## Observation of  $B_s^0 \to D_s^{*-} \pi^+$  and  $B_s^0 \to D_s^{(*)-} \rho^+$  and Measurement<br>of the  $B^0 \to D^{*-} \rho^+$  Longitudinal Polarization Fraction of the  $B_s^0 \to D_s^{*-} \rho^+$  Longitudinal Polarization Fraction

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First observations of the  $B_s^0 \to D_s^* - \pi^+$ ,  $B_s^0 \to D_s^- \rho^+$  and  $B_s^0 \to D_s^* - \rho^+$  decays are reported together<br>the measurements of their propositions fractions:  $\mathcal{R}(B_s \to D_s^* - \pi^+) = [2 A + 0.5(\text{stat}) + 0.3(\text{syst}) +$ with measurements of their branching fractions:  $\mathcal{B}(B_s^0 \to D_s^* - \pi^+) = [2.4^{+0.5}_{-0.4} \text{ (stat)} \pm 0.3 \text{ (syst)} \pm 0.4 \text{ (s.t. 1)} \times 10^{-3}$  and  $\mathcal{B}(B_s^0 \to D_s^* - \pi^+) = [8.5^{+1.3} \text{ (stat)} \pm 1.1 \text{ (syst)} \pm 1.3 \text{ (s.t. 1)} \times 10^{-3}$  and  $\mathcal$  $[0.4(f_s)] \times 10^{-3}$ ,  $(0.4(f_s)) \times 10^{-3}$ ,  $\mathcal{B}(B_s^0 \to D_s^- \rho^+) = [8.5^{+1.3}_{-1.2}(stat) \pm 1.1(syst) \pm 1.3(f_s)] \times 10^{-3}$  and  $\mathcal{B}(B_s^0 \to D_s^* \to \rho^+) = [11.9^{+2.2}_{-2.0}(stat) \pm 1.7(syst) \pm 1.8(f_s)] \times 10^{-3}$   $(f_s = N_{B_s^{(*)}, \bar{B}_s^{(*)}}/N_{b\bar{b}})$ . From helicity-angle distri-<br>b  $s_s^0 \rightarrow D_s^- \rho^+$  =  $[8.5^{+1.3}_{+1.2}$ (stat)  $\pm 1.1$ (syst)  $\pm 1.3$ ( $f_s$ )]  $\times 10^{-3}$ <br>  $s + 1.7$ (syst)  $\pm 1.8$ ( $f_s$ )]  $\times 10^{-3}$  ( $f_s = N_s$  (see ) $N_s$ ). From butions, we measured the longitudinal polarization fraction in  $\hat{B}_0^{\delta^s} \to D_s^* - \rho^+$  decays to be  $f_L(B_s^0$ <br> $D_s^* - \sigma^+ ) = 1.05 \pm 0.08 \text{(stat)} + 0.03 \text{(sust)}$ . These results are based on a 23.6 fb<sup>-1</sup> data sample collected at butions, we measured the longitudinal polarization fraction in  $B_s^0 \to D_s^+ \rho^+$  decays to be  $f_L(B_s^0 \to D_s^* \rho^+) = 1.05^{+0.08}_{-0.01} \text{(stat)}^{+0.03}_{-0.04} \text{(syst)}$ . These results are based on a 23.6 fb<sup>-1</sup> data sample collected at  $Y(5S)$  resonance with the Belle detector at the KEKB  $e^+e^-$  collider.

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The measurement of exclusive  $B_s^0 \to D_s^{(*)-} h^+$  [[1](#page-5-0)]  $(h^+ =$ <br> $\frac{1}{2}$  or  $a^+$ ) decays is an important milestone in the study of  $\pi^+$  or  $\rho^+$ ) decays is an important milestone in the study of the poorly known decay processes of the  $B_s^0$  meson. In Refs. [\[2](#page-5-1)[–5\]](#page-5-2) Belle confirmed the large potential of B factories for  $B_s^0$  investigations due to the low multiplicities of charged and neutral particles and high reconstruction efficiencies. We have now observed three new exclusive  $B_s^0$ modes with relatively large branching fractions and neutral particles such as photons or  $\pi^{0}$ 's in their final states. The leading amplitude for the four  $B_s^0 \rightarrow D_s^{(*)-} \pi^+$  and  $B_s^0$ <br> $D_s^{(*)-} \rightarrow +$  modes is a h state discreps of order  $\lambda^2$  (in leading amplitude for the four  $B_s^0 \to D_s^{\gamma}$  and  $B_s^0 \to D_s^{(*)-} \rho^+$  modes is a  $b \to c$  tree diagram of order  $\lambda^2$  (in the Wolfenstein parameterization [6] of the CKM quark-Wolfenstein parameterization [[6\]](#page-5-3) of the CKM quarkmixing matrix [\[7](#page-5-4)]) with a spectator s quark. The study of  $B_s^0$  decays provides useful tests of the heavy-quark theories that predict, based on an  $SU(3)$  symmetry, similarities between  $B_s^0$ -meson decay modes and their corresponding  $B<sup>0</sup>$ -meson counterparts. These include the unitarized quark model [[8\]](#page-5-5), the heavy-quark effective theory (HQET) [[9–](#page-5-6) [12](#page-5-7)], and a more recent approach based on chiral symmetry [\[13\]](#page-5-8). Our  $B_s^0$  branching fraction results can be used to normalize measurements of  $B_s^0$  decays made at hadron collider experiments, where the number of  $B_s^0$  mesons produced has a substantial systematic uncertainty.

