

Valley-Based Noise-Resistant Quantum Computation Using Si Quantum Dots

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We devise a platform for noise-resistant quantum computing using the valley degree of freedom of Si quantum dots. The qubit is encoded in two polarized (1,1) spin-triplet states with different valley compositions in a double quantum dot, with a Zeeman field enabling unambiguous initialization. A top gate gives a difference in the valley splitting between the dots, allowing controllable interdot tunneling between opposite valley eigenstates, which enables one-qubit rotations. Two-qubit operations rely on a stripline resonator, and readout on charge sensing. Sensitivity to charge and spin fluctuations is determined by intervalley processes and is greatly reduced as compared to conventional spin and charge qubits. We describe a valley echo for further noise suppression.

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Quantum computing (QC) requires accurate control of the two states in a quantum bit (qubit), which entails long coherence times and the ability to rotate a single qubit and entangle neighboring qubits. Solid state spin systems are an obvious choice for scalable QC, with Si known for its outstanding spin coherence times [1–4], thanks to the lack of piezoelectric electron-phonon coupling [5], weak spin-orbit interaction [6,7], and, most importantly, nuclear-spin free isotopes, enabling isotopic purification to remove hyperfine coupling [8]. Recently, Si quantum dots (QDs) have been at the forefront of QC research, with theories of spin relaxation in Si QDs further justifying this choice [9,10]. Experimental progress in Si QC has been made using QDs in Si/SiO₂ [11–14], Si/SiGe [15,16], and donor-based architectures [17–23].

The two main obstacles to Si QC are dephasing due to charge noise and the valley degree of freedom. In layered structures only the two low-lying valleys perpendicular to the interface are relevant, and the interface potential gives a valley-orbit coupling Δ , which determines the two-spin exchange [24]. The study of Si valley physics has intensified, in experiment [25–30] and theory [31–37].

Here we propose a new QC platform in Si QDs using the valley degree of freedom to overcome noise. It exploits the closeness in energy of two polarized spin-triplet states with different valley compositions. It employs available technology in Si QD in MOSFET and donor architectures, offering all-electrical control and a fundamental perspective on valley manipulation [38].

We take an inversion layer of thickness L , with a top gate setting the potential at the top Si/barrier interface to V_T and a back gate inducing V_B to the back interface. The electric field inside the inversion layer is $F = (V_B - V_T)/L$.

In a single QD defined in this environment, an electron experiences the potential

$$V_D = \frac{\hbar^2}{2m^*a^2} \left[\frac{(x - x_D)^2 + y^2}{a^2} \right] + eFz + U_0\theta(z) + eV_T, \quad (1)$$

with the origin at the top interface. The dot is located at $(x_D, 0, 0)$, with a radius a , m^* is the Si in-plane effective mass and $U_0\theta(z)$ the interface potential with $\theta(z)$ the Heaviside function. The effective-mass ground state wave function is $D_\xi(x, y, z) = \phi_D(x, y)\psi(z)u_\xi(\mathbf{r})e^{ik_\xi z}$. The lateral envelope function $\phi_D(x, y)$ is a 2D Gaussian, and $\psi(z)$ is the solution to the triangular well imposed by the interface and the potential difference in the z direction. The Bloch functions are $u_\xi(\mathbf{r})e^{ik_\xi z}$, where the valley index $\xi = \{z, \bar{z}\}$, and $k_\xi = \pm k_0$, with $k_0 = 0.85(2\pi/a_{\text{Si}})$, and $a_{\text{Si}} = 5.43 \text{ \AA}$ the Si lattice constant. In the basis $\{D_\xi\}$ the single-dot Hamiltonian reads

$$H_D = \varepsilon_D + \begin{pmatrix} 0 & \Delta_D \\ \Delta_D^* & 0 \end{pmatrix}, \quad (2)$$

with confinement energy ε_D and valley-orbit coupling

$$\Delta_D = \langle D_z | U_0\theta(z) + eFz | D_{\bar{z}} \rangle. \quad (3)$$

The top and back gates independently control the diagonal confinement energy (electron density) and the off-diagonal valley-orbit coupling (vertical field.) Gate cross talk can be circumvented using gate compensation techniques [22]. Experimentally, the lever arm of the top and back gates must be obtained in order to determine how V_T and V_B control ε_D and Δ_D . The functional form of $\varepsilon_D(V_T, V_B)$ and $\Delta_D(V_T, V_B)$ may be obtained from theory [36]. The quasitriangular potential in the z direction is not

exactly solvable. Nevertheless, it is a good approximation to adopt the exact expression for an infinite barrier $E_z = (\hbar^2/2m_z(1.13805\pi eF)^2)^{1/3}$. [39] The total energy is $\epsilon_D = \hbar^2/m^*a^2 + E_z + eV_T$. With E_z fixed, V_T shifts the diagonal terms in Eq. (2). Such control could also be realized in the setup of Ref. [30], where Al-Al₂O₃ multigate stacks provide excellent tunability of the vertical electrical field and interdot coupling.

