

## Spin-Selective Transport of Electrons in DNA Double Helix

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The experiment that the high spin selectivity and the length-dependent spin polarization are observed in double-stranded DNA [Science **331**, 894 (2011)], is elucidated by considering the combination of the spin-orbit coupling, the environment-induced dephasing, and the helical symmetry. We show that the spin polarization in double-stranded DNA is significant even in the case of weak spin-orbit coupling, while no spin polarization appears in single-stranded DNA. Furthermore, the underlying physical mechanism and the parameter dependence of the spin polarization are studied.

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Molecular spintronics, by combining molecular electronics with spintronics to manipulate the transport of electron spins in organic molecular systems, is regarded as one of the most promising research fields and is now attracting extensive interest [1–4], owing to the long spin relaxation time and the flexibility of organic materials. Unconventional magnetic properties of molecular systems reported in organic spin valves and magnetic tunnel junctions, are attributed to the hybrid states in the organic-magnetic interfaces [5–9] and to single-molecule magnet [4]. Organic molecules would not be suitable candidates for spin-selective transport because of their nonmagnetic properties and weak spin-orbit coupling (SOC) [10].

However, very recently, Göhler *et al.* reported the spin selectivity of photoelectron transmission through self-assembled monolayers of double-stranded DNA (dsDNA) deposited on gold substrate [11]. They found that well-organized monolayers of the dsDNA act as very efficient spin filters with high spin polarization at room temperature for long dsDNA, irrespective of the polarization of the incident light. The spin filtration efficiency increases with increasing length of the dsDNA and contrarily no spin polarization could be observed for single-stranded DNA (ssDNA). These results were further substantiated by direct charge transport measurements of single dsDNA connected between two leads [12]. Although several theoretical models were put forward to investigate the spin-selective properties of DNA molecule based on single helical chain-induced Rashba SOC [13,14], the models neglect the double helix feature of the dsDNA and are somewhat inconsistent with the experimental result that the ssDNA could not be a spin filter. Until now, the underlying physical mechanism remains unclear for high spin selectivity observed in the dsDNA [15,16].

In this Letter, a model Hamiltonian, including the small environment-induced dephasing, the weak SOC, and the helical symmetry, is proposed to investigate the quantum spin transport through the ssDNA and dsDNA connected to nonmagnetic leads. We interpret the experimental results that the electrons transmitted through the dsDNA exhibit

high spin polarization, the spin filtration efficiency will be enhanced by increasing the DNA length, and no spin polarization appears for the ssDNA. The physical mechanism arises from the combination of the dephasing, the SOC, and the helical symmetry. No spin polarization could be observed if any aforementioned factor is absent. In addition, the high spin polarization can be observed in a very wide range of the parameters.

The charge transport through the dsDNA, illustrated in Fig. 1, can be simulated by the Hamiltonian:

$$\mathcal{H} = \mathcal{H}_{\text{DNA}} + \mathcal{H}_{\text{lead}} + \mathcal{H}_c + \mathcal{H}_{\text{so}} + \mathcal{H}_d. \quad (1)$$

Here,  $\mathcal{H}_{\text{DNA}} = \sum_{n=1}^N [\sum_{j=1}^2 (\epsilon_{jn} c_{jn}^\dagger c_{jn} + t_{jn} c_{jn}^\dagger c_{jn+1}) + \lambda_n c_{1n}^\dagger c_{2n} + \text{H.c.}]$  is the Hamiltonian of usual two-leg ladder model including the spin degree of freedom [17], with