The decay  $B_s^0 \rightarrow D_s^{*-} h^+$  is mediated by the same tree<br>orgam as  $B^0 \rightarrow D^{*-} h^+$  but with a spectator squark. The diagram as  $B^0 \rightarrow D^{*-} h^+$ , but with a spectator *s* quark. The contribution of the strongly suppressed W-exchange diacontribution of the strongly suppressed W-exchange diagram is expected to be negligibly small. Moreover, the helicity amplitudes in  $B \to VV$  decays can be used to test the factorization hypothesis [[12](#page-5-7),[14](#page-5-9)]. The relative strengths of the longitudinal and transverse states can be measured with an angular analysis of the decay products. In the helicity basis, the expected  $B_s^0 \to D_s^{*-} \rho^+$  differen-

tial decay width is  
\n
$$
\frac{d^2\Gamma(B_s^0 \to D_s^{*-} \rho^+)}{d\cos\theta_{D_s^{*-}} d\cos\theta_{\rho^+}} \propto 4f_L \sin^2\theta_{D_s^{*-}} \cos^2\theta_{\rho^+}
$$

$$
\frac{d\cos\theta_{D_s^*} - d\cos\theta_{\rho^+}}{d\cos\theta_{D_s^*}} \propto 4J_L \sin\theta_{D_s^*} \cos\theta_{\rho^+} + (1 - f_L)(1 + \cos^2\theta_{D_s^*}) \sin^2\theta_{\rho^+},
$$
\n(1)

where  $f_L = |H_0|^2 / \sum_{\lambda} |H_{\lambda}|^2$  is the longitudinal polariza-<br>tion fraction  $H_{\lambda}$  ( $\lambda = \pm 1$ ) are the helicity amplitudes tion fraction,  $H_{\lambda}$  ( $\lambda = \pm 1$ , 0) are the helicity amplitudes, and  $\theta_{D_s^{*-}}(\theta_{\rho^+})$  is the helicity angle of the  $D_s^{*-}(\rho^+)$  defined as the supplement of the angle between the  $B_s^0$  and the  $D_s^ (\pi^+)$  momenta in the  $D_s^{*-}(\rho^+)$  frame.

Here we report measurements performed with fully reconstructed  $B_s^0 \to D_s^* - \pi^+$ ,  $B_s^0 \to D_s^- \rho^+$  and  $B_s^0 \to D_s^* - \rho^+$  decays in a data set corresponding to an integrated  $D_s^{*-} \rho^+$  decays in a data set corresponding to an integrated luminosity of  $L_{int} = (23.6 \pm 0.3)$  fb<sup>-1</sup> collected with the Relle detector at the KEKR asymmetric-energy (3.6 GeV) Belle detector at the KEKB asymmetric-energy (3.6 GeV on 8.2 GeV)  $e^+e^-$  collider [\[15\]](#page-5-10) operated at the  $\Upsilon(5S)$ <br>resonance  $\sqrt{s} = (10867.0 + 1.0)$  MeV [51]. The total  $b\bar{b}$ resonance  $[\sqrt{s} = (10867.0 \pm 1.0) \text{ MeV [5]}]$  $[\sqrt{s} = (10867.0 \pm 1.0) \text{ MeV [5]}]$  $[\sqrt{s} = (10867.0 \pm 1.0) \text{ MeV [5]}]$ . The total  $b\overline{b}$ <br>cross section at the  $Y(5S)$  energy has been measured to be cross section at the  $Y(5S)$  energy has been measured to be<br> $\sigma^{Y(5S)} = (0.302 \pm 0.014)$  pb [2,16]. Three  $P^0$  production  $\sigma_{b\bar{b}}^{Y(5S)} = (0.302 \pm 0.014)$  $\sigma_{b\bar{b}}^{Y(5S)} = (0.302 \pm 0.014)$  $\sigma_{b\bar{b}}^{Y(5S)} = (0.302 \pm 0.014)$  nb [2,[16](#page-5-11)]. Three  $B_s^0$  production<br>modes are kinematically allowed at the  $Y(5S)$ .  $P^* \bar{D}^*$ modes are kinematically allowed at the  $\Upsilon(5S)$ :  $B_s^* \overline{B}_s^*$ ,<br> $B^* \overline{B}_s^0 + B_0 \overline{B}_s^*$  and  $B_0 \overline{B}_s^0$ . The  $B^*$  decays to  $B_0$  emitting a  $B_s^* \bar{B}_s^0 + B_s^0 \bar{B}_s^*$ , and  $B_s^0 \bar{B}_s^0$ . The  $B_s^*$  decays to  $B_s^0$ , emitting a photon with energy  $F \sim 50$  MeV. The fraction of  $b\bar{b}$ photon with energy  $E_{\gamma} \sim 50$  MeV. The fraction of  $b\bar{b}$ events containing a  $B_s^{(*)} \bar{B}_s^{(*)}$  pair has been measured to be  $f_s = N_{B_s^{(*)}\bar{B}_s^{(*)}}/N_{b\bar{b}} = (19.3 \pm 2.9)\%$  [\[17\]](#page-5-12). The fraction of  $B_s^{(*)} \bar{B}_s^{(*)}$  events containing a  $B_s^* \bar{B}_s^*$  pair is predominant and<br>has been magained with  $B_s^0 \rightarrow D^- \pi^+$  suggests to be formulated has been measured with  $\overline{B_9^0} \rightarrow \overline{D_5}^+ \pi^+$  events to be  $f_{B_3^*B_3^*}$ <br>(00.1+3.8 + 0.2)% [5]. The number of  $B^0$  mesons produced  $(90.1^{+3.8}_{-4.0} \pm 0.2)\%$  [[5](#page-5-2)]. The number of  $B_s^0$  mesons produced<br>in the deminant  $P^*\bar{P}^*$  meduction mode is thus  $N =$ in the dominant  $B_s^* \bar{B}_s^*$  production mode is thus  $N_{B_s^0} =$ <br> $\frac{\gamma(55)}{24}$  (2.40 + 0.41) \t 10<sup>6</sup>  $2L_{\text{int}} \sigma_{b\bar{b}}^{Y(5S)} f_s f_{B_s^* \bar{B}_s^*} = (2.48 \pm 0.41) \times 10^6.$ 

The Belle detector is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector, a central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter comprised of CsI(Tl) crystals (ECL) located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside of the coil is instrumented to detect  $K_L^0$  and to identify muons. The detector is described in detail elsewhere [\[18\]](#page-5-13).