The valley-orbit coupling $\Delta_D = |\Delta_D|e^{-i\phi_D}$ is complex. The eigenstates of H_D (valley eigenstates) are

$$|D_{\pm}\rangle = (1/\sqrt{2})(|D_z\rangle \pm e^{i\phi_D}|D_{\bar{z}}\rangle), \quad (4)$$

with energies ϵ_{\pm} . The dominant contribution to Δ_D comes from U_0 . The direct contribution from F_D is smaller [36], yet F_D controls Δ_D by manipulating the electronic density at the interface, and $|\Delta_D|$ can be increased by an order of magnitude. For Si/SiO₂ barriers $|\Delta_D| = [(27.4 \pm 0.02)F]$ meV, with F in V/nm [39]. Figure 1 shows the way V_T , V_B control $|\Delta_D|$, ϵ_D separately.

We focus on a double quantum dot (DQD), with the left dot located at $x_L = -x_0$ and the right dot at $x_R = x_0$. The valley eigenstates $|D_{\pm}\rangle$ are identical in both dots if the interface is sharp along the growth direction and flat perpendicular to it, or if interface roughness is correlated over distances much shorter than the size of the QD [40]. We assume the top and back gates can be adjusted independently for the L , R dots, so the electric field F has different values for the two dots, F_L and F_R respectively, while their electrochemical potential is constant. The DQD confinement potential is

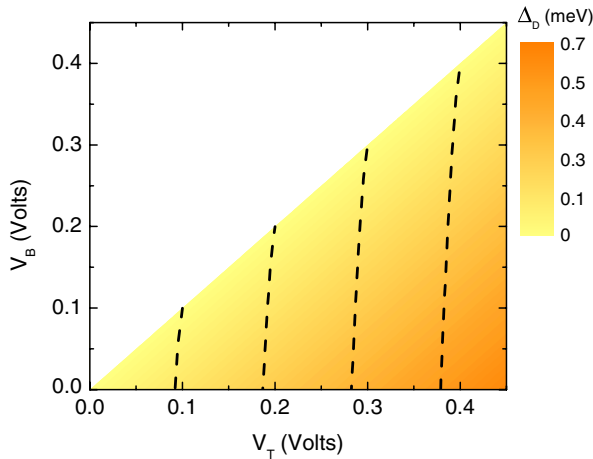


FIG. 1 (color online). Color plot of $|\Delta_D|$ as a function of the gate voltages. The dashed lines refer to paths of constant ϵ_D . If the qubit is manipulated along these lines, the back gate voltage compensates the change in orbital energy induced by the top gate voltage. We particularize our results to $V_T > V_B$, so that the electron is at the top interface at all times.

$$V_{\text{DQD}} = \frac{\hbar^2}{2m^*a^2} \{ \text{Min}[(x-x_0)^2, (x+x_0)^2] + y^2 \} + eEx + eF_Lz + eF_Rz + U_0\theta(z). \quad (5)$$

Neglecting interdot couplings due to the interface potential (of order $l\Delta_D/\epsilon_D$, with $l = \langle L_{\xi} | R_{\xi} \rangle \ll 1$), Δ_D is a constant across the two dots and we diagonalize H_D separately for $D = L, R$, obtaining Δ_L, Δ_R and their corresponding valley eigenstates. These are orthogonalized (see Supplemental Material [41]), yielding the states $|\tilde{D}_{\pm}\rangle$. We use only $|\tilde{D}_{\pm}\rangle$ in the remainder of this work. Initially we take $\Delta_L = \Delta_R$; thus, $|\tilde{D}_{\pm}\rangle$ are identical for L, R , and interdot tunneling preserves the valley eigenindex (i.e., between $|\tilde{L}_{\pm}\rangle$ and $|\tilde{R}_{\pm}\rangle$, but not between $|\tilde{L}_{\pm}\rangle$ and $|\tilde{R}_{\mp}\rangle$).

