Boundary Scattering in Ballistic Graphene

Satoru Masubuchi,^{1,2,*} Kazuyuki Iguchi,¹ Takehiro Yamaguchi,¹ Masahiro Onuki,¹ Miho Arai,¹ Kenji Watanabe,³

Takashi Taniguchi,³ and Tomoki Machida^{1,2,4,†}

¹Institute of Industrial Science, University of Tokyo, 4-6-1 Komaba, Meguro-ku, Tokyo 153-8505, Japan

²Institute for Nano Quantum Information Electronics, University of Tokyo, 4-6-1 Komaba, Meguro-ku, Tokyo 153-8505, Japan

³National Institute for Materials Science, 1-1 Namiki, Tsukuba, 305-0044, Japan

⁴PRESTO-JST, 4-1-8 Honcho, Kawaguchi, Saitama 332-0012, Japan (Descind 2 March 2012) architect 18 July 2012)

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We report magnetotransport measurements in ballistic graphene mesoscopic wires where the charge carrier mean free path is comparable to the wire width W. Magnetoresistance curves show characteristic peak structures where the peak field scales with the ratio of cyclotron radius R_c and wire width W as $W/R_c = 0.9 \pm 0.1$, due to diffusive boundary scattering. The obtained proportionality constant between R_c and W differs from that of a classical semiconductor two-dimensional electron system in which $W/R_c = 0.55$.

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The presence of unique relativistic charge carriers, massless Dirac fermions, in monolayer graphene [1] has led to the emergence of novel transport phenomena such as the half-integer [2,3] and fractional quantum Hall effect [4,5]. When the elastic mean free path of Dirac fermions becomes comparable to the sample size, the charge carrier transport mechanism enters a quasiballistic regime [6], and Dirac fermions exhibit more intriguing relativistic transport phenomena such as Klein tunneling [7], evanescent wave transport [8], and sub-Poissonian shot noise [9]. In quasiballistic graphene devices, the probability of charge carrier scattering at sample boundaries becomes significantly larger than in the bulk region, because the probabilities of charge carriers scattering from charged impurities [10], defects [11], longitudinal acoustic phonons [12,13], substrate optical phonons [12,14], and flexural phonons [15] are significantly suppressed. To understand the fundamental transport properties of quasiballistic graphene, it is highly desirable to characterize the effects of boundary scattering.

In the mesoscopic wire system made from conventional semiconductor-based two-dimensional electron systems, it has been established that, if the charge carriers travel ballistically in the bulk region and are scattered diffusively at the sample boundary, the device exhibits anomalous magnetoresistance peaks owing to the magnetic commensurability effect between cyclotron radius R_c and wire width W [6,16]. Moreover, since the anomalous magnetoresistance peaks are due to diffuse boundary scattering, the probability of specular scattering, namely the specularity parameter p, can be extracted by measuring the anomalous magnetoresistance peaks [16–19].

Recent developments of a transfer technique of graphene on hexagonal boron nitride (h-BN) [20,21] have made a breakthrough in the studies of ballistic transport phenomena in graphene [22]. Since the surface of h-BN is atomically flat and h-BN has a high optical phonon energy

as compared to SiO₂, graphene on *h*-BN exhibits an extraordinary high mobility $\mu \sim 100\,000\,\mathrm{cm^2/V\,s}$ and a long mean free path $l_{\mathrm{mfp}} = (h/2e)\mu\sqrt{n/\pi} \sim 1\,\mu\mathrm{m}$ [22,23]. In conventional graphene on SiO₂ devices, μ is relatively low, and l_{mfp} is limited to 100 nm [12]. Suspended graphene devices show a high $\mu = 200\,000\,\mathrm{cm^2/V\,s}$ [24,25], but observation of the boundary scattering effect has not been reported [26].

