Schwinger Limit Attainability with Extreme Power Lasers

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High intensity colliding laser pulses can create abundant electron-positron pair plasma [A. R. Bell and J. G. Kirk, Phys. Rev. Lett. 101[, 200403 \(2008\)\]](http://dx.doi.org/10.1103/PhysRevLett.101.200403), which can scatter the incoming electromagnetic waves. This process can prevent one from reaching the critical field of quantum electrodynamics at which vacuum breakdown and polarization occur. Considering the pairs are seeded by the Schwinger mechanism, it is shown that the effects of radiation friction and the electron-positron avalanche development in vacuum depend on the electromagnetic wave polarization. For circularly polarized colliding pulses, these effects dominate not only the particle motion but also the evolution of the pulses. For linearly polarized pulses, these effects are not as strong. There is an apparent analogy of these cases with circular and linear electron accelerators to the corresponding constraining and reduced roles of synchrotron radiation losses.

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Nowadays, lasers provide one of the most powerful sources of electromagnetic (EM) radiation under laboratory conditions and thus inspire the fast growing area of high field science aimed at the exploration of novel physical processes [[1\]](#page-3-2). Lasers have already demonstrated the capability to generate light with an intensity of 2×10^{22} W/cm² [2] and projects to achieve 10^{26} W/cm² [3] 10^{22} W/cm² [\[2\]](#page-3-3), and projects to achieve 10^{26} W/cm² [\[3\]](#page-3-4) are underway. Further intensity growth towards and above 10^{23} W/cm² will bring us to experimentally unexplored regimes. At such intensities the laser interaction with matter becomes strongly dissipative, due to efficient EM energy transformation into high energy gamma rays [[1](#page-3-2),[4\]](#page-3-5). These gamma photons in the laser field may produce electron-positron pairs via the Breit-Wheeler process [[5\]](#page-3-6). Then the pairs accelerated by the laser generate high energy gamma quanta and so on [\[6](#page-3-7)], and thus the conditions for the avalanche-type discharge are produced at the intensity $\approx 10^{25}$ W/cm². The occurrence of such "showers'' was foreseen by Heisenberg and Euler [\[7\]](#page-3-8). In Ref. [\[8\]](#page-3-9) a conclusion was made that depletion of the laser energy on the electron-positron-gamma-ray plasma (EPGP) creation could limit attainable EM wave intensity and could prevent us from approaching the critical quantum electrodynamics field. This field [\[7,](#page-3-8)[9](#page-3-10)] is also called the Schwinger field, $E_S = m_e^2 c^3 / e\hbar$, corresponding to the intensity of $\approx 10^{29}$ W/cm² $\approx 10^{29}$ W/cm².

The particle-antiparticle pair creation by the Schwinger field cannot be described within the framework of perturbation theory, and this sheds light on the nonlinear QED properties of the vacuum [\[10](#page-3-11)]. Understanding the vacuum breakdown mechanisms is challenging for other nonlinear quantum field theories [\[11\]](#page-3-12) and for astrophysics [\[12\]](#page-3-13). Reaching this field limit has been considered as one of the most intriguing scientific problems. Demonstration of the processes associated with the effects of nonlinear QED, such as vacuum polarization and vacuum electron-positron pair production, will be one of the main challenges for extreme high power laser physics [\[1](#page-3-2),[13](#page-3-14)].

In the present Letter we discuss the attainability of the Schwinger field with high power lasers. We compare the role of radiation dissipative effects in the motion of electrons (and positrons) produced via the Schwinger effect and show their dependence on the EM wave polarization.

Pair creation is determined by the Poincaré invariants $\widetilde{\gamma} = (\mathbf{E}^2 - \mathbf{B}^2)/2$, $\mathcal{G} = (\mathbf{E} \cdot \mathbf{B})$ and requires that the first invariant $\tilde{\gamma}$ be positive. This condition can be fulfilled in the vicinity of the antinodes of colliding EM waves, or/and in the configuration formed by several focused EM pulses [\[14\]](#page-3-15). This EM configuration can be locally approximated by an oscillating TM mode with poloidal electric and toroidal magnetic fields. The magnetic field in spherical coordinates \overline{R} , θ , ϕ is given by