Reconstructed charged tracks are required to have a maximum impact parameter with respect to the nominal interaction point of 0.5 cm in the radial direction and 3 cm in the beam-axis direction. A likelihood ratio  $\mathcal{R}_{K/\pi}$  =  $\mathcal{L}_K/(\mathcal{L}_{\pi}+\mathcal{L}_K)$  is constructed using ACC, TOF and CDC (ionization energy loss) measurements. A track is identified as a charged pion if  $\mathcal{R}_{K/\pi}$  < 0.6 or as a charged kaon otherwise. With this selection, the momentumaveraged identification efficiency for pions (kaons) is about 91% (86%), while the momentum-averaged rate of kaons (pions) identified as pions (kaons) is about 9% (14%).

Photons are reconstructed using ECL energy clusters within the polar angle acceptance  $17^{\circ}$  to  $150^{\circ}$  that are not associated with a charged track and that have an energy deposit larger than 50 MeV. A photon candidate is retained only if the ratio of the energy deposited in the array of the central  $3 \times 3$  cells is more than 85% of that in the array of  $5 \times 5$  cells. Neutral pions are reconstructed via the  $\pi^0 \rightarrow$  $\gamma\gamma$  decay with photon pairs having an invariant mass within  $\pm 13$  MeV/ $c^2$  of the  $\pi^0$  mass. A mass-constrained fit is then applied to the  $\pi^0$  candidates.

Neutral kaons are reconstructed via the decay  $K_9^0 \rightarrow$ <br> $\pi^-\pi^-$  with no  $R_{\text{tot}}$  requirements for the two charged  $\pi^+\pi^-$  with no  $\mathcal{R}_{K/\pi}$  requirements for the two charged pions. The  $K_S^0$  candidates are required to have an invariant mass within  $\pm$  7.5 MeV/ $c^2$  of the  $K_S^0$  mass. Requirements<br>are applied on the  $K^0$  vertex displacement from the interare applied on the  $K_S^0$  vertex displacement from the interaction point (IP) and on the difference between the  $K_S^0$ flight directions obtained from the  $K_S^0$  momentum and from the decay vertex and IP. The criteria are described in detail elsewhere [[19](#page-5-14)]. The  $K^{*0}$  ( $\phi$ ,  $\rho^+$ ) candidates are reconstructed via the decay  $K^{*0} \to K^+ \pi^-$  ( $\phi \to K^+ K^-$ ,  $\rho$ )<br> $\pi^+ \pi^0$ ) with an invariant mass within  $\pm 50$  MeV structed via the decay  $\Lambda \rightarrow \Lambda \pi$  ( $\varphi \rightarrow \Lambda \Lambda$ ),  $\rho \rightarrow \pi^{+} \pi^{0}$ ) with an invariant mass within  $\pm 50$  MeV/ $c^{2}$ <br>(+12 MeV/ $c^{2}$  +100 MeV/ $c^{2}$ ) of their nominal values  $(\pm 12 \text{ MeV}/c^2, \pm 100 \text{ MeV}/c^2)$  of their nominal values. Candidates for  $D_s^-$  are reconstructed in the three modes  $D_s^- \to \phi \pi^-$ ,  $D_s^- \to K^{*0} K^-$ , and  $D_s^- \to K_5^0 K^-$  and are<br>required to have a mass within  $\pm 10$  MeV/ $c^2$  of the  $D^$ required to have a mass within  $\pm 10 \text{ MeV}/c^2$  of the  $D_s^-$ <br>mass. The  $D^{*-}$  candidates are reconstructed via the decay mass. The  $D_s^{*-}$  candidates are reconstructed via the decay  $D_s^*$   $\rightarrow$   $D_s^ \gamma$  by adding a photon candidate to a  $D_s^-$  can-<br>didate. The  $D^ \gamma$  pair is required to have a mass difference didate. The  $D_s^- \gamma$  pair is required to have a mass difference  $m(D_s^- \gamma) - m(D_s^-)$  within  $\pm 13$  MeV/ $c^2$  of the  $D_s^{*-} - D_s^-$ <br>mass difference. All mass values are those reported in  $m(D_s \gamma) - m(D_s)$  within  $\pm 13$  MeV/c<sup>2</sup> of the  $D_s - D_s$ <br>mass difference. All mass values are those reported in Ref. [[17](#page-5-12)], and the applied mass windows correspond to  $\pm(3-4)\sigma$  around these values; the mass resolution,  $\sigma$ , is obtained from Monte Carlo (MC) signal simulations.

The  $B_s^0 \to D_s^* - \pi^+$  and  $B_s^0 \to D_s^- \rho^+$  candidates are re-<br>nstructed using two variables: the beam-energyconstructed using two variables: the beam-energyconstrained mass of the  $B_s^0$  candidate  $M_{bc} = \sqrt{E_b^*^2 - \vec{P}_{B_s}^*^2}$ and the energy difference  $\Delta E = E_{B_0^0}^* - E_b^*$ , where  $(E_{B_0^0}^*, \mathbb{R})$  $\vec{p}_{B_s^0}^*$ ) is the four-momentum of the  $B_s^0$  candidate and  $E_b^*$  is the beam energy, both expressed in the center-of-mass frame. The two angles  $\theta_{D_s^*}$  and  $\theta_{\rho^+}$  are used as additional observables for the  $B_s^0 \nightharpoonup D_s^* - \rho^+$  candidate. We select<br>candidates with  $M_s > 5.3$  GeV/ $c^2$  and  $-0.3$  GeV  $\lt$ candidates with  $M_{\text{bc}} > 5.3 \text{ GeV}/c^2$  and  $-0.3 \text{ GeV} < \Lambda F < 0.4 \text{ GeV}$  $\Delta E$  < 0.4 GeV.

