## Observation of Direct-Photon Collective Flow in Au + Au Collisions at $\sqrt{s_{NN}} = 200 \text{ GeV}$

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The second Fourier component  $v_2$  of the azimuthal anisotropy with respect to the reaction plane is measured for direct photons at midrapidity and transverse momentum  $(p_T)$  of 1–12 GeV/c in Au + Au collisions at  $\sqrt{s_{NN}} = 200$  GeV. Previous measurements of this quantity for hadrons with  $p_T < 6$  GeV/c indicate that the medium behaves like a nearly perfect fluid, while for  $p_T > 6$  GeV/c a reduced anisotropy is interpreted in terms of a path-length dependence for parton energy loss. In this measurement with the PHENIX detector at the Relativistic Heavy Ion Collider we find that for  $p_T > 4$  GeV/c the anisotropy for direct photons is consistent with zero, which is as expected if the dominant source of direct photons is initial hard scattering. However, in the  $p_T < 4$  GeV/c region dominated by thermal photons, we find a substantial direct-photon  $v_2$  comparable to that of hadrons, whereas model calculations for thermal photons in this kinematic region underpredict the observed  $v_2$ .

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Direct photons are produced in various processes during the entire space-time history of relativistic heavy ion collisions and, due to their small coupling, can leave the collision region without appreciable further interaction. This makes them a sensitive and direct probe of all stages of the collision, including initial hard scattering, formation, and evolution of the strongly interacting partonic medium, its transition to hadronic matter, and final decoupling [1,2]. The transverse momentum  $(p_T)$  ranges populated by various production mechanisms overlap. However, azimuthal asymmetries tied to the event-by-event collision geometry provide useful additional information and a means to distinguish between sources of direct photons. In this Letter we consider the second Fourier component  $(v_2, often$ referred to as elliptic flow) of the event-by-event photon distribution in azimuth with respect to the reaction plane in Au + Au collisions at 200 GeV.

At higher  $p_T$  (>4 GeV/c) there are four fundamental sources of direct photons, characterized by different  $v_2$  [2,3]. Photons from initial hard scattering (predominantly from  $qg \rightarrow q\gamma$  "gluon Compton scattering") are isotropic and so  $v_2 = 0$ . Jet-fragmentation photons have positive  $v_2$  since the energy loss of the originating parton is smaller in the reaction plane [4]. Jet-conversion photons, where a hard-scattered quark interacts with a thermal gluon in the medium and converts into a photon with almost equal  $p_T$  have negative  $v_2$  [3], because the average path length of the parton in the medium (proportional to the conversion probability) is larger out of the reaction plane than within. Finally, Bremsstrahlung photons are also emitted preferentially in the direction where the medium is thicker, leading to a negative  $v_2$  [3]. Note that in this picture the azimuthal asymmetry of high- $p_T$  photon production—while expressed in terms of  $v_2$ —reflects the pure geometry of the medium, not its dynamics; it depends on the path length, not on the boost from the hydrodynamic pressure gradients.

The picture is quite different in the low- $p_T$  range  $(1 < p_T < 4 \text{ GeV}/c)$ , which is dominated by thermal photons (as first measured in [5]), where bulk dynamics (expansion) plays an important role, since it influences both the rate and azimuthal asymmetries of photon production [3,6]. It is now established that collectivity—which already exists in the partonic phase (strongly interacting quark-gluon plasma, sQGP)—persists after transition into the hadronic phase and the resulting azimuthal asymmetries in particle production can be described by nearly ideal hydrodynamics. The expectation is that thermal radiation from both the sQGP and the hadronic phase will inherit the collective motion of the medium, i.e., will have a bona-fide elliptic flow, positive  $v_2$  at low  $p_T$  [7]. The low- $p_T$  behavior of direct-photon  $v_2$  puts constraints on the viscosity of the sQGP [6].

The PHENIX experiment has published the invariant-yield as a function of  $p_T$  for direct photons both via real photons and internal conversions of nearly-real virtual photons [5,8]. In the  $1 < p_T < 4 \text{ GeV}/c$  region, a substantial excess of direct photons was observed relative to scaling of p+p yields and was interpreted in terms of thermal photon emission from the hot medium. An early attempt to infer  $v_2$  of direct photons from a  $\pi^0$  and inclusive-photon- $v_2$  measurement performed in a limited  $p_T$  range was published in [9].

