

Bacterial Chromosomal Loci Move Subdiffusively through a Viscoelastic Cytoplasm

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Tracking of fluorescently labeled chromosomal loci in live bacterial cells reveals a robust scaling of the mean square displacement (MSD) as $\tau^{0.39}$. We propose that the observed motion arises from relaxation of the Rouse modes of the DNA polymer within the viscoelastic environment of the cytoplasm. The time-averaged and ensemble-averaged MSD of chromosomal loci exhibit ergodicity, and the velocity autocorrelation function is negative at short time lags. These observations are most consistent with fractional Langevin motion and rule out a continuous time random walk model as an explanation for anomalous motion *in vivo*.

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Subdiffusive motion, for which the mean square displacement [MSD, $\langle(\vec{R}(t+\tau) - \vec{R}(t))^2\rangle$] scales as τ^α , where $0 < \alpha < 1$ [1], has been observed *in vivo* for a variety of tracer particles in both prokaryotes [2] and eukaryotes [3]. *In vitro*, particles moving in actin networks [4] and crowded dextran solutions [5] exhibit scaling laws with $\alpha \approx 0.75$, which closely agree with most *in vivo* measurements. These experiments demonstrate that crowding, especially in combination with elastic elements, is sufficient to give rise to subdiffusive motion. However, the underlying mechanism(s) for subdiffusive motion *in vivo* is still unknown.

There are three prominent physical models for subdiffusion of particles in cells, each corresponding to a distinct potential cellular mechanism. First is the continuous time random walk (CTRW) [6]. If a particle diffusing through the cytoplasm encounters a binding partner, then it will pause for a period of time before dissociating and diffusing away. Multiple binding events with a range of rate constants generate long tails in the waiting time distribution, leading to subdiffusive behavior [7]. Broad distributions in waiting time (or jump length) are a hallmark of the CTRW. Second, cytoskeletal networks impose obstacles around which diffusing particles must navigate. If the obstacle concentration is high enough, obstructed diffusion (OD) becomes subdiffusive [8]. Third, macromolecular crowding and the presence of elastic elements, such as nucleic acids and cytoskeletal filaments, give the cytoplasm viscoelastic properties. As a particle moves through this medium, the cytoplasm “pushes back”, creating long-time correlations in the particle’s trajectory. This memory leads to subdiffusive behavior that can be modeled by fractional Langevin motion (FLM) [9].

Despite their distinct molecular origins for subdiffusive motion in the cell, CTRW, OD, and FLM generate similar

scaling laws for long-time, ensemble-averaged behavior. Thus, other measures, such as ergodicity, are needed to distinguish among these models [9–11].

In this Letter, we use fluorescently labeled chromosomal loci and RNA-protein particles as probes to explore the mechanisms underlying subdiffusive motion in live *E. coli* cells. We find that both polymer and particle trajectories are ergodic, with negative velocity autocorrelations at short time lags. These results allow us to rule out a CTRW mechanism in favor of FLM. Our analytical results for a generalized FLM Rouse model [12] exhibit a monomer MSD that has an intermediate time scaling that is one-half that of an isolated particle in the same medium, which is consistent with our experimental observations. Thus, the dynamic behavior of both chromosomal loci and RNA-protein particles within living bacterial cells can be explained by the physical properties of their viscoelastic environment.

We use time-lapse fluorescence microscopy to follow the movement of chromosomal loci, specific DNA segments on the chromosome visualized with the GFP-ParB/*parS* detection system [13], over time periods ranging from 1 to 10^3 s. Unlike the rapid, directed motion seen during chromosome segregation [13], loci appear to jiggle in place between segregation events [Fig. 1(a) and 1(b)], as observed in both *Vibrio cholerae* [14] and *E. coli* [15].

