained with single crystal samples.

A difference between $\text{RbFe}(\text{MO}_4)_2$ and $\text{Ba}_3\text{NiNb}_2\text{O}_9$ is the electric ground state at higher magnetic fields. In $\text{RbFe}(\text{MO}_4)_2$, the ferroelectricity disappears in the B phase (uud phase), which was interpreted as the inversion symmetry in the triangular uud magnetic structure being reinstated. In contrast, the ferroelectricity persists in the uud and the oblique phases of $\text{Ba}_3\text{NiNb}_2\text{O}_9$. The inset of Fig. 3(b) shows the magnetic field dependence of the polarization at 2.3 and 3.8 K obtained from the pyroelectric current measurement under ZFC. The polarization increases initially up to $H = 2$ T followed by a monotonic decrease with the increasing magnetic field up to 9 T. Then, there is a change

of curvature around 9 T, above which the polarization is larger than the projected value extrapolated from the linear behavior of the lower magnetic fields. This behavior suggests that the mechanism for the FE state in B and C phases is different from that for the A phase under lower magnetic fields.

One possible explanation for the FE phase at high magnetic fields in $\text{Ba}_3\text{NiNb}_2\text{O}_9$ is that the inversion symmetry is broken by deforming the triangular lattice via magnetostriction. In the triangular spin structure, magnetostriction driven by spin correlation ($\mathbf{S}_i \cdot \mathbf{S}_j$) cannot break the inversion symmetry, but the anisotropic magnetostriction driven by external magnetic fields can. In the distorted triangular lattice, the space inversion and the threefold rotation are not symmetric operations any more, which can lead to finite polarization in the ab plane (see online Supplemental Material for details [29]). Magnetostriction often plays an important role in inducing magnetic multiferroicity [30,31]. The polarization values close to the B - C phase boundary at fixed T are too small to draw any conclusions, but the continuous polarization increase with decreasing temperature while crossing the B - C boundary at fixed magnetic fields under the ZFC condition [Fig. 3(d)] suggests that the FE order parameter is same in the B and C phases. From these observations, we speculate that the magnetostriction starts to play an important role in inducing ferroelectricity at high magnetic fields (B and C phases), while the spin chirality in the A phase is the driving force of the multiferroicity at low magnetic fields.

In summary, although more work is needed to confirm the magnetic structure of the A , B , and C phases, the detailed magnetic and electric studies on $\text{Ba}_3\text{NiNb}_2\text{O}_9$ reveal that the system (i) is a new spin-one TLA system showing two magnetic phase transitions bracketing an intermediate up-up-down phase driven by quantum fluctuations, and (ii) is a multiferroic system with FE ground states stabilized at all three magnetic phases. These findings show that $\text{Ba}_3\text{NiNb}_2\text{O}_9$ is a rare TLA with strong couplings between the successive magnetic phase transitions and the ferroelectricity. One step further, we also confirmed the prediction that a broad range of trigonal materials with the 120 degree spin structure can be multiferroic.

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