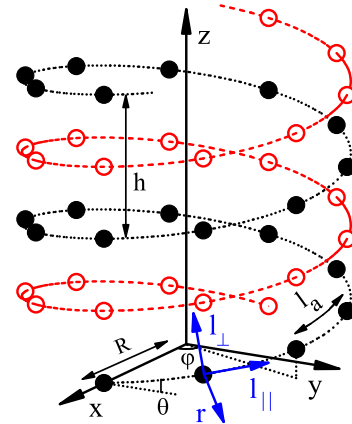


FIG. 1 (color online). Schematic view of the dsDNA with radius  $R$ , pitch  $h$ , helix angle  $\theta$ , and arc length  $l_a$ . The circles represent the nucleobases, where the full ones assemble one helical chain and the open ones form the other helical chain. The arc length satisfies  $l_a \cos \theta = R \Delta \varphi$  and  $l_a \sin \theta = \Delta h$ , with  $\Delta \varphi$  and  $\Delta h$  being the twist angle and the stacking distance between neighboring base-pairs, respectively. We set  $\Delta h = 0.34$  nm,  $\Delta \varphi = \frac{\pi}{5}$ , and  $h = 3.4$  nm, which are typical values of B-form DNA. Other parameters are:  $R = 0.7$  nm,  $\theta \approx 0.66$  rad, and  $l_a \approx 0.56$  nm.

$N$  the DNA length,  $c_{jn}^\dagger = (c_{jn}^\dagger, c_{jn}^\dagger)$  the creation operator of the spinor at the  $n$ th site of the  $j$ th chain of the dsDNA,  $\varepsilon_{jn}$  the on-site energy,  $t_{jn}$  the intrachain hopping integral, and  $\lambda_n$  the interchain hybridization interaction.  $\mathcal{H}_{\text{lead}} + \mathcal{H}_c = \sum_{k,\beta(\beta=L,R)} [\varepsilon_{\beta k} a_{\beta k}^\dagger a_{\beta k} + t_{\beta k} a_{\beta k}^\dagger (c_{1n_\beta} + c_{2n_\beta}) + \text{H.c.}]$  describe the left and right nonmagnetic leads and the coupling between the leads and the dsDNA, with  $n_L = 1$  and  $n_R = N$ .  $\mathcal{H}_{\text{so}}$  and  $\mathcal{H}_d$  are, respectively, the Hamiltonians of the SOC term and the dephasing term, which will be discussed in the following.

When a charge is moving under an electrostatic potential  $V$ , an SOC arises  $\mathcal{H}_{\text{so}} = \frac{\hbar}{4m^2c^2} \nabla V \cdot (\hat{\sigma} \times \hat{p})$ , with the electron mass  $m$ , the speed of light  $c$ , the Pauli matrices  $\hat{\sigma} = (\sigma_x, \sigma_y, \sigma_z)$ , and the momentum operator  $\hat{p}$ . For the dsDNA which is conductor or semiconductor, the differences of the potential are usually bigger along the radial direction  $\hat{r}$  than that along the helix axis ( $z$  axis in Fig. 1) [18]. On the other hand, since the differences of  $V$  are especially large between the interior and the exterior of the dsDNA,  $dV/dr$  is very large at the boundary  $r = R$  with  $R$  the radius [19]. Hence, it is reasonable to consider the  $\hat{r}$  component of  $V$  only and the SOC can be simplified in the cylindrical coordinate system  $\mathcal{H}_{\text{so}} = -\frac{\alpha}{\hbar} \hat{\sigma} \cdot (\hat{r} \times \hat{p})$  with  $\alpha \equiv \frac{\hbar^2}{4m^2c^2} \frac{d}{dr} V(r)$ . Considering a charge propagating in one helical chain of the dsDNA (e.g., the dotted line in Fig. 1), the momentum  $\hat{p} = \hat{p}_\parallel \hat{l}_\parallel$  with  $\hat{l}_\parallel$  the unit vector along the helical chain direction. Thus  $\mathcal{H}_{\text{so}}$  is reduced to  $\mathcal{H}_{\text{so}} = -\frac{\alpha}{2\hbar} [\sigma_\perp \hat{p}_\parallel + \hat{p}_\parallel \sigma_\perp]$ , where  $\sigma_\perp(\varphi) = \sigma_x \sin\varphi \sin\theta - \sigma_y \cos\varphi \sin\theta + \sigma_z \cos\theta$  with  $\theta$  the helix angle and  $\varphi$  the cylindrical coordinate. Since the dsDNA consists of two helical chains, the total SOC is  $\mathcal{H}_{\text{so}} = -\frac{\alpha}{2\hbar} \times \sum_{j=1}^2 [\sigma_\perp^{(j)} \hat{p}_\parallel^{(j)} + \hat{p}_\parallel^{(j)} \sigma_\perp^{(j)}]$  with  $\sigma_\perp^{(1)} = \sigma_\perp(\varphi)$  and  $\sigma_\perp^{(2)} = \sigma_\perp(\varphi + \pi)$ . The interchain SOC has been neglected because it is very small due to the potential symmetry. By using the second quantization [20],  $\mathcal{H}_{\text{so}}$  can be written as

