Role of the Fermi-Surface Anisotropy in Angle-Dependent Magnetic-Field Oscillations for Identifying the Energy-Gap Anisotropy of A_vFe₂Se₂ Superconductors

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We present a numerical study of the field-angle resolved oscillations of the thermal conductivity and specific heat under a rotated magnetic field in the $A_y \text{Fe}_{2-x} \text{Se}_2$ [A = K, Rb, Cs, (Tl, K)] superconductors, using realistic two-band Fermi surface parametrization. Our key finding is that even for isotropic pairing on an anisotropic Fermi surface, the thermodynamic quantities exhibit substantial oscillatory behavior in the superconducting state, even much below the upper critical field. Furthermore, in multiband systems the competition of anisotropies between two Fermi surfaces can cause a double sign reversal of oscillations as a function of temperature, irrespective of gap anisotropy. Our findings put severe constraints on simple interpretations of field-angle resolved measurements widely used to identify the angular structure of the superconducting gap.

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The identification of the symmetry of the superconducting (SC) order parameter (OP) an important step toward unraveling the pairing mechanism in any novel superconductor. For iron pnictides, the presence of hole and electron pockets at the Γ and *M* points has led to the proposal of s^{\pm} -wave pairing [1–4] due to interband nesting between them. However, the recent discovery of the layered high-temperature superconductors $A_v \operatorname{Fe}_{2-x} \operatorname{Se}_2$, with A = K, Rb, Cs, (Tl, K), has challenged the consensus for the pairing symmetry and mechanism of superconductivity in this class of materials [5]. The iron-selenide family has a crystal structure similar to the iron-pnictide material BaFe₂As₂, but with hole pockets eliminated completely from the Fermi surface (FS) at the Γ point in the Brillouin zone, yet the SC transition temperature T_c is comparable to that of iron pnictides. Various theoretical proposals have been put forward which support either the survival of s-wave pairing [6-8], the emergence of nodal d-wave gap [9,10], or more popularly nodeless d-wave gap [11–14]. Indirect experimental evidence suggests isotropic pairing symmetry [15–17], consistent with isotropic gaps reported in angle-resolved photoemission spectra [18,19]. Therefore, direct high-precision imaging of the structure of the gap function and the location of the nodes, if they exist, is required. An effective and accurate technique for measuring the angular structure of the bulk gap relies on probing thermodynamic properties in a rotating in-plane magnetic field. For cuprate, pnictide, and heavy-fermion superconductors, this technique has been used widely to identify the SC pairing symmetry by mapping the field-angle dependence of the thermal conductivity or specific heat onto the angular structure of the SC gap and its pairing symmetry [20-31].

In this Letter, we demonstrate that detailed knowledge of the FS topology and parameters is necessary for relating the nature of the oscillations to the nodes or minima of the gap structure. This is especially important for materials where the FS anisotropy is substantial, as is the case in layered iron selenides. To be quantitative and unambiguous about the shape of the SC gap, it is required to incorporate realistic FS topology, Fermi velocities, and density of states (DOS) at the Fermi level into self-consistent calculations of thermal properties.

To accomplish this goal, we focus on layered iron-selenide superconductors and study the information embedded in the angle-resolved specific heat coefficient, $\gamma = C/T$, and thermal conductivity, κ , in a rotating in-plane magnetic field using realistic tight-binding dispersions derived from firstprinciples electronic structure calculations. The main results of our calculations are: (1) For purely isotropic pairing symmetry, moderate FS anisotropies of layered iron-selenide superconductors are sufficient to introduce field-angledependent oscillations in the specific heat and thermal conductivity over a significant range of temperatures and at intermediate to high magnetic fields in the SC state. We find an inversion of the oscillation pattern as a function of temperature, which shows that oscillations are not a simple consequence of the anisotropy of the upper critical field. Therefore, not all such oscillations at intermediate fields can be taken as proof of strong anisotropy in the SC gap. (2) For isotropic gaps on the FSs, the oscillations in γ may change sign once or twice as a function of temperature. We identify the out-of-phase FS anisotropies between bands as the source for two sign reversals. (3) Complex field-angle dependence of the specific heat and thermal conductivity for anisotropic FSs suggests that comparison of both quantities with material-specific theories is needed to identify the pairing symmetry and gap structure.

