Direct Observation of Quantum Phonon Fluctuations in a One-Dimensional Bose Gas

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We report the first direct observation of collective quantum fluctuations in a continuous field. Shot-toshot atom number fluctuations in small subvolumes of a weakly interacting, ultracold atomic 1D cloud are studied using *in situ* absorption imaging and statistical analysis of the density profiles. In the cloud centers, well in the quantum quasicondensate regime, the ratio of chemical potential to thermal energy is $\mu/k_BT \approx 4$, and, owing to high resolution, up to 20% of the microscopically observed fluctuations are quantum phonons. Within a nonlocal analysis at variable observation length, we observe a clear deviation from a classical field prediction, which reveals the emergence of dominant quantum fluctuations at short length scales, as the thermodynamic limit breaks down.

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At temperature $T = 0$, classical thermodynamics predicts the complete absence of excitations; however, because of the Heisenberg uncertainty principle, quantum observables never fully come to rest. Quantum, i.e., vacuum fluctuations are key to the understanding of quantum electrodynamics effects as fundamental as spontaneous emission [[1\]](#page-3-1), the Lamb shift [\[2\]](#page-3-2), or Casimir-Polder forces near surfaces [\[3–](#page-3-3)[5](#page-3-4)], but also, Hawking radiation near black holes [\[6\]](#page-3-5), quantum phase transitions [[7\]](#page-3-6), etc. In matter fields, quantum fluctuations govern the correlations properties at low temperature. They cause quantum depletion in Bose-Einstein condensates, bringing corrections to their equation of state (EoS) [[8](#page-3-7),[9\]](#page-3-8), and are dramatically enhanced in reduced dimensions [[10](#page-3-9)]. In 1D systems, they destroy long range order and prevent Bose-Einstein condensation even at $T = 0$ [\[11\]](#page-3-10).

So far, quantum fluctuations in continuous fields have been detected only indirectly, from their macroscopic consequences at the thermodynamic scale [[5,](#page-3-4)[8\]](#page-3-7), while their microscopic observation has remained elusive [\[12](#page-3-11)[,13\]](#page-3-12). Only recently, density imaging of ultracold atomic clouds has allowed the microscopic imaging of a quantum fluctuating field (more precisely, its modulus) in discrete lattice systems [[14](#page-3-13)]. In this Letter, we report microscopic observation of quantum fluctuations for the first time in a continuous field.

Statistical analysis of *in situ* density fluctuations has indeed become a prominent tool of investigation. In dimension D, the variance of atom number $\langle \delta N^2 \rangle$ in a sufficiently large volume Λ^D is the same as for an infinite sufficiently large volume Δ^D is the same as for an infinite system in thermodynamic equilibrium at the local density *n* and chemical potential μ [\[15\]](#page-3-14):

$$
\langle \delta N^2 \rangle = \Delta^D k_B T (\partial n / \partial \mu)_T, \tag{1}
$$

where k_B is the Boltzmann constant, and $(\partial n/\partial \mu)_T/n^2$ the isothermal compressibility, derived from the EoS $n(\mu, T)$. This thermodynamic regime has allowed the observation of bosonic bunching [[16](#page-3-15),[17](#page-3-16)] and fermionic antibunching [\[18](#page-3-17)[,19\]](#page-3-18) in ideal gases. In weakly repulsive Bose gases, the suppression of density fluctuations, which defines the quasicondensate regime, was detected directly in 1D [\[16\]](#page-3-15) and 2D [[20](#page-4-0)]. Recent thermodynamic studies addressed the phase diagram for quasicondensation in 1D and elongated 3D Bose gases [[21](#page-4-1)], the universality of the 2D Bose gas [\[20\]](#page-4-0), and, in optical lattices, the superfluid to Mott insula-tor transition [\[22\]](#page-4-2). In 1D Bose gases at $k_BT < \mu$, sub-Poissonian density fluctuations, i.e., antibunching [\[23\]](#page-4-3) provided thermodynamic evidence of the quantum quasicondensate regime [\[24,](#page-4-4)[25\]](#page-4-5).