In this Letter, we present measurements by the PHENIX experiment [10] of  $v_2$  of  $\pi^0$  and inclusive photons in a much-extended  $p_T$  range (up to 12 GeV/c) in

 $\sqrt{s_{NN}} = 200 \text{ GeV Au} + \text{Au collisions. Also, at low } p_T$  the fraction  $R_{\gamma}$  of direct over inclusive photons is now measured with much higher precision [5] than before [8]. Therefore, for the first time a meaningful extraction of the direct-photon  $v_2$  itself is possible.

The data are from the 2007 run of the Relativistic Heavy Ion Collider at Brookhaven National Laboratory. The analyzed sample includes  $\sim 3.0 \times 10^9$  minimum-bias Au + Au collisions. Events are triggered by the beambeam counters (BBC), as described in [11], which comprise two arrays of Čerenkov counters covering  $3.1 < |\eta| < 3.9$  and  $2\pi$  in azimuth in both beam directions. Event centrality is determined by the charge sum in the BBC.

The event-by-event reaction plane (RP) is determined by two types of detectors, the first being the BBC itself. The RP resolution (effectively a dilution factor with which the observed  $v_2$  is normalized to obtain the true  $v_2$ ) is defined as  $\sigma_{RP} = \langle \cos[2(\Psi^{true} - \Psi^{RP})] \rangle$  and it is established by comparing event-by-event the RPs obtained separately in the two BBCs. The resolution is best in the 20%-30% centrality bin, where it reaches a value of 0.4. For the 2007 data taking period, a dedicated reaction-plane detector (RXN) [12] covers  $1.0 < |\eta| < 2.8$  and the full azimuth. The RXN is a highly segmented lead-scintillator sampling detector providing much better measurement ( $\sigma_{RP} \sim 0.7$ ) than the BBC, but it is closer to the central  $|\eta| < 0.35$ pseudorapidity region where  $v_2$  is measured, making it more sensitive to jet bias in those (rare) events, where a high- $p_T$  particle is observed. The 0.7/0.4 = 1.75 improvement on the reaction-plane resolution is a 1.75-fold improvement on point-by-point uncertainty.

Inclusive photons are measured in the PHENIX electromagnetic calorimeter [13]. Particles are identified (PID) and hadrons are rejected by a shower-shape cut and a veto on charged particles using the pad chambers [14]. Photons in each  $p_T$  range are binned according to  $\Phi - \Psi^{RP}$ , where  $\Psi^{RP}$  is the azimuth of the event-by-event reaction plane, which is established independently by the BBC and RXN. These distributions are then fit for each  $p_T$  range with  $N_0[1 + 2v_2\cos\{2(\Phi - \Psi^{RP})\}]$  to extract the raw  $v_2^{\gamma,meas}$ 

coefficient for inclusive photons. As a cross-check of the fit value, another  $v_2^{\gamma,\mathrm{meas}}$  is also calculated from the average cosine of the particles with respect to the reaction plane.

Two sources of background to direct photons are of concern—hadronic decay photons and charged hadrons surviving the photon ID cuts. The cuts eliminate virtually all hadrons above 6 GeV deposited energy, which may arise from hadrons of any  $p_T$  above 6 GeV/c. However, some lower  $p_T$  hadrons survive the cuts. We correct for the  $v_2$  of this contamination, and cross check the result using conversion photons detected as dielectrons, which are free of hadron contamination [15].

To correct for hadron contamination, pions, kaons, and protons are simulated using GEANT [16], including the calorimeter response. The fraction of charged hadrons in the sample surviving the photon ID cuts is determined as  $N^{\rm hadr}/N^{\rm meas}$ . The total hadron contamination is typically 20% at 2 GeV energy deposited in the calorimeter, 10% at 4 GeV, and negligible above 6 GeV. The weighted sum of these contributions is combined into a single  $v_2^{\rm hadr}$  using the range of hadron  $p_T$  corresponding to each bin of deposited energy. A maximum  $v_2$  of 0.18 is reached at 2 GeV. The corrected value of inclusive photons is then obtained using

$$v_2^{\gamma,\text{obs}} = \frac{v_2^{\gamma,\text{meas}} - (N^{\text{hadr}}/N^{\text{meas}})v_2^{\text{hadr}}}{1 - N^{\text{hadr}}/N^{\text{meas}}}.$$
 (1)