Anisotropy in FS and SC gap.—In the iron selenides the Fe vacancy completely eliminates the hole pocket at the Γ

point, and the FS consists of two concentric electron pockets at the M point in the 2-Fe unit cell. This picture follows from first-principles calculations [32] and photoemission spectroscopy [18,19]. Here, we use a first-principles derived tight-binding parametrization of the electronic dispersion [13] with a weak k_z dispersion as input to obtain all necessary FS parameters for a self-consistent transport calculation. Cuts of the corresponding FSs are shown in Fig. 1(a) with calculated normal-state DOS in Fig. 1(b) and moderately anisotropic Fermi velocities in Fig. 1(c). These figures demonstrate the out-of-phase in-plane anisotropies of the FS parameters on the electron pockets at the M points.

We consider three nodeless gaps with $s, s^{\pm} = \cos k_x a + \cos k_y a$, and extended $\tilde{d}_{xy} = \sin(k_x a/2) \sin(k_y a/2)$ symmetry, shown in Fig. 1(d). Since the FSs are centered around $M = (\pi, \pi, 0)$, and its equivalents, all three including \tilde{d}_{xy} are nodeless on the FS [13]. As all nodeless gaps exhibit very similar behavior, we show detailed results only for the isotropic pairings s. For the nodal SC gaps, we consider two pairings symmetries as $d_{x^2-y^2} = \cos k_x a - \cos k_y a$ and $d_{xy} = \sin k_x a \sin k_y a$, with detailed results presented for $d_{x^2-y^2}$ pairing. The gap structure for each pairing on the FSs is demonstrated in details in the Supplemental Material [33].

Brandt-Pesch-Tewordt approximation.—We solve the quasiclassical Eilenberger equation within the extended Brandt-Pesch-Tewordt approximation [31,34–40] to solve for the field-angle-induced SC DOS, $N_n(\omega, k_F; H)$, together with the self-consistency equations for the SC order parameter, $\Delta_n(\mathbf{k}_F; \mathbf{H})$, and transport lifetime, $\tau_n(\omega, \mathbf{k}_F; \mathbf{H})$. Here **H** is the magnetic field applied at angle α with respect to the (100) direction, k_F is Fermi momentum and n = 1, 2 is the band index. The transport lifetimes encode the combined effects of impurity and vortex scattering. The Brandt-Pesch-Tewordt approximation implies that the DOS is obtained by averaging the normal quasiparticle Green's function over the unit cell of the Abrikosov vortex lattice. This produces quantitatively correct results near the upper critical field over the range $0.5H_{c2} \leq H < H_{c2}$ [38,41,42] for isotropic gap, but it extends to low fields for nodal and strongly anisotropic gaps [31,40,43]. The SC gaps are evaluated by solving the coupled BCS gap equations for $\Delta_n(\mathbf{k}_F; \mathbf{H})$ at each applied field H. We simplify the problem by considering interband pairing only and eliminate the pairing potential in favor of the bare transition temperature T_{c0} within weak-coupling theory [34]. Details of the calculations are given in the Supplemental Material [33].