Thermodynamic measurements along Eq. [\(1\)](#page-0-0) require that the relevant excitations under observation have occupation numbers $n_k \gg 1$, so that thermal fluctuations dominate, and fluctuations are classical, i.e., proportional to T, as in Eq. ([1\)](#page-0-0), with no quantum contribution. This is valid only in the thermodynamic limit

$$
L_{\text{obs}} \gg l_c^T,\tag{2}
$$

where l_c^T is the thermal correlation length of density fluctuations, and L_{obs} is the length scale at which the system is probed. If $L_{obs} < l_c^T$, measured fluctuations can deviate from Eq. [\(1](#page-0-0)) [\[15](#page-3-14)[,20\]](#page-4-0), and, if $n_k < 1$, quantum fluctuations dominate. In this Letter, we analyze density fluctuations in 1D Bose gases with $\mu / k_B T \simeq 4$, reaching the crossover regime $l_c^T \sim L_{\text{obs}}$. Here, quantum fluctuations have a siz-
able contribution. Still, quantum and thermal nonthermoable contribution. Still, quantum and thermal nonthermodynamic effects cancel almost exactly, and Eq. [\(1\)](#page-0-0) apparently holds. However, quantum fluctuations are non-extensive [\[15,](#page-3-14)[23\]](#page-4-3), scaling only logarithmically with L_{obs} , while thermal fluctuations scale linearly [as in Eq. ([1](#page-0-0)), with $L_{obs} \approx \Delta$]. Hence, truly thermodynamic, i.e., purely thermal fluctuations, are observed only for $L_{obs} \gg l_c^T$. By
varying $L_{\rm b}$, we monitor the breakdown of the thermodyvarying L_{obs} , we monitor the breakdown of the thermodynamic limit at small L_{obs} as a clear deviation from a classical field theory that ignores quantum fluctuations. In the line of [[13](#page-3-12)], this criterium proves our microscopic observation of quantum fluctuations.

Our experiment uses 87Rb atoms in micromagnetic traps on an atom chip. The transverse and longitudinal trapping frequencies are $\omega_{\perp}/2\pi=3.3$ kHz and $\omega_{\parallel}/2\pi=5.5$ Hz, respectively. After forced rf evaporative cooling and thermalization for 800 ms, an absorption picture is recorded on a CCD camera. After hundreds of realizations, fluctuations in the density profiles are analyzed as detailed in [\[17\]](#page-3-16). For each profile and pixel of length $\Delta = 4.5 \mu$ m, we extract the atom number fluctuation $\delta N = N - \langle N \rangle$ where $\langle N \rangle = n\Lambda$ is the mean atom number. True atom number variances $n\Delta$ is the mean atom number. True atom number variances $\langle \delta N^2 \rangle$ are inferred from measured variances $\langle \delta N^2 \rangle_m$ using
the thermodynamic relation $\langle \delta N^2 \rangle = \kappa_0 \langle \delta N^2 \rangle$ where κ_0 the thermodynamic relation $\langle \delta N^2 \rangle_m = \kappa_2 \langle \delta N^2 \rangle$, where κ_2
is a reduction factor due to the finite rms imaging resoluis a reduction factor due to the finite rms imaging resolution δ . Assuming a Gaussian imaging response, δ is determined precisely from the correlations measured between neighboring pixels [\[17](#page-3-16)[,26\]](#page-4-6).