Since  $v_2^{\rm hadr}$  is very similar to  $v_2^{\gamma, \rm meas}$ , the largest difference  $v_2^{\gamma, \rm meas} - v_2^{\gamma, \rm obs}$  introduced by Eq. (1) is  $0.15 - (0.15 - [0.2 \times 0.18])/0.8 = 0.0075$ , or 5% of  $v_2^{\gamma, \rm meas}$ . The uncertainty of this correction (see Table I) is estimated by replacing the individual charged-hadron spectra with only charged pions, and then repeating the procedure. Finally, the true  $v_2$  for inclusive photons is obtained from  $v_2^{\gamma, \rm inc} = v_2^{\gamma, \rm obs}/\sigma_{\rm RP}$ . A large fraction of inclusive photons comes from hadron decays, predominantly from  $\pi^0$  (~80%) and  $\eta$  (~15%), with a small fraction coming from  $\rho$ ,  $\omega$ , and  $\eta'$  decays, but only the  $\pi^0$   $v_2$  is directly measured. The measurement of neutral pions and their  $v_2$  is described in detail in [4,17]. We assume that  $\eta$ ,  $\omega$ , etc., follow the same  $KE_T$ 

TABLE I. Typical systematic uncertainties  $(\delta x/x)$  contributing to the direct-photon  $v_2^{\gamma, \text{dir}}$  measurement for minimum-bias collisions over two  $p_T$  ranges, and absolute uncertainty of  $v_2^{\gamma, \text{dir}}$ . Note that the uncertainty of  $v_2^{\gamma, \text{dir}}$  is not the simple linear or quadratic sum of the uncertainties listed, but is derived by differentiation from the above expression on  $v_2^{\gamma, \text{dir}}$ . The last row shows this absolute uncertainty.

Contributing via	Source	$p_T$ range 1–3	(GeV/c) 10–12	Туре
$v_2^{\gamma,  m inc}$	Remaining hadrons	0.022		В
	$v_2$ extraction method	0.004	0.006	B
${m v}_2^{\pi^0}$	Particle ID	0.037	0.06	B
	Normalization	0.004	0.072	B
	Shower merging		0.04	B
Subtraction	$R_{\gamma}$	0.031	0.22	A
Common	Reaction plane	0.063	0.063	C
Absolute uncertainty of $v_2^{\gamma, \text{dir}}$		0.07	0.02	

scaling observed in hadrons [18], where  $KE_T = m_T - m$ . Thus,  $v_2^{\rm hadr}(p_T)$  can be calculated for all hadrons separately from  $v_2^{\pi^0}(p_T)$  and then combined. As in [5], we assume  $m_T$  scaling of hadron  $p_T$  spectra and establish a "hadron cocktail" using the measured yield ratios. This cocktail is the input of a Monte Carlo simulation to calculate the combined  $v_2^{\gamma, \rm bg}$  due to photons from hadron decays. The direct-photon  $v_2^{\gamma, \rm dir}$  is then obtained using the  $R_{\gamma}(p_T)$  "direct-photon-excess ratio" as

$$v_2^{\gamma, \text{dir}} = \frac{R_{\gamma}(p_T)v_2^{\gamma, \text{inc}} - v_2^{\gamma, \text{bg}}}{R_{\gamma}(p_T) - 1} = v_2^{\gamma, \text{inc}} + \frac{v_2^{\gamma, \text{inc}} - v_2^{\gamma, \text{bg}}}{R_{\gamma}(p_T) - 1},$$
(2)

where  $R_{\gamma}(p_T) = N^{\rm inc}(p_T)/N^{\rm bg}(p_T)$  with  $N^{\rm inc} = N^{\rm meas} - N^{\rm hadr}$ , the number of inclusive photons, while  $N^{\rm bg}(p_T)$  is the number of photons attributed to hadron decay. Values of  $R_{\gamma}(p_T)$  above 5 GeV/c are taken from the real-photon measurement with the PHENIX electromagnetic calorimeter [8], and below that from the more accurate, but  $p_T$ -range-limited internal-conversion measurement of direct photons [5]. Note that  $(R_{\gamma}-1)$  is measured with a relative uncertainty of 20% at low  $p_T$ . Even though the excess is small in this range ( $\approx 20\%$ ), the  $v_2^{\gamma, \rm inc} - v_2^{\gamma, \rm bg}$  in Eq. (2) is of the order of 0.01 [see Fig. 1(b)], yielding only a small overall correction term.