In this Letter, we report on magnetotransport measurements in ballistic graphene on hexagonal boron nitride mesoscopic wires, in which the carrier mean free path is comparable to the wire width. We observed anomalous magnetoresistance curves with characteristic peak structures where the peak field scales with the ratio of cyclotron radius R_c and wire width W as $W/R_c = 0.9 \pm 0.1$, which indicates the detection of diffusive charge carrier scattering at the graphene boundary. The obtained proportionality constant between R_c and W contrasts with that of the classical semiconductor two-dimensional electron system, in which $W/R_c = 0.55$. In addition, from the analysis of the magnetoresistance amplitude, nearly zero specularity at the graphene boundary is suggested.

The graphene on hexagonal boron nitride (GBN) mesoscopic wire system was fabricated using the following lithography steps [20,27–29]. First, relatively thick *h*-BN crystals (~ 10 nm) were deposited on a Si wafer using a mechanical exfoliation technique. A monolayer graphene flake was deposited on a spin-coated polymethylmethacrylate layer and transferred on a *h*-BN crystal using an alignment technique under an optical microscope [20]. The monolayer thickness of the graphene flake was verified by Raman spectroscopy. A bar-shaped geometry was defined using standard electron-beam lithography and subsequent oxygen plasma etching. The electrical contacts were defined by electron-beam lithography followed by the evaporation of Pd (80 nm) and lift-off. The resist



FIG. 1 (color online). (a) Conductivity σ as a function of backgate bias voltage V_g measured at T = 4, 16, 60, 120, 180, 240, and 300 K (top to bottom). For clarity, each curve was offset by 2 mS. Dashed curves are the calculated conductivity based on the Boltzmann equation discussed in the main text. The inset shows the atomic force microscopy image of the GBN sample studied in this work. The white region indicates the region of Pd metal electrodes. The white dashed lines indicate the outline of the graphene flake. (b) Short-range mean free path l_{short} and (c) longrange mean free path l_{long} as a function of gate bias voltage V_g , for T = 4, 16, 60, 120, 180, 240, and 300 K (top to bottom).

residues were removed by annealing at 300 °C in Ar/H₂ (97:3) gas flow for 6 h.

In order to study the dependence of the transport properties on the channel length L, we fabricated three devices for L = 0.6, 1.4, and 2.3 μ m with a channel width $W = 1.0 \ \mu$ m in a single graphene flake [inset in Fig. 1(a)]. Transport measurements were carried out using the standard lock-in technique with a small alternating current of $I_{ac} = 100$ nA in a variable temperature insert at T = 1.5-300 K. A heavily doped Si substrate was used as a global back-gate V_g to tune the carrier density $n = C_g(V_g - V_{\text{Dirac}})$, where $C_g = 1.07 \times 10^{-4}$ F/m² is the gate capacitance and V_{Dirac} is the value of V_g at the charge neutrality point [2]. A magnetic field was applied perpendicularly to the sample surface.

Figure 1(a) shows the conductivity σ as a function of V_g for the $L = 2.3 \ \mu$ m device measured at $T = 4, 16, 60, 120, 180, 240, and 300 K (from top to bottom). To extract the conductivity <math>\sigma$ from the measured resistance, the contribution of the contact resistance was eliminated using the transfer length method (see Supplemental Material [30]). A typical V-shaped dependence of σ on V_g was observed for all temperatures. The minimum conductivity was located close to the zero gate bias voltages $V_{\text{Dirac}} \sim -0.3 \text{ V}$, indicating small unintentional doping ($\sim 10^{10} \text{ cm}^{-2}$). The carrier mobility, limited by long-range scattering (described below) on the hole side, reached $\mu_1 = 63,000 \text{ cm}^2/\text{V} \text{ s}$ at T = 4 K. In the following discussions, we focus on the hole side of σ because the hole mobility was higher than the electron mobility.