To introduce our data, we show in Fig. [1](#page-1-0) a typical picture (a), average profiles, and relative fluctuations, for clouds deep in the 1D regime, with $k_BT/\hbar\omega_{\perp}=0.11$ (b) and 0.03 (c). As in $[21,17]$ $[21,17]$, T is measured accurately by fitting the fluctuations in the cloud centers with Eq. [\(1](#page-0-0)) and the Gross-Pitaevski (G-P) quasicondensate EoS in the 1D–3D crossover $\mu = \hbar \omega_{\perp} (\sqrt{1 + 4na} - 1)$ [\[27\]](#page-4-7) (dashed curve, see also Fig. 3) where $a = 5.3$ nm is the 3D scattering length also Fig. [3\)](#page-2-0), where $a = 5.3$ nm is the 3D scattering length. At low densities, fluctuations are super-Poissonian, i.e., exceed the shot noise (dotted line). They reach a maximum at the transition to the quasicondensate regime, around the density $n_{\text{qc}} = \left[m(k_B T)^2 \right] / \hbar^2 g^{1/3}$ [\[21\]](#page-4-1), in good agreement
with the exact Nang Nang solution for the 1D Bose gas with the exact Yang-Yang solution for the 1D Bose gas [\[28\]](#page-4-8) (solid curve) [[29](#page-4-9)]. At higher densities, for $\mu > k_B T$ (light gray areas in profiles), quantum fluctuations start dominating thermodynamically and fluctuations turn

FIG. 1 (color online). Microscopic fluctuations and thermodynamic theories, at $T = 18 \text{ nK}$ (b) and $T = 4.7 \text{ nK}$ (a),(c). (a) Typical absorption picture (optical density). (b),(c) Normalized fluctuations and average profiles (insets). Theoretical curves: classical shot noise (dotted), predictions from Eq. [\(1\)](#page-0-0) and the ideal Bose gas (short-dashed), quasicondensate (long-dashed), and Yang-Yang EoS (solid). Gray areas in the profiles indicate the quantum quasicondensate regime, the dark-gray area in the $T = 4.7$ $T = 4.7$ $T = 4.7$ nK profile is the zone Ω where the analysis of Fig. 4 is carried carried.

sub-Poissonian, as explained in [[23](#page-4-3)]. In this Letter, the region of interest is the cloud center at $T = 4.7$ nK (zone Ω), where $\langle \delta N^2 \rangle / \langle N \rangle \simeq k_B T / \mu$ reaches 0.26, and where we detect quantum phonons microscopically as where we detect quantum phonons microscopically, as explained below.

To analyze fluctuations in the cloud centers, we use Bogoliubov theory, valid for weakly interacting quasicon-densates [\[30\]](#page-4-10), and the 1D G-P EoS $\mu = gn$, where $g = 2\hbar\omega_\perp a$ is the 1D coupling constant. This is appropriate since the dimensional crossover correction to the G-P prediction is only 10% in zone Ω , and the 1D interaction parameter is $\gamma = gm/\hbar^2 n \leq 0.05$. Bogoliubov excitations have energies $\epsilon_k = \hbar^2 k^2 / 2m \sqrt{1 + 4/k^2 \xi^2}$, where $\xi = \hbar / \sqrt{m_H}$ is the healing length and thermal occupation $\hbar / \sqrt{m \mu}$ is the healing length, and thermal occupation numbers $n_k=1/(e^{\epsilon_k/k_B T}-1)$. Noting $f_k=1/\sqrt{1+4/k^2 \xi^2}$, the spectrum of density fluctuations is the spectrum of density fluctuations is

$$
\langle \delta n_k^2 \rangle = n S_k = n (S_k^Q + S_k^T), \tag{3}
$$

where $S_k^Q = f_k$ and $S_k^T = 2f_k n_k$ are the quantum and thermal static structure factors, both plotted in Fig. [2\(c\)](#page-1-1). Note that, in $S_k = 2f_k(n_k + 1/2)$, $S_k^{\mathcal{Q}}$ is the exact analog of
the zero-point energy term in the barmonic oscillator specthe zero-point energy term in the harmonic oscillator spectrum. We also show in Fig. [2\(d\)](#page-1-1) the second order correlation function $g^{(2)}(z) = 1 + \int \frac{dk}{2\pi} e^{ikz} (S_k - 1)$.
Three competing terms determine the fl