Based on the above-mentioned self-consistent solutions, the specific heat, *C*, and thermal conductivity, κ , are computed numerically from the solution of the Eilenberger equations [35,36]. However, to get a qualitative understanding of how the interplay of FS anisotropy and gap anisotropy contribute to the results of $C = C_1 + C_2$ and

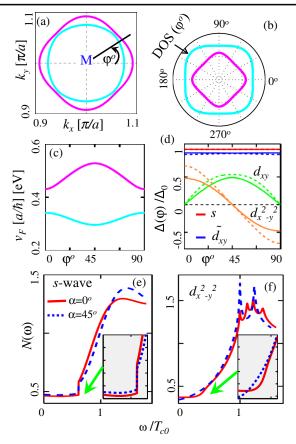


FIG. 1 (color online). (a) Different colored lines show different electron-pockets at $k_z = 0$ within the tight-binding model of the 2-Fe unit cell [13]. (b) Polar plots of computed normal-state DOS at the Fermi level show the out-of-phase anisotropy between bands [same color as in (a)]. (c) The tight-binding in-plane Fermi velocities at $k_z = 0$ vs azimuthal FS angle ϕ exhibit out-of-phase FS anisotropy in units of lattice parameter *a*. (d) Gap functions $\Delta_n(\phi)$ on FS1 (solid line) and FS2 (dashed line) for pairing symmetries considered. The nodeless states have negligible FS anisotropy. (e), (f) field-induced total SC DOS at T = 0 vs energy at two representative field-angles α for *s* and $d_{x^2-y^2}$ -pairing. Note the low-energy crossings in the DOS (arrows) related to the low-*T* sign reversals in the oscillations of γ and κ ; we used $H/H_{c2} = 0.5$ for *s*-wave and 0.1 for $d_{x^2-y^2}$ -wave.

 $\kappa = \kappa_1 + \kappa_2$, we write down the approximate low-*T* expressions:

$$C_n(\alpha) \approx \int_{-\infty}^{\infty} d\omega \frac{\omega^2 \langle N_n(\omega, \mathbf{k}_F; \mathbf{H}) \rangle_{\rm FS}}{4T^2 \cosh(\omega/2T)^2}, \qquad (1)$$

$$\kappa_n^{xx}(\alpha) \approx \int_{-\infty}^{\infty} d\omega \frac{\omega^2 \langle v_n^x(\boldsymbol{k}_F)^2 N_n(\omega, \boldsymbol{k}_F; \boldsymbol{H}) \tau_n(\omega, \boldsymbol{k}_F; \boldsymbol{H}) \rangle_{\text{FS}}}{2T^2 \cosh(\omega/2T)^2}.$$
(2)

The angle-dependent SC DOS is given by the unitcell averaged quasiclassical retarded Green's function g_n : $N_n(\omega, \mathbf{k}_F; \mathbf{H}) = -N_{fn}(\mathbf{k}_F) \text{Im} g_n(\omega, \mathbf{k}_F; \mathbf{H})/\pi$. Here $\langle \ldots \rangle_{\text{FS}}$ stands for the FS integrals and \boldsymbol{v}_n is the Fermi velocity in each band, see Fig. 1(c). In the normal state the DOS becomes $N_n(\omega, \boldsymbol{k}_F; \boldsymbol{H}) = N_{Fn}(\boldsymbol{k}_F) \sim 1/|\boldsymbol{v}_n(\boldsymbol{k}_F)|$ and $\tau_n(\omega, \boldsymbol{k}_F; \boldsymbol{H}) = \tau_{\text{imp}}$ [44].

The dominant contribution to the anisotropy in C_n at low T originates from the anisotropy in the SC DOS at $\omega = 0$,

$$\langle N_n(0, \boldsymbol{k}_F; \boldsymbol{H}) \rangle_{\text{FS}} \approx \left\langle \frac{N_{Fn}(\boldsymbol{k}_F)}{\sqrt{1 + \left[\frac{2\Lambda\tilde{\Delta}_n(\boldsymbol{k}_F; \boldsymbol{H})}{|\boldsymbol{v}_n^{\perp}(\boldsymbol{k}_F; \boldsymbol{H})|}\right]^2}} \right\rangle_{\text{FS}},$$
 (3)

