Determination of the Axial-Vector Weak Coupling Constant with Ultracold Neutrons

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A precise measurement of the neutron decay β asymmetry A_0 has been carried out using polarized ultracold neutrons from the pulsed spallation ultracold neutron source at the Los Alamos Neutron Science Center. Combining data obtained in 2008 and 2009, we report $A_0 = -0.11966 \pm 0.00089_{-0.00143}^{+0.00123}$, from
which we determine the ratio of the axial vector to vector weak coupling of the nucleon $a/a =$ which we determine the ratio of the axial-vector to vector weak coupling of the nucleon $g_A/g_V =$ $-1.27590_{-0.00445}^{+0.00409}$

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The axial-vector weak coupling constant g_A plays an important role in our understanding of the nucleon spin and flavor structure [[1](#page-3-0)[,2\]](#page-3-1). It is a central target for high precision lattice QCD calculations [[3](#page-3-2)[,4\]](#page-3-3) and an essential parameter in effective field theories [[5](#page-3-4)]. g_A is also important in a variety of astrophysical processes, including solar fusion reaction rates [\[6](#page-3-5)].

The angular distribution of emitted electrons from polarized neutron decay can be expressed as $W(E) \propto 1 + \frac{v}{c} \times$
 $\langle P \rangle A(E)$ cos θ , where $A(E)$ specifies the β asymmetry ver- $\langle P \rangle A(E) \cos \theta$, where $A(E)$ specifies the β asymmetry ver-
sus electron energy E, ν is the electron velocity c is the sus electron energy E , v is the electron velocity, c is the speed of light, $\langle P \rangle$ is the mean polarization, and θ is the angle between the neutron spin and the electron emission angle between the neutron spin and the electron emission direction [\[7](#page-3-6)]. The leading order value of $A(E)$, A_0 , is given by

$$
A_0 = \frac{-2(\lambda^2 - |\lambda|)}{1 + 3\lambda^2},\tag{1}
$$

where $\lambda = g_A/g_V$ and g_V is the vector weak coupling constant with $g_V = 1$ under the conserved vector current (CVC) hypothesis of the standard model [[8](#page-3-7)]. Higher order terms in $A(E)$ are at the 1% level, and can be calculated precisely under the standard model [[9](#page-3-8)[,10\]](#page-3-9). g_A can also be indirectly determined by combining the Fermi coupling constant G_F (measured to 5 ppm using muon decay [\[11](#page-3-10)]), the Cabibbo-Kobayashi-Maskawa (CKM) quark mixing matrix element $|V_{ud}|$ (measured to 225 ppm using $0^+ \rightarrow$ 0^+ superallowed decays [[8\]](#page-3-7)), and the neutron lifetime (measured to 0.9% [[12](#page-3-11),[13](#page-3-12)]). Thus, a measurement of the β asymmetry permits the direct determination of g_A , as well as a robust test of the consistency of measured neutron β -decay observables under the standard model.

In order to obtain $A(E)$, one must determine the polarization of the neutron beam and control all sources of systematic uncertainty due to backgrounds, including those produced by the neutrons themselves, the detector response, and electronevent reconstruction. All previous precise measurements of the β asymmetry [[14](#page-3-13)[–17](#page-3-14)] have been performed with coldneutron beams and have shown a range of results much wider than the reported uncertainties [[12\]](#page-3-11). Our measurement, UCNA, utilizes ultracold neutrons (UCN—neutrons with kinetic energyless than 200 neV) and controls key systematic uncertainties: neutron polarization and neutron-generated backgrounds. In 2007, we carried out a proof-of-principle β -asymmetry measurement [[18](#page-3-15)]. At present, the UCNA experiment is characterized by neutron polarizations greater than 99.48% and neutron-generated backgrounds that produce corrections to the asymmetry below the 0.02% level.