To analyze this motion, we calculate the ensemble-averaged MSD as a function of time interval τ and find a surprisingly robust scaling law across three decades of time, such that $\text{MSD} \sim \tau^{0.39 \pm 0.04}$ [Fig. 1(c)]. Measurements of locus position over time in cells fixed with formaldehyde give an estimate of $\sim 0.027 \mu\text{m}$ for our measurement precision [Fig. 1(c)]. Furthermore, analysis of simulated data with a range of signal-to-noise ratios

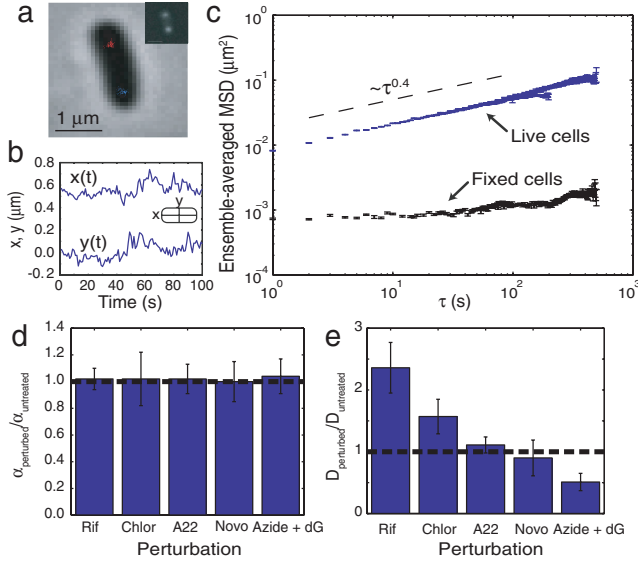


FIG. 1 (color). (a) Phase-contrast image overlaid with positions of two 84' loci tracked for 100 frames; inset shows fluorescence image of same cell. (b) Temporal trajectories along the cell's long (x) and short (y) axes for the lower (blue) locus in panel (a). (c) Ensemble-averaged MSD for live and fixed cells. Error bars are the standard error of the mean. (d),(e) Histograms displaying the fold-change in α and D_{app} upon biological perturbations [rifampin (Rif), chloramphenicol (Chlor), S-(3,4-dichlorobenzyl)isothiourea (A22), novobiocin (Novo), sodium azide and deoxyglucose (Azide + dG)].

confirms that the observed magnitude of motion is much greater than can be accounted for by experimental uncertainty (see the supplementary information [16], Figure 1). The same scaling law is observed for six loci distributed around the *E. coli* chromosome, for four loci around the *Caulobacter crescentus* chromosome (using a different detection system), and for a locus on the *E. coli* RK2 plasmid (Table I). In contrast, RNA molecules containing tandem hairpins bound by MS2-GFP [2] tracked by the same method gives the distinct scaling $MSD \sim \tau^{0.71 \pm 0.10}$ (Table I). Biological perturbations such as treatment with antibiotic drugs that inhibit transcription (rifampin), translation (chloramphenicol), polymerization of the cytoskeletal protein MreB (A22), DNA gyrase (novobiocin) and ATP synthesis (sodium azide and 2-deoxyglucose) have no effect on α [Fig. 1(d)], though they significantly change the magnitude of the apparent diffusion coefficient at $\tau = 1$ s D_{app} , where $MSD = 4D_{app}\tau^\alpha$ [Fig. 1(e)]. The robustness of α suggests that it arises from a physical, rather than biological, phenomenon. Moreover, the discrepancy with subdiffusive scaling exponents observed for particles *in vivo* (0.39 for chromosomal loci versus 0.71 for RNA-protein particles) is likely due to the additional physical forces experienced by a locus (monomer) embedded within a DNA polymer.

The motion of a monomer in a polymer depends not only on its environment but also on the movement of neighbor-

TABLE I. Mean \pm standard deviation of α for ensemble-averaged MSD measured for loci at multiple positions around the chromosome of two bacterial species and an extrachromosomal plasmid, as well as an RNA-protein particle.

