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## Spin Control of Drifting Electrons Using Local Nuclear Polarization in Ferromagnet-Semiconductor Heterostructures

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We demonstrate methods to locally control the spin rotation of moving electrons in a GaAs channel. The Larmor frequency of optically injected spins is modulated when the spins are dragged through a region of spin-polarized nuclei created at a MnAs/GaAs interface. The effective field created by the nuclei is controlled either optically or electrically using the ferromagnetic proximity polarization effect. Spin rotation is also tuned by controlling the carrier traverse time through the polarized region. We demonstrate coherent spin rotations of  $5\pi$  rad during transport.

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The ability to manipulate the state of electron and nuclear spins is a critical tool in spin-based quantum science. Control of spins typically requires pulsed optical or microwave fields to manipulate stationary spin ensembles or single spin centers [[1–](#page-3-1)[6](#page-3-2)]. Using these techniques and judiciously timed pulse sequences, it is possible to prepare confined electrons into any coherent superposition of spin- $\frac{1}{2}$  eigenstates [[7\]](#page-3-3), which enables fundamental investigations of quantum behavior and the use of dynamical decoupling to refocus spin coherence [\[1\]](#page-3-1). Another fundamental challenge with potential technological impact is the ability to transport spin states from one location to another with coherent control in transit [\[8\]](#page-3-4). We present a spin control method that uses the spatial analogue of a timed field pulse as a quantum gate to control the coherent superposition of drifting spins. In this scheme, the pulse time is controlled by the drift velocity of the spins traveling through spatially isolated fields generated by the quantum gate. Implementing a quantum gate during transport requires initialization at one end of a channel, coherent manipulation during drift, and readout of the spin state at the other end of the channel within the coherence time [[9\]](#page-3-5). Conduction electron spin ensembles in  $n$ -type GaAs are promising candidates, as they can have coherence times above 100 ns at low temperatures [[10](#page-3-6)], can be optically [\[11\]](#page-3-7) or electrically [[12](#page-3-8)] initialized, transported over distances exceeding 100  $\mu$ m [[11](#page-3-7)], and readout both optically [\[11\]](#page-3-7) and electrically [[13](#page-3-9)]. Previous experiments in lateral geometries have demonstrated nonlocal electrical, magnetic, and spin-orbit field control of drifting spins in GaAs and InGaAs quantum wells [[12](#page-3-8)[–15\]](#page-3-10) and magnetic control in Si [\[16](#page-3-11)] and graphene [\[17](#page-3-12)]. Additionally, local optical control of the spin polarization amplitude has been demonstrated in a GaAs ring interferometer structure [\[18\]](#page-3-13) using dynamic nuclear polarization.

We performed a spatially localized quantum gate operation on an ensemble of moving spins using the magnetic field generated from a prepared region of polarized GaAs nuclear spins in a lateral transport structure. Optically injected electron spin ensembles [[11](#page-3-7)] are dragged by an applied voltage through the polarized nuclear region [[19\]](#page-3-14), emerging on the other side with a rotated spin state. The nuclear spins are polarized at the interface of a lithographically patterned epitaxial MnAs ferromagnet via the ferromagnetic proximity polarization (FPP) effect [\[20](#page-3-15)[,21\]](#page-3-16). This effect can be activated either optically [\[20\]](#page-3-15) or electrically [\[22](#page-3-17)[,23\]](#page-3-18) in the channel and, in the presence of a 0.2 T magnetic field at low temperatures, has been shown to create an additional localized effective magnetic field under the MnAs up to 0.4 T [\[19\]](#page-3-14). In this region, the moving spins precess faster than they would in a bare channel, and as they emerge, optical measurements indicate they have acquired additional spin rotation about the z axis defined by the magnetic field. We tune the angle of rotation by controlling the local nuclear field strength and interaction time between the polarized nuclei and moving electrons. In our experiment, the rotation angle of the moving spins is



<span id="page-0-0"></span>FIG. 1 (color). (a) Nuclear spins are polarized at the MnAs/GaAs interface using an optical imprinting beam. (b) Nonlocal TRKR measurement geometry used to inject and detect drifting electron spins in the channel after imprinting the nuclear region. (c) Nuclear spins are also polarized by forward biasing the Schottky junction at the MnAs/GaAs interface. During both optical and electrical imprinting  $i_{channel}$  is off.

modified by  $5\pi$  rad along the Bloch sphere in 6 ns over a distance of 30  $\mu$ m.