$$
\mathbf{B}(R,\theta) = \mathbf{e}_{\phi} \frac{a_0 \sin(\omega_0 t)}{(8\pi R)^{1/2}} J_{n+1/2}(k_0 R) L_n^l(\cos\theta), \quad (1)
$$

where $a_0 = eE_0/m_e c \omega_0$, $k_0 = \omega_0/c$, and $J_\nu(x)$ and $L_n^l(x)$
are the Bessel function and associated Legendre polynoare the Bessel function and associated Legendre polynomials. The electric field is equal to $\mathbf{E} = ik_0(\nabla \times \mathbf{B})$. In evidentical coordinates r , ϕ , τ , the τ component of the cylindrical coordinates r , ϕ , z , the z component of the electric field oscillates in the vertical direction, $\sim a_0 \cos(\omega_0 t)$; the ϕ component of the magnetic field
vanishes on the axis being linearly proportional to the vanishes on the axis, being linearly proportional to the radius, $\sim (a_0/8)k_0r \sin(\omega_0 t)$; and the radial component of the electric field is relatively small, $\sim 0.1a_0k_0^2rz\cos(\omega_0 t)$.
The EM field and first Poincaré invariant $\Re(r, z)$ are shown The EM field and first Poincaré invariant $\mathfrak{F}(r, z)$ are shown in Fig. [1](#page-1-0). We see that the EM field is localized in a region of width less than the laser wavelength, $\lambda_0 = 2\pi/k_0$. The second invariant is equal to zero, $\mathcal{B} = 0$.

Using the expression for the probability of electron-positron pair creation [\[7](#page-3-8)[,9](#page-3-10)] and expanding $\mathfrak{F}(r, z)$ in the vicinity of its maximum, we find that the pairs are created

FIG. 1 (color online). (a) The vector field shows r and z components of the poloidal electric field in the r , z plane for the TM mode. The color density shows the toroidal magnetic field distribution, $B_{\phi}(r, z)$. (b) The first Poincaré invariant $\tilde{\mathfrak{F}}(r, z)$.

in a small four-volume near the electric field maximum with the characteristic size

$$
\pi r_0^2 z_0 t_0 \approx \frac{5^{3/2} \lambda_0^4}{16 \pi^5 c} \left(\frac{a_0}{a_S}\right)^2. \tag{2}
$$

Here, we introduce $a_S = eE_S/m_e \omega_0 c = m_e c^2/\hbar \omega_0$. Integrating over the four-volume the probability of the pair creation [[15](#page-3-16)], we obtain the number of pairs produced per wave period, $\left(5^{3/2}/4\pi^3\right)a_0^4 \exp(-\pi a_S/a_0)$; i.e. the first
pairs can be observed for a one-micron wavelength laser pairs can be observed for a one-micron wavelength laser intensity of the order of 2×10^{27} W/cm², which corre-
sponds to $a_0/a_0 \approx 0.075$ i.e., a characteristic size r. sponds to $a_0/a_s \approx 0.075$, i.e., a characteristic size r_0 approximately equal to $0.04\lambda_0$.

In the region where the magnetic field vanishes, the electron oscillates along the electric field. For an electron generated at small but finite radius $r_0 \ll \lambda_0$, the magnetic field bends its trajectory outwards. By solving the electron equations of motion linearized about the solution corresponding to ultrarelativistic electron oscillations in the z direction, i.e. $a_0 \omega_0 t \gg 1$, we can find the electron trajectories, which are described in terms of modified Bessel functions. The instability growth rate is approximately equal to half the EM field frequency, $\omega_0/2$; i.e. the electron remains in the close vicinity of the zero-magnetic field region, leaving it along the z direction.

The electron oscillating along the electric field emits the high frequency EM radiation with the power $\approx (2\pi r_e/$ $(3\lambda_0)\omega_e m_e c^2 \gamma_e^2$ proportional to the square of electron energy.
In order to find the angular distribution and frequency spec-In order to find the angular distribution and frequency spectrum of the radiation in this case, we should take into account its dependence on the retarded time: $t' = t - \mathbf{n} \cdot \mathbf{r}(t)/c$.
Here **n** is the unit vector in the direction of observation and Here **n** is the unit vector in the direction of observation and $r(t)$ is the electron coordinate. Introducing the angle η between vectors **n** and $\mathbf{r}(t)$, $\mathbf{n} \cdot \mathbf{r}(t) = |\mathbf{r}(t)| \cos \eta$, we can find that in the direction of electron oscillations, $\eta = 0$, the radiation intensity vanishes. The maxima of the radiated power correspond to the angle η_m , for large γ_e , inversely proportional to the particle energy: $\eta_m \approx 1/2\gamma_e$.

