

## Are Dynamical Quantum Jumps Detector Dependent?

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Dynamical quantum jumps were initially conceived by Bohr as objective events associated with the emission of a light quantum by an atom. Since the early 1990s they have come to be understood as being associated rather with the detection of a photon by a measurement device, and that different detection schemes result in different types of jumps (or diffusion). Here we propose experimental tests to rigorously prove the detector dependence of the stochastic evolution of an individual atom. The tests involve no special preparation of the atom or field, and the required efficiency can be as low as  $\eta \approx 58\%$ .

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Quantum jumps—the discontinuous change in the state of a microscopic system (such as an atom) at random times—were the first form of quantum dynamics to be introduced [1,2]. This was in the 1910s, long before the notion of entanglement, and its puzzles such as the Einstein-Podolsky-Rosen (EPR) paradox [3], had been introduced, and before the special role of measurement in quantum mechanics had been elucidated [4]. Thus these jumps were conceived of as objective dynamical events, linked to an equally objective photon emission event.

The modern concept of quantum jumps in atomic systems is based on “quantum trajectory” theory [5], introduced independently in Refs. [6–8]. This theory comprises stochastic evolution equations for the microscopic system state conditioned on the results of monitoring the bath to which it is weakly coupled. These are also known as “unravelings” [5] of the system’s master equation (ME), as the ensemble average of the quantum trajectories of the (ideally pure) state of an individual system replicates the mixture-inducing evolution of the ME. This theory has been applied also to solid-state qubits and other quantum systems [9–11]. In the atomic case, a photodetection event causes the state of the distant atom to jump because of entanglement between the bath (the electromagnetic field) and the atom. That is, the quantum jumps are detector dependent; in the absence of a measurement there would be no jumps. This is in marked contrast to the objective jumps of Bohr and Einstein, linked to a supposed emission event.

One could well be tempted to ask what difference does it make if we say a jump is caused by the emission of a photon rather than saying it is caused by the detection of a photon? If photon detection were the only way to measure the emitted quantum field then the answer would indeed be: no real difference at all. But there are many (in fact infinitely many) other ways to measure the emitted field. For instance one can interfere it with a local oscillator (LO)—that is, another optical field in a coherent state—prior to detection [5].

In quantum optical detection theory radically different stochastic dynamics for the atomic state occur depending on the detection scheme used by a distant observer [5,8,9]. Perfect “direct” (no LO) photon detection gives rise to the quantum jump model of Bohr and Einstein. Perfect heterodyne detection (with a strong, far-detuned LO), by contrast, gives rise to a particular type of pure-state quantum diffusion [12], originally proposed as an objective (i.e., detector-independent) model of “quantum state diffusion” (QSD) [13]. It is not that either the quantum jump model or the QSD model is wrong. Rather it is the fact that both are valid unravelings of the same ME that says that neither of them are objective pure-state dynamic models (OPDM); according to quantum optical measurement theory, no such model can exist.

In this Letter we drop the assumption that quantum optical measurement theory is correct in order to ask whether, and how, one could try to rule out these OPDMs experimentally. Moreover, we do not want to rule out just the quantum jump model and the QSD model as detector-independent models; we want experiments that could rule out all OPDMs. This would prove that quantum jumps (or diffusion) is measurement dependent.

We propose experimental tests on a resonantly driven two-level atom that could rule out all OPDMs for the atom, and that do not require any special preparation of the atom or field. The key to these tests is the ability to implement two different ways of monitoring the radiated field, giving rise to two different sorts of stochastic evolution. This is an instance of the EPR phenomenon, also known as “steering” [14], when understood sufficiently generally [15]. Specifically, under the assumption that an objective state exists (obeying some OPDM), we derive an EPR-steering inequality [16] that could be violated experimentally [17,18]. With two particular monitoring schemes we propose, this could be done for efficiencies as low as 0.58, which is the main result of this Letter.

This Letter is organized as follows. First we briefly explain how EPR steering can be demonstrated experimentally. Then we present the model quantum system for our investigation: resonance fluorescence of a strongly driven two-level atom. Next we present two very different monitoring schemes: a spectrally resolved photon counting (jump) scheme; and a homodyne (diffusion) scheme. We then show that an EPR-steering inequality suitable for these continuous-in-time measurements can be violated for an efficiency  $\eta > 0.58$ . We also consider the option of using two different homodyne schemes (X and Y). Although the minimum sufficient efficiency is somewhat higher in this case ( $\eta > 0.73$ ), this test would probably be more practical. Finally we derive a necessary efficiency condition  $\eta > 1/2$  which pertains even if one could implement the whole class of diffusive unravelings.

