Cavity-Free Photon Blockade Induced by Many-Body Bound States

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(Received 1 July 2011; published 21 November 2011)

The manipulation of individual, mobile quanta is a key goal of quantum communication; to achieve this, nonlinear phenomena in open systems can play a critical role. We show theoretically that a variety of strong quantum nonlinear phenomena occur in a completely open one-dimensional waveguide coupled to an N-type four-level system. We focus on photon blockade and the creation of single-photon states in the absence of a cavity. Many-body bound states appear due to the strong photon-photon correlation mediated by the four-level system. These bound states cause photon blockade, which can generate a sub-Poissonian single-photon source.

DOI: [10.1103/PhysRevLett.107.223601](http://dx.doi.org/10.1103/PhysRevLett.107.223601) PACS numbers: 42.50.Ct, 42.50.Gy, 42.79.Gn

The exchange and control of mobile qubits of information is a key part of both quantum communication and quantum information processing. A ''quantum network'' is an emerging paradigm [\[1](#page-3-1),[2](#page-3-2)] combining these two areas: local quantum nodes of computing or end users linked together by conduits of flying qubits. The deterministic approach to the interaction between the local nodes and the conduits relies on cavities to provide the necessary strong coupling. Indeed, strong coupling between light and matter has been demonstrated using cavities in both the classic cavity quantum electrodynamics (QED) systems [[3](#page-3-3)] and the more recent circuit-QED implementations [[4\]](#page-3-4). This has enabled the observation of nonlinear optical phenomena at the single-photon level, such as electromagnetically induced transparency (EIT) [[5](#page-3-5),[6\]](#page-3-6) and photon blockade [\[7,](#page-3-7)[8](#page-3-8)]. Experiments have also demonstrated the efficient exchange of information between a stationary qubit (atom) and flying qubits (photons) [[9](#page-3-9),[10](#page-3-10)]. However, scaling cavity systems to a multinode quantum network is still challenging because of the difficulty of connecting cavities and managing losses.

A new scheme for achieving strong coupling between light and atoms (or artificial atoms) has been recently proposed based on one-dimensional (1D) waveguides [[11](#page-3-11)[–16\]](#page-3-12), dubbed ''waveguide QED'' [\[14](#page-3-13)[,16\]](#page-3-12). Tremendous experimental progress in achieving strong coupling has occurred in a wide variety of such systems: a metallic nanowire coupled to a quantum dot [[17](#page-3-14)], a diamond nanowire coupled to a nitrogen-vacancy center [\[18\]](#page-3-15), a photonic nanowire with an embedded quantum dot [\[19\]](#page-3-16), and a 1D superconducting transmission line coupled to a flux qubit [[20](#page-3-17)]. In these systems, ''strong coupling'' means that the majority of the spontaneously emitted light is guided into waveguide modes; it is achieved through the tight confinement of optical fields in the transverse direction. Furthermore, waveguide systems are naturally scalable for quantum networking [[1](#page-3-1)]. The key physical element introduced by the waveguide QED geometry is that the atom couples to a continuum of modes. This relaxes the restriction of working with a narrow cavity bandwidth; more importantly, interaction with a continuum brings in novel many-body effects that have no analogue in a cavity.

In this Letter, we show that the nonlinear optical phenomena—EIT, photon blockade, and photon-induced tunneling—emerge in a waveguide system for parameters [\[20\]](#page-3-17) that are currently accessible. For these dramatic and potentially useful nonlinear effects, it is necessary to consider a four-level system (4LS) rather than simply a two- or threelevel system. Photon blockade and photon-induced tunneling have a completely different origin here from the cavity case [\[7,](#page-3-7)[21\]](#page-3-18): they are produced by many-body bound states $[12,14,15,22]$ $[12,14,15,22]$ $[12,14,15,22]$ $[12,14,15,22]$ $[12,14,15,22]$ $[12,14,15,22]$ whose amplitudes decay exponentially as a function of the relative coordinates of the photons. Such states do not exist in cavities because a continuum of modes in momentum space is needed for the formation of bound states in real space. We demonstrate the capability of such a system to generate a single-photon source, which is crucial for quantum cryptography and distributed quantum networking. Our work thus opens a new avenue toward the coherent control of light at the single-photon level based on a cavity-free scheme.