Species	Locus	α	# loci	# data sets
<i>E. coli</i>	84'	0.39 ± 0.04	16 739	32
<i>E. coli</i>	21'	0.35 ± 0.02	4906	7
<i>E. coli</i>	34'	0.43 ± 0.05	1416	3
<i>E. coli</i>	54'	0.44 ± 0.06	2588	3
<i>E. coli</i>	79'	0.38 ± 0.05	1783	3
<i>E. coli</i>	92'	0.38 ± 0.05	2225	3
<i>Caulobacter</i>	<i>ori</i>	0.38 ± 0.04	2314	4
<i>Caulobacter</i>	<i>pilA</i>	0.39 ± 0.07	2612	4
<i>Caulobacter</i>	<i>pleC</i>	0.38 ± 0.04	3118	4
<i>Caulobacter</i>	<i>podJ</i>	0.37 ± 0.10	2925	4
<i>E. coli</i>	RK2	0.40 ± 0.03	709	2
<i>E. coli</i>	RNA-MS2	0.71 ± 0.10	323	2

ing monomers. Rouse describes the elastic coupling between monomers in a polymer and predicts a monomer scaling of 0.5 for time scales less than the longest relaxation time of the polymer τ_R [17,18]. For crowded melts, de Gennes's reptation theory predicts a monomer scaling of 0.25 due to the topological constraints of entangled polymers combined with the Rouse modes [18,19]. The Zimm model accounts for hydrodynamic interactions, which increase the monomer scaling to 0.67 [20]. However, the degree of crowding *in vivo* is assumed to screen out hydrodynamic effects over the relevant length and time scales [18], so we do not consider hydrodynamic interactions in our present treatment. The *E. coli* chromosome is a circular polymer confined within a cell that is orders of magnitude smaller than its unconfined radius of gyration. Since these properties differ from the assumptions made in the Rouse and reptation models, we have used Brownian dynamics simulations to determine what physical forces are relevant for our system. The simulations, described in an accompanying paper [12], gave a monomer scaling of 0.5, regardless of contour length, chain topology (linear versus circular), self-interaction strength, and degree of confinement. This indicated that the elastic Rouse modes must dominate monomer behavior for strongly confined polymers. These simulation results also demonstrated that our experimental observations of chromosomal loci are more subdiffusive than can be accounted for by polymer theory.

The classic Rouse model assumes that the medium surrounding a polymer is purely viscous. However, this is not the case *in vivo*. Macromolecular crowding and the presence of semiflexible polymers cause the cytoplasm to behave as a viscoelastic medium [4,21,22]. To determine how viscoelasticity affects Rouse's prediction, we introduced a FLM memory kernel into the Rouse framework and derived an analytical expression for the MSD of a monomer embedded in a polymer chain [12]. The analyti-

cal result gives two scaling regimes: $\langle(\vec{R}(t) - \vec{R}(0))^2\rangle \sim b(\frac{k_B T}{\xi})^{1/2} t^{\alpha/2}$ for $t \ll \tau_R$, and $\langle(\vec{R}(t) - \vec{R}(0))^2\rangle \sim b(\frac{k_B T}{N\xi}) t^\alpha$ for $t \gg \tau_R$, where b is the Kuhn length, $k_B T$ is thermal energy, ξ is the drag coefficient, and N is the number of monomers in the chain. Our analytical result provides the general observation that the monomer MSD is expected to scale as one-half of the particle's MSD scaling in the same medium for $t \ll \tau_R$. Indeed, for a viscous medium with no memory ($\alpha = 1$ for a particle), we recover Rouse's original prediction. However, if we set $\alpha = 0.70$, as is observed for RNA-protein particles in the cytoplasm [2] (Table I), then our theory gives a monomer MSD scaling of 0.35. Thus, we would expect a locus on the chromosome to move with a scaling of ~ 0.35 *in vivo*.