Some of the experimental details of UCNA are explained in [\[18\]](#page-3-15). We used the UCN source at the Los Alamos Neutron Science Center accelerator at Los Alamos National Laboratory [\[19\]](#page-3-16). The UCN were polarized by a 7 T primary polarizer coupled to an adiabatic fast passage spin flipper to control the spin state [\[18](#page-3-15)[,20\]](#page-3-17). Polarized UCN entered the superconducting spectrometer [[21](#page-3-18)] and were confined in a 3 m long, 12.4 cm diameter electropolished Cu tube (decay trap) with variable thickness mylar end caps. The inside surface of each end cap was coated with 200 nm of Be. A 1 T magnetic field was oriented parallel to the decay trap, along which decay electrons spiraled toward one of two identical electron detector packages, each covering a 2π sr angular hemisphere. Each detector package consisted of a lowpressure multiwire proportional chamber (MWPC) [\[22\]](#page-3-19) backed by a plastic scintillator, with scintillation light measured by four photomultiplier tubes (PMT). Each MWPC had thin front and back mylar windows which separated low-Z chamber gas (neopentane) from the spectrometer vacuum. To study key systematics due to electron energy loss and backscattering in the windows, we operated the experiment in four different geometries with different decay trap end caps and MWPC window thicknesses—A: 0.7 and 25; B: 13.2 and 25; C: 0.7 and 6; and D [\[23\]](#page-3-20): 0.7 and 6 $\,\mu$ m, respectively.

Cosmic-ray muon backgrounds were identified by a combination of plastic scintillator veto paddles and sealed drift tube assemblies [[24](#page-4-0)] surrounding the electron detectors. γ -ray backgrounds were vetoed by a coincidence between the MWPC and the main β scintillator.

A gate valve separated the UCN source from the experimental apparatus. A typical run unit consisted of a background run (gate valve closed), a β -decay run (gate valve open), and a UCN depolarization run to measure the equilibrium UCN polarization for the accompanying β -decay run. The UCN spins were flipped back and forth (while the magnetic field in the superconducting spectrometer was held fixed) between run units [Fig. [1\(a\)\]](#page-1-0), which partially canceled systematic rate variation over the period of a spin cycle (\sim 1.5 h). During a depolarization run, the guide serving as input to the 7 T polarizing field was first connected to a UCN detector [[25](#page-4-1)] so that UCN exiting the experiment could be counted, while the gate valve was closed and the proton pulses [[19](#page-3-16)] were discontinued. This cleaning phase, which lasted 25 s, produced a signal in the UCN detector proportional to the number of correctly polarized UCN present in the experimental geometry at the end of the β -decay measurement interval. Following the cleaning phase, the state of the spin flipper was changed, allowing only incorrectly polarized UCN

FIG. 1 (color online). Panel (a): schematic of the experiment and definition of the asymmetry. Panel (b): background subtracted electron E_{recon} spectrum (solid circles with the uncertainty of E_{recon} reflected by the horizontal error bars), combining both sides of the detectors and two spin states, overlaid with the Monte Carlo spectrum (histogram). The open circles represent the measured ambient background spectrum. Panel (c): A_0 vs E_{recon} , combining all four geometries. The horizontal line represents the extracted A_0 within [275, 625] keV. Drawn on the same scale below the graph are four sets of bands representing the sum of energy-dependent backscattering and angle effect corrections (light color), the positive sign indicating a larger $|A_0|$, and their uncertainties (dark) for the four geometries. The positive (negative) correction at low (high) energy is a consequence of the backscattering (angle effect) dominating in this energy region. The number of β events for each geometry is also indicated in the figure.

 E_{recon} (keV)

remaining downstream of the spin flipper to pass through the 7 T polarizing field and be counted. Counting during this *unloading* phase was performed for \sim 200 s in order to measure background as well as incorrectly polarized UCNs. Since the measured depolarization was consistent with zero at the 1σ level, we folded together statistical and systematic errors to produce a global polarization lower limit of 99.48% at the 68% CL [[20](#page-3-17)], covering all four geometries and both polarization states.

The experimental triggers were formed by requiring at least two of the four PMT signals over threshold in either of the scintillator detectors. Electron positions were determined with the MWPC to an accuracy of better than 2 mm based on the distribution of charge on two perpendicular cathode grids in the MWPC [\[22](#page-3-19)]. A fiducial cut of $r < 45$ mm was placed on the trigger side to reduce background and to eliminate electrons that could strike the decay trap walls.

Reconstructed event energies E_{recon} were measured using the signals from the scintillator PMTs as calibrated with conversion electron sources $(^{109}Cd, ^{139}Ce, ^{113}Sn, ^{85}Sr,$ and 207Bi). The position dependence of the response of each PMT was mapped out by comparing the neutron betadecay spectrum endpoint observed at different positions. The energy reconstruction uncertainty was determined to be the larger of \pm 5 keV or \pm 2.5%, which covered the uncertainty in the position response of the scintillator as uncertainty in the position response of the scintillator, as well as possible variation of the energy response allowed by the calibration data.