We seek a two-dimensional subspace of the full DQD Hilbert space that consists of two states with different valley compositions that can be coupled controllably. The full Hilbert space includes spin and valley degrees of freedom. A high enough magnetic field (≈ 1 T) lifts the spin degeneracy, and only the lowest-energy $\downarrow\downarrow$ polarized triplet states are energetically accessible; thus, below it is understood that $\tilde{T}_{\pm\pm}^{LR} \equiv \tilde{T}_{\pm\pm}^{LR,\downarrow\downarrow}$, etc.

$$\begin{aligned} \tilde{T}_{\pm\pm}^{LR} &= (1/\sqrt{2})(\tilde{L}_{\pm}^{(1)}\tilde{R}_{\pm}^{(2)} - \tilde{L}_{\pm}^{(2)}\tilde{R}_{\pm}^{(1)}), \\ \tilde{T}_{\mp\mp}^{LR} &= (1/\sqrt{2})(\tilde{L}_{\mp}^{(1)}\tilde{R}_{\mp}^{(2)} - \tilde{L}_{\mp}^{(2)}\tilde{R}_{\mp}^{(1)}), \\ \tilde{T}_{+-}^{RR} &= (1/\sqrt{2})(\tilde{R}_{+}^{(1)}\tilde{R}_{-}^{(2)} - \tilde{R}_{+}^{(2)}\tilde{R}_{-}^{(1)}). \end{aligned} \quad (6)$$

The hopping integral $\tilde{t} = \langle \tilde{L}_{\xi} | H_0 | \tilde{R}_{\xi} \rangle + \langle \tilde{L}_{\xi} \tilde{L}_{\xi} | V_{ee} | \tilde{L}_{\xi} \tilde{R}_{\xi} \rangle$, the exchange integral $\tilde{j} = \langle \tilde{L}_{\xi}^{(1)} \tilde{R}_{\xi}^{(2)} | V_{ee} | \tilde{L}_{\xi}^{(2)} \tilde{R}_{\xi}^{(1)} \rangle = \langle \tilde{L}_{\xi}^{(1)} \tilde{R}_{-\xi}^{(2)} | V_{ee} | \tilde{L}_{-\xi}^{(2)} \tilde{R}_{\xi}^{(1)} \rangle$, and $\tilde{\delta} = (\tilde{\epsilon}_L - \tilde{\epsilon}_R) - (\tilde{u} - \tilde{k})$ is an effective two-particle detuning between dots, with $\tilde{u} = \langle \tilde{D}_{\xi}^{(1)} \tilde{D}_{\xi}^{(2)} | V_{ee} | \tilde{D}_{\xi}^{(1)} \tilde{D}_{\xi}^{(2)} \rangle = \langle \tilde{D}_{\xi}^{(1)} \tilde{D}_{-\xi}^{(2)} | V_{ee} | \tilde{D}_{\xi}^{(1)} \tilde{D}_{-\xi}^{(2)} \rangle$ the on-site Coulomb interaction and $\tilde{k} = \langle \tilde{L}_{\xi}^{(1)} \tilde{R}_{\xi}^{(2)} | V_{ee} | \tilde{L}_{\xi}^{(1)} \tilde{R}_{\xi}^{(2)} \rangle$ the direct Coulomb interaction between electrons on the two dots. In the basis $\{ \tilde{T}_{--}^{LR}, \tilde{T}_{++}^{LR}, \tilde{T}_{+-}^{LR}, \tilde{T}_{-+}^{LR}, \tilde{T}_{+-}^{RR} \}$ the effective Hamiltonian is

$$\tilde{H}_T = \begin{pmatrix} -|\tilde{\Delta}|_{\text{tot}} - \tilde{j} & 0 & 0 & 0 & 0 \\ 0 & |\tilde{\Delta}|_{\text{tot}} - \tilde{j} & 0 & 0 & 0 \\ 0 & 0 & |\tilde{\Delta}|_E & -\tilde{j} & \tilde{t} \\ 0 & 0 & -\tilde{j} & -|\tilde{\Delta}|_E & -\tilde{t} \\ 0 & 0 & \tilde{t} & -\tilde{t} & -\tilde{\delta} \end{pmatrix}, \quad (7)$$

with $|\tilde{\Delta}|_{\text{tot}} = |\tilde{\Delta}_L| + |\tilde{\Delta}_R|$ and $|\tilde{\Delta}|_E = |\tilde{\Delta}_L| - |\tilde{\Delta}_R|$. In the absence of interdot tunneling between opposite valley eigenstates, the states \tilde{T}_{--}^{LR} and \tilde{T}_{++}^{LR} are decoupled from the other three states; thus, we do not include them in the rest of our analysis. The relevant eigenstates are