Motivated by recent experimental advances [\[20\]](#page-3-17), we consider an N-type 4LS [\[23,](#page-3-22)[24\]](#page-3-23) coupled to a continuum of modes in a 1D waveguide. Figure [1](#page-1-0) shows both a schematic and a possible realization using superconducting circuits [\[24\]](#page-3-23). The Hamiltonian of the system is [\[12,](#page-3-19)[14\]](#page-3-13)

$$
H = \int dx (-i) \hbar c \left[a_R^{\dagger}(x) \frac{d}{dx} a_R(x) - a_L^{\dagger}(x) \frac{d}{dx} a_L(x) \right] + \int dx \hbar V \delta(x) \left[[a_R^{\dagger}(x) + a_L^{\dagger}(x)] (|1\rangle\langle 2| + |3\rangle\langle 4|) + \text{H.c.} \right],
$$

+
$$
\sum_{j=2}^4 \hbar \left(\epsilon_j - \frac{i\Gamma_j}{2} \right) |j\rangle\langle j| + \frac{\hbar \Omega}{2} (|2\rangle\langle 3| + \text{H.c.}), \tag{1}
$$

where $a_{L,R}^{\dagger}(x)$ are the creation operators for left- and right-
going photons at position x and c is the group velocity of going photons at position x and c is the group velocity of photons. In the 4LS, the energy reference is the energy of

FIG. 1 (color online). Schematic diagram of the waveguide system and EIT. (a) N-type four-level system interacting with the waveguide continuum. The transitions $|1\rangle \leftrightarrow |2\rangle$ and $|3\rangle \leftrightarrow |4\rangle$ are coupled to the waveguide modes with strength V and detuning δ . The transition $|2\rangle \leftrightarrow |3\rangle$ is driven by a semiclassical control field with Rabi frequency Ω and detuning Δ . Here, ω and ω are the frequencies of the incoming photons and the and ω_c are the frequencies of the incoming photons and the control field. (b) Schematic of a possible experimental setup based on superconducting charge qubits [\[24\]](#page-3-23). Two charge qubits, each formed from two Josephson junctions [dark gray (green) regions], are coupled capacitively to each other and to a transmission line (1D waveguide). (c) Single-photon transmission probability as a function of incident photon detuning. EIT occurs when the control field is on $(\Omega = 1.6, \text{ solid})$; when it is off, the 4I S becomes a two-level system and EIT disappears. Here, the 4LS becomes a two-level system and EIT disappears. Here, the effective Purcell factor is $P = 6$.

state |1) (the ground state), and $\epsilon_2 = \omega_{21}$, $\epsilon_3 = \epsilon_2 - \Delta$,
and $\epsilon_4 = \epsilon_2 + \omega_{12}$, where ω_{21} and ω_{12} are the $|1\rangle \leftrightarrow |2\rangle$ and $\epsilon_4 = \epsilon_3 + \omega_{43}$, where ω_{21} and ω_{43} are the $|1\rangle \leftrightarrow |2\rangle$
and $|3\rangle \leftrightarrow |4\rangle$ transition frequencies respectively. In the and $|3\rangle \leftrightarrow |4\rangle$ transition frequencies, respectively. In the spirit of the quantum jump picture [\[25\]](#page-4-0), an imaginary term is included in the 4LS to model the spontaneous emission of the excited states at the rate Γ_i to modes other than the 1D waveguide continuum. We have assumed a linear dispersion and a frequency-independent coupling strength V for the relevant frequency range [[13](#page-3-24)]. The decay rate into the waveguide modes is $\Gamma = 2V^2/c$ from Fermi's golden rule. Below, we assume that level $|3\rangle$ is metastable ((Γ_3 = 0) and levels $|2\rangle$ and $|4\rangle$ have the same loss rate ($\Gamma_2 = \Gamma_4$).

A figure of merit to characterize the coupling strength is given by the effective Purcell factor, $P = \Gamma/\Gamma_2$. In an experiment with surface plasmons coupled to a quantum dot [\[17\]](#page-3-14), $P = 1.5$ was achieved. In more recent experiments, even larger Purcell factors, $P = 3$ and $P \ge 9$, were demonstrated with a superconducting transmission line [\[20\]](#page-3-17) and a GaAs photonic nanowire [[19](#page-3-16),[26](#page-4-1)], respectively. These recent dramatic experimental achievements suggest that the large Purcell-factor physics, which we now discuss, is presently within reach experimentally.