Three competing terms determine the fluctuation regimes in quasicondensates. For $k\xi \gg 1$, $S_k^Q \approx 1$ [solid line in Fig. [2\(c\)](#page-1-1)] is the trivial autocorrelation "shot noise" [\[16](#page-3-15)[,17\]](#page-3-16) of uncorrelated particles [\[31\]](#page-4-11), for which $g^{(2)}(z) \equiv 1$. At smaller k repulsive interactions give a negative 1. At smaller k , repulsive interactions give a negative contribution to $S_k - 1$ and to $g^{(2)}(z) - 1$ [\[23\]](#page-4-3). Finally, in S^T [dashed lines in Fig. 2(c)] statistical bosonic bunching S_k^T [dashed lines in Fig. [2\(c\)](#page-1-1)], statistical bosonic bunching brings a positive contribution. Let us now focus on the quantum and thermal density correlation lengths l_c^Q and l_c^T , respectively defined as the inverse widths of S_k^Q and S_k^T . For quantum fluctuations, equally present in all modes k , one

FIG. 2 (color online). Quantum vs thermal fluctuations in 1D quasicondensates. (a),(b) Fluctuation regimes for thermal (a) and quantum (b) quasicondensates. (c) S_k^Q (solid) and S_k^T (dashed) in Bogoliubov theory for various k_BT/μ . (d) $g^{(2)}(z)$ for $\gamma = 0.01$.

has $l_c^Q = \xi$ [[33](#page-4-12)]. For thermal fluctuations, two cases need be distinguished be distinguished.

In thermal quasicondensates $[k_B T \gg \mu, \text{ see Fig. 2(a)],$ $[k_B T \gg \mu, \text{ see Fig. 2(a)],$ $[k_B T \gg \mu, \text{ see Fig. 2(a)],$ S_k^T decays fast for $kl_c^Q \gg 1$, so one has a single $l_c = l_c^T$
 l_c^Q [25.33]. However, thermal fluctuations dominate, Ω_k decays rast for $\kappa_l \geq 1$, so one has a single $\iota_c - \iota_c =$
 Ω_k^Q [\[25](#page-4-5)[,33\]](#page-4-12). However, thermal fluctuations dominate, i.e., $n_k \gg 1$, for length scales $L \sim 1/k \gg \lambda_{dB}$, where $\lambda_{dB} = \sqrt{2\pi\hbar^2/mk_B T}$ is the thermal de Broglie wavelength. Three $\sqrt{2\pi\hbar^2/mk_BT}$ is the thermal de Broglie wavelength. Three regimes are thus present [\[15\]](#page-3-14). For $L \gg l_c$, thermal phonons dominate: this is the thermodynamic regime, here with super-Poissonian fluctuations. For $\lambda_{dB} \ll L \ll l_c$, thermal particles dominate, but correlations are partly lost [[34](#page-4-13)]. Finally, for $L \ll \lambda_{dB}$, only the Poissonian quantum shot noise is detected.

In quantum quasicondensates $[k_B T \ll \mu, \text{ see Fig. 2(b)}],$ noting $c = \sqrt{\mu/m}$ the speed of sound, n_k and S_k^T are both suppressed at length scales lower than [36] suppressed at length scales lower than [\[36\]](#page-4-14)

$$
l_c^T = \frac{\hbar c}{k_B T} = l_c^Q \frac{\mu}{k_B T},
$$
\n(4)

which, to our knowledge, has been proposed only recently [\[13](#page-3-12)[,15,](#page-3-14)[37](#page-4-15)]. The familiar regimes of Poissonian shot noise and thermodynamic thermal phonon fluctuations (now sub-Poissonian) are still present. However, in the range l_c^Q $\tilde{c} \ll$ ed in $L \ll l_c^T$, one now has a crucial new regime [highlighted in Fig. 2(b)] where $n \ll 1$ and quantum phonons govern the Fig. [2\(b\)](#page-1-1)], where $n_k \ll 1$ and quantum phonons govern the physics.