*EPR-steering.*—In the original EPR paradox [3], the ability of one party (Alice) to measure different observables—position and momentum—on her half of an entangled state allows her to collapse the state of the other half (Bob’s) into different and incompatible states—position and momentum eigenstates—at will. That is, the essence of the phenomenon is that Alice can disprove the hypothesis that Bob’s system has an objective quantum state (i.e., one existing independent of her measurement choice) [15]. It is this general phenomenon of EPR steering that lies behind our tests.

In our case Bob has a two-level system, or qubit. For any qubit state  $\rho$  it is easy to verify that

$$f_1(\rho) + f_2(\rho) \leq 1, \quad (1)$$

with  $f_1(\rho) \equiv (\text{Tr}[\hat{\sigma}_x \rho])^2$ ,  $f_2(\rho) \equiv (\text{Tr}[\hat{\sigma}_y \rho])^2 + (\text{Tr}[\hat{\sigma}_z \rho])^2$ . Now under the objective quantum state assumption, Bob’s system is in some pure state  $\rho_\psi^0 = |\psi\rangle\langle\psi|$ . This state may be unknown to him, and chosen at random from an ensemble  $\{\rho_\psi^0\}$ . Here we are using unnormalized states  $\tilde{\rho}_\psi^0 = p_\psi^0 \rho_\psi^0$ , where  $p_\psi^0 d\mu(\psi)$  is the probability distribution over the pure states, with  $d\mu(\psi)$  being a standard measure. Now Eq. (1) applies for all  $\rho$ , so

$$E[f_1(\rho^0)] + E[f_2(\rho^0)] \leq 1, \quad (2)$$

where  $E[f(\rho^0)] \equiv \int d\mu(\psi) p_\psi^0 f(\rho_\psi^0)$ .

Say now that Alice can choose between two different measurements, called S and Y (for reasons that will become apparent later). Under the objective state assumption, Alice’s measurement can do nothing except provide some information about which state  $\rho_\psi^0$  pertains to Bob’s system. That means that the ensemble of possible states for Bob’s system, conditioned on the result of Alice’s measurement S, is a coarse graining of Bob’s objective pure-state ensemble [19]. Since  $f_1$  is convex on the state space of  $\rho$ , it follows that  $E[f_1(\rho^S)] \leq E[f_1(\rho^0)]$  [16]. The same remarks hold for the Y ensemble and  $f_2$ , so  $E[f_2(\rho^Y)] \leq E[f_2(\rho^0)]$ . Thus from Eq. (2) we have

$$S^{S,Y} \equiv E[f_1(\rho^S)] + E[f_2(\rho^Y)] \leq 1. \quad (3)$$

The two terms in this EPR-steering inequality can be measured experimentally by Alice choosing between measurements S and Y, and by Bob correlating the results of measurements on his qubit with the results Alice reports. If Eq. (3) is violated then the experiment disproves the hypothesis that Bob has an objective pure state. This is possible only if (as in the EPR paradox) Bob’s system is entangled with Alice’s prior to her measurement. Further details on the above argument, in particular, how it works when each of Alice’s measurements is a continuous-in-time readout of a quantum field, are given below.

*Example quantum optical system.*—Let Bob’s quantum system be a single two-level atom, driven by a resonant laser field. This is described by the resonance fluorescence ME; in the usual interaction frame [9], which removes the atomic transition frequency  $\omega_0$ , this is

$$\dot{\rho} = \mathcal{L}\rho \equiv -i[\hat{H}_\Omega, \rho] + \gamma\mathcal{D}[\hat{\sigma}_-]\rho. \quad (4)$$