$$\mathcal{H}_{\text{so}} = \sum_{j,n} i t_{\text{so}} c_{jn}^\dagger [\sigma_n^{(j)} + \sigma_{n+1}^{(j)}] c_{jn+1} + \text{H.c.}, \quad (2)$$

where  $t_{\text{so}} = -\frac{\alpha}{4l_a}$ ,  $\sigma_{n+1}^{(1)} = \sigma_\perp(n\Delta\varphi)$ , and  $\sigma_{n+1}^{(2)} = \sigma_\perp(n\Delta\varphi + \pi)$ .  $l_a$  and  $\Delta\varphi$  are, respectively, the arc length and the twist angle between successive base-pairs.

On the other hand, a charge transmitting through the dsDNA will experience inelastic scattering from the phonons due to the fluctuation of each nucleobase around its equilibrium position and other inelastic collisions with the absorbed counterions in the dsDNA due to the negatively charged sugar-phosphate backbones [21]. Such inelastic scattering will give rise to the lose of the phase and spin memory of the charge. Actually, other previous works have clearly indicated the presence of the phase-breaking processes in the DNA molecule [22,23]. To simulate these processes, Büttiker's virtual lead is introduced by

connecting to each nucleobase [24,25], with the Hamiltonian of the dephasing term being

$$\mathcal{H}_d = \sum_{j,n,k} (\varepsilon_{jnk} a_{jnk}^\dagger a_{jnk} + t_d a_{jnk}^\dagger c_{jn} + \text{H.c.}). \quad (3)$$

$a_{jnk}^\dagger = (a_{jnk}^\dagger, a_{jnk}^\dagger)$  is the creation operator of the virtual lead and  $t_d$  is the coupling between the nucleobase and the virtual lead.

Let us demonstrate analytically that the ssDNA could not behave as a spin filter. In continuous real-space spectrum, the Hamiltonian of the ssDNA containing the SOC term is written as  $\mathcal{H}_{\text{ss}} = \frac{\hat{p}_\parallel^2}{2m} - \frac{\alpha}{2\hbar} [\sigma_\perp \hat{p}_\parallel + \hat{p}_\parallel \sigma_\perp] + V(l)$  with  $V(l)$  the potential energy of the helical chain. By taking a unitary transformation with the operator  $U(l) = e^{(i\alpha/\hbar^2) \int_l \sigma_\perp dl}$ , [26]  $\mathcal{H}_{\text{ss}}$  is transformed into  $\mathcal{H}'_{\text{ss}} = U^\dagger \mathcal{H}_{\text{ss}} U = \frac{\hat{p}_\parallel^2}{2m} - \frac{m\alpha^2}{2\hbar^2} + V(l)$ , which is independent of spin. Therefore, no spin polarization could be observed in the ssDNA, regardless of the SOC term, the existence of the dephasing, and other model parameters. This result can be obtained also by using the discrete Hamiltonians of Eqs. (1) and (2). Similarly, we can also verify that any kind of SOC could not give rise to spin polarization in the ssDNA. However, for the dsDNA, the charges can transport not only along the helical chain direction, but also within the base-pairs. In this situation, the Hamiltonian cannot be transformed into a spin-independent one, then the results will present a fundamental distinction.