The Fourier components of the four-vector potential of the EM field according to Ref. [\[16\]](#page-3-17) are

$$
A^{\mu}(\omega) = \frac{e}{R} \int_{-\infty}^{+\infty} \frac{u^{\mu}}{c} \exp\left\{ i\omega \left[t - \frac{1}{c} \mathbf{n} \cdot \mathbf{r}(t) \right] \right\} dt, \quad (3)
$$

where $u^{\mu} = p^{\mu}/m_e \gamma_e$ is the four-velocity. $\mathbf{r}(t) =$ $e_z(c/\omega_0)$ arcsin[$\beta_m \sin(\omega_0 t)$] and $\beta_m = a_0(1 + a_0^2)^{-1/2}$.
Expanding the phase in expression (3) $\Phi(t) =$ $\mathbf{e}_z(c/\omega_0)$ arcsin[β_m sin(ω_0 t)] and $\beta_m = a_0(1 + a_0^2)^{-1/2}$.
Expanding the phase in expression [\(3\)](#page-1-1), $\Phi(t) = \omega_0^t t - (\cos \theta/\omega_0)$ arcsin[β sin($\omega_0 t$]], over small pa- $\omega\{t - (\cos\eta/\omega_0)\arcsin[\beta_m \sin(\omega_0 t)]\}$, over small parameters $\gamma_{e,m}^{-1}$ and $\omega_0 t$, for $\eta = \eta_m \approx 1/2\gamma_{e,m}$, we obtain

$$
\Phi(t) \approx \omega \bigg[(1 - \beta_m \cos \eta) t + \frac{\beta_m \cos \eta}{6 \omega_0 \gamma_{e,m}^2} (\omega_0 t)^3 \bigg].
$$
 (4)

Using the Airy integral, we can find the y component of the four-vector potential of the EM field ([3\)](#page-1-1) and the radiation power density. Since $\eta \sim 1/\gamma_{e,m} \ll 1$, and thus cos η – $1 \sim 1/2\gamma_{e,m}^2$, the maximum frequency of the radiation
emitted by the linearly oscillating electron is $\omega_z \approx$ emitted by the linearly oscillating electron is $\omega_m \approx$ $0.21\omega_0\gamma_{e,m}^2$.

To take into account the radiation friction, we use the equation of motion of a radiating electron [[16](#page-3-17)]. We can estimate the regime where the radiation friction can become relatively large by comparing the energy losses with the maximal energy gain of an electron accelerated by the electric field, $\mathcal{E}^{(+)} \approx \omega_0 m_e c^2 a_0$, i.e. $\omega_0 m_e c^2 a_0 = \varepsilon_{\text{rad}} \omega_0 m_e c^2 \gamma_e^2$, where $\varepsilon_{\text{rad}} = 4 \pi r_e / 3 \lambda_0$, with $r_e = e^2 / m_c c^2$. As is apparent although an electron moving along $m_e c^2$. As is apparent, although an electron moving along the oscillating electric field loses energy, radiation friction effects may become important only at $a_0 = 2\varepsilon_{\text{rad}}^{-1}$, i.e., at the
electric field $F_0 = 3m^2c^4/c^3$, which is of the order of the electric field $E_0 = 3m_e^2c^4/e^3$, which is of the order of the critical electric field of classical electrodynamics (see also critical electric field of classical electrodynamics (see also Ref. [[15](#page-3-16)]). This is 137 times larger than the field E_S .