To compare Bogoliubov theory to our data, we use the imaging transfer function $\mathcal{U}_k = 2 \frac{(1-\cos(k\Delta))}{k^2} e^{-k^2 \delta^2}$ [\[23\]](#page-4-3), obtained from our Gaussian optical response model [\[17](#page-3-16)[,26\]](#page-4-6), and we compute, for $j = Q, T$,

$$
\langle \delta N^2 \rangle_m^j = \int \frac{dk}{2\pi} n S_k^j U_k. \tag{5}
$$

 \mathcal{U}_k is peaked at $k = 0$, and its inverse width is $L_{obs} \sim$
max $\{\delta \}$. The thermodynamic limit Eq. (2) is thus max{ δ , Δ }. The thermodynamic limit Eq. ([2\)](#page-0-1) is thus
equivalent to measuring $\langle \delta N^2 \rangle = \kappa_2 \langle N \rangle S_0$ [15.26] i.e. equivalent to measuring $\langle \delta N^2 \rangle_m = \kappa_2 \langle N \rangle S_0$ [[15](#page-3-14)[,26](#page-4-6)], i.e.,
to only probe the contribution $S_0 = S_1^T$ of thermal photo only probe the contribution $S_0 = S_0^T$ of thermal pho-
nons, always proportional to T [see Fig. 2(c)]. In other nons, always proportional to T [see Fig. [2\(c\)\]](#page-1-1). In other words, since $S_0 = 1 + \int dz [g^{(2)}(z) - 1]$, a thermodynamic
observation probes only the integral of $g^{(2)}(z) = 1$, without observation probes only the integral of $g^{(2)}(z) - 1$, without resolving its microscopic details [see Fig. 2(d)] resolving its microscopic details [see Fig. [2\(d\)\]](#page-1-1).

In Fig. [3,](#page-2-0) we compare the measured fluctuations $\langle \delta N^2 \rangle_m$ (for the same data as in Fig. [1](#page-1-0)) to the spectral 1D Bogoliubov predictions $\langle \delta N^2 \rangle_m^Q$ and $\langle \delta N^2 \rangle_m^T$, and their sum $\langle \delta N^2 \rangle^{\text{tot}}$ (dot-dashed lines). At low densities one has sum $\langle \delta N^2 \rangle_m^{\text{tot}}$ (dot-dashed lines). At low densities, one has $l_c^Q \gg L_{obs}$, which explains that $\langle \delta N^2 \rangle_m^Q$ follows the linear shot noise prediction [see inset to Fig. 3(a)]. At higher shot noise prediction [see inset to Fig. [3\(a\)\]](#page-2-1). At higher densities, $\langle \delta N^2 \rangle_m^Q$ is reduced by repulsive interactions [[38\]](#page-4-16).
At $T = 18 \text{ nK}$ [Fig. 3(a)], the ratio $\langle \delta N^2 \rangle^Q$ // δN^2 /tot is 70%. At $T = 18$ nK [Fig. [3\(a\)\]](#page-2-1), the ratio $\langle \delta N^2 \rangle_m^Q / \langle \delta N^2 \rangle_m^{\text{tot}}$ is 7%
and cannot be resolved as in [23]. However at $T = 4.7$ nK and cannot be resolved, as in [[23](#page-4-3)]. However, at $T = 4.7 \text{ nK}$ [Fig. [3\(b\)](#page-2-1)], it reaches 20% in the cloud center, which now exceeds the experimental uncertainty. Thus, the contribution of quantum fluctuations in the total fluctuations is here

FIG. 3 (color online). Quantum vs thermal contributions in the measured fluctuations $\langle \delta N^2 \rangle_m$ (same data as in Fig. [1\)](#page-1-0). Dot-
dashed lines are the spectral 1D Bogoliubov predictions $\langle \delta N^2 \rangle^Q$ dashed lines are the spectral ID Bogoliubov predictions $\langle \delta N^2 \rangle_{mn}^B$
(low-lying green) $\langle \delta N^2 \rangle^T$ (middle red) and $\langle \delta N^2 \rangle^{\text{tot}}$ (upper (low-lying green), $\langle \delta N^2 \rangle_m^T$ (middle red) and $\langle \delta N^2 \rangle_m^{\text{tot}}$ (upper
blue) Thermodynamic predictions as in Fig. 1 are here rescaled blue). Thermodynamic predictions as in Fig. [1](#page-1-0) are here rescaled by $\kappa_2 = 0.34$ (a) and 0.41 (b) for $\delta = 3.5$ and 2.8 μ m, respectively. The square in (b) is the zone O tively. The square in (b) is the zone Ω .

