Electromagnons in the Spin Collinear State of a Triangular Lattice Antiferromagnet

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Terahertz time-domain spectroscopy was performed to directly probe the low-energy (1–5 meV) electrodynamics of triangular lattice antiferromagnets $CuFe_{1-x}Ga_xO_2$ ($x = 0.00, 0.01$, and 0.035). We discovered an electromagnon (electric-field-active magnon) excitation at 2.3 meV in the paraelectric $\uparrow \downarrow \downarrow \downarrow$ collinear magnetic phase, while this electromagnon vanishes in the ferroelectric helimagnetic phase. Anticorrelation with noncollinear magnetism excludes the exchange-striction mechanism as the origin of dynamical magnetoelectric coupling, and hence evidences the observation of a spin-orbit coupling mediated electromagnon in the present compound.

The magnetoelectric (ME) effect, i.e., the electric (magnetic) control of magnetic (dielectric) properties, has long been an important issue in condensed matter physics [[1\]](#page-3-1). While magnetic and dielectric properties usually show minimal coupling, recent discoveries of magnetically induced ferroelectricity in frustrated magnets have enabled unprecedentedly large and versatile ME responses [\[2–](#page-3-2)[4\]](#page-3-3). Jia et al. suggested that at least three microscopic ME coupling mechanisms can be considered: When a ligand ion is placed at the center of two magnetic ions, magnetically induced local electric polarization \vec{P}_{ij} is described as

$$
\vec{P}_{ij} = \vec{\Pi} (\vec{S}_i \cdot \vec{S}_j) + A \vec{e}_{ij} \times (\vec{S}_i \times \vec{S}_j)
$$

+ B[($\vec{e}_{ij} \cdot \vec{S}_i$) $\vec{S}_i - (\vec{e}_{ij} \cdot \vec{S}_j)$ \vec{S}_j]. (1)

where A and B are coupling coefficients, Π is a vector unique to the underlying crystal structure, and \vec{e}_{ij} is a unit vector connecting two magnetic moments \vec{S}_i and \vec{S}_j , respectively [\[5](#page-3-4)]. The first term represents the exchange striction, and is considered as the origin of ferroelectricity in some collinear antiferromagnets such as $Ca₃CoMnO₆$ [[6\]](#page-3-5). The second term comes from the inverse effect of Dzyaloshinskii-Moriya (DM) interaction [[7\]](#page-3-6), which well explains the ferroelectricity in many noncollinear spiral magnets such as $RMnO₃$ [\[2](#page-3-2)[,8\]](#page-3-7) and $Ni₃V₂O₈$ [[9](#page-3-8)]. The third term arises from spin-dependent modulation of covalency (hybridization) between the metal d state and the ligand p state [\[5\]](#page-3-4), while this term usually oscillates and cancels out within the crystal. Note that the second and third terms in Eq. ([1\)](#page-0-0) rely on the spin-orbit interaction, but the first term (exchange striction) does not [[5](#page-3-4)]. With any mechanism, a modification of magnetic structure, e.g., by an external magnetic field H , leads to a significant change of induced electric polarization P.

One important consequence of such a strong ME coupling is the appearance of a novel collective excitation