Here  $\hat{H}_\Omega = (\Omega/2)\hat{\sigma}_x$  is the Hamiltonian describing resonant driving,  $\hat{\sigma}_- = (\hat{\sigma}_x - i\hat{\sigma}_y)/2$  is the atomic lowering operator, and  $\mathcal{D}[\hat{c}]\rho \equiv \hat{c}\rho\hat{c}^\dagger - \frac{1}{2}(\hat{c}^\dagger\hat{c}\rho + \rho\hat{c}^\dagger\hat{c})$  as usual. Now move into the  $\Omega$ -rotating frame with respect to the Hamiltonian  $\hat{H}_\Omega$ . This effects the transformation

$$\hat{\sigma}_- \rightarrow \frac{1}{2}(\hat{\tau}_-^+ e^{-i\Omega(t-t_0)} + \hat{\sigma}_x - \hat{\tau}_-^- e^{+i\Omega(t-t_0)}), \quad (5)$$

where  $\hat{\tau}_+^\pm = (\hat{\tau}^\pm)^\dagger \equiv |+\rangle\langle-|$  and  $\hat{\sigma}_x|\pm\rangle = \pm|\pm\rangle$ . Now if  $\Omega \gg \gamma$  then in this rotating frame we can make the secular approximation, dropping terms in the ME rotating at frequency  $\Omega$  or  $2\Omega$ . This gives the approximate ME

$$\dot{\rho} = \bar{\mathcal{L}}\rho \equiv \frac{\gamma}{4}(\mathcal{D}[\hat{\tau}_+^\dagger] + \mathcal{D}[\hat{\sigma}_x] + \mathcal{D}[\hat{\tau}_+^-])\rho. \quad (6)$$

The simplicity of this equation allows us to obtain the semianalytical results for EPR steering below. Some experimental considerations are discussed in Ref. [20].

*Spectral adaptive interferometric detection (SAID).*—The three irreversible terms in Eq. (9) correspond to the three spectral peaks in resonance fluorescence, at frequencies  $\omega_0 - \Omega$ ,  $\omega_0$ , and  $\omega_0 + \Omega$  respectively. If Alice uses a spectrally resolving detection technique in the limit of large  $\Omega$ , the atom will undergo three types of jump [21]. The jump operator from the first term ( $\hat{\tau}_+^\dagger$ ) collapses the atom into the  $|-\rangle$  state; that from the last ( $\hat{\tau}_+^-$ ) into the  $|+\rangle$  state. These are “good” jumps in terms of making the system state pure. The jump operator from the middle term ( $\hat{\sigma}_x$ ), however, does not change the purity of the state. This makes it a “bad” jump because, if the efficiency is less than unity, the purity of the system state decays monotonically following a jump, and can be restored only when it next jumps. However these “bad” jumps can be made “good” if Alice adds a weak LO to the fluorescence before detection, resonant with the atom, so that the source field is proportional not to  $\hat{\sigma}_-$ , but to

$\hat{\sigma}_- \pm 1/2$ . Here the two cases correspond to opposite signs for the LO. Then the jump operator from the middle term becomes proportional to  $\hat{\sigma}_x \pm 1$ , which equals  $2\hat{\pi}_\pm$ , where  $\hat{\pi}_\pm = |\pm\rangle\langle\pm|$ .

The optimal scheme, for maximizing the purity of the state, is to choose the LO phase adaptively, using real time feedback [9]. Specifically, Alice should choose the  $\pm$  case when the preceding jump put the atom into the  $|\pm\rangle$  state. This choice maximizes the rate of jumps, which is optimal because every jump repurifies the atom. Following a jump into state  $|+\rangle$ , the quantum trajectory theory appropriate to an efficiency  $\eta_S \leq 1$  [9] predicts that the unnormalized state will evolve according to

$$\dot{\tilde{\rho}}^S = \tilde{\mathcal{L}}\tilde{\rho}^S - \frac{\gamma\eta_S}{4}(\mathcal{J}[\hat{\pi}_-^+] + 4\mathcal{J}[\hat{\pi}_+] + \mathcal{J}[\hat{\pi}_+^-])\tilde{\rho}^S, \quad (7)$$

where the ‘‘S’’ superscript means the state is conditioned on this SAID scheme and  $\mathcal{J}[\hat{c}]\rho \equiv \hat{c}\rho\hat{c}^\dagger$  as usual. This state is unnormalized, with the decaying norm equal to the probability of lasting so long without another jump.