sizable, i.e., non-negligible, in each pixel, in contrast to the thermodynamic regime. Yet, $\langle \delta N^2 \rangle_m^{\text{tot}}$ is still in good
agreement with the 1D thermodynamic Yang-Yang agreement with the 1D thermodynamic Yang-Yang prediction (solid line) [\[39\]](#page-4-17). This is because S_k^Q and S_k^T have opposite slopes $\pm k\xi/2$ at small $k\xi$ for all T [see Fig. [2\(c\)](#page-1-1)], so that nonthermodynamic (i.e., finite k [[15](#page-3-14)]) quantum and thermal contributions cancel each other at first order.

To obtain smoking-gun evidence for our detection of quantum fluctuations, we turn to a nonlocal analysis. Since quantum fluctuations scale only logarithmically with L_{obs} [\[15](#page-3-14)[,23\]](#page-4-3), thermal fluctuations always dominate for $L_{obs} \gg$ l_c^T , and fluctuations are well described by a classical field model (CFM) that ignores the quantum term S_k^Q [\[13\]](#page-3-12), On the other hand, a CFM is expected to fail for $L_{obs} \leq l_c^T$. To check this, we focus on the zone Ω , i.e., the 3 central bins $39 \langle N \rangle$ < 54 at T = 4.7 nK, containing 58% of the atoms [see inset to Fig. [1\(d\)](#page-1-2) and Fig. [3\(b\)\]](#page-2-1). There, the profile is the flattest, many data points are available, and error bars are the smallest. The cloud center is indeed the most reliable fraction of the data.

To vary L_{obs} , we merge the imaging pixels in macropixels of variable size $n_{pix} = 1$ to 8, and compute fluctuations accordingly [see Fig. [4\(a\)](#page-3-20) and [[26](#page-4-6)]]. Figure [4\(b\)](#page-3-20) shows $\langle \delta N^2 \rangle / \langle N \rangle$ obtained in the zone Ω , for $L_{\text{pix}} =$
An_{ther} = 4.5 to 36 um. The key criterium as in [13], is $\Delta n_{\text{pix}} = 4.5$ to 36 μ m. The key criterium, as in [\[13\]](#page-3-12), is to compare the data either to a full Bogoliubov model (FBM) that includes the quantum term (solid line) or to a CFM that ignores it (dashed line). At large $L_{\text{pix}}(\simeq L_{\text{obs}})$, both models converge as expected towards the thermodynamic 1D G-P prediction (dot-dashed line), with a logarithmic vanishing of the quantum contribution. At short L_{pix} , the data clearly deviate from the CFM prediction, which displays a noticeable dip. Note that the gap saturates at small L_{pix} , due to the finite optical resolution that cuts off high k fluctuations, which confirms that shot noise is irrelevant in our data.

FIG. 4 (color online). Fluctuations at variable length scales in the cloud center (zone Ω) at $T = 4.7$ nK. (a) Typical profile N
(triangles) reference profile $\langle N \rangle$ (circles) and fluctuations δN (triangles), reference profile $\langle N \rangle$ (circles) and fluctuations δN
(squares) for three pixel sizes $L = \langle h \rangle / \delta N^2 \rangle / \langle N \rangle$ in zone Q (squares), for three pixel sizes L_{pix} . (b) $\langle \delta N^2 \rangle / \langle N \rangle$ in zone Ω
compared to full Bogoliuboy (EBM) prediction $\langle \delta N^2 \rangle$ ^{tot}/ μ compared to full Bogoliubov (FBM) prediction $\langle \delta N^2 \rangle_m^{\text{tot}}/\kappa_2$
(solid) classical field (CFM) prediction $\langle \delta N^2 \rangle^T/\kappa_2$ (dashed) (solid), classical field (CFM) prediction $\langle \delta N^2 \rangle_m^T / \kappa_2$ (dashed)
and thermodynamic G-P prediction (dot-dashed) at $T^* =$ and thermodynamic G-P prediction (dot-dashed) at T_{1D}^* = and thermodynamic G-P prediction (dot-dashed) at $T_{1D} =$
5.0 nK. Inset: same data fitted with FBM at $T_{1D}^* =$ 5.0 nK
(solid) or CFM at $T^C =$ 5.5 nK (dashed) (solid) or CFM at $T_{1D}^C = 5.5$ nK (dashed).