The PMT gains were monitored based on frequent calibrations with a removable 113 Sn calibration source, which also measured the energy resolution of the system $(\sim 400$ photoelectrons per MeV), and by observing shifts in the minimum-ionizing peak of cosmic-ray muons during β -decay–background runs.

The majority of the β -decay events were single detector triggers. However, due to electron backscattering, a small fraction of the events, varying between 1.7% and 3.4% for the four geometries, triggered both scintillators, and another small fraction $({\sim} 2\%)$ were detected by both MWPCs, but triggered only one of the scintillators. In the first case, the initial direction of the electron could be determined by the relative timing of the triggers, while in the second case a fixed cut (4.1 keV) or a likelihood function based on the energy loss in the trigger side MWPC yielded an identification efficiency of $\sim 80\%$ based on Monte Carlo calculations (discussed later).

In addition to the ambient backgrounds (measured with the UCN gate valve closed and suppressed by the pulsed nature of the UCN source [\[19\]](#page-3-16)), which were subtracted run by run, neutron captures in the vicinity of the detectors could create prompt γ 's with energies up to ~8 MeV, generating an irreducible background in the experiment. This background was significantly suppressed, compared to cold-neutron beam experiments, by the relatively low density and low capture and upscatter probability of neutrons in and around the spectrometer. Combining direct measurements with Monte Carlo calculations, we obtained an upper limit of 0.02% on the correction to the asymmetry.

For each run, events were sorted into 25 keV E_{recon} bins from 0 to 1200 keV and assigned an initial direction. The rates in the two detectors were then computed based on the experiment live time. We applied separate spin-dependent blinding factors to the two detector rates, effectively adding an unknown scaling factor to the measured asymmetry that was constrained to be within 1.00 ± 0.05 . After deter-
mination of all cuts, corrections, and uncertainties, this mination of all cuts, corrections, and uncertainties, this factor was removed. For each β -decay–background run pair, the background rate was subtracted from the β -decay–run rate bin by bin. The reconstructed energy spectrum (background subtracted, averaged over the two spin states) is shown in panel (b) of Fig. [1,](#page-1-1) overlaid with the measured background. The S/B is about 40 in our analysis energy window between 275 and 625 keV (discussed later). Also overlaid is the Monte Carlo–predicted reconstructed energy spectrum, with all detector effects (efficiencies, resolutions, etc.) taken into account. The systematic effect due to the small discrepancy between the two spectra is well covered by the energy reconstruction uncertainty in Table [I.](#page-2-0)

For a given geometry, a ''super ratio'' of count rates among the two detectors and UCN spin states was calculated (as defined in [[18](#page-3-15)]), from which the raw measured asymmetry was determined [see also Fig. [1\(a\)\]](#page-1-0). To extract A_0 , we first multiplied the raw measured asymmetry by $1/\langle v/c \rangle$ in each energy bin to remove the strongest energy dependence. As in [[18](#page-3-15)], two scattering-related effects dominated subsequent systematic corrections: the residual backscattering correction and the angle effect. In addition to a small residual correction due to incorrect identification of the initial electron direction for the measured electron backscatters (where both detectors observed the electron), there were corrections for backscattering from the decay trap windows and the front windows of the MWPC that could not be identified experimentally. Angle effects arose from the fact that the energy loss of an electron in the thin windows was strongly angle dependent. Low-energy, large

TABLE I. Summary of experimental corrections and uncertainties in % (all fractional to A_0). Upper table: geometryindependent effects (with zero corrections). Lower table: $geometry-dependent$ effects (first value $=$ correction, second value = uncertainty in each column), with σ_{stat} , Δ_{back} , Δ_{ang} , and ϵ_{MWPC} referring to statistical uncertainty, backscattering correction, angle effect correction, and the uncertainty associated with MWPC inefficiency, respectively.