In QED the charged particle interaction with EM fields is determined by relativistically and gauge invariant pa-rameters [\[17\]](#page-3-18), $\chi_e = [(F_{\mu\nu}p_\nu)^2]^{1/2}/m_e cE_S$. The parameter χ_e characterizes the probability of the gamma-photon emission by the electron with the Lorentz factor γ_e . It is of the order of the ratio E/E_S in the electron rest frame of reference. Another parameter, $\chi_{\gamma} = [(F_{\mu\nu}\hbar k_{\nu})^2]^{1/2}$ /
m cF is similar to χ with the photon four-momentum $m_e c E_S$, is similar to χ_e with the photon four-momentum $\hbar k_{\mu}$ instead of the electron four-momentum p_{μ} . It characterizes the probability of the electron-positron pair creation due to the collision between the high energy photon and the EM field. QED effects come into play when the energy of a photon emitted by an electron becomes comparable to the electron kinetic energy, i.e., for $\hbar \omega_m = m_e c^2 \gamma_e$. In a linearly polarized oscillating electric field the maximum frequency of emitted photons, ω_m , is proportional to γ_0^2 , and, therefore, quantum effects should be incorporated into the theoretical description at the electron energy corresponding to the gamma factor $\gamma_{Q}^{L} = m_{e}c^{2}/0.21\hbar\omega_{0}$, which is above the Schwinger limit. We see that in the case of electron motion in a linearly polarized oscillating electric field, neither radiation friction nor quantum recoil effects are important.

Reaching the threshold of an avalanche-type discharge with EPGP generation discussed in Refs. [\[6](#page-3-7),[8](#page-3-9)] requires high enough values of the parameters χ_e and χ_{γ} defined above, because for $\chi_{\gamma} \ll 1$, the rate of the pair creation is
exponentially small [18] $W(\gamma) \approx \alpha (m^2 c_1^4 / b^2 \alpha) y$ exponentially small [\[18\]](#page-3-19), $W(\chi_{\gamma}) \approx \alpha (m_e^2 c^4 / \hbar^2 \omega_{\gamma}) \chi_{\gamma}$
exp(-8/3) In the limit $\chi \gg 1$ the pair creation rate $\exp(-8/3\chi_{\gamma})$. In the limit $\chi_{\gamma} \gg 1$ the pair creation rate is given by $W(\chi_{\gamma}) \approx \alpha (m_e^2 c^4/\hbar^2 \omega_{\gamma})(\chi_{\gamma})^{2/3}$ (for details see Bef [17]). Here he is the energy of the photon which see Ref. [[17\]](#page-3-18)). Here $\hbar \omega_{\gamma}$ is the energy of the photon which creates an electron-positron pair.

Since for $\gamma_e \ge \gamma_O$ the photon is emitted by the electron (positron) in a narrow angle almost parallel to the electron momentum with the energy of the order of the electron energy, the parameters χ_e and χ_{γ} are approximately equal to each other. The parameter χ_e can be expressed via the electric and magnetic fields as (see Ref. [[17\]](#page-3-18))

$$
\chi_e^2 = \left(\gamma_e \frac{\mathbf{E}}{E_S} + \frac{\mathbf{p} \times \mathbf{B}}{m_e c E_S}\right)^2 - \left(\frac{\mathbf{p} \cdot \mathbf{E}}{m_e c E_S}\right)^2. \tag{5}
$$

In order to find the threshold for the avalanche development, we need to estimate the QED parameter χ_e . The condition for avalanche development corresponding to the parameter χ_e should become of the order of unity within one-tenth of the EM field period (e.g. see Ref. [[8\]](#page-3-9)). Because of the trajectory bending by the magnetic field, the electron transverse momentum changes as $p_{\perp} \approx (a_0/16) \times$
k r $(a_0 t)^2$ where k r = $(2.5a_0/\pi a_0)^{1/2}$ Eq. (2) As $k_0 r_0(\omega_0 t)^2$, where $k_0 r_0 = (2.5a_0/\pi a_s)^{1/2}$ $k_0 r_0 = (2.5a_0/\pi a_s)^{1/2}$ $k_0 r_0 = (2.5a_0/\pi a_s)^{1/2}$, Eq. (2). Assuming $\omega_0 t$ to be equal to 0.1π we obtain from Eq. (5) suming $\omega_0 t$ to be equal to 0.1π , we obtain from Eq. [\(5\)](#page-2-0) that χ_e becomes of the order of unity; i.e., the avalanche can start at $a_0/a_s \approx 0.105$, which corresponds to the laser intensity 4×10^{27} W/cm². The radiation losses in this limit
can be described as the synchrotron losses of an electron can be described as the synchrotron losses of an electron with the energy $\approx m_e c^2$ moving in the magnetic field $a_0(k_0r_0)/8$. Using formulas for synchrotron radiation [[16](#page-3-17)], it is easy to show that they do not become significant until $a_0 \approx 5 \times 10^4$. At that limit the Schwinger mechanism provides approximately 5×10^5 pairs per one period vides approximately 5×10^5 pairs per one period.
In the case of two colliding circularly polari