where $\Lambda = (\hbar c/2|e|H)^{1/2}$ is the magnetic length of order the coherence length ξ between $0.5H_{c2} < H < H_{c2}$, $|\boldsymbol{v}_n^{\perp}|$ is the component of the rescaled Fermi velocity normal to \boldsymbol{H} , and $\tilde{\Delta}_n$ is the impurity renormalized order parameter [35]. For a cylindrically symmetric FS, the angledependence of $|\boldsymbol{v}_n^{\perp}|$ is determined solely by the field direction [35], its interplay with the profile of $\tilde{\Delta}_n(\boldsymbol{k}_F; \boldsymbol{H})$ gives the anisotropy of $C_n(\alpha)$. For complex FSs, there is an additional weighting of the integral due to momentumdependence of $N_{Fn}(\boldsymbol{k}_F)$ and $\boldsymbol{v}_n(\boldsymbol{k}_F)$, leading to strong fieldangle oscillations even for an isotropic gap.

Calculations for single-band models [31,35,45,46] and experiments on several classes of materials [29,47,48] demonstrated that the anisotropy in heat capacity undergoes inversion as *T* and *H* change. We qualitatively reproduce the general sign reversal of the oscillations for nodal pairings even after replacing quasicylindrical FSs with more realistic and material-specific FS anisotropies. In addition, for an *isotropic* gap, we find that even for a single strongly anisotropic FS, one or more inversion(s) of the oscillation can occur. Multiband effects add additional complexity due to competing FS anisotropies and selfconsistently evaluated multiple gap amplitudes, and the intuitive one-to-one mapping between oscillations and nodal directions becomes easily lost at finite temperatures and fields.

Results and discussions.—Figures 1(e) and 1(f) show the field-induced SC DOS as a function of quasiparticle energy below the SC gap for $\alpha = 0^{\circ}$ and $\alpha = 45^{\circ}$ for *s* and $d_{x^2-y^2}$ OPs. We immediately see that the difference between SC DOS at these two representative angles changes sign at finite ω for both cases, opening the possibility for the low-*T* sign reversal of the oscillations in the specific heat as a function of temperature.

We present the full angle-dependent profiles of $C(\alpha)$ and $\kappa(\alpha)$ for several temperatures at a representative low field for an isotropic *s*-wave gap (at $H/H_{c2} = 0.5$) and a nodal $d_{x^2-y^2}$ gap (at $H/H_{c2} = 0.1$) in Fig. 2. It is interesting to note that there is a prominent angle dependence for the *s*-wave gap [Figs. 2(a) and 2(b)], whose nature is far more complex than what can be interpreted by conventional harmonics of pairing symmetries. Especially, at low *T* the peak position of $C(\alpha)$ is shifted from high-symmetry values and lies somewhere between $\alpha = 0^{\circ}$ to 45°, see

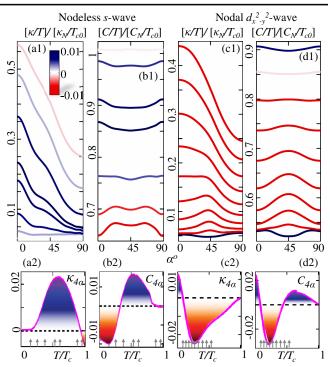


FIG. 2 (color online). (a1) Normalized thermal conductivity κ/T along (100) direction (normalized to its normal-state value κ_N/T_c) as a function of in-plane field-angle α at fixed $H/H_{c2} = 0.5$ for *s*-wave, plotted from low to high *T* (bottom to top curves). Each subsequent curve is shifted vertically by 0.01 for clarity. Each curve is colored by the amplitude of the fourfold oscillation given in panel (a2); a uniform color map is used for values below -0.01 and above 0.01. (a2) The fourfold amplitude of κ/T is plotted as a function of *T*. The vertical arrows in the bottom row depict the temperatures at which curves in top panels are shown. Panels (b1)-(b2): Normalized specific heat for same parameters as in (a1)-(a2). Panels (a) and (b) are for purely isotropic *s*-wave case, while similar plots in (c) and (d) are shown for nodal $d_{x^2-y^2}$ -wave symmetry at $H/H_{c2} = 0.1$.