To extract the mean free path, we fitted the conductivity using the transport formula, assuming long- and



FIG. 2. (a) Two-terminal resistance *R* as a function of *B* measured at T = 4 K for the device with channel length $L = 2.3 \ \mu m$ with applied gate bias voltage $V_g = -45$ V. (inset) Schematic of electrotrajectories in mesoscopic wire for (solid curve) $R_c > W$ and (dotted curve) $R_c < W$. (b) *R* as a function of *B* measured at T = 4 K for (top curve) $L = 1.4 \ \mu m$ and (bottom curve) $L = 0.6 \ \mu m$. (c) Amplitude of magnetoresistance signal ΔR vs channel length *L*.

short-range scattering as the major contributors to charge carrier scattering [31–33], $\sigma^{-1} = (ne\mu_1)^{-1} + \rho_s$, where μ_1 is the mobility from long-range scattering, and ρ_s is the resistivity from short-range scattering, which are both independent of the charge carrier density n [20]. For $-35 \text{ V} < V_g < 0 \text{ V}$, the experimental data are well fitted to the calculated conductivity [dashed curve in Fig. 1(a)]. For $-50 \text{ V} < V_g < -35 \text{ V}$, the calculated conductivity deviates from the experimental data. This deviation can indicate the presence of an additional scattering mechanism, which is neither long- nor short-range scattering.

From the obtained values of μ_1 and ρ_s for varying temperatures T, we evaluated the mean free path for longrange scattering $l_{\text{long}} = \hbar \sqrt{n\pi} \mu_1 e^{-1}$ and the mean free path for short-range scattering $l_{\text{short}} = \hbar \sqrt{\pi n^{-1}} \rho_{\text{s}}^{-1} e^{-2}$ [32]. The values of l_{long} and l_{short} as a function of V_{g} for T = 4, 16, 60,120, 180, 240, and 300 K are shown in Figs. 1(b) and 1(c) (from top to bottom). The value of l_{long} increased with $|V_g|$ [Fig. 1(b)], whereas the value of l_{short} decreased with $|V_g|$ [Fig. 1(c)]. As the temperature increased, both l_{long} and l_{short} decreased. These observations were qualitatively consistent with the previous transport measurements in graphene on SiO₂. Quantitatively, however, the obtained values of $l_{\rm long} \sim 1.2~\mu{\rm m}$ and $l_{\rm short} \sim 2~\mu{\rm m}$ for $V_{\rm g} = -45~{\rm V}$ were substantially larger than the typical values in graphene on SiO₂, which were around the hundred-nanometer range [12]; moreover, these values were larger than the sample width W.

Figure 2(a) shows the two-terminal resistance *R* as a function of magnetic field *B* at $V_g = -45$ V and T = 4 K for the $L = 2.3 \ \mu$ m and $W = 1.0 \ \mu$ m device. As we increased *B* from zero, *R* increased with *B* and exhibited a maximum at $B_{\text{max}} = \pm 0.21$ T. As *B* was further increased, *R* decreased with *B* and exhibited a minimum at $B_{\text{min}} = \pm 0.5$ T. For larger *B*, *R* oscillated as a function

of B, which can be attributed to the Shubnikov–de Haas oscillation.

In the standard theory for ballistic transport phenomena in two-dimensional electron systems in a small magnetic field [6], if the cyclotron radius is larger than the sample width, $R_c > W$, and if the electrons are scattered diffusively at the sample boundary, the boundary scattering effect leads to an increase in the backscattering probability as schematically shown by solid curves in the inset of Fig. 2(a). When the magnetic field is increased, the cyclotron diameter becomes smaller than the sample width, $2R_{\rm c} < W$. Under this condition, a skipping orbit of charge carriers at the sample boundary is formed, and the backscattering probability is suppressed as schematically shown by the dashed curves in the inset of Fig. 2(a). Moreover, for this condition, the quantization of the cyclotron orbit, i.e., Landau quantization, is allowed because $2R_{\rm c} < W$; thus, the Shubnikov–de Haas oscillation can be observed. The observation of anomalous peak structures and the Shubnikov-de Haas oscillation in Fig. 2 is thus qualitatively consistent with the expectations from ballistic transport with diffusive boundary scattering in the mesoscopic wire system [34].

