## Experimental Realization of Plaquette Resonating Valence-Bond States with Ultracold Atoms in Optical Superlattices

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The concept of valence-bond resonance plays a fundamental role in the theory of the chemical bond and is believed to lie at the heart of many-body quantum physical phenomena. Here we show direct experimental evidence of a time-resolved valence-bond quantum resonance with ultracold bosonic atoms in an optical lattice. By means of a superlattice structure we create a three-dimensional array of independent four-site plaquettes, which we can fully control and manipulate in parallel. Moreover, we show how small-scale plaquette resonating valence-bond (RVB) states with *s*- and *d*-wave symmetry can be created and characterized. We anticipate our findings to open the path towards the creation and analysis of many-body RVB states in ultracold atomic gases.

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In his theory of the chemical bond, Pauling developed the concept of quantum resonance: a quantum superposition of resonant structures with different arrangements of the valence bonds [1]. Such resonant states are essential to explain the chemical properties of certain organic molecules like benzene [2]. In the context of high temperature superconductivity, Anderson extended Pauling's notion to a macroscopic level, by proposing that electrons in Mott insulating solid state materials could form resonating valence-bond (RVB) states [3,4]. In a Mott insulating phase, electrons are localized to individual atoms or molecules, and the fluctuations in the charge (density) degree of freedom are strongly suppressed. The physics is dictated by the remaining spins, which interact via superexchange interactions. Under certain conditions, the localized spins are expected to evade local order and continue to fluctuate down to zero temperature, forming a coherent superposition of many different arrangements in which the spins are paired up into singlets or valence bonds.

Ultracold atomic gases in optical lattices [5–7] and other quantum optical systems are promising candidates for the quantum simulation of RVB states [8]. Their realization would allow one to gain valuable insight into the entanglement properties of these states as well as to answer fundamental questions in condensed matter physics like their stability under specific Hamiltonians such as the Hubbard model, or to test their exotic superconducting properties upon doping [9,10]. In this work we create an array of small-scale versions of Pauling-like RVB states in four-site plaquettes and study their basic physical properties. Our techniques can be directly generalized to a gas of fermionic atoms, for which one expects that the adiabatic connection of such isolated plaquette RVB states could lead to the creation of a macroscopic *d*-wave superfluid state [9–11].

Let us consider an ultracold gas of bosonic atoms in two internal states, loaded into a two-dimensional superlattice structure whose elementary cell is a plaquette made out of four wells arranged in a square pattern [Fig. 1(a)]. In the regime in which the tunneling amplitude between adjacent plaquettes is strongly suppressed, the system can be regarded as a collection of independent replicas of a single plaquette, the object of our study. At half filling, and when the on-site interaction U dominates over the tunneling amplitude t between wells in a plaquette, atoms are site localized, one per site, and the physics is governed by the remaining four effective  $\frac{1}{2}$  spins, which interact with their next neighbors via a ferromagnetic Heisenberg interaction  $J\vec{S}_i \cdot \vec{S}_i$ , with  $J = -4t^2/U$  [12–16].

To gain insight into the RVB states on a plaquette, it is convenient to write the Heisenberg interaction in terms of the swap operator  $\hat{X}_{ij} = 2\vec{S}_i \cdot \vec{S}_j + 1/2$ , a unitary operator that exchanges the states of the spins on the sites *i* and *j*. The plaquette Hamiltonian then takes the form [17]:

$$\hat{H} = J_x \hat{X}_x + J_y \hat{X}_y, \tag{1}$$

where  $\hat{X}_{x(y)}$  involves exchanges of two spins along an x(y)bond:  $\hat{X}_x = (\hat{X}_{AB} + \hat{X}_{CD})/2$ ,  $\hat{X}_y = (\hat{X}_{AD} + \hat{X}_{BC})/2$ , with A, B, C, D labeling the four sites of the plaquette [Fig. 1(a)]. From now on, we consider solely the subspace of total spin zero, where all spins are part of a singlet state or valence bond. This subspace is generated by two states, which correspond