While our analytical result for the MSD scaling is consistent with our experiments, other possible mechanisms for subdiffusion, such as binding interactions or spatial obstacles, must also be considered. To identify the underlying mechanism of subdiffusion *in vivo*, we calculate the time-averaged MSD for individual chromosomal loci. The scaling for the time-averaged MSD is 0.41 ± 0.17 [Fig. 2(a) and 2(b)], which is the same as that found for the ensemble-averaged MSD [Fig. 1(c), Table I]. This agreement indicates an underlying ergodic process like OD or FLM, but not CTRW [9,10]. RNA-protein particles also exhibit ergodicity, though with an α almost twice as large, where the time-averaged MSD scales as 0.69 ± 0.20 (see also Ref. [2]). Furthermore, the broad distribution of D_{app} as measured for individual loci over time does not necessarily indicate a CTRW, as has been suggested [10,23]. Rather, we propose an alternative explanation, namely, that this distribution is expected from trajectories of finite length [24]. Indeed, our experimental distribution falls just below the distribution for simulated trajectories of 100 time steps [Fig. 2(c), [16]]. Since our movies are 100 frames long, and not all trajectories are complete (due to photobleaching and focus drift), this suggests that the

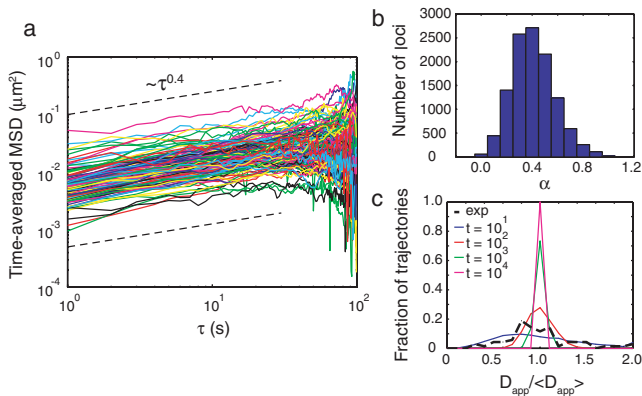


FIG. 2 (color). (a) Time-averaged MSD for 124 loci from a single movie. (b) Histogram of α for 11580 loci from 29 data sets. (c) Distributions of $D_{\text{app}}/\langle D_{\text{app}} \rangle$ for experimental data shown in (a) (black dashed curves) and simulated trajectories over finite time steps t (colored solid curves).

spread in the data is due to the finite measurement rather than a nonstationary process such as CTRW.

To further distinguish between subdiffusion models, we calculate the velocity autocorrelation function $C_v^{(\delta)}(\tau) = \langle v(t+\tau) \cdot v(t) \rangle$, where $v(t) = \frac{1}{\delta}[r(t+\delta) - r(t)]$ and $\delta = 1$ s, for both a monomer (chromosomal loci) and a particle (RNA-protein particles). Both probes have a negative autocorrelation at short time lags (Fig. 3), indicating a tendency to move back to a previous position. This antipersistent behavior at short time scales is characteristic of a viscoelastic environment. CTRW and OD, in contrast, produce random, uncorrelated trajectories. Since the RNA-protein particles exhibit a negative autocorrelation, this result supports an underlying FLM mechanism and rules out both CTRW and OD. The intrinsic elasticity of the DNA polymer may also contribute to the negative velocity autocorrelation for chromosomal loci, resulting in a larger negative autocorrelation for the chromosomal loci than for the RNA-protein particles.

Using our analytical results for a FLM polymer [12], the velocity autocorrelation function of a discrete process with time step δ is given by

$$C_v^{(\delta)}(t) = \frac{1}{\delta^2} \langle (\vec{R}(t+\delta) - \vec{R}(t)) \cdot (\vec{R}(\delta) - \vec{R}(0)) \rangle$$

$$= \begin{cases} \frac{C_v(\tau)}{\eta^2 \alpha (1-\alpha)} [2 - (1-\eta)^\alpha - (1+\eta)^\alpha], & \tau \geq \delta \\ \frac{C_v(\tau)}{\eta^2 \alpha (1-\alpha)} [2 + (\eta-1)^\alpha - (\eta+1)^\alpha] + \\ \frac{3k_B T}{\xi} \frac{\sin(\alpha\pi)}{\pi(1-\alpha/2)(1-\alpha)} \frac{1}{\delta^2} (\delta-t)^\alpha, & \tau < \delta \end{cases} \quad (1)$$

