

## Ferromagnetism and Electronic Structures of Nonstoichiometric Heusler-Alloy $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$ Epilayers Grown on Ge(111)

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For the study of ferromagnetic materials which are compatible with group-IV semiconductor spintronics, we demonstrate control of the ferromagnetic properties of Heusler-alloy  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  epitaxially grown on Ge(111) by tuning the Mn composition  $x$ . Interestingly, we obtain  $L2_1$ -ordered structures even for nonstoichiometric atomic compositions. The Curie temperature of the epilayers with  $x \approx 0.6$  exceeds 300 K. Theoretical calculations indicate that the electronic structures of the nonstoichiometric  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  alloys become half-metallic for  $0.75 \leq x \leq 1.5$ . We discuss the possibility of room-temperature ferromagnetic  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}/\text{Ge}$  epilayers with high spin polarization.

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By introducing spin degrees of freedom into group-IV semiconductor-based electronic devices, it becomes possible to add novel functions to existing silicon large-scale integrated circuit (LSI) technologies [1–5]. Group-IV semiconductor spintronics also enables us to overcome the scaling limits of silicon-based complementary metal–oxide–semiconductor devices. To realize highly efficient spin injection and detection in group-IV semiconductor devices, it is crucial to develop compatible ferromagnetic materials, which can be grown epitaxially on Si and/or Ge, with high spin polarization and high Curie temperature. In this context, we have focused on ferromagnetic full Heusler alloys with the chemical formula  $X_2YZ$ , where  $X$  and  $Y$  are transition metals and  $Z$  is a main group element such as Si and Ge. In general, full Heusler alloys become half-metallic ferromagnets (HMFs) with a fully spin-polarized density of states (DOS) at the Fermi level (100% spin polarization) [6–9].

Recently, we demonstrated highly epitaxial growth of ferromagnetic Heusler-type alloys, including  $\text{Fe}_3\text{Si}$  and  $\text{Fe}_2\text{MnSi}$  thin films, on the group-IV semiconductors Si and Ge, using low-temperature molecular beam epitaxy (LT-MBE) [10–12]. Note that the interface between these ferromagnets and Si or Ge has atomic-scale abruptness and an ordered structure can be obtained in spite of low-temperature growth at 130° and 200 °C [10–12]. Since  $\text{Fe}_3\text{Si}$  has a high Curie temperature above 800 K, we can expect that spin devices made with this material will exhibit room-temperature operation. For this material, the highest reported spin polarization to date is  $|P| \sim 45 \pm 5\%$  [13].  $\text{Fe}_2\text{MnSi}$  is predicted to be an HMF [14,15], and it is anticipated that this material can be successfully applied to

highly efficient spin injection and detection through Schottky tunnel barriers in group-IV semiconductor devices. However, epitaxial  $\text{Fe}_2\text{MnSi}$  thin films have a Curie temperature of  $\sim 210$  K, which is much lower than room temperature [11]. To realize group-IV semiconductor spintronics, we require a convenient ferromagnetic material that simultaneously exhibits the advantages of the above two characteristics, namely, an HMF with a high Curie temperature.

The study of bulk  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$ , reported by Yoon and Booth [16], shows that the magnetic properties can be tuned by controlling the Mn composition  $x$ . Bulk samples with  $x \leq 0.85$  yield room-temperature ferromagnetism, although we note that the samples were fabricated only by high-temperature annealing (800 °C) and rapid quenching. In this Letter, we focus on *epitaxial*  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  layers grown on a group-IV semiconductor Ge for use in semiconductor-based spintronic applications. We demonstrate control of the ferromagnetic properties of  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  and achieve room-temperature ferromagnetic epilayers with an ordered  $L2_1$  structure even for nonstoichiometric atomic compositions. Theoretical calculations suggest that  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  alloys with compositions in the range  $0.75 \leq x \leq 1.5$  become HMFs. We confirm that a high spin polarization ( $P \geq 0.9$ ) can be achieved for compositions in the range  $0.5 \leq x \leq 0.75$ . We also discuss the possibility of room-temperature ferromagnetic  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}/\text{Ge}$  epilayers with a high spin polarization.

$\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  layers with a thickness of  $\sim 50$  or  $\sim 100$  nm were grown on  $n$ -type Ge (111) by molecular beam epitaxy (MBE). We employed a surface cleaning process described in a previous work [11]. Prior to the growth of the

$\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  layers, 30 nm-thick Ge buffer layers were grown at 400 °C with a growth rate of 0.60 nm/min. After confirming streak patterns by *in situ* reflection high energy electron diffraction (RHEED), the substrate temperature was reduced to 200 °C. Using Knudsen cells, we coevaporated Fe, Mn, and Si. In order to change the Mn composition  $x$ , the growth rate of Mn was tuned by adjusting the cell temperature. After the growth, we observed RHEED patterns of the  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  layers for various  $x$ , as shown in Fig. 1(a). We determined  $x$  by energy dispersive x-ray spectroscopy and Rutherford backscattering spectroscopy measurements. All the RHEED patterns clearly show symmetrical streaks, indicating good two-dimensional epitaxial growth of the  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  layers on Ge(111). We note that even for nonstoichiometric atomic compositions, epitaxial growth is indicated.