According to the Landauer-Büttiker (LB) formula, the current in the  $q$ th lead (real or virtual) with spin  $s$  can be written as [27]:  $I_{qs} = (e^2/h) \sum_{m,s'} T_{qs,ms'} (V_m - V_q)$ , where  $V_q$  is the voltage in the  $q$ th lead and  $T_{qs,ms'} = \text{Tr}[\Gamma_{qs} \mathbf{G}^r \Gamma_{ms'} \mathbf{G}^a]$  is the transmission coefficient from the  $m$ th lead with spin  $s'$  to the  $q$ th lead with spin  $s$ . The Green function  $\mathbf{G}^r = [\mathbf{G}^a]^\dagger = [E\mathbf{I} - \mathbf{H}_{\text{DNA}} - \mathbf{H}_{\text{so}} - \sum_{qs} \Sigma_{qs}^r]^{-1}$  and  $\Gamma_{qs} = i[\Sigma_{qs}^r - \Sigma_{qs}^a]$ , with  $E$  the incident electron energy (or the Fermi energy).  $\Sigma_{qs}^r$  is the retarded self-energy due to the coupling to the  $q$ th lead. For the real left/right lead,  $\Sigma_{L/Rs} = -i\Gamma_{L/R}/2 = -i\pi\rho_{L/R}t_{L/R}^2$ ; while for the virtual leads,  $\Sigma_{qs}^r = -i\Gamma_d/2 = -i\pi\rho_d t_d^2$ , with the dephasing parameter  $\Gamma_d$  and  $\rho_{L/R/d}$  being the density of states of the leads. Since the net currents through the virtual leads are zero, their voltages can be calculated from the LB formula by applying an external bias  $V_b$  between the left and right leads with  $V_L = V_b$  and  $V_R = 0$ . Finally, the conductances for spin-up ( $G_\uparrow$ ) and spin-down ( $G_\downarrow$ ) electrons can be obtained  $G_s = (e^2/h) \sum_{m,s'} T_{Rs,ms'} V_m/V_b$ , and the spin polarization is  $P_s = (G_\uparrow - G_\downarrow)/(G_\uparrow + G_\downarrow)$ .

For the dsDNA,  $\varepsilon_{jn}$  is set to  $\varepsilon_{1n} = 0$  and  $\varepsilon_{2n} = 0.3$ ,  $t_{jn}$  is taken as  $t_{1n} = 0.12$  and  $t_{2n} = -0.1$ , and  $\lambda_n = -0.3$ . All these parameters are extracted from first-principles calculations [28–31] and the unit is eV. The helix angle and the twist angle are set to  $\theta \approx 0.66$  rad and  $\Delta\varphi = \frac{\pi}{5}$ ,

respectively. The SOC is estimated to  $t_{so} = 0.01$ , which is an order of magnitude smaller than the intrachain hopping integral. For the real leads, the parameters  $\Gamma_L = \Gamma_R = 1$  are fixed. For the virtual leads, the dephasing strength is small with  $\Gamma_d = 0.005$ , at which the phase coherence length is about  $L_\phi = 14$  [24]. The values of all above-mentioned parameters will be used throughout the Letter except for specific indication in the figure. In fact, the high spin polarization can hold well in a very wide range of the parameters (see below).

Figure 2(a) shows the conductances  $G_{\uparrow/\downarrow}$  and the corresponding spin polarization  $P_s$ . One notices two transmission bands—the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO)—in the energy spectrum, where several transmission peaks are found for both spin-up and spin-down electrons (holes) due to the coherence of the system. For the HOMO band,  $G_\uparrow$  and  $G_\downarrow$  are almost identical, while for the LUMO band,  $G_\uparrow$  and  $G_\downarrow$  are very different. A bell-shaped configuration is observed in the curve of  $P_s$  vs energy  $E$ , where the spin polarization of the dsDNA at  $N = 30$  can achieve 0.44, which is comparable with the experimental results [11].