It is easy to verify that the solution of Eq. (7) is a mixture of  $x$  eigenstates, and that each jump repurifies it to  $x = \pm 1$ . Thus the stationary ensemble  $\{\tilde{\rho}_x^S\}$  of conditional states under the SAID scheme is indexed by a single real parameter,  $x = \langle\hat{\sigma}_x\rangle$ . We can quantify how well the scheme maintains the state purity by  $E[(\langle\hat{\sigma}_x\rangle^S)^2]$ , the ensemble average of the square of  $x$ . We show in Ref. [20] how to calculate this analytically. The result is shown as a function of  $\eta_S$ , in Fig. 1(a) as a red dashed line. As expected, it is monotonically increasing with  $\eta_S$  and attains unity as  $\eta_S \rightarrow 1$ .

*Y-homodyne detection.*—As our second unraveling of the ME (4) we consider homodyne detection. The quantum trajectories for the normalized conditioned state under this monitoring are obtained by adding the following (zero-mean) term to the ME (4) [9]

$$d\rho^Q = \sqrt{\gamma}\mathcal{H}[dZ^*(t)\hat{\sigma}_-]\rho^Q. \quad (8)$$

Here  $\mathcal{H}[\hat{c}] \equiv \hat{c}\rho + \rho\hat{c} - \text{Tr}[(\hat{c} + \hat{c}^\dagger)\rho]\rho$ , and  $Z(t)$  is a complex random Wiener increment (related to the noise in the photocurrent), normalized so that  $\langle|dZ(t)|^2\rangle = \eta_Q dt$ . The phase  $\phi$  of the LO appears in  $\langle dZ(t)^2\rangle = e^{2i\phi}\eta_Q dt$ . This allows different quadratures (‘‘Q’’) to be monitored, and the Y quadrature corresponds to  $\phi = \pi/2$ .

For homodyne detection to maintain a high-purity conditioned atomic state in the  $\Omega \gg \gamma$  limit requires the effective bandwidth [9] of the detector to be much greater than  $\Omega$ , as the spectrum of the homodyne photocurrent will have a signal at zero frequency and at  $\pm\Omega$  [12]. These correspond to the three terms in Eq. (9), and in that rotating frame the additional terms describing conditioning on Y-homodyne detection are

$$d\rho^Y = \sqrt{\frac{\eta_Y\gamma}{4}}\mathcal{H}[idV_\Omega\hat{\pi}_-^\pm + idW_x\hat{\sigma}_x - idV_\Omega^*\hat{\pi}_+^\mp]\rho^Y. \quad (9)$$

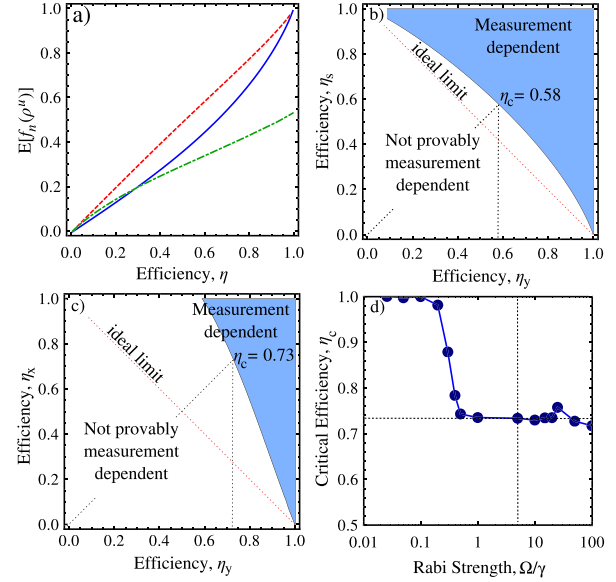


FIG. 1 (color online). (a) As a function of efficiency  $\eta$ , we plot: (red dashed)  $E[(\langle\hat{\sigma}_x\rangle^S)^2]$  for the SAID unraveling, large  $\Omega$  limit; (solid blue)  $E[(\langle\hat{\sigma}_y\rangle^Y)^2 + (\langle\hat{\sigma}_z\rangle^Y)^2]$  for the Y-homodyne unraveling, in the large  $\Omega$  limit; (green dot-dashed)  $E[(\langle\hat{\sigma}_x\rangle^S)^2]$  for the X-homodyne unraveling from simulations with  $\Omega = 5\gamma$ . (b)  $S^{S,Y}(\eta_Y, \eta_S)$  is plotted with the blue shaded regime ( $S > 1$ ) representing when the experiment would rule out all theories of objective atomic state reduction. (c) is the same as (b) with SAID replaced by X-homodyne detection and  $\Omega = 5\gamma$  for both unravelings. (d) The efficiency required for X and Y homodyne to have  $S > 1$ , as a function of  $\Omega/\gamma$ . For more details see text.