Further selection criteria are developed using MC samples based on the EVTGEN [\[20\]](#page-5-15) event generator and the GEANT [[21](#page-5-16)] full-detector simulation. The most significant source of background is continuum processes,  $e^+e^- \rightarrow q\bar{q}$  ( $q = u, d, s, c$ ). In addition, peaking back-<br>grounds can arise from specific  $R^0$  decays. Using a MC grounds can arise from specific  $B_s^0$  decays. Using a MC sample of  $e^+e^- \rightarrow B_s^{(*)}\bar{B}_s^{(*)}$  events corresponding to 3<br>times the integrated luminosity we find that  $B^0 \rightarrow$ times the integrated luminosity, we find that  $B_s^0 \rightarrow$ times the integrated luminosity, we find that  $B_s^0 \rightarrow D_s^- \pi^+$  and  $B_s^0 \rightarrow D_s^- \rho^+$  events make a significant contri-<br>bution to the background in the  $B^0 \rightarrow D_s^*^- \pi^+$  analysis bution to the background in the  $B_s^0 \to D_s^{*-} \pi^+$  analysis.<br>However they are well separated from the signal in the  $\Lambda F$ However, they are well separated from the signal in the  $\Delta E$ distribution. If a  $B_s^0 \to \overline{D_s} \pi^+$  decay is combined with an extra photon, the energy is larger than the signal; the four extra photon, the energy is larger than the signal; the four charged tracks of a  $B_s^0 \nightharpoonup D_s^- \rho^+$  event can be selected with<br>an additional photon giving a  $R^0$  candidate with a smaller an additional photon giving a  $B_s^0$  candidate with a smaller energy. Similarly,  $B_s^0 \nightharpoonup D_s^* \nightharpoonup \rho^+$  decays give a significant<br>contribution to the  $B_0^0 \nightharpoonup D^- \rho^+$  analysis at lower energies contribution to the  $B_8^0 \rightarrow D_5^0 \rho^+$  analysis at lower energies.<br>For the  $B^0 \rightarrow D^{*-} \rho^+$  analysis, there is no significant peak-For the  $B_s^0 \rightarrow D_s^{*-} \rho^+$  analysis, there is no significant peak-<br>ing background MC studies show that for the three ing background. MC studies show that, for the three modes, all the other background sources (mainly  $B^0$  and  $B^+$  events) are smooth and small enough to be well described by the same shape that is used for the continuum. The contribution of nonresonant  $B_s^0 \to D_s^{(*)-} \pi^+ \pi^0$  decays<br>is studied by relaxing the  $(\pi^+ \pi^0)$  mass  $(M)$  requirement is studied by relaxing the  $(\pi^+\pi^0)$  mass  $(M_{\pi\pi})$  requirement and doing a two-dimensional fit in  $M_{bc}$  and  $\Delta E$  (see below). The signal  $M_{\pi\pi}$  distribution is then obtained using the <sub>s</sub>Plot method [[22](#page-5-17)]. The resulting  $M_{\pi\pi}$  spectrum shows no indication of  $B_s^0 \to D_s^{(*)-} \pi^+ \pi^0$  decays (consistent with<br>results for  $B_s^0 \to D_s^{(*)+} \pi^0 \pi^-$  [231), and we neglect this results for  $B^0 \to D^{(*)+} \pi^0 \pi^-$  [\[23\]](#page-5-18)), and we neglect this component in our fit component in our fit.

To improve signal significance, criteria for each of the three  $B_s^0$  modes are chosen to maximize  $N_{\text{sig}}/\sqrt{N_{\text{sig}} + N_{\text{bkg}}^{q\bar{q}}} + N_{\text{bkg}}^{\text{peak}}$ , evaluated in the  $\pm 2.5\sigma B_s^* \bar{B}_s^*$ signal region in the  $(M_{bc}, \Delta E)$  plane. The expected continuum background,  $N_{\text{bkg}}^{q\bar{q}}$ , is estimated using MC-<br>concreted continuum quante corresponding to 2 times the generated continuum events corresponding to 3 times the data. The expected signal,  $N_{\text{sig}}$ , and peaking background,  $N_{\text{bg}}^{\text{peak}}$ , are obtained assuming  $\mathcal{B}(B_s^0 \to D_s^- \pi^+) = \mathcal{B}(B_s^0 \to D_s^+ \pi^+)$  $N_{\text{bkg}}^{\text{c}}$ , are obtained assuming  $\mathcal{B}(B_s^0 \to D_s^-\pi^+) = \mathcal{B}(B_s^0 \to D_s^+\pi^+) = 3.3 \times 10^{-3}$  [\[17\]](#page-5-12) and  $\mathcal{B}(B_s^0 \to D_s^-\rho^+) =$ <br> $\mathcal{B}(B_s^0 \to D_s^*-\rho^+) = 7.0 \times 10^{-3}$  [\[9](#page-5-6)]. The efficiencies of exclusive  $B^0$  decays are determ exclusive  $B_s^0$  decays are determined using MC simulations.

To suppress the continuum background, we use the ratio of the second and zeroth Fox-Wolfram moments [[24](#page-5-19)],  $R_2$ . This variable has a broad distribution between zero and one for jetlike continuum events and is concentrated in the range below 0.5 for the more spherical signal events. This property allows an efficient continuum reduction with a low systematic uncertainty ( $\sim$  2%). Candidates for  $B_s^0 \to D_s^{*-} \pi^+$   $(B_s^0 \to D_s^- \rho^+$  and  $B_s^0 \to D_s^{*-} \rho^+$  are<br>required to have  $B_s < 0.5$  ( < 0.35). This selection rejects required to have  $R_2 < 0.5$  (  $< 0.35$ ). This selection rejects 40% (69%, 64%) of the background while retaining 93%  $(82\%, 86\%)$  of the  $B_s^0 \to D_s^{*-} \pi^+$   $(B_s^0 \to D_s^- \rho^+, B_s^0 \to D_s^* \to \rho^+$ , isomal  $D_s^{*-} \rho^+$ ) signal.