Samples were fabricated from a layer structure of 25 nm type-A MnAs/1  $\mu$ m Si-doped *n*-GaAs (*n* = 1  $\times$  $10^{17}$  cm<sup>-3</sup> $/250$  nm Al<sub>0.45</sub>Ga<sub>0.55</sub>As/semi-insulating (001) GaAs substrate grown by molecular beam epitaxy. Similar samples with lower Si doping  $(3 \times 10^{16} \text{ and } 7 \times$  $10^{16}$  cm<sup>-3</sup>) demonstrated similar results but are not shown. The ferromagnetic MnAs layer exhibited square hysteresis with a coercivity of 2000 Oe at 10 K along the easy axis, in the  $\langle 110 \rangle$  direction of the GaAs substrate. Using standard lithographic methods, we fabricated electrically isolated 10  $\mu$ m wide GaAs channels with 30  $\mu$ m long MnAs islands above the center of the channel [Fig. [1\(b\)\]](#page-0-0). We made Ohmic contact to the GaAs channel with a two-point resistance of 5 k $\Omega$ .

Electron spin dynamics were measured using timeresolved Kerr rotation (TRKR) in the Voigt geometry [\[24\]](#page-3-19) with the sample growth axis parallel to the optical axis. A saturating external field  $B_{ext}$  of 0.2850 T was applied along the MnAs easy axis, parallel to the channel, as shown in Fig. [1\(b\)](#page-0-0). Optical excitation and readout were performed using a mode-locked Ti:sapphire laser producing  $\sim$ 150 fs pulses at a repetition rate of 76 MHz. Its wavelength was tuned to 807 nm to excite carriers above the GaAs band gap. A circularly polarized, 670  $\mu$ W pump beam was used to inject spin-polarized electrons with an initial spin projection parallel to the optical axis. After a time delay  $\Delta t$ , a linearly polarized, 90  $\mu$ W beam was used to probe the electron spin component along the optical axis via the magneto-optic Kerr effect. Both pump and probe beams were focused to a 10  $\mu$ m spot size and were modulated at 50 kHz and 500 Hz, respectively, for lock-in detection, while  $\Delta t$  was controlled by a mechanical delay line. Measurements were conducted at  $T = 8$  K.

The pump and probe beams were focused on the GaAs channel to the right and left of the MnAs island, respectively [Fig. [1\(b\)\]](#page-0-0). A voltage bias was applied to the channel causing the injected spins to drift from the pump spot to the probe spot. The 13.15 ns repetition time of the laser exceeds the 6 ns spin lifetime of our samples; therefore, the contrast in the probe signal is due solely to a single initialization pulse.

For nuclear spin polarization, a circularly polarized, 5 mW imprinting beam, derived from the same laser, was focused onto the MnAs island with no bias applied as shown in Fig. [1\(a\).](#page-0-0) Excited electron spins spontaneously polarize along the ferromagnetic magnetization direction via the FPP effect [[25](#page-3-20)]. The injected spins then transfer their angular momentum to the nuclear spins via the hyperfine interaction. This aligns the nuclear spins preferentially along the MnAs magnetization direction [[20](#page-3-15)] adding a spatially isolated [[19](#page-3-14)] effective magnetic field,  $B_{\text{nuc}}$  to the external field  $B_{ext}$  under the MnAs, which we measured to be near 0.4 T. After imprinting for 20 min to saturate the nuclear spin polarization, the imprinting beam was blocked. We then turned on the channel voltage dragging the injected electron spins through the polarized nuclear region. Their spin projection was measured by Kerr rotation as they emerged on the other side.