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called an electromagnon (i.e., a magnon driven by an ac electric field E^{ω}) in the dynamical regime. With detailed polarization analyses of absorption spectra, the existence of electromagnon (EM) excitation has been established for ferroelectric (FE) helimagnets $R M nO₃$ [\[10,](#page-3-9)[11\]](#page-3-10), $R M n₂O₅$ [\[12\]](#page-3-11), and $Ba_2Mg_2Fe_{12}O_{22}$ [[13](#page-3-12)]. Here, the most crucial is the microscopic origin of dynamical ME coupling, which is not necessarily identical to that of the magnetically induced static P in the same compound. According to the inverse DM scheme, the EM excitation in FE helimagnets emerges as the rotational oscillation of the spin-spiral plane and the associated P vector [\[14\]](#page-3-13). While this rotational mode should be active only with E^{ω} perpendicular to the spin-spiral plane, the observed selection rule for $RMn₂O₅$ contradicted this prediction [[12](#page-3-11),[15](#page-3-14)]. For $RMnO₃$ and $Ba₂Mg₂Fe₁₂O₂₂$, the selection rules remain unchanged even after the spin-flop transition under applied H [[11](#page-3-10),[13](#page-3-12)]. The latest theoretical studies suggest that the exchange-striction mechanism can also host the EM activity in noncollinear magnets, but with the selection rule tied to the chemical lattice [[16](#page-3-15)]. Importantly, this exchangestriction-induced EM is inactive in the collinear magnetic phase, since the differential polarization $\delta P_{ij} \propto S_i \cdot \delta S_j$ always becomes zero $(S_i \perp \delta S_i)$. This latter model well reproduces the observed selection rules or absorption spectra of EM in all the three helimagnetic compounds [\[13](#page-3-12)[,15–](#page-3-14) [17](#page-3-16)], whereas the firm experimental evidence of spin-orbit coupling mediated EM excitation is still lacking.

In this Letter, we report the experimental discovery of electromagnon excitation in the paraelectric collinear magnetic $(\dagger \dagger \dagger \dagger)$ phase of triangular lattice antiferromagnets $CuFe_{1-x}Ga_xO_2$. This EM mode was found to vanish in the FE helimagnetic phase. The anticorrelation between the electromagnon and the noncollinear magnetism excludes the exchange-striction mechanism as the origin of dynamical ME coupling, and hence suggests that the observed electromagnon is electrically activated by the spinorbit coupling.

 $CuFe_{1-x}Ga_xO_2$ crystallizes into a delafossite structure with centrosymmetric space group $R\bar{3}m$ [Fig. [1\(a\)\]](#page-1-0), which consists of the stacking of triangular lattices along the c axis [\[18\]](#page-3-17). Each Fe³⁺ ($S = 5/2$) ion is surrounded by O²⁻ octahedra, and the magnetic frustration leads to several complex spin structures with propagation vector $k =$ $(q, q, 3/2)$ [[19\]](#page-3-18). For simplicity, we define the q vector (\vec{q}) as the in-plane component of the magnetic propagation vector. CuFeO₂ is characterized by the collinear $\int \int \int$ (CM4) magnetic ground state below 11 K, with commensurate $q = 0.25$ and spin direction along the c axis [Fig. [1\(e\)\]](#page-1-0) [\[20\]](#page-3-19). In a Ga-doped specimen with $x > 0.02$, the CM4 phase is replaced by a ferroelectric proper screw (NC) magnetic phase with incommensurate $q \sim 0.202$ [[21](#page-3-20)[–23\]](#page-3-21), where the spin rotates within a plane perpendicular to the q vector and P appears parallel to $\vec{q} \parallel [110]$ [Fig. [1\(d\)\]](#page-1-0) [\[24\]](#page-3-22). The ferroelectricity in the NC phase can be explained by neither exchange striction nor the inverse DM mechanism. Instead, Arima suggested that the third term in Eq. [\(1](#page-0-0)) can induce a finite $\vec{P} \parallel \vec{q}$ component on the delafossite lattice with proper screw magnetic order [[25](#page-3-23)]. This model predicts that the reversal of the P vector is coupled with the reversal of vector spin chirality (i.e., clockwise or counterclockwise manner of spin rotation), which was later