To study interaction effects during photon transmission, we obtain an exact solution of the scattering problem defined by Eq. [\(1\)](#page-0-0). The scattering eigenstates are obtained by imposing an open boundary condition and requiring that the incident photon state be a free plane wave, an approach adopted previously to solve an interacting resonant-level model [\[22\]](#page-3-21) and a two-level system problem [[14](#page-3-13)]. For an incident photon from the left (with wave vector k) and the 4LS initially in its ground state, the transmitted part of the single-photon eigenstate is

$$
\phi_R(x) = t_k e^{ikx},
$$
\n
$$
t_k = \frac{\left[ck - \epsilon_2 + \Delta + \frac{i\Gamma_3}{2}\right] \left[ck - \epsilon_2 + \frac{i\Gamma_2}{2}\right] - \frac{\Omega^2}{4}}{\left[ck - \epsilon_2 + \Delta + \frac{i\Gamma_3}{2}\right] \left[ck - \epsilon_2 + \frac{i\Gamma_2}{2} + \frac{i\Gamma_2}{2}\right] - \frac{\Omega^2}{4}},
$$
\n(2)

where t_k is the transmission coefficient. In the two-photon scattering eigenstate, the transmitted wave is

$$
\phi_{RR}(x_1, x_2) = t_{k_1} t_{k_2} (e^{ik_1x_1 + ik_2x_2} + e^{ik_1x_2 + ik_2x_1}) + b_1 e^{-\gamma_1 |x_2 - x_1|} + b_2 e^{-\gamma_2 |x_2 - x_1|}, \quad (3)
$$

where $b_{1,2}$ and $\gamma_{1,2}$ ($>$ 0) are functions of system parame-ters [[27](#page-4-2)]. The first term of ϕ_{RR} corresponds to transmission of the two photons as independent (identical) particles, with the momentum of each photon conserved individually. The second term is a two-body bound state—note the exponential decay in the relative coordinate $|x_2 - x_1|$ with two characteristic binding strengths γ_1 and γ_2 . Such a state results from the nonlinear interaction between photons mediated by the 4LS. Physically, it originates from the momentum nonconserved processes of each individual photon (with conservation of total momentum). A similar bound state has been found in a 1D waveguide coupled to a two-level system [\[12](#page-3-19)[,14\]](#page-3-13), a Λ -type three-level system [[15\]](#page-3-20), and even an open interacting resonant-level model [[22](#page-3-21)].

We evaluate the transmission and reflection probabilities using the S matrices constructed from the exact scattering eigenstates [\[14\]](#page-3-13). Because any state containing a finite number of photons is, in practice, a wave packet, we consider a continuous-mode input state [\[28\]](#page-4-3) whose spectrum is Gaussian with central frequency ω_0 and width σ . Throughout this Letter, we set the loss rate as the reference unit for all other quantities: $\Gamma_2 = \Gamma_4 = 1$. The Purcell factor becomes $P = \Gamma/\Gamma_2 = \Gamma$. For all the numerical results shown, we take the detuning of the control field to be zero, $\Delta = 0$, and choose $\sigma = \Gamma_2/5 = 0.2$. In addition, we assume that the transitions $|1\rangle \leftrightarrow |2\rangle$ and $|3\rangle \leftrightarrow |4\rangle$ are at the same frequency ($\omega_{21} = \omega_{43}$).

Figure [1\(c\)](#page-1-1) shows that the transmission probability T_1 of a single photon has a sharp peak as a function of its detuning $\delta \equiv \omega_0 - \omega_{21}$, demonstrating the familiar EIT phenomenon [[15](#page-3-20),[29](#page-4-4)] produced by interference between two scattering pathways. The width of the EIT peak is field strength Ω . Here, we use $P = 6$, a conservative value
oiven the recent advances in experiments [19.20.26]. When $\sim \Omega$ for $P \gg 1$ and is mainly determined by the control given the recent advances in experiments [\[19,](#page-3-16)[20](#page-3-17)[,26\]](#page-4-1). When the control field is turned off, the 4LS becomes a two-level system, which acts as a reflective mirror [\[13\]](#page-3-24).