After the event selection described above, about 15%, 15%, and 28% of  $D_s^{*-}\pi^+$ ,  $D_s^- \rho^+$  and  $D_s^{*-}\rho^+$  candidate events, respectively, have multiple candidates. We select one candidate per event according to the following criteria. The  $D_s^+$  with the mass closest to the nominal value is preferred. The  $D_s^{*+}$  formed with the preferred  $D_s^+$  and with the mass difference  $m(D_s^*) - m(D_s)$  closest to the nominal value is preferred. The  $B^0 \to D^{*-}\pi^+$  candidate nominal value is preferred. The  $B_s^0 \to D_s^* - \pi^+$  candidate<br>with the preferred  $D_s^*$  and the  $\pi^+$  with the best  $\mathcal{R}_{\kappa\ell}$  is with the preferred  $D_s^*$  and the  $\pi^+$  with the best  $\mathcal{R}_{K/\pi}$  is retained. The preferred  $\rho^+$  is the one with the  $\pi^0$  mass (before the mass-constrained fit) closest to the nominal value and the  $\pi^+$  with the best  $\mathcal{R}_{K/\pi}$ . The  $B_s^0 \to D_s^- \rho^+$ <br>( $B_s^0 \to D_s^* = \rho^+$ ) candidate with the preferred  $D^- (D_s^* )$  and  $(B_s^0 \rightarrow D_s^{*-} \rho^+)$  candidate with the preferred  $D_s^- (D_s^{*-})$  and<br>the preferred  $\rho^+$  is retained. After this selection in MC the preferred  $\rho^+$  is retained. After this selection, in MC signal simulations, 76%, 68% and 51% (64%) of the selected  $B_s^0 \to D_s^* \pi^+$ ,  $B_s^0 \to D_s^- \rho^+$  and longitudinally<br>(transversally) polarized  $B_0^0 \to D_s^* \pi^+$  candidates are con-(transversally) polarized  $B_s^0 \to D_s^{*-} \rho^+$  candidates are correctly reconstructed rectly reconstructed.

The  $B_s^0 \to D_s^* - \pi^+$  and  $B_s^0 \to D_s^- \rho^+$  signals are ex-<br>cted from a two-dimensional unbinned extended maxitracted from a two-dimensional unbinned extended maxi-mum likelihood fit [[25](#page-5-20)] in  $M_{bc}$  and  $\Delta E$ . The three decays of the  $\Upsilon(5S)$   $(B_{s}^{*}\bar{B}_{s}^{*}, B_{s}^{*}\bar{B}_{s}^{0} + B_{s}^{0}\bar{B}_{s}^{*}$  and  $B_{s}^{0}\bar{B}_{s}^{0}$  are considered.<br>Each signal probability density function (PDF) is described Each signal probability density function (PDF) is described with sums of Gaussian or so-called ''Novosibirsk functions'' [\[26\]](#page-5-21); the latter function is used to describe the distribution if it is asymmetrical around its central value. Each signal PDF is composed of two components with their respective proportions fixed, representing the correctly and the incorrectly reconstructed candidates. In a simulated signal event, a candidate is correctly (incorrectly) reconstructed when the selected decay products do (do not) match the true combination. The fractions of correctly reconstructed candidates are fixed from MC samples and their uncertainties are included in the systematic error. The  $M_{bc}$  and  $\Delta E$  resolutions for  $B_s^0 \to D_s^{*-} \pi^+$ <br>  $(B^0 \to D^- a^+$  and  $B^0 \to D^{*-} a^+$ ) are calibrated by a multi- $(B_s^0 \rightarrow D_s^- \rho^+$  and  $B_s^0 \rightarrow D_s^*^- \rho^+$  are calibrated by a multi-<br>plying factor measured with the  $B_0^0 \rightarrow D^- \pi^+$  [5]  $(B_0^0 \rightarrow$ plying factor measured with the  $B_s^0 \to D_s^- \pi^+$  [\[5](#page-5-2)]  $(B^0 \to D_s^* - a^+)$  signal. The mean values of M, and AE for the  $\overline{D^*- \rho}^+$ ) signal. The mean values of  $M_{bc}$  and  $\overline{\Delta E}$  for the three  $R^0$  production modes (6 parameters) are related to three  $B_s^0$  production modes (6 parameters) are related to two floating parameters corresponding to the  $B_s^0$  and  $B_s^*$ meson masses [[27](#page-5-22)]. The peaking background PDFs are analytically defined and fixed from specific MC samples. The continuum (together with possible  $B^+$  and  $B^0$  back-ground) is modeled with an ARGUS function [[28](#page-5-23)] for  $M_{bc}$ and a linear function for  $\Delta E$ . The endpoint of the ARGUS function is fixed to the beam energy, while the two other parameters are left free. All the yields can float.

For the  $B_s^0 \rightarrow D_s^{* -} \rho^+$  candidates, we perform a four-<br>mensional fit using the two observables  $cos\theta_{\text{max}}$  and dimensional fit using the two observables  $\cos\theta_{D_s^*}$  $\int_{s}^{*}$  and  $\cos\theta_{\rho^+}$  in addition to  $M_{bc}$  and  $\Delta E$ . Only the main  $B_s^0$ <br>production mode is considered  $(B^*\bar{B}^*)$  and three compoproduction mode is considered  $(B_s^* \bar{B}_s^*)$ , and three compo-<br>pants are used in the likelihood, the transverse and longinents are used in the likelihood: the transverse and longitudinal signals, and the background. We define the PDF for  $M_{\text{bc}}$  and  $\overline{\Delta}E$  in the same way as described above, while the angular distributions are analytically described with nolvangular distributions are analytically described with polynomials of order up to five. The shape parameters are floated for the background PDF but are fixed for the two signal PDFs.