FIG. 1 (color online). (a) Crystal structure and (b) $x-T$ magnetic phase diagram at $H = 0$ for CuFe_{1-x}Ga_xO₂. (c) H-T magnetic phase diagram for the $x = 0.01$ specimen with static $H \parallel c$. Circles and squares are the data points obtained from the measurements of magnetization with T- and H-increasing runs, respectively. Open (closed) symbols represent the data points determined in this work (the previous work by Terada et al. [\[22\]](#page-3-25)). Panels (d) and (e) indicate magnetic structures of the NC (FE) and CM4 phase, respectively. Dashed square in (e) represents the magnetic unit cell in the CM4 phase. The directions of magnetic q vector and electric polarization P are also indicated.

confirmed by the polarized neutron scattering experiments [\[26\]](#page-3-24). The x -T phase diagram [[22](#page-3-25)] as well as the H -T phase diagram for the $x = 0.01$ specimen (by the present study) are summarized in Figs. $1(b)$ and $1(c)$. Note that the transition from CM4 into NC (FE) can also be induced by H applied along the c axis [[19](#page-3-18)[,21](#page-3-20)]. Starting from either of these magnetic ground states, increase of temperature (T) first induces partially disordered collinear (ICM1 or ICM2) magnetic phases [[20](#page-3-19),[27](#page-3-26)] and then produces a paramagnetic (PM) phase. All magnetic phases other than NC (FE) are paraelectric [\[21,](#page-3-20)[22\]](#page-3-25).

Single crystals of $CuFe_{1-x}Ga_xO_2$ ($x = 0.00, 0.01,$ and 0.035) were grown by a floating zone method [[18\]](#page-3-17). Magnetization was measured with a SQUID magnetometer. Complex transmittance t is obtained by terahertz timedomain spectroscopy and further converted into complex domain spectroscopy and further converted into
refractive index $n = \sqrt{\epsilon \mu}$ using the relationship

$$
t = \frac{2\mu}{n+\mu} \frac{2n}{n+\mu} \exp\left[-i\frac{\omega}{c}d(n-1)\right],
$$
 (2)

where ϵ , μ , d , ω , and c represent the complex dielectric constant, complex magnetic permeability, sample thickness, frequency of light, and velocity of light, respectively. To numerically solve Eq. [\(2](#page-1-1)), we make the preexponential factor approximate $4n/(n + 1)^2$ by assuming $\mu \approx 1$ unless otherwise noted. The experimental detail is described in the supplementary material [[28](#page-3-27)] and Ref. [\[11](#page-3-10)].

We first investigated the low-energy electrodynamics in the paraelectric CM4 collinear magnetic phase. Note that symmetry of triangular lattice allows the existence of three equivalent $\vec{q} \parallel \langle 110 \rangle$. The spectra observed in the present study reflect the contributions from all the three q domains. Figures [2\(a\)](#page-1-2) and [2\(b\)](#page-1-2) indicate the real and imaginary parts of $\epsilon \mu$ spectra (Re[$\epsilon \mu$] and Im[$\epsilon \mu$]) with various polarization configurations for the $x = 0.01$ specimen at 4.4 K,

FIG. 2 (color online). Real and imaginary parts of $\epsilon \mu$ spectra $(Re[\epsilon \mu]$ and Im $[\epsilon \mu]$) for the $x = 0.01$ specimen measured at 4.4 K with various light-polarization configurations.

respectively. With $E^{\omega} \parallel [110]$ and $H^{\omega} \parallel [1\bar{1}0]$, two resonance modes are observed at 1.2 and 2.3 meV. Only the former one survives for $E^{\omega} \parallel [001]$ and $H^{\omega} \parallel [1\bar{1}0],$ whereas only the latter one survives for E^{ω} || [110] and H^{ω} || [001]. These results reveal that the excitation at 2.3 meV is an EM mode driven by E^{ω} || [110], while the one at 1.2 meV is a conventional magnon mode driven by H^{ω} || [1 $\overline{1}0$].

