## Mapping the Magnetostructural Quantum Phases of Mn<sub>3</sub>O<sub>4</sub>

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(Received 9 December 2009; published 30 March 2010)

We present temperature-dependent x-ray diffraction and temperature- and field-dependent Raman scattering studies of single-crystal Mn<sub>3</sub>O<sub>4</sub>, which reveal the magnetostructural phases that evolve in the spinels due to the interplay between strong spin-orbital coupling, geometric frustration, and applied magnetic field. We present evidence that the magnetoelastic and magnetodielectric behavior in this material is governed by magnetic-field-controlled tetragonal-to-monoclinic phase changes. Most interestingly, for an applied field transverse to the ferrimagnetic ordering direction, **H** || [110], we find evidence for a field-tuned quantum phase transition to a tetragonal spin-disordered phase, indicating that a structurally symmetric, spin frustrated phase can be recovered at  $T \sim 0$  for intermediate transverse fields in Mn<sub>3</sub>O<sub>4</sub>.

DOI: 10.1103/PhysRevLett.104.136402

PACS numbers: 71.70.Ej, 73.43.Nq, 78.30.-j

The development at low temperatures of some form of long-range order-such as magnetism, orbital-order, charge-order, or superconductivity-is ubiquitous in materials [1], and reflects the tendency of a material to lower its ground state degeneracy and minimize its entropy near T = 0 K. Recently, there has been substantial interest in materials in which atomic geometry, competing interactions, and applied fields conspire to "frustrate" the onset of long-range magnetic and/or orbital order, even down to T = 0. Frustrated systems are of interest because of the novel low temperature phase behavior they have been proposed to exhibit—including orbital [2,3] and spin liquids and glasses [4,5], and spin-ice states [6]-and because of the opportunity they provide to study how quantum fluctuations impact low temperature phases of materials [7].

One of the prototypical materials families that exhibit orbital frustration and spin frustration are the spinels, in which strong interactions and geometrical frustration result in a rich variety of exotic magnetic and structural phases among family members: sulfur-based spinels such as  $FeB_2S_4$  (B = Cr, Sc) exhibit orbital-liquid or -glass ground states; [3–5] the chromium-oxide spinels  $AB_2O_4$  (A = Zn, Cd, Hg; B = Cr) exhibit three-dimensional spin-Peierls transitions involving coupled magnetic and structural transitions [8]; and the vanadium-oxide spinels  $AB_2O_4$  (A = Zn, Cd, Mn; B = V) display complex spin-orbital ordering and large magnetoelastic and magnetodielectric effects [9,10]. The frustration and diversity of low temperature phase behavior in the spinels is believed to be governed primarily by the interplay between spin-orbital coupling, applied field, and frustrated exchange interactions [7]. However, there has been little experimental investigation of the microscopic details of this interplay.

In this Letter, we study the temperature- and fielddependent magnetostructural phases of the spinel  $Mn_3O_4$ using a combination of Raman spectroscopy and x-ray scattering. In spite of its simpler chemical compositionwith Mn ions at both tetrahedral ( $A = Mn^{2+}$ ) and octahedral ( $B = Mn^{3+}$ ) sites—Mn<sub>3</sub>O<sub>4</sub> exhibits the rich magnetostructural transitions characteristic of more complex ternary magnetic spinels: this includes ferrimagnetic ordering below  $T_C = 43$  K, in which the net spin of the octahedrally coordinated  $Mn^{3+}$  spins is antiparallel to the [110] direction of the tetrahedrally coordinated Mn<sup>2+</sup> spins [10,11]; incommensurate spin ordering of the  $Mn^{3+}$  spins below  $T_1 = 39$  K; and commensurate ferrimagnetic ordering below  $T_2 = 33$  K, in which the net Mn spins are oriented in the [110] direction and the magnetic unit cell doubles the chemical unit cell [11,12]. Our studies of this simple spinel illustrate the importance of magnetoelastic energies-which have been largely ignored in theoretical investigations-in governing the low temperature phase behavior of the spinels. Of particular interest is the discovery of a quantum ( $T \sim 0$ ) phase transition to a structurally isotropic, disordered spin-orbital state for magnetic fields applied *transverse* to the ferrimagnetic moments, i.e., for **H**  $\|$  [110], which demonstrates the important role that magnetoelastic interactions can play in frustrating spin and orbital order at T = 0.