$$\begin{aligned}\tilde{T}_{+-}^{\leftarrow} &= (\varepsilon_0^{\leftarrow} / \sqrt{\varepsilon_0^{\leftarrow 2} + 2\tilde{t}^2}) [(\tilde{t} / \varepsilon_0^{\leftarrow}) (\tilde{T}_{+-}^{LR} - \tilde{T}_{-+}^{LR}) + \tilde{T}_{+-}^{RR}], \\ \tilde{T}_{+-}^{\text{sym}} &= (1/\sqrt{2})(\tilde{T}_{+-}^{LR} + \tilde{T}_{-+}^{LR}), \\ \varepsilon_0^{\leftarrow} &= (1/2)[- \tilde{\delta} + \tilde{j} - \sqrt{(\tilde{\delta} + \tilde{j})^2 + 8\tilde{t}^2}].\end{aligned}\quad (8)$$

The qubit is defined by the states $\tilde{T}_{+-}^{\leftarrow}$ and $\tilde{T}_{+-}^{\text{sym}}$. Restricting our attention to the qubit subspace

$$\tilde{H}_{\text{qubit}} = \begin{pmatrix} -j & |\tilde{\Delta}|_E \\ |\tilde{\Delta}|_E & \tilde{\varepsilon}_0^{\leftarrow} \end{pmatrix} = -\tilde{j} - \frac{\hbar\omega_z}{2} + \frac{\hbar}{2} \begin{pmatrix} \omega_z & \Omega \\ \Omega & -\omega_z \end{pmatrix}. \quad (9)$$

Here $\hbar\omega_z = -\tilde{\varepsilon}_0^{\leftarrow} - j = -\tilde{E}_{\text{HM}}$, the Hund-Mulliken energy that in one-valley systems denotes the singlet-triplet energy difference. In multivalley systems, due to the additional degree of freedom, \tilde{E}_{HM} is not necessarily related to the spin part of the wave functions [42].

Referring to Fig. 2, two electrons can be unambiguously initialized into \tilde{T}_{+-}^{RR} when $\tilde{\delta}$ is raised and $\tilde{\varepsilon}_R \ll \tilde{\varepsilon}_L$. Then $\tilde{\delta}$ is swept to the (1,1) regime, with \tilde{T}_{+-}^{RR} evolving into $\tilde{T}_{+-}^{\leftarrow}$. This setup allows readout by charge sensing using a quantum point contact [43]. Raising $\tilde{\delta}$ again, the two-qubit states have different occupancies, realizing a valley blockade. Readout of the charge state of one QD (e.g., R) automatically yields the qubit state.

A workable quantum computer requires tunable x and z rotations, i.e., the σ_x and σ_z gates. A gate electric field $\parallel \hat{z}$ generates the σ_x gate. In the far-detuned regime the states $\tilde{T}_{\text{sym}}^{LR,\parallel}$ and $\tilde{T}_{+-}^{\leftarrow,\parallel}$ are effectively degenerate. Ramping up F_L induces a small difference $\tilde{\Delta}_E$ in the valley splitting on the left dot. With an electric field difference of 10^{-3} V/nm, $\tilde{\Delta}_E \approx 27.4 \mu\text{eV}$, and the gating time for a 2π rotation around the X axis is 0.15 ns. For σ_z rotations \tilde{E}_{HM} can be altered by changing $\tilde{\delta}$, providing a σ_z gate of arbitrary strength. Thus, with $|\tilde{\Delta}_E| \gg \tilde{E}_{\text{HM}}$ or $\tilde{E}_{\text{HM}} \gg |\tilde{\Delta}_E|$, a σ_x or a σ_z gate can be obtained.

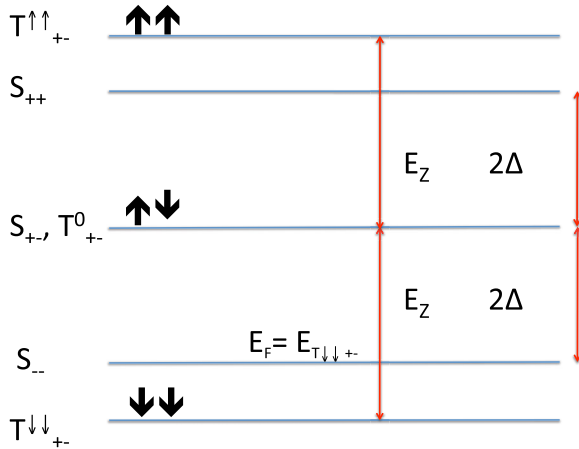


FIG. 2 (color online). Two-electron levels in a Si QD. For $E_z > 2\Delta$, T_{+-}^{\leftarrow} becomes the ground state and is initialized unambiguously.