The fitted signal yields are listed in Table [I,](#page-3-0) while Figs. [1](#page-4-0) and [2](#page-4-1) show the observed distributions in the  $B_s^* \bar{B}_s^*$  signal<br>region with the projections of the fit goals. The signifiregion with the projections of the fit result. The significance is defined by  $S = \sqrt{2 \ln(\mathcal{L}_{\text{max}}/\mathcal{L}_0)}$ , where  $\mathcal{L}_{\text{max}}$  $(\mathcal{L}_0)$  is the value at the maximum (with the corresponding yield set to zero) of the likelihood function convolved with a Gaussian distribution that represents the systematic errors of the yield. The linearity of the floating parameters in the region near the results has been extensively checked with MC simulations, as well as the statistical uncertainty

Mode	Prod. mode	$\varepsilon$ (%)	$N_{S}$	S
	$B_{s}^{*}\bar{B}_{s}^{*}$	9.13	$53.4^{+10.3}_{-9.4}$	$7.1\sigma$
$B_s^0 \rightarrow D_s^{*-} \pi^+$	$B_{s}^{*}\bar{B}_{s}^{0}+B_{s}^{0}\bar{B}_{s}^{*}$	$\cdots$	$-1.9_{-2.9}^{+4.0}$	.
	$B_{s}^{0}\bar{B}_{s}^{0}$	$\cdots$	$2.9^{+3.9}_{-3.0}$	$\cdots$
	$B^*_{s}\bar{B}^*_{s}$	4.40	$92.2^{+14.2}_{-13.2}$	$8.2\sigma$
$B_s^0 \rightarrow D_s^- \rho^+$	$B_{s}^{*}\bar{B}_{s}^{0}+B_{s}^{0}\bar{B}_{s}^{*}$	$\cdots$	$-4.0^{+5.2}_{-3.7}$	$\cdots$
	$B_{s}^{0}\bar{B}_{s}^{0}$	$\cdots$	$-3.0^{+5.7}_{-4.0}$	$\cdots$
$B_s^0 \to D_s^{*-} \rho^+$	$B^*_{s} \bar{B}^*_{s}$	$\cdots$	$77.8^{+14.5}_{-13.4}$	$7.4\sigma$
Longitudinal component		2.66	$81.3^{+16.0}_{-14.9}$	.
Transverse component		2.68	$-3.5^{+8.0}_{-6.1}$	$\cdots$

<span id="page-3-0"></span>TABLE I. Total efficiencies ( $\varepsilon$ ), signal yields ( $N<sub>S</sub>$ ) with statistical errors, and significance (S) including systematic uncertainties, for the three measured modes.

<span id="page-4-0"></span>

FIG. 1 (color online). Left (right):  $M_{bc}$  ( $\Delta E$ ) distributions for the  $B_s^0 \to D_s^* \pi^+$  (top) and  $B_s^0 \to D_s^- \rho^+$  (bottom) candidates with  $\Delta E$ <br>(*M*.) restricted to the  $\pm 2.5\sigma$   $B_s^* \bar{R}_s^*$  signal region. The blu  $(M_{\text{bc}})$  restricted to the  $\pm 2.5 \sigma B_s^* \bar{B}_s^*$  signal region. The blue solid curve is the total PDF, while the green (black) dotted curve is the peaking (continuum) background and the red dashed curve is the signal. peaking (continuum) background and the red dashed curve is the signal. The errors bars correspond to the Poissonian standard deviation.

of  $f_L(B_s^0 \to D_s^{*-} \rho^+)$ , which lies near the limit of the physically allowed range  $(0-1)$ physically allowed range (0–1).

The dominance of the  $Y(5S) \rightarrow B_s^* \bar{B}_s^*$  mode is con-<br>med. For better precision, we therefore extract the firmed. For better precision, we therefore extract the branching fractions (BFs) using only the yields in this mode. Table [II](#page-5-24) shows the values obtained with the relations  $\mathcal{B} = N_S/(N_{B_s^0} \times \varepsilon)$ , for the  $B_s^0 \rightarrow D_s^{*-} \pi^+$  and  $B_s^0 \rightarrow$ <br>  $D_s^- \rho^+$  modes. The values for  $\mathcal{B}(B_s^0 \rightarrow D_s^{*-} \rho^+)$  and  $f_L =$ 

 $1.05^{+0.08}_{-0.10}$ (stat) $^{+0.03}_{-0.04}$ (syst) are obtained by floating these two<br>parameters in a fit where the longitudinal (transverse) vield parameters in a fit where the longitudinal (transverse) yield is replaced by the relation  $N_{B_0^0} \times B \times f_L \times \varepsilon_L$   $(N_{B_0^0} \times R \times (1 - f_C) \times \varepsilon_L)$ , with  $N_{\varepsilon_0}$  and a heing fixed  $\mathcal{B} \times (1 - f_L) \times \varepsilon_T$ , with  $N_{B_v^0}$ ,  $\varepsilon_T$  and  $\varepsilon_L$  being fixed.<br>Since the transverse vield fluctuated to a negative central Since the transverse yield fluctuated to a negative central value,  $f_L > 1$ . The corresponding Feldman-Cousins [\[29\]](#page-5-25) 68% confidence interval is [0.93, 1.00].