We first characterize the drift and diffusion characteristics of a 10  $\mu$ m wide channel without a MnAs island. We measured TRKR versus delay and pump-probe separation  $(\Delta x)$  for channel currents ( $i_{channel}$ ) between 0.5 and 2 mA. Figure [2\(a\)](#page-1-0) is a density plot of KR versus delay and pumpprobe separation for a channel current of 1.0 mA. The data are in good agreement with the one-dimensional spin drift equation  $[12,14]$  $[12,14]$  $[12,14]$  $[12,14]$  $[12,14]$ 

<span id="page-1-1"></span>
$$
s(x, t) = \frac{S_0}{\sqrt{2\pi\sigma^2}} \exp\left(\frac{-(x - v_d \Delta t)^2}{4\sigma^2}\right) \exp\left(\frac{-\Delta t}{T_2^*}\right)
$$
  
× cos( $\omega_L \Delta t$ ), (1)

where  $S_0$  is the amplitude,  $v_d$  is the spin drift velocity, x is the position of injection,  $T_2^*$  is the spin lifetime,  $\sigma$  is the pump spot diameter, and  $\omega_L = g \mu_B (B_{ext} + B_{nuc})/\hbar$  is the electron Larmor frequency. We also use the effective electron g-factor g, the Bohr magneton  $\mu_B$ , and the Planck constant  $\hbar$ . In the absence of applied current, KR measurements did not show significant spatial diffusion over the same delay range, indicating that drift dominates diffusion in these structures. The data in Fig.  $2(a)$  fit well to Eq.  $(1)$ with  $B_{\text{ext}} = 0.2850$  T,  $\sigma = 10 \mu \text{m}$ ,  $T_2^* = 6 \text{ ns}$ ,  $g = 0.44$ , and  $v_d = 12 \times 10^6$  cm/s with  $i_{channel} = 1$  mA. We extract  $v_d$  from these data by taking the slope  $\Delta x/\Delta t$  of line cuts along the density plot [Fig. [2\(a\)](#page-1-0)]. As shown in Fig. [2\(b\)](#page-1-0), the drift velocity is a linear function of channel current  $i_{channel}$ . Separate two-point resistivity measurements indicated no measurable sample heating for the range of currents we used.

On a channel with a MnAs island, we separated the pump and probe beams by 35  $\mu$ m and focused them on either side of the 30  $\mu$ m long MnAs island [Fig. [1\(b\)\]](#page-0-0). First, we measured KR versus delay time for various settings of  $i_{channel}$  without polarizing the nuclear region



<span id="page-1-0"></span>FIG. 2 (color). (a) TRKR versus delay time in a control GaAs channel (with no MnAs) as the pump beam is rastered away from the probe beam along the channel with  $B_{ext} = 0.2850$  T at  $T =$ 8 K. The drift velocity is extracted from line cuts taken along these data. (b) Drift velocity measured from rastered TRKR scans as a function of channel current.

as shown in Fig. [3\(a\)](#page-2-0). The measured Kerr rotation signal was strongest for delays between 2 to 7 ns after injection, when the maximum amplitude of the spin ensemble emerged from under the MnAs. Next, we polarized the localized nuclear spins with the imprinting beam. To probe the nuclear dynamics, we measured KR at a fixed pumpprobe delay indicated by the arrow in Fig. [3\(a\)](#page-2-0) for  $i_{channel} = 0.75$  mA as a function of time after blocking the imprinting beam. Figure [3\(b\)](#page-2-0) shows how the electron spin projection measured at the probe spot evolved over 20 min. We extract the spin rotation under the MnAs by fitting traces of these data at fixed delay to the following expression:

<span id="page-2-1"></span>
$$
S_0 \left[ 1 - s_0 \exp\left(\frac{-t}{\tau_N}\right) \right] \cos \left[ \Delta \phi_{\text{probe}} \exp\left(\frac{-t}{\tau_N}\right) \right], \quad (2)
$$

where  $\Delta \phi_{\text{probe}}$  is the maximum acquired spin rotation from nuclear polarization,  $s_0$  scales the signal due to inhomogeneous nuclear polarization, t is time, and  $\tau_N$  is the nuclear spin relaxation time. The evolution of the spin rotation in time is plotted in the inset of Fig. [3\(b\).](#page-2-0) The solid red line in Fig. [3\(b\)](#page-2-0) shows a fit to Eq. ([2](#page-2-1)) with  $s_0 = 0.44$ ,  $\tau_N = 163$  s, and  $\Delta \phi_{\text{probe}} = 10.6$  rad. These data suggest that  $B_{\text{nuc}}$  relaxes after active imprinting is turned off, with a time scale on the order of minutes, which is consistent with nuclear



<span id="page-2-0"></span>FIG. 3 (color). (a) Nonlocal TRKR delay scans at fixed pumpprobe separation of 35  $\mu$ m for specified channel currents between 0.5 and 2.0 mA with no imprinting at  $T = 8$  K. These data are taken in a patterned MnAs/GaAs device using the scheme shown in Fig. [1\(b\).](#page-0-0) (b) Nonlocal TRKR versus time data at fixed delay indicated by arrow in (a) for  $i_{channel} = 0.75$  mA at  $T =$ 8 K. Data are taken after optically polarizing the nuclei [Fig. [1\(a\)\]](#page-0-0) with a 1.75 mW imprinting beam for 20 min. Solid line shows a fit to Eq. ([2\)](#page-2-1). Inset: Time dependence of the nuclearinduced spin rotation measured in (b). (c) Maximum electron spin rotation as a function of temperature at  $\Delta t = 5$  ns,  $i_{channel} =$ 0:75 mA after applying a 1.75 mW imprinting beam for 20 min. For all data  $B_{ext} = 0.2850$  T. Error bars are comparable to the size of the data points.

relaxation times [\[24\]](#page-3-19). To confirm that this interaction is due to nuclear spins, we also studied the temperature dependence of this spin rotation at fixed delay, imprinting beam power, and channel current [Fig.  $3(c)$ ]. As the temperature increased, we measured less spin rotation over the 20 min wait time, and by 50 K no spin rotation was measured. Previous studies have observed similar reduction of the FPP effect [[19,](#page-3-14)[20](#page-3-15)].

Since we place the pump and probe beams near the boundaries of the MnAs island, we can ignore the unpolarized regions and model our experiment as an electron spin ensemble traveling through a uniform polarized nuclear environment. The maximum spin rotation angle at the probe spot is described by  $\Delta \phi_{\text{probe}} = g \mu_B (B_{\text{ext}} +$  $B_{\text{nuc}}/\Delta t_{\text{nuc}}/h$ , where  $\Delta t_{\text{nuc}}$  is the traverse time across the region.

This model suggests we can tune the spin rotation by controlling the strength of  $B_{\text{nuc}}$  at fixed values of  $B_{\text{ext}}$  and  $\Delta t_{\text{nuc}}$ . In Fig. [4\(a\)](#page-3-22) we plot the spin rotation we extract from fits to Eq. [\(2\)](#page-2-1) as a function of imprinting power over the range of 500 nW–6 mW. We observed less rotation at lower power since the reduced presence of injected spinpolarized carriers weakens the FPP effect, resulting in a reduced  $B_{\text{nuc}}$ . The spin rotation saturated near 1 mW, suggesting  $B_{\text{nuc}}$  was maximized. We calculated this maximum optically induced value to be 0.4 T. At even higher powers, sample heating limits the FPP, thus reducing the spin rotation. At optimal power conditions, we measured nearly  $5\pi$  rad of nuclear field-induced spin rotation during transport.