The EIT picture changes dramatically when there are two or more photons injected into the system. The 4LS mediates an effective photon-photon interaction, which in turn affects the multiphoton transmission. We define T_2

 (T_3) to be the two- (three-) photon transmission probability of the two- (three-) photon scattering process. The strength of the photon blockade P_{21} is given by the conditional probability T_2/T_1 for transmitting a second photon given that the first photon has already been transmitted, normalized by the single-photon transmission probability T_1 : $P_{21} \equiv T_2/T_1^2$. For independent photons, there is no photon blockade and $P_{21} = 1$ In the opposite limit of strong blockade and $P_{21} = 1$. In the opposite limit of strong
photon, blockade, P_{21} is suppressed towards, zero photon blockade, P_{21} is suppressed towards zero.
Similarly we define $P = T_{1}/T_{2}^{3}$ to quantify photon Similarly, we define $P_{31} = T_3/T_1^3$ to quantify photon
blockade in the three-photon case blockade in the three-photon case.

A pronounced photon blockade is shown in Fig. [2\(a\)](#page-2-0) in the strong coupling regime: the single-photon EIT effect does not carry over to the multiphoton case. For increasing coupling strength, both P_{21} and P_{31} approach zero. Such a photon blockade regulates the flow of photons in an ordered manner, enabling coherent control over the information transfer process in our cavity-free scheme. Taking $P = 9$, achieved in Ref. [\[19\]](#page-3-16), we obtain the values $P_{21} \sim 30\%$ and $P_{31} \sim 7\%$, showing that the effects pre-
dicted here are already within reach of experiments dicted here are already within reach of experiments.

The photon blockade occurs despite being in the EIT regime: as shown in Fig. [2\(b\)](#page-2-0), both P_{21} and P_{31} are

FIG. 2 (color online). Photon blockade in transmission. (a) Photon blockade strengths P_{21} (solid line) and P_{31} (dashed line) as functions of the decay rate Γ into the waveguide modes (photon blockade is strongest when P_{21} is smallest). The photons are on resonance with the 4LS ($\delta = 0$), and $\Omega = 1.6$. Strong
counting produces substantial photon blockade, despite EIT coupling produces substantial photon blockade, despite EIT being present in the single-photon properties. (b) P_{21} and P_{31} as functions of the incident photon detuning δ for $\Gamma = 6$ and as photon-induced tunneling $(P_{21}, P_{31} > 1)$ on the sides of the
resonance $\Omega = 1.6$. There is clear photon blockade on resonance, as well resonance.

suppressed within the EIT window, whose width is set by the control field strength Ω . However, away from the EIT window P_{21} and P_{21} become larger than 1 signaling a new window, P_{21} and P_{31} become larger than 1, signaling a new regime of multiphoton transmission—photon-induced tunneling [[21](#page-3-18)]. Previously, photon blockade and photoninduced tunneling have been observed in cavity-QED and circuit-QED systems [[7](#page-3-7)[,8,](#page-3-8)[21\]](#page-3-18), where the underlying mechanism is the anharmonicity of the spectrum caused by the atom-cavity coupling. We emphasize that such anharmonicity is absent in the present cavity-free scheme: the photon blockade and photon-induced tunneling here must be caused by a different mechanism.

To understand the origin of these phenomena, we separate the two-photon transmission probability T_2 into two parts (Fig. [3](#page-2-1)): $(T_2)_{PW} = T_1^2$ is the contribution from inde-
pendent transmission (PW denotes "plane wave"), and pendent transmission (PW denotes ''plane wave''), and $(T_2)_{\text{BS}}$ is the contribution from both the bound-state (BS) term in Eq. [\(3](#page-1-2)) and the interference between the planewave and bound-state terms. $(T_2)_{\text{BS}}$ is the result of the many-body interactions in the waveguide and is absent for cavities. Similarly, T_3 can be separated into $(T_3)_{\text{PW}} =$ T_1^3 and $(T_3)_{BS}$. Figure [3\(a\)](#page-2-2) shows that, when the photons
are on resonance $(T_{23})_{BS}$ is always negative suppressing are on resonance, $(T_{2,3})_{BS}$ is always negative, suppressing the overall transmission. The cause of the observed photon blockade is, thus, the destructive interference between the