A single-crystal sample of  $Mn_3O_4$  was grown at the University of Illinois using a floating zone technique. Field-dependent Raman measurements were performed as described previously [13] on an as-grown surface of single-crystal  $Mn_3O_4$  with surface normal along the easyaxis [110] direction. Temperature-dependent x-ray measurements were carried out on the as-grown [110] surface of  $Mn_3O_4$  using Mo  $K_{\alpha}$  radiation from a Rigaku rotaflex RU-300 rotating anode source. A graphite (004) monochromator was employed to remove Bremsstrahlung from the source, and an energy-resolving, solid state detector was used with a multichannel analyzer to reject sample fluorescence. A closed cycle He refrigerator was used to control the sample temperature. A Phillips MRD X'Pert system was used for high precision measurements at room temperature. A least squares program was used to determine the lattice parameters of the crystal from the data.

The room-temperature Raman spectrum of our  $Mn_3O_4$  sample exhibits 5 phonon peaks, consistent with previous reports [14]: a  $T_{2g}$  symmetry mode at 290 cm<sup>-1</sup>, an  $E_g$  symmetry mode at 320 cm<sup>-1</sup>,  $T_{2g}$  symmetry modes at 375 and 479 cm<sup>-1</sup>, and an  $A_{1g}$  symmetry mode at 660 cm<sup>-1</sup>. In this Letter, we focus on the lowest energy  $T_{2g}$  phonon mode, which involves Mn-O bond-stretching vibrations of the tetrahedral site ions [14].

Figure 1(b) shows the temperature dependence of the  $T_{2g}$  mode intensity and the  $T_{2g}$  mode energy and linewidth for light polarized along the [110] crystallographic direction of Mn<sub>3</sub>O<sub>4</sub>. Two distinct temperature regimes can be identified in Fig. 1(b): (i)  $T > T_2 = 33$  K. Above the cell-doubling commensurate magnetic transition at  $T_2 = 33$  K,



FIG. 1 (color). (a) Illustrations of  $Mn_3O_4$  in the monoclinic  $(T < T_2 = 33 \text{ K})$  and tetragonal  $(T > T_2 = 33 \text{ K})$  stuctures. (b) Contour plot of the  $T_{2g}$  phonon mode intensity as functions of energy and increasing temperature; red, 700 counts; blue, 0 counts. (inset) Contour plot of the  $T_{2g}$  phonon mode intensity between 7–290 K. (c) Temperature dependence of  $\gamma$ —the angle between the *a*- and *b*-axis directions—as functions of increasing temperature (closed symbols) and decreasing temperature (open symbols). (inset) Temperature dependence [in K] of lattice constants *a* (squares), *b* (triangles), and *c* (circles) [in Å] for Mn\_3O<sub>4</sub> with increasing (closed symbols) and decreasing (open symbols) temperature.

the  $T_{2g}$  mode exhibits conventional behavior: with decreasing temperature from 290 to 33 K, this mode narrows and shifts from  $\sim 290$  to  $\sim 295$  cm<sup>-1</sup> in a manner consistent with anharmonic (multiphonon) effects [15] [see inset, Fig. 1(b)]. Although there is a slight decrease in the  $T_{2a}$ mode frequency in the incommensurate magnetic phase regime between  $T_2 = 33$  K and  $T_1 = 39$  K, presumably due to magnetoelastic effects, this mode exhibits no evidence for a change in structural symmetry above  $T_2 =$ 33 K. (ii)  $T < T_2 = 33$  K. Below the cell-doubling commensurate magnetic transition  $T_2 = 33$  K, the  $T_{2g}$  mode abruptly splits into two modes near 290 cm<sup>-1</sup> and  $300 \text{ cm}^{-1}$ . This splitting is consistent with a tetragonalto-monoclinic distortion below  $T_2$ , which splits the degenerate  $T_{2g}$  mode by expanding the Mn<sup>2+</sup> – O<sup>2-</sup> bond length along the easy-axis [110] direction and contracting the  $Mn^{2+} - O^{2-}$  bond length along the [110] direction [see illustrations, Fig. 1(a)]. The relative intensities of the modes shown in Fig. 1(b) for  $T < T_2$  confirm that the  $Mn^{2+} - O^{2-}$  bond length expands along the easy-axis [110] direction below  $T_2 = 33$  K: the higher-energy  $(\sim 300 \text{ cm}^{-1})$  split mode—associated with vibrations of the contracted  $Mn^{2+} - O^{2-}$  bond—exhibits the strongest light scattering intensity, indicating that the contracted  $Mn^{2+} - O^{2-}$  bond is oriented in the direction of the incident light polarization, i.e., along the  $[1\overline{1}0]$  direction. By contrast, the intensity of the lower-energy ( $\sim 290 \text{ cm}^{-1}$ ) split mode-associated with vibrations of the expanded  $Mn^{2+} - O^{2-}$  bond—has a substantially weaker intensity than the 300  $\text{cm}^{-1}$  split mode, indicating that the expanded  $Mn^{2+} - O^{2-}$  bond is oriented perpendicular to the incident light polarization, i.e., along the [110] direction.