Fig. 2(b1). Such complex field-angle dependence is a manifestation of the out-of-phase anisotropies on both FSs, shown in Figs. 1(a)–1(c). For nodal $d_{x^2-y^2}$ -pairing, the behavior of oscillations of $C(\alpha)$ and $\kappa(\alpha)$ is similar to results obtained for quasicylindrical FSs [34], however the amplitude of oscillations and the location of sign reversals are modified [49].

We estimate the amplitudes of the fourfold oscillations by defining $C_{4\alpha}(T) = \prod_{c}^{0} - \prod_{45}^{C}$, where $\prod_{\alpha}^{C} = [C(\alpha, T)/T]/[C_N/T_c]$ and $\kappa_{4\alpha}(T) = [\prod_{0}^{\kappa} + \prod_{90}^{\kappa}]/2 - \prod_{45}^{\kappa}$, where $\prod_{\alpha}^{\kappa} = [\kappa^{xx}(\alpha, T)/T]/[\kappa_N^{xx}/T_c]$, and C_N and κ_N are their corresponding normal-state values at T_c [50]. Such definition removes any twofold contribution from κ . The corresponding results are plotted in the lower panels of Fig. 2. We obtain several sign reversals in $C_{4\alpha}(T)$ and $\kappa_{4\alpha}(T)$ for both isotropic *s*-wave and nodal *d*-wave gaps. Earlier such a sign-reversal feature was only found for a highly anisotropic or nodal gap structure [29,31,34,35,47,48]. For this realistic FS parametrization of the double layered iron-selenide, we find indications of two sign reversals even for the *s*-wave gap. Although the second sign reversal at high *T* may be difficult to discern, it is visible in Figs. 2(b1) and 2(b2) and as a white region in Fig. 3(a1). We verified that the magnitude of oscillations depends on the out-of-plane electronic hopping, defined in the Supplemental Material [33]. In addition, our calculations show that the amplitude of fourfold oscillations for *s*-wave pairing is roughly half of that for nodal pairing.

It is noteworthy that the *T*-dependence of the fourfold oscillations in Figs. 2(b2) and 2(d2) reflects on the energy dependence of the SC DOS in Figs. 1(e) and 1(f) at the same value of *H*. For example, for the *s*-wave gap $C(\alpha = 45^{\circ}) > C(\alpha = 0^{\circ})$ at low *T* in Fig. 2(b2), which corresponds to $N(\alpha = 45^{\circ}) > N(\alpha = 0^{\circ})$ at low energy in Fig. 1(e). The opposite anisotropy in $C(\alpha)$ at high *T* corresponds to the inversion of the DOS anisotropy at higher energies. We conclude that the anisotropy in $C(\alpha)$ for isotropic *s*-wave pairing is not merely a manifestation of the anisotropy in H_{c2} (irrelevant at low fields, since it is tied to the FS shape), but is a reflection of the field-induced spectral-weight redistribution inside the gap.

In Fig. 3, we show the contour map of the amplitude of the fourfold oscillations extracted from the normalized

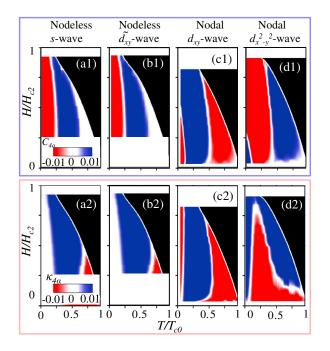


FIG. 3 (color online). Contour maps of fourfold amplitude oscillations of normalized specific heat, $C_{4\alpha}$ (top row), and normalized thermal conductivity $\kappa_{4\alpha}$ (bottom row) in the H-T phase diagram. Each column denotes a different gap symmetry. All plots use the same color map (red to blue); a uniform color map is used for values below -0.01 and above 0.01. Note the fourfold amplitude is given with respect to $H \parallel (100)$, i.e., a negative value corresponds to a minimum at $\alpha = 0^{\circ}$. Here $T_c(H)$ is defined by the vanishing of both gaps for each symmetry, which determines the line of the upper critical field H_{c2} .