FIG. 3 (color online). Many-body bound-state effect causing photon blockade. (a) Transmission as a function of the decay rate $\hat{\Gamma}$ into the waveguide modes for $\Omega = 1.6$. The presence of the many-body bound states suppresses the multiphoton transmismany-body bound states suppresses the multiphoton transmission. (b) Transmission as a function of incident photon detuning δ for $\Gamma = 6$ and $\Omega = 1.6$. The bound states strikingly oppose
multiphoton FIT: off resonance their constructive interference multiphoton EIT; off resonance, their constructive interference produces photon-induced tunneling.

FIG. 4 (color online). Nonclassical photon states. Photonnumber statistics quantified by $log_{10}(P_n/P_{n,\text{Poisson}})$, where the probability of *n* photons in the output state is P_n and $P_{n, \text{Poisson}}$ is for a coherent state with the same mean photon number. Panels (a)–(d) show results for $n = 0, 1, 2,$ and 3, respectively, as functions of the control field strength Ω and the decay rate Γ .
The dashed line is a quide to the eve indicating equal proba-The dashed line is a guide to the eye indicating equal probabilities, $P_n/P_{n,\text{Poisson}} = 1$. Note the large range of parameters for which the single-photon probability is enhanced while the multiphoton content is suppressed—an improved single-photon source.

two transmission pathways: passing by the 4LS as independent particles or as a composite particle in the form of bound states. Within the EIT window, this conclusion always holds [see Fig. [3\(b\)\]](#page-2-2)—both two- and three-photon transmission are strongly suppressed by the many-body bound-state effect. In contrast, away from the EIT window, $(T_{2,3})_{\rm BS}$ changes sign and becomes positive [\[27\]](#page-4-2). Destructive interference changes to constructive interference, producing photon-induced tunneling.

As an application, we now show that the 4LS can generate nonclassical photon states. We assume that the 4LS is in its ground state initially. We consider an incident continuous-mode coherent state of mean photon number $n = 1.0$, on resonance with the 4LS. The photon-number statistics in the transmitted field can be obtained using the S-matrix method [[14](#page-3-13)] and is presented in Fig. [4](#page-3-25) by taking the ratio of the photon-number distribution of the output state P_n ($n = 0, 1, 2, 3$) to that of a coherent state $P_{n, \text{Poisson}}$ having the same mean photon number. It is remarkable that, in most of the parameter space, we have P_1 > $P_{1,\text{Poisson}}$, while $P_2 < P_{2,\text{Poisson}}$ and $P_3 < P_{3,\text{Poisson}}$. This gives rise to a sub-Poissonian single-photon source: for example, for $\Gamma = 9$ ($P = 9$) and $\Omega = 1.6$, we have $P_0 = 64\%$ and $P_1 = 34\%$ with the multiphoton probability 64% and $P_1 = 34\%$, with the multiphoton probability $P_{n\geq 2}$ less than 3%, in comparison with $P_{n\geq 2} = 26\%$ in the input. This single-photon source comes about because, under EIT conditions, a single photon passes through the system with high probability, while multiphoton states experience photon blockade caused by the bound-state effect. A systematic way of improving the quality of the single-photon source is to let a coherent state with a large mean photon number pass through multiple 4LS devices in series with Faraday isolators inserted between each stage.

In summary, we present a cavity-free scheme to realize a variety of nonlinear quantum optical phenomena—including EIT, photon blockade, and photon-induced tunneling in a 1D waveguide. Photon blockade and photon-induced tunneling have a distinctly different origin here compared to the cavity case: a many-body bound-state effect. Furthermore, we outline how to use EIT and photon blockade in this system to produce a single-photon source on demand. On the one hand, the demonstrated ability to control the flow of light quanta using EIT and photon blockade is a critical step towards the realization of an open quantum network. On the other hand, the strong photon-photon interaction mediated by the 4LS provides a new candidate system to study strongly correlated 1D systems, one complementary to condensed-matter systems.

The work of H. U. B. and H. Z. was supported by the U.S. Office of Naval Research.

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pressions of scattering eigenstates and phase analysis of photon blockade and photon-induced tunneling.

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