In the case of two colliding circularly polarized EM waves, the resulting electric field rotates with frequency ω_0 being constant in magnitude. The power emitted by the electron is $\approx \varepsilon_{rad} \omega_0 m_e c^2 \gamma_e^4$. This is a factor of γ_e^2 larger
than in the case of linear polarization. The properties of than in the case of linear polarization. The properties of radiation emitted by a rotating electron are well known from the theory of synchrotron radiation [[15](#page-3-16),[16](#page-3-17)] and from Ref. [\[19](#page-3-20)]. In the limit $\gamma_e \gg 1$ the emitted power is proportional to the fourth power of the electron energy. The radiation is directed almost along the electron momentum, being localized within the angle inversely proportional to the electron energy: $\delta \eta \approx 1/\gamma_e$. The frequency spectrum given by the well-known expression [\[16\]](#page-3-17) has a maximum frequency, $\omega_m = 0.29 \omega_0 \gamma_e^3$, proportional to the cube of the electron energy. This is a factor of γ larger than in the the electron energy. This is a factor of γ_e larger than in the case of linear polarization. For the electron rotating in the circularly polarized colliding EM waves, the emitted power becomes equal to the maximal energy gain at the field amplitude $a_0 = a_{\text{rad}} = \varepsilon_{\text{rad}}^{-1/3}$. For the laser

wavelength $\lambda_0 = 0.8 \mu m$, $\varepsilon_{rad} = 2.2 \times 10^{-8}$. The nor-
malized amplitude $a_{\text{max}} \approx 400$ corresponding to the laser malized amplitude a_{rad} is ≈ 400 , corresponding to the laser intensity $I_{\text{rad}} = 4.5 \times 10^{23} \text{ W/cm}^2$.
We represent the electric field and

We represent the electric field and the electron momentum in the complex form $E = E_y + iE_z = E_0 \exp(-i\omega_0 t)$ and $p = p_y + ip_z = p_{\perp} \exp[-i(\omega_0 t - \varphi)]$, where φ is the phase equal to the angle between the electric field vector and the electron momentum. In the stationary regime, when the electron rotates with constant energy, the equations for the electron energy, $\gamma_e = [1 + (p_{\perp})]$ $\frac{1}{m_e c}$ ² $]^{1/2}$, and for the phase φ have the form

$$
a_0^2 = (\gamma_e^2 - 1)(1 + \varepsilon_{\text{rad}}^2 \gamma_e^6) \quad \text{and} \quad \tan \varphi = -\frac{1}{\varepsilon_{\text{rad}} \gamma_e^3}.
$$
 (6)

In the limit of weak radiation damping, $a_0 \ll \varepsilon_{\text{rad}}^{-1/3}$, the absolute value of the electron momentum is proportional to absolute value of the electron momentum is proportional to the electric field magnitude, $p_{\perp} = m_eca_0$, while in the regime of dominant radiation damping effects, i.e., at $a_0 \gg$ $\varepsilon_{\text{rad}}^{-1/3}$, it is given by $p_{\perp} = m_e c (a_0/\varepsilon_{\text{rad}})^{1/4}$. For the mo-
mentum dependence given by this expression, the power mentum dependence given by this expression, the power radiated by an electron is $P_{\gamma,C} = \omega_0 m_e c^2 a_0$; i.e., the energy obtained from the driving electromagnetic wave is completely reradiated in the form of high energy gamma rays. At $a_0 \approx \varepsilon_{\text{rad}}^{-1/3}$ we have, for the gamma-photon energy,
 $b\omega_{\text{rad}} = 0.29b\omega_{\text{rad}}^3 \approx 0.45b\omega_{\text{rad}}(mc^3/c^2)$ For example if $\hbar \omega_{\gamma} = 0.29 \hbar \omega_0 a_{\text{rad}}^3 \approx 0.45 \hbar \omega_0 (mc^3/e^2)$. For example, if $\lambda_0 \approx 0.8$ μ m and $a_0 \approx 400$, the circularly polarized laser pulse of intensity $I_{\text{rad}} = 4.5 \times 10^{23} \text{ W/cm}^2$ generates a burst of gamma photons of energy about 20 MeV with the burst of gamma photons of energy about 20 MeV with the duration determined either by the laser pulse duration or by the decay time of the laser pulse in a plasma.