To explore the physical scenario to high spin polarization observed in the dsDNA, Figs. 2(b) and 2(c) plot the conductance  $G_\uparrow$  and  $P_s$  in the absence of the dephasing ( $\Gamma_d = 0$ ) and of the helical symmetry ( $\theta = \frac{\pi}{2}$ ), respectively. It clearly appears that the spin polarization vanishes when  $\Gamma_d = 0$  or  $\theta = \frac{\pi}{2}$ , although the conductance is very robust in both cases. When  $\Gamma_d = 0$ , the dsDNA decouples with the virtual leads and the charge transport through the dsDNA is completely coherent. In this case, the SOC cannot generate any spin polarization due to the time-reversal symmetry, the helical symmetry, and the

phase-locking effect [32]. A small dephasing is necessary for the existence of the spin polarization. Indeed, it is reasonable to assume a small  $\Gamma_d$  because the dephasing occurs inevitably in the experiment. On the other hand, the spin polarization strongly depends on the DNA helix. If there is no helix ( $\theta = \frac{\pi}{2}$ ), no spin polarization could be observed ( $P_s = 0$ ). If the right-handed helical dsDNA is transformed into the left-handed one (Z-form DNA) with  $\theta \rightarrow \pi - \theta$ ,  $P_s(\pi - \theta) = -P_s(\theta)$  exactly.

We then focus on the spin polarization  $P_s$  and the averaged one  $\langle P_s \rangle$ , where  $\langle P_s \rangle \equiv (\langle G_\uparrow \rangle - \langle G_\downarrow \rangle) / (\langle G_\uparrow \rangle + \langle G_\downarrow \rangle)$  with  $\langle G_s \rangle$  averaged over the LUMO band. Figs. 3(a) and 3(b) show  $P_s$  at a fixed energy  $E$  and  $\langle P_s \rangle$  vs length  $N$ , respectively, for several values of the dephasing parameter. One notices that  $P_s$  and  $\langle P_s \rangle$  are enhanced by increasing  $N$  at first and then saturate or slightly decline after a critical length  $N_c$ . With increasing  $\Gamma_d$ ,  $N_c$  shrinks monotonically [Fig. 3(d)]. The behavior of  $N_c$  vs  $\Gamma_d$  can be fitted well by a simple function  $N_c \propto \Gamma_d^{-1}$ .  $N_c$  is about 3 times longer than the phase coherence length  $L_\phi$ , implying that high  $P_s$  can be observed even if the noncoherent charge transport mechanism dominates. For relatively large  $\Gamma_d$  (diamond and triangle symbols),  $P_s$  and  $\langle P_s \rangle$  increase faster in the beginning and saturate at shorter length with smaller values because the device is more open. While for smaller  $\Gamma_d$ ,  $P_s$  and  $\langle P_s \rangle$  increase slower with increasing  $N$  in a wider range of  $N$  and have larger saturation values. Let us see  $\Gamma_d = 0.0004$  for instance (circle symbols).  $P_s$  and  $\langle P_s \rangle$  will keep rising even for  $N > 100$ , and  $P_s = 0.42$  at  $N = 40$  and  $P_s = 0.55$  at  $N = 80$ . These results are quantitatively consistent with the experiment [11]. In fact, the dephasing has two effects: (i) it promotes the openness of the two-terminal device and produces the spin polarization [32]; (ii) it makes the charge