The theoretical predictions in Fig. [4\(b\)](#page-3-20) are computed at $T_{1D}^* = 5.0$ nK, that we obtain fitting the FBM to the data, with T as only free parameter [see inset to Fig. 4(b)]. This with T as only free parameter [see inset to Fig. [4\(b\)\]](#page-3-20). This fit has an rms deviation of only 1.0%, i.e., much less than the plotted error bars [[40](#page-4-18)] and is thus a very accurate 1D thermometry [\[41\]](#page-4-19). On the contrary, the fit to the CFM, yielding $T_{1D}^C = 5.5$ nK, has a strong systematic error and
an rms deviation of 5% [see inset to Fig. 4(b)]. This clear an rms deviation of 5% [see inset to Fig. [4\(b\)\]](#page-3-20). This clear breakdown of the CFM proves our observation of quantum fluctuations, and reveals the emergence of dominant quantum phonons at short distances.

As for length scales, in the zone Ω , $l_c^Q = 0.6 \mu m$ and $l_c^T = 2.2 \mu m$, while L_{obs} is determined by $\Delta = 4.5 \mu m$ and $\delta = 2.8 \mu m$. Thus $L_f \sim l_f^T$ and this explains our and $\delta = 2.8 \mu \text{m}$. Thus, $L_{obs} \sim l_c^T$ and this explains our unprecedented observations. On the contrary in [12] at unprecedented observations. On the contrary, in [[12\]](#page-3-11), at $T = 33$ nK, one has $l_c^T = 0.63 \mu m$, and $L_{obs} \ge \Delta = 10 \mu m$ i.e. $L = \frac{V}{c}$ All observations in [12] were 10 μ m, i.e., $L_{obs} \gg l_c^T$. All observations in [\[12\]](#page-3-11) were
thus well in the thermal fluctuations regime indistinguishthus well in the thermal fluctuations regime, indistinguishable from a CFM prediction [[13](#page-3-12)]. In the quantum regime $z \ll l_c^T$, the decay of the first order (phase) correlation
function $g^{(1)}(z)$ is algebraic whereas in the thermal regime function $g^{(1)}(z)$ is algebraic, whereas, in the thermal regime $z \gg l^T$ it is exponential, over a thermal phase correlation $z \gg l_c^T$, it is exponential, over a thermal phase correlation
length $l^T = l^T / \sqrt{\gamma} \gg l^T$ [11.32.42]. The misinterpretalength $l_{\phi}^{T} = l_{c}^{T}/\sqrt{\gamma} \gg l_{c}^{T}$ [[11](#page-3-10)[,32](#page-4-20)[,42\]](#page-4-21). The misinterpretation in [[12](#page-3-11)] came from identifying the quantum regime with $z \ll l_{\phi}^T$.

In summary, we have reported the first microscopic observation of vacuum fluctuations in a continuous field, using a nonlocal analysis that reveals a clear deviation from a classical field theory. Our observation of emerging dominant quantum phonons is a first microscopic insight into the regime of quasi-long-range order, i.e., algebraic decay of $g^{(1)}(z)$, in the 1D Bose gas [\[11\]](#page-3-10). We also demon-
strated the possibility of imaging vacuum phonon fluctuastrated the possibility of imaging vacuum phonon fluctuations in single density pictures, like Fig. [1\(a\)](#page-1-2). By further reducing T and L_{obs} , one could monitor the full crossover from thermal to quantum fluctuations [[26](#page-4-6)]. Dark solitons, which are defects localized over a length scale $\sim l_c^Q$, could
also be used as sensitive probes for the microscopic physics also be used as sensitive probes for the microscopic physics of quantum fluctuations [[37](#page-4-15),[43](#page-4-22)].

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