Since in the case of circular polarization ω_m is proportional to the cube of the electron gamma-factor quantum effects should be incorporated into the theoretical description at $\gamma_e \approx \gamma_Q^C = (m_e c^2 / 0.29 \hbar \omega_0)^{1/2} \approx 1300$. For $\gamma_e =$ a_0 this limit is reached at the intensity of $\approx 3.4 \times 10^{24}$ W/cm². The electron motion should be described within the framework of quantum mechanics described within the framework of quantum mechanics. These effects change the radiative loss function (see Ref. [[17](#page-3-18)]). In the quantum regime, it is necessary to take into account not only radiative damping effects, but also recoil momentum effects, which change the direction of motion of the electron because the outgoing photon carries away the momentum $\hbar k_m = \hbar \omega_m/c$.

In the regime when the radiation friction effects are important, i.e., when $a_0 \gg \varepsilon_{\text{rad}}^{-1/3}$, the angle φ between
the electron momentum and the electric field is small the electron momentum and the electric field is small, being equal to $(\epsilon_{rad}a_0^3)^{-1/4}$; i.e. the electron moves almost
in the electric field direction. The electron momentum is being equal to $(\varepsilon_{rad}a_0^2)$ \rightarrow \rightarrow i.e. the electron moves almost
in the electric field direction. The electron momentum is given by $p_{\perp} = m_e c (a_0/\varepsilon_{\text{rad}})^{1/4}$. This yields an estimation
 $\chi \approx (a_0/a^2 \varepsilon_{\text{rad}})^{1/2}$. This becomes greater than unity $\chi_e \approx (a_0/a_s^2 \varepsilon_{\text{rad}})^{1/2}$. This becomes greater than unity
for $a_0 > \varepsilon_{\text{rad}}^2 \approx 5.5 \times 10^3$ which corresponds to the for $a_0 > \varepsilon_{\text{rad}} a_S^2 \approx 5.5 \times 10^3$, which corresponds to the
laser intensity equal to 6×10^{25} W/cm². In Ref. [8] an laser intensity equal to 6×10^{25} W/cm². In Ref. [\[8](#page-3-9)] an avalanche threshold intensity several times lower has been avalanche threshold intensity several times lower has been found, neglecting the effects of the radiation friction force (see also [\[20\]](#page-3-21)). However, the radiation friction time is of the order of $t_{\text{rad}} = 1/\omega_0 (\varepsilon_{\text{rad}} a_0^3)^{1/2}$, which for $a_0 \approx 5.5 \times 10^3$ is approximately one-tenth of the laser period. Hence $10³$ is approximately one-tenth of the laser period. Hence the radiation friction effects do not prevent the EPGP cascade development for circularly polarized colliding waves. Such a prolific electron-positron pair and gamma ray creation [[6](#page-3-7)] should result in the EPGP generation.

While creating and then accelerating the electronpositron pairs, the laser pulse generates an electric current and an EM field. The electric field induced inside the EPGP cloud with a size of the order of the laser wavelength λ_0 can be estimated to be $E_{pol} = 2\pi e(n_+ + n_-)\lambda_0$. Here $n_+ \approx n_-$ are the electron and positron densities, respectively Coherent scattering of the laser pulse away from the tively. Coherent scattering of the laser pulse away from the focus region occurs when the polarization electric field becomes equal to the laser electric field. This yields, for the electron and positron density, $n_+ \approx n_- = E/4\pi e\lambda_0$. The particle number per λ_0^3 volume is about $a_0\lambda_0/r_e$. This is a factor a_0 smaller than required for the laser energy depletion.