To provide more definitive evidence for a tetragonal-tomonoclinic phase transition below  $T_2$  in Mn<sub>3</sub>O<sub>4</sub>, we used x-ray diffraction to study a number of Bragg reflections; in particular, we measured the temperature dependence of the  $\theta$ ,  $2\theta$ ,  $\phi$ , and  $\chi$  angles of the (440) and (231) Bragg reflections. From these data, we deduced the temperature dependence-on both cooling and warming-of the lattice parameters a, b, c, as well as  $\gamma$ —the angle between the a and b axis [see Fig. 1(c)]. While  $\gamma$  exhibits an abrupt decrease near  $T_2 = 33$  K, the *a*- and *b*-axis lattice parameters exhibit no significant temperature dependence, and the *c*-axis lattice parameter exhibits only a weak temperature dependence, and hysteretic behavior. These results confirm that Mn<sub>3</sub>O<sub>4</sub> exhibits a first-order tetragonal-to-monoclinic structural phase transition near  $T_2 = 33$  K, as illustrated schematically in Fig. 1(a). Notably, this result disagrees with the interpretation of earlier powder x-ray diffraction measurements of  $Mn_3O_4$  by Boucher *et al.*, who identified the low temperature structural phase of Mn<sub>3</sub>O<sub>4</sub> as tetragonal [16]. However, powder diffraction measurements are less sensitive than our single-crystal diffraction measurements to the observation of a transition to a monoclinic phase, which involves a change in the angle between a- and *b*-axis directions, but no change in the lattice parameters.

The application of a magnetic field along different crystallographic directions in the ferrimagnetic phase of Mn<sub>3</sub>O<sub>4</sub> provides a means of either enhancing the magnetic ordering tendencies of Mn<sub>3</sub>O<sub>4</sub>—for fields applied along the easy-axis [110] direction-or frustrating those ordering tendencies-for fields applied transverse to the [110] direction. For example, Figs. 2(a) and 2(c) show that, in the incommensurate magnetic phase regime  $T_2 = 33 \text{ K} <$  $T \le T_1 = 39$  K, the 295 cm<sup>-1</sup> mode associated with the undistorted tetragonal phase [structure II in Fig. 2(b)] exhibits a field-induced splitting similar to that induced upon cooling below  $T_2 = 33$  K in zero magnetic field [Fig. 1(b)]. Thus, in the incommensurate magnetic phase, an applied magnetic field along the [110] direction generates a tetragonal-to-monoclinic distortion in Mn<sub>3</sub>O<sub>4</sub> by inducing the cell-doubled ferrimagnetic structure associated with the monoclinic phase [Fig. 2(b)]. This strong magnetoelastic response likely arises from a field-induced



increase—via spin-orbital coupling—in the hybridization between the  $d_{3z^2-r^2}$  and  $d_{xy}$  orbitals of (octahedral) Mn<sup>3+</sup> for **H** || [110]. Figure 2(d) summarizes the different magnetic and structural phases of Mn<sub>3</sub>O<sub>4</sub> as functions of magnetic field and temperature for **H** || [110].

More interesting is the magnetostructural phase diagram that results when applying the magnetic field in a direction *transverse* to the ferrimagnetic moment, **H** || [110], i.e., in a direction that places the applied field in competition with the internal field in Mn<sub>3</sub>O<sub>4</sub>. Figures 3(a) and 3(c) show that three different phase regimes are apparent for this magnetic field orientation at T = 7 K( $\ll T_2$ ). In the low-field regime, i.e., for H < 1T and  $T \ll T_2$ , the phonon spectrum is identical to that observed at zero field and low temperatures in Mn<sub>3</sub>O<sub>4</sub>, indicative of a monoclinic ferrimagnetic phase with the Mn spins oriented in the [110] direction [structure I in Fig. 3(b)]. On the other hand, in the high-



FIG. 2 (color). (a) Field dependence of the Raman spectra at T = 39 K for **H** || [110]. (b) Illustrations of the Mn<sub>3</sub>O<sub>4</sub> structure in (top) the low-field undistorted phase and (bottom) the high-field monoclinic phase. (c) Intensities of the split phonon modes as functions of energy and field at (left) T = 34 K, (middle) 39 K, and (right) 44 K; red, 700 counts; blue, 0 counts. (d) H - T phase diagram for **H** || [110]; orange, structure I; yellow, structure II; IC, incommensurate magnetic phase; C, commensurate (cell-doubled) magnetic phase.