The spin rotation also depends on the traverse time of the spins moving through the nuclear region. Using the same method described above, we measured the spin rotation as a function of  $\Delta t_{\text{nuc}}$  at 8 K and fixed imprinting power. To ensure that a measurable quantity of spins emerged at each delay, we used  $i_{channel} = 0.75$ , 1.25, and 1.75 mA for different ranges of  $\Delta t_{\text{nuc}}$  during the measurement [Fig. [4\(b\)\]](#page-3-22). The data show a linear relationship between the spin rotation and traverse time. A fit to the 0.75 and 1.25 mA data sets indicates a slope and intercept of  $0.76\pi \pm$  $0.03\pi$  rad/ns and  $-0.01\pi \pm 0.16\pi$  rad, respectively. We excluded the data at 1.75 mA from our analysis because, starting near the corresponding electric field  $(2.5 \text{ kV/cm})$ , the drift velocity peaks as a function of electric field due to a turn on of electron scattering into satellite valleys of the conduction band. This narrows the velocity distribution within the spin packet. Nevertheless, we show that by adjusting the drift velocity of the spins moving through the channel we are able to control the time of this spatial pulsing technique.

We repeated our measurements on a second sample [Fig. [1\(c\)](#page-0-0)] designed to control the nuclear field strength electrically rather than optically. After processing this sample in an identical manner, an additional metal contact was deposited onto the MnAs to enable electrical biasing



<span id="page-3-22"></span>FIG. 4 (color). (a) Maximum electron spin rotation measured as a function of the imprinting beam power at  $\Delta t = 6$  ns,  $i_{channel} = 0.75$  mA after imprinting for 20 min. (b) Maximum electron spin rotation measured as a function of delay time for  $i_{channel} = 0.75, 1.25,$  and 1.75 mA after imprinting with a 1.75 mW beam for 20 min. (c) Schottky current and maximum electron spin rotation measured versus forward bias Schottky voltage at  $\Delta t = 4.5$  ns,  $i_{channel} = 0.75$  mA after imprinting for 20 min. For all data  $B_{ext} = 0.2850$  T and  $T = 8$  K. Error bars are comparable to the size of the data points.

of the Schottky junction diode at the MnAs/GaAs interface. Current-voltage characterization of this junction demonstrated rectifying behavior as shown by the solid line in Fig. [4\(c\)](#page-3-22). For these measurements no imprinting beam was applied; instead, the nuclear spins were polarized by forward biasing the Schottky junction between the MnAs and GaAs as illustrated in Fig. [1\(c\).](#page-0-0) The Schottky current drives electrons from the GaAs to the MnAs inducing spin-dependent reflections at the ferromagnetsemiconductor interface [\[23\]](#page-3-18). The resulting spin-polarized electron population at the interface polarizes the nuclear spins through the dynamic nuclear polarization mechanism [\[22](#page-3-17)[,23\]](#page-3-18).

For measurements using electrical polarization, the pump and probe beams were blocked and  $i_{channel}$  was set to zero while a voltage was applied to the Schottky junction with  $B_{\text{ext}} = 0.2850$  T. After 20 min the Schottky voltage was turned off, the pump and probe beams were unblocked, and  $i_{channel} = 0.75$  mA was applied. We observed the onset of spin rotation [open circles in Fig.  $4(c)$ ] near the 2 V Schottky turn-on voltage. As the Schottky voltage increased further, the concentration of spin-polarized electrons and resulting nuclear polarization at the MnAs/GaAs interface increased correspondingly. We calculate the maximum electrically induced value of  $B_{\text{nuc}}$  to be 0.4 T. Beyond 50  $\mu$ A, however, we observed a systematic reduction of the measured rotation, suggesting that currentinduced heating begins to reduce the strength of the FPP effect.

In summary, we have demonstrated the ability to both electrically and optically manipulate the spin rotation of moving electrons through localized effective magnetic fields in a semiconductor channel. Extensions of these techniques may generate sequenced spin rotation about different axes, potentially also using spatially localized electric fields, spin-orbit interactions, or pulsed microwaves. Such a device could perform successive operations on moving spins to enable environmental decoupling and quantum metrology of the semiconductor host. Localized control of drifting spins in different materials may also help realize room temperature [\[26\]](#page-3-23) quantum information processing based on existing transport-based technologies.

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