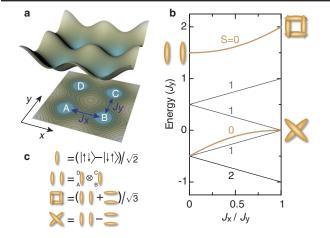


FIG. 1 (color). Schematics of a single plaquette and energy levels at half filling. (a) Scheme of the lattice potential in the *x*, *y* plane, created by a pair of bichromatic optical lattices. The elementary cell is made of four wells arranged in a square configuration. (b) Energy levels of four atoms on a plaquette in a Mott insulating state at half filling, with superexchange spin couplings along *x* (*y*) denoted by  $J_x(J_y)$ . For any ratio  $J_x/J_y$ , the highest energy state is a total spin- $\frac{1}{2}$  singlet. In the case of  $J_x/J_y = 0$ , it corresponds to the valence-bond state  $|00\rangle$ , whereas for  $J_x/J_y = 1$  it is the *s*-wave RVB state  $|\Phi_+\rangle$ . The other total singlet for  $J_x = J_y$ , lower in energy, is the *d*-wave RVB state  $|\Phi_-\rangle = |\boxtimes\rangle$ . (c) Symbols used for a singlet bond and for the *s*-wave and *d*-wave plaquette RVB states.

to arrangements in either vertical  $|00\rangle$  or horizontal bonds  $|\otimes\rangle$  [Fig. 1(b)].

Within this subspace and for identical superexchange couplings  $J_x = J_y \equiv J$ , the Hamiltonian of Eq. (1) reduces to  $\hat{H} = -J\hat{X}_{xy}$ , where  $\hat{X}_{xy} = (\hat{X}_{AC} + \hat{X}_{BD})/2$  swaps two spins along a diagonal. As can directly be seen, this diagonal exchange is equivalent to a 90° rotation of the plaquette and converts the state  $|00\rangle$  into  $|00\rangle$  and vice versa, giving rise to a resonance. The eigenstates are then coherent superpositions of the form

$$|\Phi_{\pm}\rangle \propto |00\rangle \pm |\Xi\rangle.$$

These minimum instances of RVB states exhibit no local magnetic order, and cannot be distinguished from each other by measuring single-site spin observables. However they are distinct with respect to an exchange of two spins along a diagonal: the *s*-wave RVB state  $|\Phi_+\rangle$  is symmetric; the *d*-wave RVB state  $|\Phi_-\rangle$  is antisymmetric, owing to its singlet structure along the diagonals of the plaquette,  $|\Phi_-\rangle = |\boxtimes\rangle$ .

Our experiments began with a quasipure Bose-Einstein condensate of about  $5 \times 10^4$  <sup>87</sup>Rb atoms in the Zeeman state  $|F = 1, m_F = -1\rangle$ . The atoms were loaded into a tetragonal optical lattice potential, formed by three mutually orthogonal standing waves with wavelengths  $\lambda_s = 767$  nm ("short lattices") along x and y, and  $\lambda_z = 844$  nm along z. Two additional standing waves with

wavelengths of  $\lambda_l = 1534$  nm ("long lattices") that were superimposed with the short lattices [18] along x and y were then used to realize a three-dimensional periodic potential whose elementary cell is a plaquette [Fig. 1(a)]. The final lattice depths were chosen to access the Mott insulating regime with at most one atom per lattice site for our total particle number. We then employed a sequence of site merging, spin changing collision (SCC) [19] and singlet-triplet oscillation (STO) operations [17,20,21] on