FIG. 3 (color). (a) Field dependence of the Raman spectra at T = 7 K for **H** || [110]. (b) Illustrations of the Mn<sub>3</sub>O<sub>4</sub> structure in (top) the low-field monoclinic phase, (middle) intermediate undistorted tetragonal phase, and (bottom) high-field monoclinic phases. (c) Intensities of the split phonon modes as functions of energy and field at (left) T = 7 K, (middle) 29 K, and (right) 39 K; red, 700 counts; blue, 0 counts. (d) H - T phase diagram for **H** || [110]; orange, structure I; yellow, structure II; green, structure III; *SD*, spin disordered; and *C*, commensurate (cell-doubled) magnetic phase.

field regime, i.e., for H > 4T and  $T \ll T_2$ , the lowest energy  $T_{2g}$  phonon is split into distinct modes near 290 and 300 cm<sup>-1</sup>, but the lower-energy 290 cm<sup>-1</sup> split mode—associated with vibrations of the expanded  $Mn^{2+} - O^{2-}$  bond—has greater scattering intensity than the 300 cm<sup>-1</sup> split mode. This spectrum indicates that the expanded  $Mn^{2+} - O^{2-}$  bond, and therefore the Mn spins, are reoriented by the applied field along the applied field direction, i.e., along the [110] direction [structure III in Fig. 3(b)].

Most remarkable, however, is the intermediate-field regime, i.e., 1T < H < 4T and  $T \ll T_2$ , with  $\mathbf{H} \parallel [1\overline{1}0]$ , shown in Figs. 3(a) and 3(c): in this regime, the phonon spectrum is the same as that in the paramagnetic tetragonal phase, i.e., the dominant mode is the  $\sim 295 \text{ cm}^{-1}T_{2g}$  phonon associated with structure II in Figs. 3(b). Thus, in this field range, Mn<sub>3</sub>O<sub>4</sub> adopts a symmetric (tetragonal) structural configuration, in order to resolve the frustration imposed on the Mn spins by the competing internal  $(\mathbf{M} \parallel [110])$  and transverse external  $(\mathbf{H} \parallel [1\overline{1}0])$  fields. This field-induced tetragonal configuration is expected to be associated with a disordered spin state near  $T \sim 0$  similar to that observed in the high temperature paramagnetic phase—because of the degeneracy between [110] and  $[1\overline{1}0]$  Mn spin orientations in this structural phase. Indeed, magnetization measurements of Mn<sub>3</sub>O<sub>4</sub> by Dwight and Menyuk showed that the application of a  $\sim 1$  T field transverse to the easy-axis direction of Mn<sub>3</sub>O<sub>4</sub> at 4.2 K results in slow spin relaxation processes consistent with a disordered spin system [17]. The full H - T phase diagram for Mn<sub>3</sub>O<sub>4</sub> with  $\mathbf{H} \parallel [110]$  inferred from our Raman results is summarized in Fig. 3(d).