 $\gamma = C/T$ (top row) and κ/T (bottom row) for two nodeless and two nodal gaps. Earlier calculation using quasicylindrical FSs showed that the specific heat oscillation simply changes sign between the d_{xy} and $d_{x^2-y^2}$ symmetries, while the overall phase diagram remains very much the same between them [35]. After the inclusion of realistic and material-specific FSs in this Letter, we find substantial quantitative differences in the location of the sign-reversal lines between these nodal gaps in Figs. 3(c1) and 3(d1), due to the interplay of the SC OP with the FS anisotropies. Hitherto unknown is the intriguing result of both low-T(strong) and high-T (weak) sign reversals in the fourfold oscillations of $C(\alpha)$ and $\kappa(\alpha)$ for isotropic gaps, at moderate and high magnetic fields, see Figs. 3(a) and 3(b). We verified for s-wave pairing that the high-T sign reversal is robust and remains at nearly the same location for a singleband superconductor with identical FS, while the low-Tfeature disappears [note that using the low-T approximations in Eqs. (1) and (2) may shift the location of the high-T inversion line to slightly lower T than a fully selfconsistent calculation]. Similarly, the low-T sign change does not exist for two-band models with similar (in-phase) angular variations of Fermi velocities.

The striking feature of the phase diagrams for the heat capacity for nodal and nodeless cases in the top panels of Fig. 3 is that they all look qualitatively similar in the sense that they all exhibit sign reversals around the same T and *H*. The same is true for the phase diagram of the $\kappa_{4\alpha}$ term in the thermal conductivity. Furthermore, the sign of the fourfold oscillations can sometimes be different for $C_{4\alpha}$ and $\kappa_{4\alpha}$ in the same region of phase diagram, as in the high-H and low-T region and vice versa for $d_{x^2-y^2}$ -pairing in Fig. 3(d). This suggests that field-angle studies of each quantity alone are insufficient to distinguish between pairing symmetries. A simultaneous study of both $C(\alpha)$ and $\kappa(\alpha)$, including the comparison of the complex angledependent profiles and T behavior, is necessary to image the gap structure. Our field-angle-dependent results of the nodal $d_{x^2-y^2}$ -wave gap in the H-T phase diagram are in qualitative agreement with recent specific heat data of CeIrIn₅ [48].

Conclusions.—The main conclusion of our work is that a mere observation of oscillations and sign reversals in $C(\alpha)$ or $\kappa(\alpha)$, combined with the H_{c2} anisotropy, is insufficient to identify the presence of nodes or minima in the gap, and their interpretations require detailed knowledge of the underlying FS anisotropy. For multiband systems, the situation is further complicated by the interplay between multiband FS anisotropies and multiple SC gaps in that substantial fourfold oscillations and sign reversals can occur even for a purely isotropic gap. These results are robust in the region of $0.5H_{c2} < H < H_{c2}$ for isotropic gaps, and its region of validity extends to lower field with increasing gap anisotropy. Our results suggest that not only are realistic theoretical calculations including field-induced impurity effect on multiband systems necessary [51], but the field-angle measurements should also be compared with the *T*-dependence of the penetration depth, specific heat, and residual electronic term of κ/T measurements for the detection of pairing symmetry [52–54]. In fact, in other probes such as quasiparticle interference pattern seen in scanning tunneling microscopy and spectroscopy [55], the consideration of the field-induced impurity effect and the inclusion of realistic FS anisotropy should play an equally important role in the interpretation of data [56].

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