For the 100 nm-thick epilayers, we performed structural characterization by high-resolution x-ray diffraction with  $\text{CuK}\alpha$  radiation. As described in Ref. [11], since the (111) diffraction peak of the  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  layers could not be separated from the Ge(111) peak in  $\theta$ - $2\theta$  scans, we could not measure the out-of-plane lattice constant. To separate the diffraction peaks of the Ge substrate from those of the  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  layers, we measured reciprocal space maps for  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}(224)$ , together with Ge (331). Assuming a cubic crystal structure, we can estimate the lattice constant for various  $x$  from the (224) spacing  $d_{224}$ . A plot of lattice constant (calculated from  $d_{224}$ ) vs  $x$  is displayed in Fig. 1(b), together with that of an epitaxial  $\text{Fe}_3\text{Si}$  ( $x = 0$ ) layer grown on Ge(111) [10]. The figure shows that the lattice constant lengthens almost linearly with increasing  $x$ . This tendency is in good agreement with that of bulk samples in previous works [16,17]. This result indicates that the doped Mn is systematically tuned. We also present cross-sectional selected-area diffraction (SAD) patterns of an  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  epilayer with  $x \approx 0.6$  in Fig. 1(c). The SAD patterns clearly show superlattice reflections due to

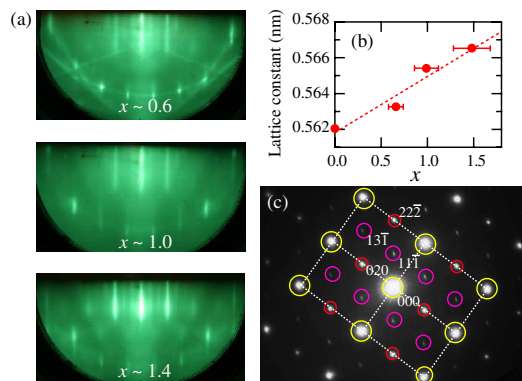


FIG. 1 (color online). (a) RHEED patterns observed along the  $[\bar{2}11]$  azimuth for  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  layers grown at 200 °C with  $x \approx 0.6, 1.0,$  and  $1.4$ . (b) Lattice constant calculated from  $d_{224}$  vs  $x$ . (c) Cross-sectional selected-area diffraction patterns for  $x \approx 0.6$ . The zone axis is parallel to the  $[101]$  direction.

the presence of the ordered  $L2_1$  structure, indicated by the pink solid circles. The two other diffraction patterns express the fundamental and superlattice reflections, corresponding to the  $A2 + B2 + L2_1$  (yellow) and the ordered  $B2 + L2_1$  structures (red), respectively. Namely, the  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  epilayers include the ordered  $L2_1$  structure even for nonstoichiometric atomic compositions.

Using a superconducting quantum interference device (SQUID) magnetometer, we measured the magnetic properties of  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  epilayers for various  $x$ . Figure 2(a) shows the field-dependent magnetization plot ( $M$ - $H$ ) for  $x \approx 0.6, 1.0,$  and  $1.4$  at 7 K, where the vertical axis expresses the magnetic moment per formula unit. The magnetic field is applied parallel to the film plane with crystal orientation  $[111]$ . All the epilayers exhibit clear ferromagnetic hysteretic curves and the shape of the  $M$ - $H$  curves varies slightly for changes in  $x$ . For  $x \approx 0.6$ , the coercivity is quite small compared to that of  $\text{Fe}_2\text{MnSi}/\text{Ge}$  layers (i.e.,  $x = 1$ ) [11] and is similar to that of  $\text{Fe}_3\text{Si}/\text{Ge}$  layers [10,13,18]. The saturation magnetization ( $M_s$ ) at 7 K is summarized for various  $x$  in Fig. 2(b).  $M_s$  gradually changes with doping Mn composition [16]. Figure 2(c) shows the temperature-dependent magnetization plot ( $M$ - $T$ ) for various  $x$  in a small magnetic field of 20 Oe, where the magnetization is normalized by that at 7 K ( $M/M_{7\text{K}}$ ). For  $x \approx 1.0$  (nearly stoichiometric composition),  $M/M_{7\text{K}}$  disappears at  $\sim 230$  K, i.e., a Curie temperature ( $T_C = 230$  K), largely consistent with that of bulk  $\text{Fe}_2\text{MnSi}$  samples [15,19]. For a nonstoichiometric composition of  $x \approx 0.6$  or  $1.4$ ,  $T_C$  becomes higher or lower