The σ_x and σ_z gates also allow a valley-echo experiment. Both σ_x and σ_z rotations can be gated quickly, providing a fast two-axis control, in contrast to, e.g., singlet-triplet qubits, where one axis is the fixed Overhauser field gradient. With the available fast gates, advanced dynamical decoupling techniques [44,45] can restore coherence. If $\tilde{\Delta}_E < \tilde{E}_{\text{HM}}$, X rotations may be implemented through valley resonance (cf. Ref. [46]). An alternating $\tilde{\Delta}_E(t)$ at a frequency resonant with ω_z enables Rabi-like flips of the valley qubit.

Initialization requires only a magnetic field, while in the far-detuned regime, where operations are performed, the magnitude of $\tilde{\Delta}$ is irrelevant. Coherent rotations can be demonstrated without precise knowledge of $\tilde{\Delta}$, even for $\tilde{\Delta} \leq k_B T$. Knowledge of $\tilde{\Delta}$ is required for controlled rotations, whose characteristic time scale and coherence time may be estimated by Ramsey interferometry.

The universal set of quantum gates is completed using a superconducting transmission line resonator to provide entanglement. Superconducting resonators have exceptionally small mode volumes for strong couplings to qubits, and very high quality factors. They can mediate interactions between singlet-triplet qubits [47,48] and can couple valley qubits. An array of DQDs can each be coupled to a superconducting transmission line resonator, with only the right dot coupled out of each DQD. The (quantized) resonator voltage is an addition to the detuning, and the effective interaction is

$$H_{\text{res}} = g(\hat{a} + \hat{a}^\dagger)|\tilde{T}_{+-}^{RR}\rangle\langle\tilde{T}_{+-}^{\leftarrow}|, \quad (10)$$

where \hat{a} is the annihilation operator for the lowest-energy mode of the resonator. H_{res} is mapped onto a Jaynes-Cummings Hamiltonian. For Si shallow donor electrons coupling to Si cavities, g has been estimated at 30 MHz [49], and for QDs we expect an improvement of an order of magnitude. Type-II superconducting alloy strip lines have high B_{c2} : NbTi, which is already used, has $B_{c2} = 15$ T, and can be operated at the magnetic fields required here to freeze out the spin degree of freedom.

Valley qubits have good coherence properties. First, relaxation mediated by a generic phonon potential V_{phn} is quantified by T_1 , and strongly suppressed, because

$$\frac{1}{T_1} = \frac{2\pi}{\hbar} \sum_{\mathbf{k}} |\langle \tilde{D}_+ | V_{\text{phn}} | \tilde{D}_- \rangle|^2 \delta(\varepsilon_+ - \varepsilon_- - \hbar\omega) \quad (11)$$

requires phonons with energies $\hbar\omega \approx 2\tilde{\Delta}$ and \mathbf{k} of the order of \mathbf{k}_0 . Optical phonons bridge the difference in \mathbf{k} but have energies $\gg 2\tilde{\Delta}$, whereas acoustic phonons with energies $\approx 2\tilde{\Delta}$ have wave vectors $\ll \mathbf{k}_0$ [50]. For the same reason, the qubit does not relax to the lower-lying \tilde{T}_{+-}^{LR} states with orthogonal valley composition.

Valley qubits are immune to charge noise due to dangling bonds (DBs), which hamper conventional charge and spin qubits [51]. Since a large wave vector $2\mathbf{k}_0$ separates

the z and \bar{z} valleys, intervalley matrix elements are only appreciable for real-space interactions sharp in the \hat{z} direction. For interactions nonsingular in z , matrix elements between $|\tilde{D}_z\rangle$ and $|\tilde{D}_{\bar{z}}\rangle$, likewise between $|\tilde{D}_+\rangle$ and $|\tilde{D}_-\rangle$, are suppressed. The Coulomb potential $v(x, y)$ of a DB in the QD plane has intervalley matrix element $\langle v \rangle = \langle \tilde{D}_z | v(x, y) | \tilde{D}_{\bar{z}} \rangle = 0$, since the overlap of valley states vanishes (see Supplemental Material [41]). For a DB not in the plane, the intervalley matrix element of $v(x, y)$ is still suppressed, since quasi-2D screened Coulomb potentials remain long range. Thus the σ_x gate is immune to noise.