In conclusion, a high enough laser intensity pulse with arbitrary polarization plus high enough density of seed electrons, e.g., generated in the laser interaction with solid targets, can provide necessary and sufficient conditions for the avalanche development [[6\]](#page-3-7). Instead, in vacuum, when the seed electrons (positrons) are created via the Schwinger mechanism, we see a fundamental difference between the circularly and linearly polarized waves. In the case of the circularly polarized EM wave, the electron radiation is strong and the threshold for the avalanche is low enough for an avalanche starting at the laser intensity well below the Schwinger limit. Since, as noted in Ref. [[6](#page-3-7)], the electron-positron avalanche parameters are insensitive to the seed electrons (positrons), the parameters of the Schwinger created pairs become hidden and can hardly be revealed. Contrary to this, the linearly polarized EM wave is more favorable for the realization and reaching of "pure" Schwinger electron-positron pair creation. An electron moving along the electric field with velocity and acceleration parallel to the field emits much fewer photons with substantially lower energy, experiencing neither the radiation friction nor quantum recoil effects. We see an analogy of these cases with circular and linear electron accelerators to the corresponding constraining and reduced roles of synchrotron radiation losses. The electron-positron pair creation in the Breit-Wheeler–type process is also suppressed because the dependence of the key parameters χ_e and χ_{γ} on the electron and photon momenta, in the laser field with the same intensity, is much weaker.