Contributors to systematic uncertainties for representative  $p_T$  values are listed in Table I. The total uncertainty is then derived by differentiating the formula on  $oldsymbol{\upsilon}_2^{\gamma, \mathrm{dir}}$  and using the  $\delta x/x$  values listed in Table I. Type A are point-by-point uncertainties, which are uncorrelated with  $p_T$ ; type B are uncertainties, which are correlated (with  $p_T$ ); and type C is the overall normalization uncertainty, moving all points by the same fraction up or down. Since the  $v_2$  measurement is relative (the azimuthal anisotropy is fit without the need to know the absolute normalization), the  $\pi^0$  and inclusivephoton- $v_2$  measurements are largely immune to energyscale uncertainties, which are typically the dominant source of uncertainty in an absolute (invariant-yield) measurement. The uncertainties on  $v_2$  are dominated by the common uncertainty on determining  $\sigma_{RP}$  and by uncertainties in particle identification. Uncertainties from absolute yields enter indirectly via the hadron cocktail (normalization) and more directly at higher  $p_T$  (where the real-photon measurement is used) by the  $R_{\gamma}(p_T)$  needed to establish the direct-photon  $v_2$ . Note that due to the way  $v_2^{\gamma, \text{dir}}$  is calculated, once  $R_{\gamma}$  is large, its relative uncertainty contributes to the uncertainty on  $v_2^{\gamma, \mathrm{dir}}$  less and less.

Figure 1 shows steps of the analysis using the minimumbias sample, as well as the differences between results obtained with BBC and RXN. First,  $v_2$  of  $\pi^0$  and inclusive photons  $(v_2^{\pi^0}, v_2^{\gamma, \text{inc}})$  are measured, as described above [panels (a) and (b)]. Then, using the  $v_2^{\gamma, \text{bg}}$  of photons from hadronic decays and the  $R_{\gamma}$  direct-photon excess

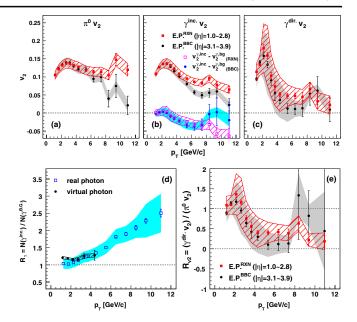


FIG. 1 (color online). (a)–(c)  $v_2$  in minimum-bias collisions, using two different reaction-plane detectors: (solid black circles) BBC and (solid red squares) RXN for (a)  $\pi^0$ , (b) inclusive photon, and (c) direct photon. (d) direct-photon fraction  $R_\gamma$  for (solid-black circles) virtual photons [5] and (open-blue squares) real photons [8] and (e) ratio of direct-photon to  $\pi^0$   $v_2$  for (solid-black circles) BBC and (solid-red squares) RXN. The vertical error bars on each data point indicate statistical uncertainties and shaded (gray and cyan) and hatched (red) areas around the data points indicate sizes of systematic uncertainties. On panel (b) the difference of  $v_2^{\gamma, \rm inc}$  and  $v_2^{\gamma, \rm bg}$  is also shown.

ratio, we derive the  $v_2^{\gamma, {\rm dir}}$  of direct photons [panel (c)]. Panel (d) shows the  $R_{\gamma}(p_T)$  values from the direct-photon invariant-yield measurements using internal conversion [5] and real [8] photons, with their respective uncertainties. Panel (e) shows the ratio of  $v_2^{\gamma, {\rm dir}}/v_2^{\pi^0}$ . We observe substantial direct-photon flow in the low- $p_T$  region (c), commensurate with the hadron flow itself (e). However, in contrast to hadrons, the direct-photon  $v_2$  rapidly decreases with  $p_T$ , and for  $p_T \geq 5~{\rm GeV}/c$ , it is consistent with zero (c). The rapid transition from large direct-photon flow at  $3~{\rm GeV}/c$  to zero flow at  $5~{\rm GeV}/c$  is also demonstrated on panel (e), since the  $\pi^0$   $v_2$  changes little in this region [4].