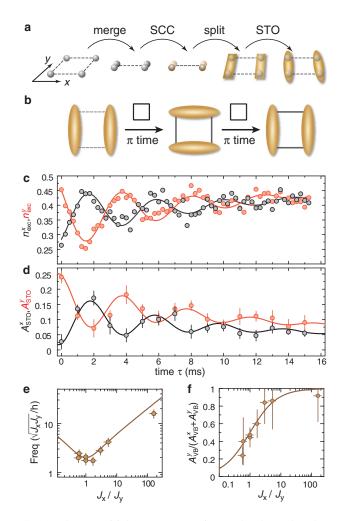


FIG. 2 (color). Initial state preparation and valence-bond oscillations. (a) Schematics of the preparation of an array of valence-bond states  $|00\rangle$  from a unit-filling Mott insulator. (b) Schematics of the valence-bond oscillation: starting from  $|00\rangle$ , we switch on identical superexchange couplings along x and y, leading to a coherent oscillation between  $|00\rangle$  and  $|\odot\rangle$ . (c,d) Fraction of band excitations  $n_{exc}^{x,y}$  (c) and STO amplitude  $A_{STO}^{x,y}$  (d) as a function of the hold time  $\tau$ , with  $J_x \simeq J_y =$ h × 120(10) Hz. (e) Frequency of the valence-bond oscillation as a function of  $J_x/J_y$ . (f) Ratio  $A_{VB}^y/(A_{VB}^x + A_{VB}^y)$  as a function of  $J_x/J_y$ , where  $A_{VB}^{x,y}$  is the initial amplitude of the valence-bond oscillations as shown in (c). The solid lines in (e) and (f) are calculated from Eq. (1). The horizontal error bars represent the uncertainties in lattice depths and the vertical ones represent the 1 $\sigma$  uncertainties of the fits to the STO traces.

plaquettes [see Fig. 2(a)] in order to create the initial state  $|00\rangle$  out of the atomic spin states  $|F = 1, m_F = -1\rangle$  and  $|F = 1, m_F = +1\rangle$  [22]. In total we operate in parallel over about  $10^3$  identical plaquettes with unit atom filling. Lattice depths of  $V_{xl} = V_{yl} = 35E_r^l$  and  $V_z = 40E_r^z$  ensure negligible atom tunneling between plaquettes [23].

To directly observe the valence-bond resonance, the initial state  $|00\rangle$  was evolved under the Hamiltonian of Eq. (1) with identical superexchange couplings along x and y. To this aim we ramped down the short-lattice depths in 200  $\mu$ s to  $V_{xs} = V_{ys} = 12E_r^s$ , resulting in equal couplings  $J_x \simeq J_y = h \times 120(10)$  Hz and a suppression of first order tunneling as  $t/U \simeq 1/8$ . Since  $\hat{X}_{xy}^2 = 1$ , the evolved quantum state at time  $\tau$  is

$$|\Psi(\tau)\rangle = \cos\frac{\omega\tau}{2}|00\rangle - i\sin\frac{\omega\tau}{2}|\Xi\rangle, \qquad (2)$$

oscillating between the states  $|00\rangle$  and  $|\otimes\rangle$  with frequency  $\omega = 2J_{x(y)}/\hbar$ .

To characterize this state evolution, we measured the projections onto the two valence-bond states  $C_x$ :  $|\langle \Psi(\tau)| \otimes \rangle|^2$ , and  $C_y = |\langle \Psi(\tau)| 00 \rangle|^2$ , which are expected to show oscillations of amplitude 3/4, since  $\langle \Im | 0 \rangle = 1/2$ . Within the subspace of total singlets, the observable  $C_x$  can be obtained either by measuring the fraction of band excitations  $n_{\text{exc}}^x = C_x/2$  after merging pairs of wells along the x direction, or by measuring the amplitude  $A_{\text{STO}}^x$  of STO [17,20,21] induced by a magnetic-field gradient along x [22]. As shown in Fig. 2(c) and 2(d), we indeed observed a coherent evolution of both  $n_{\text{exc}}^{x,y}$  and  $A_{\text{STO}}^{x,y}$ . This dynamics corresponds to anticorrelated oscillations of the projections  $C_x$  and  $C_y$ that reveal the periodic swapping of the valence-bond direction. The measured oscillation frequency  $\omega/2\pi =$ 250(10) Hz is compatible with twice the value of the superexchange couplings, in agreement with Eq. (2). While the damping of the valence-bond oscillation (1/e)decay time of 6(1) ms) could be attributed to inhomogeneities of the different plaquette parameters across the atomic sample, the slow overall increase of  $n_{\text{exc}}^x$  and  $n_{\text{exc}}^y$ could be caused by decoherence within a plaquette. We provide further evidence of the valence-bond dynamics governed by superexchange interactions by studying the dynamics for anisotropic couplings  $J_x \neq J_y$ . As shown in Fig. 2(e) and 2(f), the measured oscillation frequencies and amplitudes as a function of  $J_x/J_y$  agree well with the values predicted from the Hamiltonian dynamics of Eq. (1). Site-resolved population measurements were used to check that throughout the evolution the four plaquette sites remained equally populated [18,22]. In the absence of residual magnetic-field gradients we expect the atoms to remain in the singlet subspace S = 0. This was checked by holding singlet atom pairs after the initial state preparation, and observing no conversion to triplet pairs.