We studied R as a function of B for shorter channel lengths of L = 1.4 and 0.6 μ m [Fig. 2(b)]. The amplitude of the anomalous magnetoresistance curve, $\Delta R = R_{\text{max}} - R_{\text{min}}$ [indicated by solid and dotted arrows in Fig. 2(a), respectively], decreased with decreasing channel length L[Fig. 2(c)]. In the standard theory for diffusive boundary scattering, the amplitude of anomalous magnetoresistance peaks is expected to decrease with L, because the probability of backscattering decreases. Therefore, the observed decrease in the amplitude of the magnetoresistance peaks for L = 1.4 and 0.6 μ m devices is also consistent with the expectations from boundary scattering in the mesoscopic wire system. From the observations in Fig. 2, it can be concluded that we have observed magnetoresistance peak structures due to diffusive boundary scattering in a ballistic graphene mesoscopic wire system.

For a quantitative understanding of the observed magnetoresistance curves, we discuss here the positions of the magnetoresistance peaks B_{max} . For diffusive boundary scattering, the value of B_{max} scales with the ratio of the cyclotron radius $R_c(B, n)$ to the channel width W as $W/R_c(B, n) = \alpha$, where α is the proportionality constant. For Dirac fermions in monolayer graphene, the cyclotron radius can be written as $R_c(B, n) = \frac{\hbar}{eB}\sqrt{\pi n}$, where e is an elementary charge and \hbar is Planck's constant. Therefore, the expected positions of the resistance peaks in graphene can be expressed as

$$B_{\max} = \alpha \frac{\hbar}{e} \frac{\sqrt{\pi n}}{W}.$$
 (1)

To study the relationship between R_c and W, we measured the magnetoresistance curves at varying gate bias voltages for the sample with $(L, W) = (2.3 \ \mu \text{m}, 1.0 \ \mu \text{m})$.



FIG. 3 (color online). (a) *R* as a function of *B* measured at T = (a) 4 and (b) 1.6 K for the device with $(L, W) = (a) (2.3 \ \mu m)$, 1.0 μm) and (b) (3.1 μm , 1.5 μm) with applied gate bias voltage $V_g = -50, -48, \dots, -28$ V (bottom to top). Each curve was offset vertically so that the peak positions were separated by 0.01 k Ω . The blue dotted curves and colored area indicate the expected peak positions for $\alpha = 0.55$ and 0.9 \pm 0.1, respectively.

Figure 3(a) shows the two-terminal resistance *R* as a function of magnetic field *B* at $V_g = -50, -48, \dots, -28$ V (bottom to top). In this plot, each curve was offset vertically so that the peak positions were separated by 0.01 k Ω . At $V_g = -50$ V (bottom curve), we observed anomalous peak structures at $B_{\text{max}} = \pm 0.21$ T. As we increased the gate bias V_g , the positions of the peak structures were shifted to smaller *B*. At $V_g = -28$ V (top curve), the peak positions were located at $B_{\text{max}} = \pm 0.14$ T. The peak positions were compared with the calculated B_{max} using Eq. (1). As shown by the colored areas in Fig. 3(a), the peak positions were well fitted with the calculated positions for $\alpha = 0.9 \pm 0.1$.

To investigate the dependence of α on the channel width, we studied another sample for a larger channel width $(L, W) = (3.1 \ \mu m, 1.5 \ \mu m)$ [Fig. 3(b)]. Compared with the device with a smaller W [Fig. 3(a)], the values of B_{max} were decreased [Fig. 3(b)]. Moreover, the peak positions were also fitted by Eq. (1) for $\alpha = 0.9 \pm 0.1$, as indicated by the colored area in Fig. 3(b). These analyses were also valid for other samples for (L, W) = $(1.4 \ \mu m, 1.0 \ \mu m)$ and $(2.5 \ \mu m, 0.95 \ \mu m)$. These observations indicate the independence of the proportionality constant α on channel width W.

The obtained proportionality constant α was larger than that of classical massive charge carriers in the conventional semiconductor two-dimensional electron system (2DES) where $\alpha = 0.55$ [16]. For comparison, we plot the expected positions of peak structures for $\alpha = 0.55$ (blue curve) in Figs. 3(a) and 3(b). The curves for $\alpha = 0.55$ could not explain the position of the peak structures. The conventional proportionality constant between R_c and Whas to be modified to explain the observed transport phenomena in graphene.