In the following, we focus on the behavior with the E^{ω} || [110] and H^{ω} || [110] configuration. To further analyze the aforementioned $\epsilon \mu$ spectrum, the corresponding absorption coefficient α (= -2(ln|t|)/d) and the decomposed ϵ and μ spectra are plotted in Figs. [3\(a\)](#page-2-0)–[3\(c\)](#page-2-0), respectively. To separate the ϵ and μ contributions to the $\epsilon \mu$ spectrum, we first assumed $\mu = 1$ for $\hbar \omega > 2.0$ meV. The obtained ϵ spectrum can be fitted well with the sum of two Lorentzian functions; a higher-frequency mode represents the lowest-lying optical phonon to give rise to the tail absorption observed below 5 meV. By substituting this ϵ -fitting function into Eq. [\(2\)](#page-1-1), the μ spectrum is deduced for $\hbar \omega$ < 2.0 meV. It can be fitted as well with a single Lorentzian function.

In Fig. [4\(b\),](#page-2-1) we show the T dependence of the Im $[\epsilon \mu]$ spectrum for the $x = 0.01$ specimen. An increase of temperature leads to broadening of two resonance peaks, and they become almost undiscernible in the ICM1 magnetic phase above 10 K. ICM1 and ICM2 are partially disordered

FIG. 3 (color online). (a)–(c) Absorption coefficient α , real and imaginary part of ϵ and μ spectra for the $x = 0.01$ specimen at 4.4 K with E^{ω} || [110] and H^{ω} || [110]. Solid lines in (b) and (c) represent the fits with the sum of Lorentzian functions. (d) Spin structure of the CM4 magnetic ground state. Panels (e) and (f) indicate the possible excitation modes corresponding to the observed genuine magnon (AFMR) and electromagnon (EM), respectively. In (f), S_1 and S_3 rotate to the opposite direction of S_2 and S_4 within a plane perpendicular to \vec{q} . (g) Spin-wave (magnon) dispersion of CuFeO₂ along the $(h, h, 0)$ direction as suggested in Ref. [\[30\]](#page-3-29).

magnetic phases [\[20](#page-3-19)[,27\]](#page-3-26), and may lose the spin correlation enough for magnons or EM excitations to be observed. The undoped $x = 0.00$ specimen also has two resonance modes at the same frequency in the CM4 magnetic ground state [Fig. [4\(a\)](#page-2-1)], and shows a similar T dependence of the Im[$\epsilon \mu$] spectrum as observed for the $x = 0.01$ specimen. In contrast, the $x = 0.035$ specimen with the NC (FE) ground state shows no discernible peak structure in the whole temperature range, neither for $E \parallel [110]$ and $H \parallel [1\bar{1}0]$ [Fig. [4\(c\)](#page-2-1)] nor for $E \parallel [001]$ and $H \parallel [1\bar{1}0]$ (not shown). To summarize, the EM excitation driven by E^{ω} || [110] is active only in the paraelectric collinear CM4 magnetic phase, not in the ferroelectric NC helimagnetic phase.

Next, we discuss the microscopic origin of these excitations. The spin-wave (SW) dispersion for $CuFeO₂$ has been investigated by a previous inelastic neutron diffraction study [[29](#page-3-28)], and the analysis clarified the existence of two SW branches as reproduced in Fig. [3\(g\)](#page-2-0) [\[30\]](#page-3-29). In general, an antiferromagnetic resonance (AFMR) appears as the excitation of the zone-center mode at $k = 0$ by H^{ω} perpendicular to the collinear spin direction [Fig. [3\(e\)\]](#page-2-0). From this criterion, we concluded that the excitation at 1.2 meV driven by H^{ω} || [110] is AFMR on the lower SW branch. In contrast, the excitation energy of the observed EM (\sim 2.3 meV) agrees with that of the zone-center mode on the upper SW branch.