Here  $dV_\Omega$  is an irreducibly complex Wiener increment satisfying  $\langle|dV_\Omega|^2\rangle = dt$  but  $\langle dV_\Omega^2\rangle = 0$ , independent of the *real* increment  $dW_x$ . The minus sign before the last term comes from the corresponding minus sign in Eq. (5).

It is not difficult to show that the long-time solution of this Y-homodyne quantum trajectory is confined to the  $x = 0$  plane of the Bloch sphere, and so is parametrized by two numbers,  $y = \langle\hat{\sigma}_y\rangle$  and  $z = \langle\hat{\sigma}_z\rangle$ . That is, the ensemble  $\{\tilde{\rho}_{(y,z)}^Y\}$  of conditioned states in this case is as different as possible from the ensemble  $\{\tilde{\rho}_x^S\}$  in the SAID monitoring case, which is confined to the  $x$  axis. As above, we can quantify how well this monitoring scheme maintains the state purity by the long-time expectation for the square of the conditional average of the Bloch vector length,  $E[(\langle\hat{\sigma}_y\rangle^Y)^2 + (\langle\hat{\sigma}_z\rangle^Y)^2]$ . As we show in Ref. [20], this can easily be calculated to arbitrary numerical precision. The result is shown in Fig. 1(a) as the solid blue line. It is similar to that for SAID, but is smaller (the conditioned states tend to be less pure).

*EPR-steering criterion.*—Assume now, as imagined in OPDMs, that the atom has some ‘‘true’’ pure state  $\rho_\psi^O = |\psi\rangle\langle\psi|$  at every instance of time. The index  $\psi$  that pertains at any particular time changes stochastically in some manner defined by the model. In the standard quantum jump model  $\psi$  would evolve deterministically and smoothly apart from the occasional jump, while in the QSD model,

for example,  $\psi$  would evolve nondeterministically and nonsmoothly at all times. Once the system has reached equilibrium it will be described by a stationary ensemble  $\{\tilde{\rho}_\psi^0\}$  as described earlier.

Now under the above OPDM assumption, the stationary ensemble  $\{\tilde{\rho}_x^S\}$  realized by Alice's SAID scheme must be merely a coarse-graining of  $\{\tilde{\rho}_\psi^0\}$ . That is, there must exist a conditional probability distribution  $\varphi(x|\psi)$  such that  $\forall x$ ,  $\tilde{\rho}_x^S = \int d\mu(\psi)\varphi(x|\psi)\tilde{\rho}_\psi^0$ . The same statements hold for the Y-homodyne ensemble  $\{\tilde{\rho}_{(y,z)}^Y\}$ , *mutatis mutandis*. Thus from the arguments rehearsed earlier, we can derive the EPR-steering inequality Eq. (3), where the value of  $S^{S,Y}$  depends only upon the efficiencies.

Experimentally, the quantity  $S^{S,Y}(\eta_S, \eta_Y)$  could be measured as follows. In any given run, Alice randomly chooses to implement either the SAID or the Y-homodyne monitoring of the atomic fluorescence. After some randomly chosen time  $T \gg \gamma^{-1}$ , Bob halts the experiment (so that no further light reaches Alice), and immediately reads out the state of the atom. More particularly, he randomly measures either  $\hat{\sigma}_x$ ,  $\hat{\sigma}_y$  or  $\hat{\sigma}_z$ . Alice reveals to Bob which monitoring scheme she performed, and the parameters ( $x$  in case 1, and  $y, z$  in case 2) of her conditioned state for the atom at time  $T$ , which she can determine at her leisure from her measurement record using the above quantum trajectory theory. Bob then stores the results of his measurements in different “bins” for different values of  $x$  (in case 1) or  $y, z$  (in case 2). He can then calculate, for example, the first term in Eq. (3) by first determining the average of his measurement of  $\hat{\sigma}_x$  in each bin, then squaring it, then averaging over all bins, weighted by the number of entries in each bin.