FIG. 4 (color online). (a) ΔR (top panel), l_{long} (blue curve in bottom panel), and l_{short} (black curve in bottom panel) as a function of T measured in the device with channel length $L = 2.3 \ \mu\text{m}$ at $V_{\text{g}} = -35 \ \text{V}$. (b) ΔR (top panel), l_{long} (blue curve in bottom panel), and l_{short} (black curve in bottom panel) as a function of V_{g} at $T = 4 \ \text{K}$. The dotted line is the channel width of the GBN mesoscopic wire.

The differing value of W/R_c for graphene compared to that of the conventional semiconductor 2DES indicates that the scattering process of massless Dirac fermions at sample boundaries can be different from that of the conventional 2DES. As a possible explanation for the differing values of W/R_c , the interference of charge carriers at sample boundaries can be pointed out [35]. Since the charge carriers in graphene are chiral, when the charge carrier scattering at the sample boundaries changes the momentum, the phase of their wave function is shifted. This phase shift of the wave function at sample boundaries induces a complex interference of charge carriers, which can alter the transport properties of ballistic graphene [35]. Moreover, the first-principle numerical calculations of the magnetoresistance in graphene nanoribbon suggested $W/R_{\rm c} = 0.8-1.0$ [36], which seems to be consistent with our results. Albeit, for the exact understandings of the reason for the differing values of W/R_c , more elaborated works will be needed in the future.

Finally, we study the magnetoresistance curves for varying temperatures T and gate bias voltages V_g . Figure 4(a) shows the amplitude of the magnetoresistance ΔR , longrange mean free path l_{long} , and short-range mean free path l_{short} as a function of T at $V_g = -35$ V. As T was increased from 4 to 200 K, the value of ΔR decreased, but was retained to T = 240 K [Fig. 4(b)]. This observation implies that the channel region of graphene mesoscopic wire was still ballistic at T = 240 K, because of the relatively small electron-phonon scattering probability in monolayer graphene compared to that of conventional semiconductors [12], which demonstrates the characteristic electronic properties of graphene.

Figure 4(b) shows ΔR , l_{long} , and l_{short} as a function of V_{g} at T = 4 K. The value of ΔR increased with $|V_{\text{g}}|$ from 20 to 40 V and saturated for 40 to 50 V [Fig. 4(b)]. In principle, ΔR increases with the mean free path in the

bulk region, and ΔR saturates as the mean free path in the bulk region exceeds the sample width [6]. In Fig. 4(b), as we increased $|V_g|$, l_{long} increased, and for 40 V < $|V_g| < 50$ V, l_{long} exceeded the sample width [indicated by the dotted line in Fig. 4(b)]. On the other hand, l_{short} decreased with $|V_g|$ and was larger than W. The standard theory for ballistic transport suggests that, if the specularity parameter p is zero, ΔR emerges when the carrier mean free path in the bulk region becomes comparable to the sample width W [16]. If we assume that the charge carrier scattering in the bulk region is dominated by long-range scattering, the emergence of ΔR at $l_{\text{long}} \sim 1 \ \mu \text{m}$ indicates an almost zero p in our device.

In summary, we conducted magnetotransport measurements in quasiballistic graphene mesoscopic wires, in which the carrier mean free path is comparable to the wire width. Magnetoresistance curves show characteristic peak structures where the peak field scales with the ratio of cyclotron radius R_c and electronic wire width W, which indicates the detection of a diffusive scattering effect at the sample boundary. The analysis suggests that the values of R_c and W scale as $R_c/W = 0.9 \pm 0.1$. This is in contrast to the semiconductor two-dimensional electron system where $R_{\rm c}/W = 0.55$. The analysis also suggests nearly zero probability for specular scattering at the sample boundary. These findings are a fundamental step forward in the understanding of the effects of boundary scattering on the transport properties of nanostructured graphene devices such as graphene nanoribbons [37] and graphene single electron transistors [38,39].

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*msatoru@iis.u-tokyo.ac.jp [†]tmachida@iis.u-tokyo.ac.jp

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