where $C_v(\tau) = -\frac{3k_B T}{\xi} \frac{\sin(\alpha\pi)}{\pi(2-\alpha)} |\tau|^{\alpha-2}$ [limit of $C_v^{(\delta)}(\tau)$ as $\delta \rightarrow 0$] and $\eta = \delta/\tau$ [12]. This theoretical prediction is plotted in Fig. 3 with the experimentally measured values of α and no additional fitting parameters, showing excellent agreement with the data.

Finally, we return to Brownian dynamics simulations to confirm that FLM, and not CTRW, can produce results consistent with our experiments (see [16]). When mono-

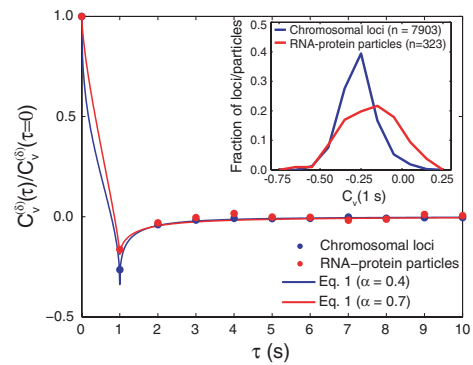


FIG. 3 (color). Velocity autocorrelation function $C_v^{(\delta)}(t)$ for chromosomal loci and RNA-protein particles. Points are experimental data, and lines are our theoretical predictions [Eq. (1)]. (Inset) Histogram of autocorrelation values at $\tau = 1$ s for 7903 chromosomal loci and 323 RNA-protein particles.

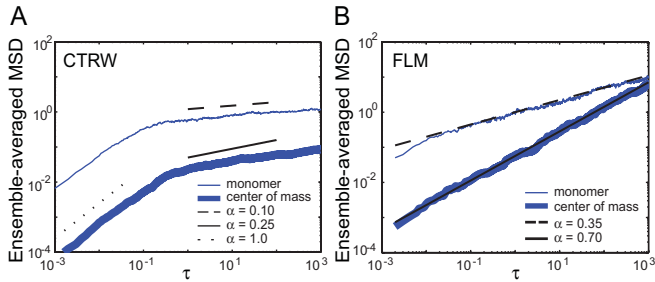


FIG. 4 (color). Polymer simulations with subdiffusive monomers showing the MSD of a monomer and the center of mass for CTRW (a) and FLM (b) models (see [16] for parameter values). Data are the ensemble average of 100 simulations. Black lines in (a) are scaling guides; in (b), they give our analytical solutions from Ref. [12].

mers in a polymer undergo a CTRW, as described in Ref. [12], the resulting behavior is more subdiffusive than seen in experiments [Fig. 4(a)]. For example, a particle with an α value of 0.7 scales as ~ 0.10 when embedded in a polymer. In contrast, polymers whose monomers move according to FLM exhibit scalings consistent with our experimental observations [Fig. 4(b)]. The center of mass, which behaves like a large particle [12], moves subdiffusively with the same input scaling α , while the monomer MSD scales as $\alpha/2$. These simulations agree with both our experimental and analytical results.

Our results provide strong evidence for a FLM mechanism for subdiffusive motion *in vivo*. This conclusion confirms the viscoelastic nature of the cytoplasm, which has dramatic consequences for molecular transport. Specifically, subdiffusive molecules take longer than expected to reach distant targets, but they are also more likely to retrace local regions of space than a freely diffusing particle. Furthermore, our results demonstrate that the robust scaling laws observed for macromolecules *in vivo* can arise from physical principles, rather than tightly regulated biological processes.