<span id="page-4-1"></span>

FIG. 2 (color online). Distributions for the  $B_s^0 \to D_s^{*-} \rho^+$  candidates. Top:  $M_{bc}$  and  $\Delta E$  distributions, as in Fig. [1](#page-4-0). Bottom: helicity distributions of the  $D^{*-}$  (left) and  $\sigma^+$  (right) with  $M_{+-}$  and  $\Delta E$  re distributions of the  $D_s^*$  (left) and  $\rho^+$  (right) with  $M_{bc}$  and  $\Delta E$  restricted to the  $B_s^* \bar{B}_s^*$  kinematic region. The components of the total PDF (blue solid line) are shown separately: the black dotted curve PDF (blue solid line) are shown separately: the black dotted curve is the background and the two red dashed curves are the signal. The large (small) signal shape corresponds to the longitudinal (transverse) component.

<span id="page-5-24"></span>TABLE II. Top: measured BF values with statistical, systematic (without  $f_s$ ) and  $f_s$  uncertainties, and HQET predictions from the factorization hypothesis [\[11\]](#page-5-26). Bottom: BF ratios where several systematic uncertainties cancel out. We use our previous measurement of  $\mathcal{B}(B_s^0 \to D_s^- \pi^+)$  [\[5\]](#page-5-2).

Mode	$\mathcal{B}(10^{-3})$	HQET $(10^{-3})$	
$B_s^0 \rightarrow D_s^{*-} \pi^+$	$2.4^{+0.5}_{-0.4} \pm 0.3 \pm 0.4$	2.8	
$B_s^0 \rightarrow D_s^- \rho^+$	$8.5^{+1.3}_{-1.2} \pm 1.1 \pm 1.3$	7.5	
$B_s^0 \to D_s^{*-} \rho^+$	$11.9_{-2.0}^{+2.2} \pm 1.7 \pm 1.8$	89	



The common systematic uncertainties on the BFs are due to the errors on the integrated luminosity (1.3%),  $\sigma_{b\bar{b}}^{Y(5S)}$  (4.6%),  $f_s$  (15.0%),  $f_{B_s^* \bar{B}_s^*}^*$  (4.3%), the  $D_s^-$  BFs (6.4%), the  $R_2$  cut (2.0%), the tracking efficiency (4.0%) and the charged-particle identification (5.4%). In addition, uncertainties due to the MC statistics (1.6%, 2.3%, 1.5%), the neutral-particle identification (8.8%, 5.4%, 8.8%) and the PDF shapes  $(4.6\%, 4.7\%, 4.3\%)$  depend on the  $(B_s^0 \rightarrow D^* - \pi^+$   $B^0 \rightarrow D^- \rho^+$   $B^0 \rightarrow D^{*-} \rho^+$  mode. The system- $D_s^* - \pi^+$ ,  $B_s^0 \rightarrow D_s^- \rho^+$ ,  $B_s^0 \rightarrow D_s^* - \rho^+$ ) mode. The system-<br>atic errors on f, are due to the uncertainties in PDF shapes atic errors on  $f<sub>L</sub>$  are due to the uncertainties in PDF shapes.

Our values for the BFs are in good agreement with predictions based on HQET and the factorization approxi-mation [[11](#page-5-26)]. The large value of  $f_L(B_s^0 \to D_s^{*-} \rho^+)$  is consistent with the value measured for  $B^0 \to D_s^{*-} \rho$  decays sistent with the value measured for  $B^0 \rightarrow D^{*-} \rho$  decays<br>[30] and with the predictions of Refs [9.31] [\[30\]](#page-5-27) and with the predictions of Refs. [[9](#page-5-6),[31](#page-5-28)].

In summary, we report the first observation of three CKM-favored exclusive  $B_s^0$  decay modes, we extract their branching fractions, and, for  $B_s^0 \rightarrow D_s^{*-} \rho^+$ , we measure<br>the longitudinal polarization fraction Our results are conthe longitudinal polarization fraction. Our results are con-sistent with theoretical predictions based on HOET [\[11\]](#page-5-26) and are similar to analogous  $B^0$  decay branching fractions. The dominance of the unexpectedly large  $\Upsilon(5S) \rightarrow B_s^* \overline{B}_s^*$ <br>mode [5] is confirmed mode [[5](#page-5-2)] is confirmed.