Note that Bob does not have to put any trust in the state parameters that Alice reports; they are merely labels for his bins. Nevertheless, for sufficiently fine binning, if Alice really can implement the above detection schemes, we would expect the result of Bob's averaging procedure to agree with the ensemble averages  $E[(\langle\hat{\sigma}_x\rangle^S)^2]$  and  $E[(\langle\hat{\sigma}_y\rangle^Y)^2 + (\langle\hat{\sigma}_z\rangle^Y)^2]$  computed above. If the results violate the inequality (3), then the experiment would have proven that the initial assumption, that there exists an OPDM for the atom, must be wrong. In Fig. 1(b) we plot  $S^{S,Y}(\eta_Y, \eta_S)$ , and see that the EPR-steering inequality (3) is violated in the blue shaded regime. In particular, if  $\eta_Y = \eta_S = \eta$ , one could prove that quantum jumps are detector-dependent with  $\eta \geq 0.58$ . This is the main result of this Letter.

Achieving  $\eta \geq 0.58$  is still very challenging experimentally. One might hope that choosing a different pair of unravelings, or using a better EPR-steering inequality, could substantially lower this requirement. This is not the case, as we now show. If  $\eta_Y + \eta_S \leq 1$  then it would be possible for a hypothetical observer to implement simultaneously the SAID and the Y-homodyne monitorings, giving rise to a doubly conditioned ensemble  $\{\tilde{\rho}_{(x,y,z)}^{S+Y}\}$ . This ensemble has exactly the right properties to be an

OPDM ensemble  $\{\tilde{\rho}_\psi^0\}$ , since coarse graining by ignoring the Y conditioning would give  $\{\tilde{\rho}_x^S\}$  and *vice versa*. Thus to disprove all OPDMs we clearly need  $\eta_Y + \eta_S > 1$ . That is, the necessary condition is  $\eta > 0.5$ , scarcely less onerous than the sufficient condition of  $\eta \geq 0.58$ .

*X- and Y-homodyne detection.*—In practice, photon counters (at least fast ones, as required here) are less efficient than the photoreceivers used for homodyne detection [9]. The SAID scheme has the additional challenges of spectral resolution, and feedback much faster than the atomic lifetime  $\gamma^{-1}$ . Also, the above analysis is valid only in the limit  $\Omega/\gamma \rightarrow \infty$ . For these reasons we now consider replacing the SAID scheme by X-homodyne detection, and we keep  $\Omega/\gamma$  finite. Although the X-homodyne scheme does not confine the conditioned system state to the  $x$  axis (as in the SAID unraveling) it does tend to do so [9,12]. Thus we expect that for a high enough efficiency we could violate the same EPR-steering inequality (3), but with “S” replaced by “X”. The quantum trajectories for the X- and Y-homodyne schemes are obtained by adding Eq. (8) to Eq. (4), with the LO phases  $\phi = 0$  and  $\pi/2$ , respectively. Numerical simulations of  $S^{Y,X}(\eta_Y, \eta_X)$  are shown in Fig. 1(c) for  $\Omega = 5\gamma$  and yield a violation (blue shaded regime) for  $\eta \geq 0.73$ . Furthermore this is the critical efficiency for all  $\Omega > \gamma$ , as shown in Fig. 1(d).

*General diffusive unravelings.*—With two homodyne schemes of efficiency  $\eta$  the same reasoning as earlier implies that a necessary condition for proving the subjectivity of quantum unravelings is  $\eta > 1/2$ . Now if one can measure the X and Y quadratures then typically one can measure any quadrature, and one might think that being able to choose between say  $N$  different quadratures would make it easier to demonstrate EPR steering, as the obvious necessary condition would be  $\eta > 1/N$ . In fact,  $\eta > 1/2$  is still necessary, as shown in Ref. [20].

To conclude, the original notion of quantum jumps, from almost 100 years ago, is that atoms radiate via an objective stochastic process. Although quantum trajectory theory developed in the early 1990s asserts that there can be no detector-independent pure-state atomic dynamics—regardless of the nature of jumps (or diffusion) proposed—no experiment has ever been done to rigorously test this assertion. With the experimental tests we have proposed here, it should be possible to rule out all such objective models, proving finally that dynamical quantum jumps are indeed detector dependent.

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