FIG. 4 (color online). T dependence of $\text{Im}[\epsilon \mu]$ spectra measured with $E^{\omega} \parallel [110]$ and $H^{\omega} \parallel [1\bar{1}0]$ for (a) $x = 0.00$, (b) $x = 0.01$, and (c) $x = 0.035$ specimens, respectively. (d) Im[ϵ] spectra for the $x = 0.01$ specimen measured at 6 K with E^{ω} || [110] and H^{ω} || [001] in various magnitudes of static H (H^{dc}) applied along the [001] direction. H dependence of observed EM peak positions (circle), as well as the development of resonance modes previously reported by the ESR study for the $x = 0.00$ specimen [\[32\]](#page-3-30) (square), are plotted in (e).

So far, the most successful scheme to explain the dynamical ME coupling is the exchange striction. However, this mechanism is inactive in the collinear spin system like the present CM4 phase, since the relationship $\delta P_{ij} \propto$ $S_i \cdot \delta S_j = 0$ always holds [\[16,](#page-3-15)[17\]](#page-3-16). This strongly suggests the relevance of spin-orbit coupling to the present EM mode; the relatively weak peak intensity in the $\text{Im}[\epsilon]$ spectrum (1 order of magnitude smaller than that of $DyMnO₃$ [\[11\]](#page-3-10)) also supports this scenario. Since the static P in NC (FE) is induced by the proper screw magnetic order through the spin-orbit-interaction mediated modulation of Fe $3d$ –O 2p hybridization [\[5](#page-3-4),[25](#page-3-23)], we may anticipate the analogous origin for the presently observed dynamical ME coupling in CM4. For example, the magnetic excitation as depicted in Fig. $3(f)$ can dynamically generate a proper-screw-like spin texture with a finite spin chirality, which is expected to induce a nonzero electric dipole along the $\delta P \parallel q \parallel [110]$ direction. This mode should be active only with E^{ω} || [110], which is consistent with the experimental results. The disappearance of the EM mode in the NC (FE) phase may reflect the alteration of magnetic symmetry or Brillouin-zone folding.

We further investigated the development of the EM mode in static H applied along the [001] direction. Fig-ure [4\(d\)](#page-2-1) indicates the H dependence of the $\text{Im}[\epsilon]$ spectrum measured at 6 K for the $x = 0.01$ specimen with E^{ω} || [110] and H^{ω} || [001], where only the EM excitation can be observed. As H increases, the EM mode is found to split linearly with H and form two peak structures. This reflects the H-linear splitting of SW branches, which is generally expected for collinear antiferromagnets with H applied parallel to the magnetic easy axis. Since the spectral shape of the two-magnon excitation should be independent of H [\[31\]](#page-3-31), this ensures that the present EM mode is excited by the one-magnon process. The observed evolution of EM peak positions under applied H is summarized in Fig. $4(e)$. Note that similar H dependence of resonance modes has been reported by Fukuda et al. from the ESR study for the $x = 0.00$ specimen [\[32\]](#page-3-30), while they conventionally assigned these modes to AFMR driven by H^{ω} . The peak structure observed in the $\text{Im}[\epsilon]$ spectrum becomes almost invisible after the transition from CM4 into NC (FE) at 6.3 T, which confirms the inactivity of the EM mode in the latter NC phase.

In conclusion, we have experimentally revealed the electromagnon excitation in the paraelectric \prod collinear magnetic phase of triangular lattice antiferromagnet $CuFe_{1-x}Ga_xO_2$. This mode was found to vanish in the ferroelectric helimagnetic phase. These facts prove that neither ferroelectricity nor noncollinear magnetism is a necessary condition for the appearance of electromagnon excitation, while the existing theories on electromagnon have focused on noncollinear magnets like helimagnets. The anticorrelation between the noncollinear magnetism and the emergence of electromagnon excludes the exchange-striction mechanism as the origin of dynamical ME coupling: The electric activity of the magnon in this compound is ascribed to the modulation of the p-d hybridization at the spin-twisted excited state via the spin-orbit interaction. Our discovery suggests that similar electromagnon modes will be observable in a wide range of paraelectric collinear magnets.

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