Noise in the σ_z gate could lead to pure dephasing [51]. Variations in \tilde{E}_{HM} are given by $\Delta\tilde{E}_{\text{HM}} = (\partial\tilde{E}_{\text{HM}}/\partial\tilde{t})\Delta\tilde{t} + (\partial\tilde{E}_{\text{HM}}/\partial\tilde{\delta})\Delta\tilde{\delta}$. In the far-detuned regime, where the qubit is operated, there is little variation in \tilde{t} [51]. With the σ_x gate off, $\tilde{H}_{\text{qubit}} = (\tilde{E}_{\text{HM}} + \Delta\tilde{E}_{\text{HM}})\sigma_z$ and consider the decay of the off-diagonal element ρ_{12} of the density matrix. Random telegraph noise causes $\rho_{12} \propto e^{-t/\tau} \cos\eta t$, with $\eta \approx \Delta E_{\text{HM}}/\hbar$ and τ the switching time of the fluctuator, which can reach ms [51]. For $1/f$ noise, $\rho_{12} \propto e^{-\chi(t)}$, where

$$\chi(t) = \frac{1}{2\hbar^2} \left(\frac{d\tilde{E}_{\text{HM}}}{d\tilde{\delta}} \right)^2 \int_{\omega_0}^{\infty} d\omega S_{\tilde{\delta}}(\omega) \left(\frac{\sin\omega t/2}{\omega/2} \right)^2 \quad (12)$$

where $S_{\tilde{\delta}}(\omega)$ is the spectral density of fluctuations in $\tilde{\delta}$ and ω_0 a cutoff (the inverse measurement time.) Since the two-qubit states have the same envelope functions, \tilde{E}_{HM} is effectively independent of $\tilde{\delta}$ (Fig. 2 of Supplemental Material [41]). The sensitivity of the σ_z gate to charge noise can be reduced to any desired level by reducing $d\tilde{E}_{\text{HM}}/d\tilde{\delta}$.

Charge noise is dominated by the low-frequency part of the spectrum, is a long wavelength, and cannot differentiate valleys. In conventional charge qubits with different charge distributions, charge noise and electron-phonon coupling differentiate the states and lead to dephasing. We have devised a charge qubit that is immune to charge noise, and whose coherence can be further improved through valley echo. The valley-based qubit states have the same spin configuration, so this architecture is also insensitive to magnetic noise. (A forthcoming publication [52] obtains an intervalley dephasing time of μs , rather than ns for GaAs charge qubits.) These arguments still hold if the effective-mass approximation is relaxed by including k states in the vicinity of $\pm k_0$.

Charge defects in the dielectric and interface roughness affect the vertical field, and may cause $|\tilde{\Delta}_L| \neq |\tilde{\Delta}_R|$. The operation of the qubit is unaltered, since a change in $|\tilde{\Delta}|$ still induces mixing between the eigenstates of \tilde{H}_T . Any difference $|\tilde{\Delta}_L| - |\tilde{\Delta}_R|$ can be offset by gate control of Δ prior to operating the qubit. The proposal is robust with respect to unavoidable differences between the two dots.

The top gate may alter the phase of $\tilde{\Delta}$ by a small amount [36], inducing tunneling between the qubit space and the

states $\tilde{T}_{\pm\pm}^{LR}$. Yet $\tilde{T}_{\pm\pm}^{LR}$ are separated by $2|\tilde{\Delta}|$, and the intervalley tunneling matrix element is a fraction of the intra-valley one (which is \approx tens of μeV [42], an order of magnitude less than $|\tilde{\Delta}|$ as measured recently [28–30].)

We have devised a new valley-based QC platform in Si QDs that offers full electrical control with current technology. The qubit is initialized using a Zeeman field, rotated using gate electric fields, and read out via charge sensing. Coupling to a superconducting resonator allows entanglement. The platform is tailored to Si, with the valleys perpendicular to the interface, and $\tilde{\Delta}$ controlled by a top gate [27,36]. Valley-based qubits in carbon QDs must be studied separately [53,54]. Charge-based QC schemes, being easier to control, yield insight into qubit manipulation and coherence, and spur better design.

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