The surprising result that at low- $p_T$   $v_2^{\gamma, \text{dir}}$  is quite large with relatively small uncertainty hinges upon two facts. On the one hand,  $v_2^{\gamma, \text{inc}}$  is virtually equal to  $v_2^{\gamma, \text{bg}}$  with small uncertainty, as shown on panel (b) of Fig. 1 (note that the uncertainty on their difference is small since it is dominated by the common reaction-plane uncertainty). On the other hand,  $R_{\gamma}(p_T)$  is larger than 1.0 with small uncertainty [5]; these combine to make the second term in Eq. (2) small, also with small uncertainty.

A major issue in any azimuthal-asymmetry measurement is the potential bias from where in pseudorapidity the (event-by-event) reaction plane is measured. At low  $p_T$ —where multiplicities are high and particle production is dominated by the bulk with genuine hydrodynamic behavior—there is no difference between the flow derived with BBC and RXN. However, at higher  $p_T$  we observe that the  $v_2$  values using BBC and RXN diverge less for inclusive photons, particularly for  $\pi^0$  [panel (a) in Fig. 1]. For direct photons [panel (c)], the two results are apparently consistent within their *total* uncertainty, including the uncertainty  $\delta R_{\gamma}/R_{\gamma}$  (see Table I). However,  $R_{\gamma}$  is a common correction factor in the  $v_2$  measurements with both reaction-plane detectors.

Event substructure not related to bulk properties and expansion—most notably jets—can bias the reaction-plane measurement, particularly at higher  $p_T$  and lower multiplicity. Observation of a high- $p_T$  particle practically guarantees the presence of a jet, which in turn modifies the event structure over a large  $\eta$  range. The bias on the true event plane (with the bulk as its origin) is stronger if the overall multiplicity is small and if the  $\eta$  gap between the central arm (where  $v_2$  is measured) and the reaction-plane detector is reduced. The bias in Fig. 1 is largest for  $\pi^0$ , since high- $p_T$  hadrons are always jet fragments. Inclusive photons are a mixture of hadron decay photons, inheriting the bias seen in  $\pi^0$  and the mostly unbiased direct photons, therefore, the difference between BBC and RXN is smaller. Finally, the bias is smallest (but nonzero) for direct photons, of which only a relatively small fraction (jet-fragmentation photons) exhibit bias.

Figure 2 shows  $v_2$  for minimum-bias collisions and two centrality bins versus  $p_T$  for  $\pi^0$ , inclusive photons, and direct photons. For reaction-plane determination the BBC is used because it is farthest from midrapidity where  $v_2$  is measured. Despite the fact that there is a significant direct (thermal) photon yield at low  $p_T$  [5], the  $\pi^0$  and inclusivephoton  $v_2$  is virtually identical there. Note that the surprisingly large inclusive-photon  $v_2$  is confirmed by the (so far preliminary) results with a completely different analysis technique [15]. For direct photons at low  $p_T$  we observe a pronounced positive  $v_2^{\gamma, \text{dir}}$  signal, increasing with decreasing centrality and comparable to the  $\pi^0$  flow, but then rapidly going toward zero at 5–6 GeV/c. Qualitatively this shape is similar to the prediction for very early thermalization times, 0.4–0.6 fm/c in [19], namely, the  $p_T$ where  $v_2^{\gamma, \text{dir}}$  reaches its maximum is consistent with our measurement [see panel (d) in Fig. 2], but its calculated magnitude is too small. The situation is similar for the calculation with  $\tau_0 = 0.2$  fm/c and vanishing viscosity in [7]. The model in [20] combines somewhat later thermalization time (0.6 fm/c) with partial chemical equilibrium in the hadronic phase, reproducing the shape, but still predicts smaller  $v_2^{\gamma, \text{dir}}$  at low  $p_T$  than the observed one. While such large direct-photon  $v_2$  could be attributed in principle to a dominant production mechanism at the later stage when bulk flow is already developed [21,22], simultaneously explaining the large values of  $v_2^{\gamma, \mathrm{dir}}$  at  ${\sim}2~\mathrm{GeV}/c$  and its vanishing above 5 GeV/c remains a challenge to current