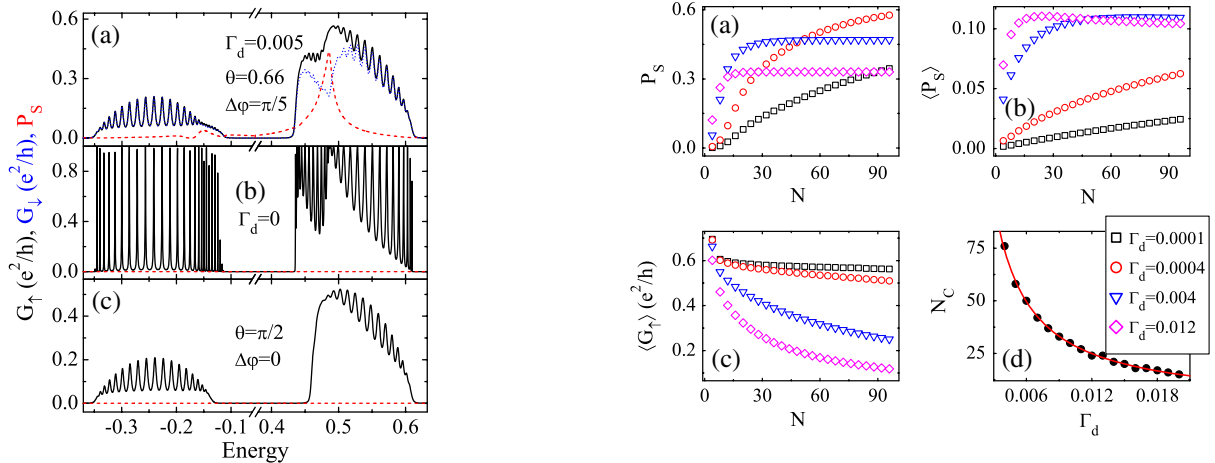


FIG. 2 (color online). (a) Energy dependence of conductance  $G_\uparrow$  (solid line),  $G_\downarrow$  (dotted line), and spin polarization  $P_s$  (dashed line) for realistic situation. (b) and (c) show  $G_\uparrow$  and  $P_s$  in the absence of the dephasing and of the helical symmetry, respectively. Here,  $N = 30$ .

FIG. 3 (color online). Length dependence (a) of  $P_s$  at  $E = 0.486$ , (b) of  $\langle P_s \rangle$ , and (c) of  $\langle G_\uparrow \rangle$  for different values of the dephasing parameter. (d) The critical length  $N_c$  vs  $\Gamma_d$ . Here  $N_c$  is extracted from the curve of  $\langle P_s \rangle$ - $N$  and the solid line is the fitting curve with  $N_c \propto \Gamma_d^{-1}$ . The legends in (d) are for panels (a), (b), and (c).

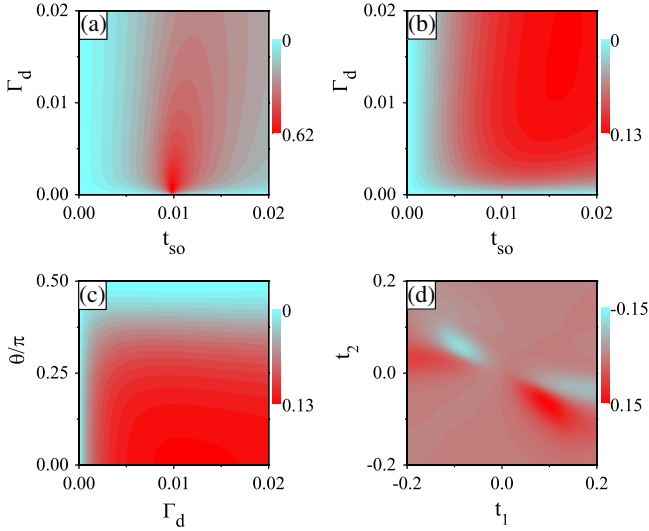


FIG. 4 (color online). (a)  $P_s$  vs the SOC  $t_{so}$  and the dephasing  $\Gamma_d$  at  $E = 0.486$  with  $N = 80$ . (b), (c), and (d) show  $\langle P_s \rangle$  with  $N = 30$  as functions of  $t_{so}$  and  $\Gamma_d$ , of  $\Gamma_d$  and  $\frac{\theta}{\pi}$ , and of  $t_1$  and  $t_2$ , respectively.