Geometry-independent effect							Uncertainty $(\%)$		
Polarization							$+0.52$ -0		
Field nonuniformity							$+0.20$ -0		
Rate-dependent gain shift							0.08		
Gain fluctuation							0.20		
Dead time							0.01		
Energy reconstruction							0.47		
UCN-induced background							0.02		
Muon veto efficiency							0.30		
Live time uncertainty							0.24		
Fiducial cut							0.24		
	Geometry-dependent effect								
	A $(\%)$		$B(\%)$		$C(\%)$		D $(\%)$		
$\sigma_{\rm stat}$		1.23		1.22		2.00		2.10	
Δ_{back}	1.34	± 0.40	4.32	± 1.30	1.07	± 0.32	1.08	± 0.32	
Δ_{ang}	-1.81	± 0.45	-3.22	± 0.81	-0.60	± 0.15	-0.36	± 0.09	
ϵ_{MWPC}	θ	0.02	θ	0.01	θ	0.16	θ	0.5	

FIG. 2 (color online). Ideogram comparing the previous measurements that are included in the 2009 Particle Data Group best value for A_0 along with the new result reported here. The dashed line is the ideogram with the previous four data points, and the solid line shows the result of including the present data.

pitch angle electrons were more likely to fall below the scintillator threshold, leading to a suppression of the acceptance at large angles $(\langle \cos \theta \rangle)$ deviating from 1/2). Both
of these effects were evaluated with two independent of these effects were evaluated with two independent simulation programs: Penelope [\[26](#page-4-2)] and GEANT4 [\[27\]](#page-4-3). The resulting corrections for all four geometries are shown in Table [I.](#page-2-0) Based on the observed difference between the calculations and the data, we assigned an uncertainty of 30% to the backscattering correction and 25% to the angle effect correction.

Recoil-order corrections to $A(E)$ (see also [[18](#page-3-15)]) were calculated within the context of the standard model according to the formalism of [[9](#page-3-8)[,10\]](#page-3-9), leading to a correction of $(-1.79 \pm 0.03)\%$ to A_0 . The value for the radiative correction to A_0 was taken from the calculations of [28] rection to A_0 was taken from the calculations of [\[28\]](#page-4-4), yielding a small theoretical correction of $(0.10 \pm 0.05)\%$.
Applying all corrections mentioned above the extracted

Applying all corrections mentioned above, the extracted A_0 is plotted against E_{recon} (all geometries combined) in panel (c) of Fig. [1.](#page-1-1) Energy-dependent corrections (backscattering and angle effects) and their uncertainty are indicated as bands in the figures. The final A_0 is obtained from a constant fit over a range of energy [[29](#page-4-5)]. The energy window, 275 to 625 keV, was chosen to optimize combined statistical and systematic uncertainties before unblinding the asymmetries. The value of A_0 was insensitive to the choice of energy window, with the variation less than 15% of the statistical uncertainty for windows between 150 and 750 keV.

The experimental uncertainties and systematic corrections to A_0 are summarized in Table [I.](#page-2-0) Geometry-dependent systematic uncertainties (backscattering, angle effect, and MWPC inefficiency) are treated as completely correlated among the different geometries. Combining the four geometries, we find $A_0 = -0.11966 \pm 0.00089_{-0.0014}^{+0.00123}$
(with a x^2/u of 2.4/3) where the first uncertainty is statis-(with a χ^2/ν of 2.4/3), where the first uncertainty is statistical and the second systematic [29]. Based on Eq. (1), we tical and the second systematic [\[29\]](#page-4-5). Based on Eq. ([1\)](#page-0-0), we then determine $g_A/g_V = -1.27590^{+0.004}_{-0.00445} = g_A$, where the second equality assumes CVC [[8\]](#page-3-7).

Our result for A_0 is compared with the world data [\[14–](#page-3-13)[17\]](#page-3-14) in Fig. [2.](#page-3-21) Our result is in good agreement with the most recent and precise result for A_0 [\[14\]](#page-3-13). We note that the direct extraction of g_A/g_V from the β asymmetry is, unlike extraction from the neutron lifetime [\[12,](#page-3-11)[30\]](#page-4-6), independent of the Cabibbo-Kobayashi-Maskawa matrix element $|V_{ud}|$. This strongly motivates UCN-based measurements of the neutron β asymmetry, where the key neutron-related systematic uncertainties can be reduced below the 0.1% level. Recently demonstrated improvements to the UCN source and refinement of the energy response and gain monitoring will permit the collection of a much larger data set and the reduction of all major systematic uncertainties.

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