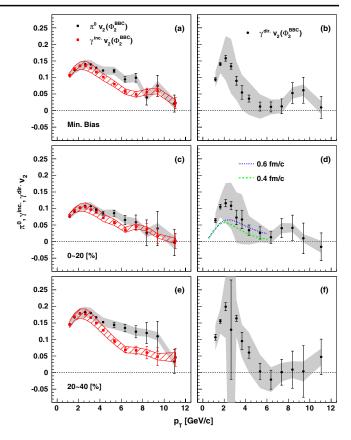


FIG. 2 (color online). (a),(c),(e) Centrality dependence of  $v_2$  for (solid-black circles)  $\pi^0$ , (solid-red squares) inclusive photons, and (b),(d),(f) (solid-black circles) direct photons measured with the BBC detector for (a),(b) minimum-bias (c),(d) 0%–20% centrality, and (e),(f) 20%–40% centrality. For (b),(d),(f) the direct-photon fraction is taken from [5] up to 4 GeV/c and from [8] for higher  $p_T$ . The vertical error bars on each data point indicate statistical uncertainties and the shaded (gray) and hatched (red) areas around the data points indicate sizes of systematic uncertainties. Also shown on panel (d) are two calculations from [19] using two different  $\tau_0$  initial times: 0.6 fm/c (upper curve) and 0.4 fm/c (lower curve).

theories (see, for instance, a recent model comparison to the current data in Fig. 5 of [22]).

Figure 3 shows the high- $p_T$  integrated  $v_2$  ( $p_T > 6~{\rm GeV}/c$ ) for  $\pi^0$  and photons (inclusive and direct) as a function of centrality. The low- $N_{\rm part}$  behavior is strongly influenced by the location in pseudorapidity of the reaction-plane detector. The  $\pi^0$   $v_2$  is comparable to other hadrons and is higher than the inclusive-photon  $v_2$ , which is diluted by direct photons. The two direct-photon- $v_2$  measurements [panel (c)] are consistent with zero (and each other) at all centralities within their total systematic uncertainties. While zero  $v_2^{\gamma, {\rm dir}}$  would be expected if initial hard scattering is the dominant (sole considered) source of photons, the typical contribution from jet conversion only is  $v_2^{\gamma, {\rm dir}} \sim -0.02$  and from fragmentation is  $v_2^{\gamma, {\rm dir}} \leq 0.01$ , weighted with the fraction of photons coming from these

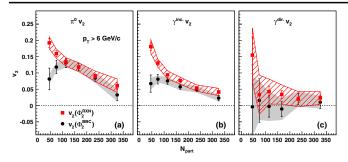


FIG. 3 (color online). High- $p_T$  ( $p_T > 6$  GeV/c) integrated  $v_2$  vs  $N_{\rm part}$  for (a)  $\pi^0$ , (b) inclusive photon, and (c) direct photon. Results are shown with both reaction-plane detectors: (solid-black circles) BBC and (solid-red squares) RXN. Each point represents a 10% wide centrality bin from 60%–0%. The vertical error bars on each data point indicate statistical uncertainties and the shaded (gray) and hatched (red) areas around the data points indicate sizes of systematic uncertainties.

specific processes [3,7]. Currently the experiment is not sensitive to their negative/positive contributions to  $v_2^{\gamma,\text{dir}}$ .

In conclusion, we measured  $v_2$  of  $\pi^0$ , inclusive and direct photons in the  $1 < p_T < 12 \text{ GeV}/c$  range for minimum bias and selected centralities in  $\sqrt{s_{NN}} = 200 \text{ GeV}$  Au + Au collisions. At higher  $p_T$  (> 6 GeV/c) the direct-photon  $v_2$  is consistent with zero at all centralities, as expected if the dominant source of photon production is initial hard scattering. However, the experimental uncertainties are currently about a factor of 2 higher than the predicted (small) positive and negative contributions from fragmentation and jet-conversion photons, respectively. In the thermal region  $(p_T < 4 \text{ GeV}/c)$ , a positive direct-photon  $v_2$  is observed, which is comparable in magnitude to the  $\pi^0$   $v_2$  and consistent with early thermalization times and low viscosity.

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