lose its phase and spin memory and then  $P_s$  is decreased by further increasing  $\Gamma_d$ . Accordingly, for large  $\Gamma_d$  with the phase coherence length being several base-pairs,  $P_s$  will be quite small.  $P_s < 0.05$  for  $\Gamma_d = 0.5$  and  $P_s \rightarrow 0$  if  $\Gamma_d \rightarrow \infty$ . Because of the interplay between the above two effects, a small  $\Gamma_d$ , ranging from 0.0002 to 0.01, is optimal for large  $P_s$ . Notice that the optimal range of  $\Gamma_d$  is very wide. In addition, Fig. 3(c) shows the averaged conductance  $\langle G_T \rangle$  vs  $N$ .  $\langle G_T \rangle$  is declined by increasing  $N$  or  $\Gamma_d$ , because large  $N$  or  $\Gamma_d$  will enhance the scattering. However,  $\langle G_T \rangle$  remains quite large for  $N = 100$  and  $\Gamma_d = 0.012$ , because of the noncoherent charge transport mechanism [23]. Therefore, the dsDNA is a well spin filter due to the large  $P_s$  and  $\langle G_T \rangle$ .

Let us further study the spin polarization by varying other model parameters. Figures 4(a) and 4(b) show  $P_s$  at  $E = 0.486$  with  $N = 80$  and  $\langle P_s \rangle$  with  $N = 30$ , respectively, as functions of the SOC  $t_{so}$  and the dephasing strength  $\Gamma_d$ .  $P_s$  and  $\langle P_s \rangle$  are zero exactly when  $\Gamma_d = 0$  or  $t_{so} = 0$ . Of course,  $t_{so}$  is a key factor for the spin polarization or equivalently  $t_{so}$  is “the driving force” of  $P_s$ . If there is no SOC, no spin polarization would appear for whatever other parameters are. In general, strong SOC usually leads to large  $\langle P_s \rangle$  [Fig. 4(b)]. However, for fixed  $E$ ,  $P_s$  will not increase monotonically with  $t_{so}$ , as seen in Fig. 4(a). A large  $P_s$  can be obtained for long dsDNA even for quite small  $t_{so}$ , because the spin polarized electrons will accumulate gradually when the electrons are transmitting along the dsDNA. In addition, we observe a large area with red color in Fig. 4(b), where  $\langle P_s \rangle$  exceeds 0.1 for short dsDNA. This implies that the dsDNA would be an efficient spin filter in a wide parameters range.

Figure 4(c) plots the averaged spin polarization  $\langle P_s \rangle$  vs  $\Gamma_d$  and  $\frac{\theta}{\pi}$  by fixing the radius  $R$  and the arc length  $l_a$  to account for the rigid sugar-phosphate backbones. The helix angle  $\theta$  can be changed by stretching the DNA molecule [33]. It is obvious that  $\langle P_s \rangle$  is zero in the absence of the helical symmetry ( $\theta = \frac{\pi}{2}$ ) and is increased by decreasing  $\theta$ . This indicates that the helix of the dsDNA plays a vital role to the existence of the spin polarization. Finally, we present the influence of the hopping integrals  $t_1$  and  $t_2$  on the spin polarization, as illustrated in Fig. 4(d). We can see that  $\langle P_s \rangle$  is much bigger in a wide range of  $t_1$  and  $t_2$  when they have opposite sign, and the sign of  $\langle P_s \rangle$  can be reversed by switching  $t_1$  and  $t_2$ . Besides, further studies indicate that the spin polarization remains considerably large even in the presence of the disorder, e.g., the on-site energy disorder, the twist angle disorder. Accordingly, our results can also hold for other aperiodic DNA molecules.

In summary, we propose a model Hamiltonian to simulate the quantum spin transport through the dsDNA. This two-terminal dsDNA-based device would exhibit high spin polarization by considering the SOC, the dephasing, and the helical symmetry, although no spin polarization exists in the ssDNA. The spin polarization increases with increasing the DNA length. Additionally, the spin polarization could be improved by properly modifying the hopping integral and decreasing the helix angle.

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