In order to create the s-wave RVB state  $|\Phi_+\rangle$ , we made use of the fact that it is adiabatically connected to the initial state  $|00\rangle$  [Fig. 1(b)]. To follow this adiabatic path we started from a situation in which  $V_{xs} = 22E_r^s$  and  $V_{vs} =$  $12E_r^s$ . For these parameters,  $J_x/J_y$  is negligible and  $|00\rangle$  is an eigenstate of the Hamiltonian in Eq. (1). We then decreased  $V_{xs}$  to  $12E_r^s$  within 5 ms using an exponential ramp, converting the initial state into the s-wave RVB state. In order to check the adiabaticity of the lattice-depth ramps, we then increased the short lattice along x(y) to  $22E_r^s$  in 5 ms, transforming the RVB state back into a valence-bond state  $|00\rangle$  (or  $|\Xi\rangle$ , respectively). By using STO we measured the singlet correlations along both directions x and y for the initial, intermediate and final states of the ramp  $|00\rangle \rightarrow |\Phi_+\rangle \rightarrow |00\rangle$  or  $|\otimes\rangle$  [Fig. 3(a)]. As expected, for the initial state we observe oscillations close to maximum amplitude only along y and none along x. In the intermediate state, the oscillation amplitudes are approximately equal, as expected for a nondegenerate eigenstate of the Hamiltonian in Eq. (1) with symmetric couplings. After the second ramp, depending on whether the superexchange coupling was decreased along x or y, we observe singlet correlations mostly along the direction of strong coupling. The measured amplitude of STO in the final state was found to be smaller than in the initial state, due to decoherence in our atomic sample which occurred on a time scale of 30 ms in our setup. As can be seen in Fig. S2 of the supplementary material, for a total ramp time of 10 ms (gray bar) the value of  $A_{\text{STO}}^x$  is 0.22(2), which is comparable to the STO amplitude of 0.24(2) obtained for the initial state  $|00\rangle$  [see Fig. 2(d)].

In the RVB state  $|\Phi_+\rangle$ , the projections on the valencebond states are given by  $C_x = C_y = 3/4$ . They can be obtained from the STO amplitudes according to  $C_{x,y} = 1/4 + 3/2A_{\text{STO}}^{x,y}$  [22]. By averaging the measured STO amplitudes around  $J_x = J_y$ , we obtain  $C_x = C_y = 0.76(7)$ [Fig. 3(b)], in good agreement with the theoretical prediction. We also measured  $C_x, C_y$  as a function of the coupling anisotropy  $J_x/J_y$ , by following the adiabatic path  $|00\rangle \rightarrow |\Phi_+\rangle \rightarrow |\psi(J_x/J_y)\rangle$  with a fixed total ramp time of 10 ms. As shown in Fig. 3(b), the measurement results are in good agreement with the theoretical values in the adiabatic limit (solid lines) and with a model taking into account the finite ramp time (shaded lines).

The *d*-wave RVB state  $|\Phi_-\rangle$  is obtained from the state  $|00\rangle$  by exchanging two spins along a bond in the *x* direction:

$$\dot{X}_x|00\rangle = |\otimes\rangle. \tag{3}$$

This unitary operation was implemented by a quantum evolution of the state  $|00\rangle$  under the Hamiltonian Eq. (1) for  $J_y = 0$ , yielding:

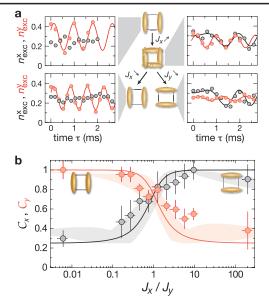


FIG. 3 (color). Preparation of the s-wave RVB state and adiabatic valence-bond swap. (a) Scheme of the adiabatic conversion  $|00\rangle \rightarrow |\Phi_{+}\rangle \rightarrow |00\rangle$  or  $|\approx\rangle$ , together with STO for each state. The STO period along x is not constant due to an increasing magnetic gradient field during the measurements that was caused by a finite response time of the coils producing the magneticfield gradient along x. The solid lines are fits of the STO taking into account the finite rise time of the magnetic-field gradient for the x direction. (b) Projections  $C_x$ ,  $C_y$  on the valence-bond states as a function of the ratio  $J_x/J_y$  of superexchange couplings, measured from the STO amplitudes. The latter were rescaled in order to give the expected value of 0.5 for the valence-bond states  $|\Im\rangle$  and  $|00\rangle$ , using the data points at  $J_x/J_v = 0.006(2)$ and  $J_x/J_y = 10(3)$ . For the point at  $J_x/J_y = 200(50)$  the rate of change of the couplings was the largest and adiabaticity was not maintained. The horizontal error bars represent the uncertainties in lattice depths and the vertical ones represent the  $1\sigma$  uncertainties of the fits to the STO traces. The solid lines are calculated from the eigenstates of the Hamiltonian in Eq. (1). The shaded lines are calculated by modeling the experimental ramps using the Schrödinger equation. Their widths represent the uncertainties in the lattice calibration.

$$|\Psi(t)\rangle = \cos\frac{\omega\tau}{2}|00\rangle - i\sin\frac{\omega\tau}{2}|\boxtimes\rangle, \qquad (4)$$

with  $\omega = 2J_x/\hbar$ . For a hold time  $\tau = \pi/\omega$  the initial state evolves into  $|\boxtimes\rangle$ , characterized by  $C_x = C_y = 1/4$ , and reduced STO amplitudes  $A_{\text{STO}}^x = A_{\text{STO}}^y = 1/8$ . As shown in Fig. 4, in that state the amplitude of STO was indeed much reduced, in our case below the noise level. However, the large STO amplitude along y, observed both in the initial state and after one period of evolution  $(\tau = 2\pi/\omega)$ , demonstrates the coherence of the evolution and rules out a reduction of contrast at  $\tau = \pi/\omega$  due to decoherence. Alternatively, after preparing the  $|\Phi_-\rangle$  state, we inverted the coupling direction by increasing in 200  $\mu s$ the short-lattice depth along x to  $22E_s^r$  and decreasing

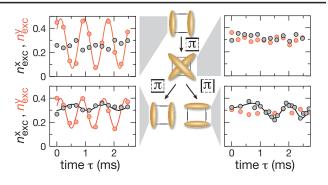


FIG. 4 (color). Preparation of the *d*-wave RVB state. Schematics of the experimental sequence: starting from the state  $|\emptyset|\rangle$  we suddenly switch on the superexchange coupling along *x*. The *d*-wave RVB state  $|\Phi_{-}\rangle$  is obtained at the  $\pi$  time of the subsequent periodic evolution. Measured STO are shown at the 0,  $\pi$  and  $2\pi$  times of the evolution. For the lower right state, we inverted the coupling direction at the  $\pi$  time.

the one along y to  $12E_r^s$ . As shown in Fig. 4, we then observed a coherent evolution to a state with a large overlap with  $|\Xi\rangle$ , according to the measured STO.

In conclusion, we have shown direct experimental evidence of a valence-bond quantum resonance in an array of replicas of optical plaquettes, preparing and detecting minimum versions of RVB states. The s-wave and d-wave plaquette states created here could be used to encode a minimum instance of a topologically protected qubit. When stabilized by a Hamiltonian  $H = J(\hat{X}_x + \hat{X}_y + \hat{X}_y)$  $\hat{X}_{xy}$ ), corresponding to a situation in which superexchange interaction takes also place along the diagonal bonds, these two states form a degenerate two level system which is immune to local decoherence arising, for instance, from on-site fluctuations of the external magnetic field. Such an arrangement could also be directly adapted to a setting of four coupled quantum dots to realize protected qubits in a solid state setting [24]. Further extensions enabled by this work include the adiabatic connection of the plaquette RVB and valence-bond solid states, or the study of their nonequilibrium dynamics upon instantaneous coupling in quantum ladders or extended two-dimensional systems. Moreover, the plaquette tools developed here could be used as building blocks for more complex protocols leading to a variety of topologically ordered states, like Laughlin states or string net condensates [17,25]. Finally, we note that all presented results could also be obtained using fermions instead of bosons, where the singlet valence bond is the true ground state of a two-spin dimer. In that case, the adiabatic connection of isolated RVB states could lead to the formation of a *d*-wave superfluid upon doping [9,10].

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- [22] See Supplemental Material at http://link.aps.org/ supplemental/10.1103/PhysRevLett.108.205301 for the experimental sequence, the decoherence measurement and the detection and data analysis methods.
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