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- <span id="page-5-0"></span>[1] Unless specified otherwise, charge-conjugated modes are implied throughout.
- <span id="page-5-1"></span>[2] A. Drutskoy et al. (Belle Collaboration), [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.98.052001) 98[, 052001 \(2007\)](http://dx.doi.org/10.1103/PhysRevLett.98.052001).
- [3] A. Drutskoy *et al.* (Belle Collaboration), [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.76.012002) 76, [012002 \(2007\).](http://dx.doi.org/10.1103/PhysRevD.76.012002)
- [4] J. Wicht et al. (Belle Collaboration), [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.100.121801) 100, [121801 \(2008\).](http://dx.doi.org/10.1103/PhysRevLett.100.121801)
- <span id="page-5-2"></span>[5] R. Louvot et al. (Belle Collaboration), [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.102.021801) 102[, 021801 \(2009\)](http://dx.doi.org/10.1103/PhysRevLett.102.021801).
- <span id="page-5-3"></span>[6] L. Wolfenstein, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.51.1945) **51**, 1945 (1983).
- <span id="page-5-4"></span>[7] M. Kobayashi and T. Maskawa, [Prog. Theor. Phys.](http://dx.doi.org/10.1143/PTP.49.652) 49, 652 [\(1973\)](http://dx.doi.org/10.1143/PTP.49.652); N. Cabibbo, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.10.531) 10, 531 (1963).
- <span id="page-5-5"></span>[8] N. A. Törnqvist, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.53.878) **53**, 878 (1984).
- <span id="page-5-6"></span>[9] J.L. Rosner, *Phys. Rev. D* **42**[, 3732 \(1990\)](http://dx.doi.org/10.1103/PhysRevD.42.3732).
- [10] B. Block and M. Shifman, [Nucl. Phys. B](http://dx.doi.org/10.1016/0550-3213(93)90330-R) 389, 534 (1993).
- <span id="page-5-26"></span>[11] A. Deandrea et al., [Phys. Lett. B](http://dx.doi.org/10.1016/0370-2693(93)91554-Z) 318, 549 (1993).
- <span id="page-5-7"></span>[12] T. Mannel, W. Roberts, and Z. Ryzak, [Phys. Lett. B](http://dx.doi.org/10.1016/0370-2693(91)90841-D) 259, [359 \(1991\)](http://dx.doi.org/10.1016/0370-2693(91)90841-D).
- <span id="page-5-8"></span>[13] W. A. Bardeen, E. J. Eichten, and C. T. Hill, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.68.054024) 68[, 054024 \(2003\)](http://dx.doi.org/10.1103/PhysRevD.68.054024).
- <span id="page-5-9"></span>[14] J.G. Körner and G.R. Goldstein, [Phys. Lett. B](http://dx.doi.org/10.1016/0370-2693(79)90085-6) 89, 105 [\(1979\)](http://dx.doi.org/10.1016/0370-2693(79)90085-6).
- <span id="page-5-10"></span>[15] S. Kurokawa and E. Kikutani, [Nucl. Instrum. Methods](http://dx.doi.org/10.1016/S0168-9002(02)01771-0) [Phys. Res., Sect. A](http://dx.doi.org/10.1016/S0168-9002(02)01771-0) 499, 1 (2003), and other articles included in this volume.
- <span id="page-5-11"></span>[16] G. S. Huang et al. (CLEO Collaboration), [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.75.012002) 75, [012002 \(2007\).](http://dx.doi.org/10.1103/PhysRevD.75.012002)
- <span id="page-5-12"></span>[17] C. Amsler et al. (Particle Data Group), [Phys. Lett. B](http://dx.doi.org/10.1016/j.physletb.2008.07.018) 667, 1 [\(2008\)](http://dx.doi.org/10.1016/j.physletb.2008.07.018).
- <span id="page-5-13"></span>[18] A. Abashian et al. (Belle Collaboration), [Nucl. Instrum.](http://dx.doi.org/10.1016/S0168-9002(01)02013-7) [Methods Phys. Res., Sect. A](http://dx.doi.org/10.1016/S0168-9002(01)02013-7) 479, 117 (2002).
- <span id="page-5-14"></span>[19] F. Fang, Ph.D. thesis, University of Hawaii, 2003.
- <span id="page-5-15"></span>[20] D. J. Lange, [Nucl. Instrum. Methods Phys. Res., Sect. A](http://dx.doi.org/10.1016/S0168-9002(01)00089-4) 462[, 152 \(2001\).](http://dx.doi.org/10.1016/S0168-9002(01)00089-4)
- <span id="page-5-16"></span>[21] CERN Application Software Group, CERN Program Library Report No. W5013, 1993.
- <span id="page-5-17"></span>[22] M. Pivk and F.R. Le Diberder, [Nucl. Instrum. Methods](http://dx.doi.org/10.1016/j.nima.2005.08.106) [Phys. Res., Sect. A](http://dx.doi.org/10.1016/j.nima.2005.08.106) 555, 356 (2005).
- <span id="page-5-18"></span>[23] M. S. Alam et al. (CLEO Collaboration), [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.50.43) 50, [43 \(1994\).](http://dx.doi.org/10.1103/PhysRevD.50.43)
- <span id="page-5-19"></span>[24] G.C. Fox and S. Wolfram, [Phys. Rev. Lett.](http://dx.doi.org/10.1103/PhysRevLett.41.1581) 41, 1581 [\(1978\)](http://dx.doi.org/10.1103/PhysRevLett.41.1581).
- <span id="page-5-20"></span>[25] R. Barlow, [Nucl. Instrum. Methods Phys. Res., Sect. A](http://dx.doi.org/10.1016/0168-9002(90)91334-8) 297[, 496 \(1990\).](http://dx.doi.org/10.1016/0168-9002(90)91334-8)
- <span id="page-5-21"></span>[26] The Novosibirsk function is defined as  $f(x) = \exp[-\frac{1}{2}$ <br>(1-21) (1-21) with  $A = \sinh(-\sqrt{2})$  $\left(\ln^2\left\{1 + \Lambda(x - x_0)\right\}/\tau^2 + \tau^2\right)$  with  $\Lambda = \sinh(\tau \sqrt{\ln 4})/\tau^2$  $(\sigma\sqrt{\ln 4})$ . The parameters represent the mean  $(x_0)$ , the width  $(\sigma)$  and the tail asymmetry  $(\sigma)$ width  $(\sigma)$  and the tail asymmetry  $(\tau)$ .
- <span id="page-5-22"></span>[27] See Table I of Ref. [[5\]](#page-5-2) for the detailed parameterization.
- <span id="page-5-23"></span>[28] H. Albrecht et al. (ARGUS Collaboration), [Phys. Lett. B](http://dx.doi.org/10.1016/0370-2693(87)91558-9) 185[, 218 \(1987\).](http://dx.doi.org/10.1016/0370-2693(87)91558-9)
- <span id="page-5-25"></span>[29] G.J. Feldman and R.D. Cousins, [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.57.3873) 57, 3873 [\(1998\)](http://dx.doi.org/10.1103/PhysRevD.57.3873).
- <span id="page-5-27"></span>[30] S. E. Csorna et al. (CLEO Collaboration), [Phys. Rev. D](http://dx.doi.org/10.1103/PhysRevD.67.112002) 67, [112002 \(2003\).](http://dx.doi.org/10.1103/PhysRevD.67.112002)
- <span id="page-5-28"></span>[31] A. Ali *et al.*, Z. Phys. C 1[, 269 \(1979\)](http://dx.doi.org/10.1007/BF01440227).