What are the main lessons of the rich field-induced magnetostructural phases observed here in Mn<sub>3</sub>O<sub>4</sub>? The most significant result is the observation of a quantum phase transition to an intermediate-field, spin-orbital frustrated state at  $T \sim 0$  for **H** || [110]. This result reveals a novel mechanism for frustrating spin–orbital-order at  $T \sim$ 0: the balancing of elastic and magnetic energies in the presence of a transverse applied field in Mn<sub>3</sub>O<sub>4</sub> favors a transition to a more symmetric structural configuration that protects the spin-orbital degeneracy over a wide field range. Hydrostatic pressure frustrates orbital order similarly, by creating more symmetric structural configurations [18]. Similar field-tuned frustrated phases should be observable in other materials with strong magnetoelastic coupling, such as MnV<sub>2</sub>O<sub>4</sub> [10]. Second, our results show that the rich magnetodielectric and magnetoelastic effects in Mn<sub>3</sub>O<sub>4</sub> [19] are associated with the field-induced manipulation of tetragonal-to-monoclinic phase changes, caused by tuning the hybridization between the  $d_{3r^2-r^2}$  and  $d_{xy}$  orbitals of octahedral Mn<sup>3+</sup>. Finally, our results identify Mn<sub>3</sub>O<sub>4</sub> as a particularly simple, model system in which to study a rare state of matter—a field-tuned  $T \sim 0$  spinorbital frustrated phase-that is accessible without introducing disorder. Field-dependent heat capacity measurements of  $Mn_3O_4$  would be useful for studying the change in entropy in the spin-orbital frustrated phase—e.g., to test whether this state is a quantum spin liquid. Neutron scattering studies are also needed to explore the fielddependent evolution of spin dynamics in the spin-orbital frustrated phase of  $Mn_3O_4$ , e.g., to look for evidence of quantum criticality, such as  $\omega/T$  scaling of the spin excitations, and to compare with unconventional spin dynamics observed near magnetic order-disorder phase transitions in other systems, such as quasi-one-dimensional CoNb<sub>2</sub>O<sub>6</sub> [20].

This material is based on work supported by the U.S. Department of Energy, Division of Materials Sciences, under DE-FG02-07ER46453, through the Frederick Seitz Materials Research Laboratory at the University of Illinois at Urbana-Champaign, and by the National Science Foundation under Grant No. NSF DMR 08-56321.

- M. Imada, A. Fujimori, and Y. Tokura, Rev. Mod. Phys. 70, 1039 (1998).
- [2] L.F. Feiner, A.M. Oles, and J. Zaanen, Phys. Rev. Lett. 78, 2799 (1997).
- [3] V. Tsurkan et al., J. Phys. Chem. Solids 66, 2036 (2005).
- [4] B. Canals and C. Lacroix, Phys. Rev. Lett. 80, 2933 (1998).
- [5] N. Büttgen et al., New J. Phys. 6, 191 (2004).
- [6] A. P. Ramirez et al., Nature (London) **399**, 333 (1999).
- [7] S. B. Lee and L. Balents, Phys. Rev. B 78, 144417 (2008).
- [8] S.-H. Lee *et al.*, Phys. Rev. Lett. **84**, 3718 (2000); A.B.
  Sushkov *et al.*, Phys. Rev. Lett. **94**, 137202 (2005); M.
  Matsuda *et al.*, Nature Phys. **3**, 397 (2007).
- [9] M. Onoda and J. Hasegawa, J. Phys. Condens. Matter 15, L95 (2003); H. Tsunetsugu and Y. Motome, Phys. Rev. B 68, 060405(R) (2003); S.-H. Lee *et al.*, Phys. Rev. Lett. 93, 156407 (2004); T. Suzuki *et al.*, Phys. Rev. Lett. 98, 127203 (2007).
- [10] J.-H. Chung et al., Phys. Rev. B 77, 054412 (2008).
- [11] G.B. Jensen and O.V. Nielsen, J. Phys. C 7, 409 (1974).
- [12] B. Chardon and F. Vigneron, J. Magn. Magn. Mater. 58, 128 (1986).
- [13] J.F. Karpus et al., Phys. Rev. Lett. 93, 167205 (2004).
- [14] C. M. Julien and M. Massot, J. Phys. Condens. Matter 15, 3151 (2003); B. Ammundsen *et al.*, J. Phys. Chem. B 103, 5175 (1999); L. Malavasi *et al.*, Phys. Chem. Chem. Phys. 4, 3876 (2002); following these references we use the cubic space group notation to index the Raman-active phonons in tetragonal Mn<sub>3</sub>O<sub>4</sub>.
- [15] D. Mihailovic, K. F. McCarty, and D. S. Ginley, Phys. Rev. B 47, 8910 (1993).
- [16] B. Boucher, R. Buhl, and M. Perrin, J. Phys. Chem. Solids 32, 2429 (1971).
- [17] K. Dwight and N. Menyuk, Phys. Rev. 119, 1470 (1960).
- [18] F. Nakamura *et al.*, Phys. Rev. B **65**, 220402(R) (2002); P. Steffens *et al.*, Phys. Rev. B **72**, 094104 (2005).
- [19] T. Suzuki and T. Katsufuji, Phys. Rev. B 77, 220402(R) (2008); R. Tackett *et al.*, Phys. Rev. B 76, 024409 (2007).
- [20] R. Coldea et al., Science 327, 177 (2010).