Recently, Szymanski and Weiss used fluorescence correlation spectroscopy (FCS) and simulations to show that a stationary propagator drives crowding-induced subdiffusion [25]. In contrast to FCS, our particle-tracking method provides trajectories of individual particles or loci. This additional information enables us to make a clearer distinction between possible subdiffusive mechanisms. In particular, the velocity autocorrelation function is a key diagnostic measure, as it offers an unambiguous test for viscoelasticity.

Our results also have implications for chromosome organization and dynamics. The monomer MSD scaling of fluorescently tagged genetic loci seems to be universal: we have observed $\alpha \approx 0.4$ in three bacterial species (Table I) [14], and the same behavior is found in budding yeast [26] and human cells [23]. The scaling is independent of both genomic and cellular position, as well as transcriptional

state. This invariance is consistent with a viscoelastic mechanism, which will permeate the entire cell, whereas binding sites and cytoskeletal networks may not be uniformly distributed. This subdiffusive motion may contribute to the maintenance of chromosome territories [27] in both prokaryotes and eukaryotes.

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- [1] J.P. Bouchaud and A. Georges, *Phys. Rep.* **195**, 127 (1990).
 - [2] I. Golding and E.C. Cox, *Phys. Rev. Lett.* **96**, 098102 (2006).
 - [3] I.M. Tolic-Nørrelykke *et al.*, *Phys. Rev. Lett.* **93**, 078102 (2004).
 - [4] F. Gittes *et al.*, *Phys. Rev. Lett.* **79**, 3286 (1997).
 - [5] D.S. Banks and C. Fradin, *Biophys. J.* **89**, 2960 (2005).
 - [6] E.W. Montroll and G.H. Weiss, *J. Math. Phys. (N.Y.)* **6**, 167 (1965).
 - [7] M.J. Saxton, *Biophys. J.* **70**, 1250 (1996).
 - [8] M.J. Saxton, *Biophys. J.* **66**, 394 (1994).
 - [9] W.H. Deng and E. Barkai, *Phys. Rev. E* **79**, 011112 (2009).
 - [10] Y. He *et al.*, *Phys. Rev. Lett.* **101**, 058101 (2008).
 - [11] R. Metzler *et al.*, *Acta Phys. Pol. B* **40**, 1315 (2009).
 - [12] S.C. Weber, J.A. Theriot, and A.J. Spakowitz (to be published).
 - [13] H.J. Nielsen *et al.*, *Mol. Microbiol.* **61**, 383 (2006).
 - [14] A. Fiebig, K. Keren, and J.A. Theriot, *Mol. Microbiol.* **60**, 1164 (2006).
 - [15] O. Espeli, R. Mercier, and F. Boccard, *Mol. Microbiol.* **68**, 1418 (2008).
 - [16] See supplementary information at <http://link.aps.org/supplemental/10.1103/PhysRevLett.104.238102>.
 - [17] P.E. Rouse, *J. Chem. Phys.* **21**, 1272 (1953).
 - [18] M. Doi and S.F. Edwards, *The Theory of Polymer Dynamics* (Oxford University Press, Oxford, 1986).
 - [19] P.G. de Gennes, *J. Chem. Phys.* **55**, 572 (1971).
 - [20] B.H. Zimm, *J. Chem. Phys.* **24**, 269 (1956).
 - [21] W. Pan *et al.*, *Phys. Rev. Lett.* **102**, 058101 (2009).
 - [22] D. Wirtz, *Annu. Rev. Biophys.* **38**, 301 (2009).
 - [23] I. Bronstein *et al.*, *Phys. Rev. Lett.* **103**, 018102 (2009).
 - [24] M.J. Saxton, *Biophys. J.* **72**, 1744 (1997).
 - [25] J. Szymanski and M. Weiss, *Phys. Rev. Lett.* **103**, 038102 (2009).
 - [26] G.G. Cabal *et al.*, *Nature (London)* **441**, 770 (2006).
 - [27] T. Cremer *et al.*, *Curr. Opin. Cell Biol.* **18**, 307 (2006).