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- [1] G. A. Mourou et al., [Rev. Mod. Phys.](http://dx.doi.org/10.1103/RevModPhys.78.309) **78**, 309 (2006); M. Marklund and P. Shukla, [Rev. Mod. Phys.](http://dx.doi.org/10.1103/RevModPhys.78.591) 78, 591 (2006); Y. I. Salamin et al., Phys. Rep. 427[, 41 \(2006\)](http://dx.doi.org/10.1016/j.physrep.2006.01.002).
- [2] V. Yanovsky *et al.*, Opt. Express **16**[, 2109 \(2008\).](http://dx.doi.org/10.1364/OE.16.002109)
- [3] M. Dunne, [Nature Phys.](http://dx.doi.org/10.1038/nphys208) 2, 2 (2006); <www.eli-laser.eu>.
- [4] Ya. B. Zel'dovich, [Sov. Phys. Usp.](http://dx.doi.org/10.1070/PU1975v018n02ABEH001947) 18, 79 (1975); A. Zhidkov et al., Phys. Rev. Lett. 88[, 185002 \(2002\);](http://dx.doi.org/10.1103/PhysRevLett.88.185002) S. V. Bulanov et al., [Plasma Phys. Rep.](http://dx.doi.org/10.1134/1.1687021) 30, 196 (2004).
- [5] G. Breit and J. A. Wheeler, Phys. Rev. 46[, 1087 \(1934\)](http://dx.doi.org/10.1103/PhysRev.46.1087); C. Bamber et al., Phys. Rev. D 60[, 092004 \(1999\)](http://dx.doi.org/10.1103/PhysRevD.60.092004); H. Hu, C. Muller, and C. H. Keitel, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.105.080401) 105, 080401 [\(2010\).](http://dx.doi.org/10.1103/PhysRevLett.105.080401)
- [6] A. R. Bell and J. G. Kirk, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.101.200403) 101, 200403 [\(2008\)](http://dx.doi.org/10.1103/PhysRevLett.101.200403); J. G. Kirk et al., [Plasma Phys. Controlled Fusion](http://dx.doi.org/10.1088/0741-3335/51/8/085008) 51[, 085008 \(2009\)](http://dx.doi.org/10.1088/0741-3335/51/8/085008).
- [7] W. Heisenberg and H. Euler, Z. Phys. 98[, 714 \(1936\)](http://dx.doi.org/10.1007/BF01343663).
- [8] A. M. Fedotov et al., Phys. Rev. Lett. **105**[, 080402 \(2010\).](http://dx.doi.org/10.1103/PhysRevLett.105.080402)
- [9] F. Sauter, Z. Phys. 69[, 742 \(1931\)](http://dx.doi.org/10.1007/BF01339461); J. Schwinger, [Phys.](http://dx.doi.org/10.1103/PhysRev.82.664) Rev. 82[, 664 \(1951\)](http://dx.doi.org/10.1103/PhysRev.82.664).
- [10] W. Dittrich and H. Gies, Probing the Quantum Vacuum (Springer, Berlin, 2000).
- [11] A. Casher, H. Neuberger, and S. Nussinov, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.20.179) 20, [179 \(1979\)](http://dx.doi.org/10.1103/PhysRevD.20.179); Y. Kluger, E. Mottola, and J. M. Eisenberg, Phys. Rev. D 58[, 125015 \(1998\);](http://dx.doi.org/10.1103/PhysRevD.58.125015) C. K. Dumlu and G. V. Dunne, Phys. Rev. Lett. 104[, 250402 \(2010\)](http://dx.doi.org/10.1103/PhysRevLett.104.250402).
- [12] R. Ruffini et al., [Phys. Rep.](http://dx.doi.org/10.1016/j.physrep.2009.10.004) 487, 1 (2010).
- [13] A. Ringwald, [Phys. Lett. B](http://dx.doi.org/10.1016/S0370-2693(01)00496-8) **510**, 107 (2001); V. S. Popov, [Phys. Lett. A](http://dx.doi.org/10.1016/S0375-9601(02)00057-9) 298, 83 (2002); N. B. Narozhny et al., [Phys.](http://dx.doi.org/10.1016/j.physleta.2004.07.013) Lett. A 330[, 1 \(2004\);](http://dx.doi.org/10.1016/j.physleta.2004.07.013) S. S. Bulanov et al., [JETP](http://dx.doi.org/10.1134/S106377610601002X) 102, 9 [\(2006\)](http://dx.doi.org/10.1134/S106377610601002X); A. Di Piazza et al., [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.103.170403) 103, 170403 [\(2009\)](http://dx.doi.org/10.1103/PhysRevLett.103.170403); R. Schutzhold, Adv. Sci. Lett. 2, 121 (2009); G. V. Dunne, H. Gies, and R. Schutzhold, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.80.111301) 80, [111301\(R\) \(2009\)](http://dx.doi.org/10.1103/PhysRevD.80.111301).
- [14] S. S. Bulanov et al., Phys. Rev. Lett. **104**[, 220404 \(2010\).](http://dx.doi.org/10.1103/PhysRevLett.104.220404)
- [15] J. Schwinger, Phys. Rev. **75**[, 1912 \(1949\)](http://dx.doi.org/10.1103/PhysRev.75.1912).
- [16] L.D. Landau and E.M. Lifshitz, The Classical Theory of Fields (Pergamon Press, Oxford, 1975); V. B. Berestetskii, E.M. Lifshitz, and L.P. Pitaevskii, Quantum Electrodynamics (Pergamon, New York, 1982).
- [17] V. I. Ritus, Tr. Fiz. Inst. Akad. Nauk SSSR 111, 6 (1979).
- [18] H. R. Reiss, [J. Math. Phys. \(N.Y.\)](http://dx.doi.org/10.1063/1.1703787) 3, 59 (1962); A. I. Nikishov and V. I. Ritus, [Sov. Phys. Usp.](http://dx.doi.org/10.1070/PU1970v013n02ABEH004234) 13, 303 (1970).
- [19] E. Sarachik and G. Schappert, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.1.2738) ¹, 2738 [\(1970\)](http://dx.doi.org/10.1103/PhysRevD.1.2738); E. Esarey, S. K. Ride, and P. Sprangle, [Phys.](http://dx.doi.org/10.1103/PhysRevE.48.3003) Rev. E 48[, 3003 \(1993\).](http://dx.doi.org/10.1103/PhysRevE.48.3003)
- [20] We note here that using the Landau-Lifshitz approximation for the radiation friction force in the limit $a_0 > a_{rad}$ leads to the losses scaling as $\sim \epsilon_{\text{rad}} a_0^2 \gamma_e^2$ instead $\sim \epsilon_{\text{rad}} \gamma_e^4$ and to underestimation of the laser intensity at which the parameter χ_e becomes equal to unity.