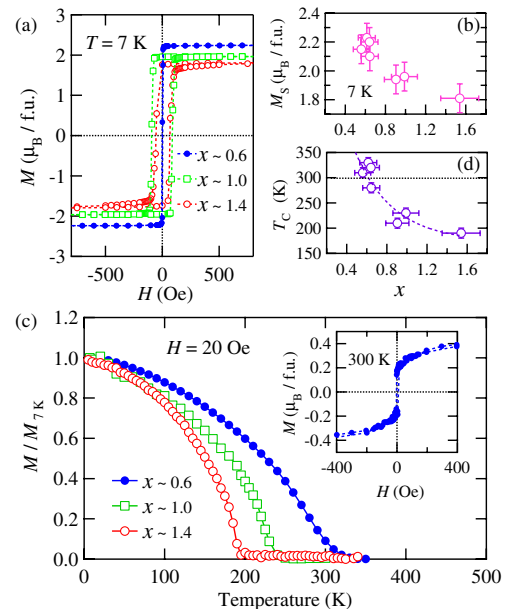


FIG. 2 (color online). (a)  $M$ - $H$  curves of  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  epilayers for various  $x$ , measured at 7 K. (b)  $M_s$  vs  $x$  at 7 K. (c) Temperature dependence of the normalized magnetization for three samples with  $x \approx 0.6, 1.0,$  and  $1.4$ . The inset shows the  $M$ - $H$  curve for  $x \approx 0.6$ , measured at 300 K. (d)  $T_C$  vs  $x$ .

than 230 K, respectively. It should be noted that for  $x \approx 0.6$ , finite magnetic moments are observed at 300 K. We also measured the  $M$ - $H$  curve at 300 K, as shown in the inset of Fig. 2(c), and an evident ferromagnetic feature can be seen, i.e., room-temperature ferromagnetism. Figure 2(d) displays  $T_C$  as a function of  $x$ .  $T_C$  also systematically changes with varying  $x$  and room-temperature ferromagnetism is obtained at  $x \approx 0.6$ . These results demonstrate that our LT-MBE technique can realize control of ferromagnetism of  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  epilayers. We emphasize that the room-temperature ferromagnetic  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  epilayers include an  $L2_1$ -ordered structure, as described in Fig. 1(c).

In order to discuss the electronic structure of the examined  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  with nonstoichiometric atomic compositions ( $0 \leq x \leq 1.5$ ), we carried out first-principles band calculations using the Vienna *ab initio* simulation package (VASP) [20]. The calculations are based on density functional theory (DFT) in the generalized gradient approximation (GGA). Although the electronic structure of  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  has been studied for  $0 \leq x \leq 0.5$  [21] using the TB-LMTO-ASA method [22], the electronic structure for  $x > 0.5$  has not yet been clarified. We hereafter consider that the crystal lattice structures of  $\text{Fe}_3\text{Si}$  and  $\text{Fe}_2\text{MnSi}$  are  $DO_3$  and  $L2_1$  types, respectively, and that the unit cell is composed of four interpenetrating fcc sublattices originating at A: (0,0,0), B: ( $\frac{1}{4}, \frac{1}{4}, \frac{1}{4}$ ), C: ( $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$ ), and D: ( $\frac{3}{4}, \frac{3}{4}, \frac{3}{4}$ ). For both  $\text{Fe}_3\text{Si}$  and  $\text{Fe}_2\text{MnSi}$ , (A, C) sites and D sites are occupied by Fe atoms and Si atoms, respectively, and B sites are occupied by Fe atoms for  $\text{Fe}_3\text{Si}$  and by Mn atoms for  $\text{Fe}_2\text{MnSi}$ . For nonstoichiometric compositions, we consider supercells consisting of eight atoms ( $x = 0.5$ ), 16 atoms ( $x = 0.25, 0.75, 1.25$ , and  $1.5$ ), 32 atoms ( $x = 0.125$  and  $0.875$ ), and 128 atoms ( $x = 0.625$ ). For  $0 < x \leq 1$ , we assume that Mn atoms enter B sites, as indicated by previous experiments [16]. For  $1 < x \leq 1.5$ , we assume that all B sites and some (A, C) sites are occupied by Mn atoms. Figures 3(a) and 3(b) show the densities of states (DOS),  $D_\sigma(E)$ , calculated for spin-up ( $\sigma = \uparrow$ ) and spin-down ( $\sigma = \downarrow$ ) states, respectively. Here, we used a lattice constant  $a_0$  optimized theoretically for  $L2_1$ -ordered  $\text{Fe}_2\text{MnSi}$ . For the stoichiometric composition  $x = 1$ , the Fermi level ( $E_F$ ) is situated within the band gap of the down-spin band, i.e., the electronic structure is half-metallic, which is consistent with previous predictions [14,15]. We note that a half-metallic electronic structure can be seen even for a nonstoichiometric composition of  $x = 0.75$ . We define the spin polarization  $P$  of the DOS as  $[D_\uparrow(E_F) - D_\downarrow(E_F)]/[D_\uparrow(E_F) + D_\downarrow(E_F)]$ . Then, the half-metallic electronic structure ( $P = +1$ ) is obtained in the range  $0.75 \leq x \leq 1.5$ . With decreasing  $x$ , the half-metallicity tends to be lost and  $P$  begins to decrease, but a high spin polarization of  $P = 0.9$  remains down to  $x = 0.5$ . When  $x$  is further reduced,  $P$  decreases steeply and takes a negative value of  $P = -0.36$  for  $x = 0$ . It might be

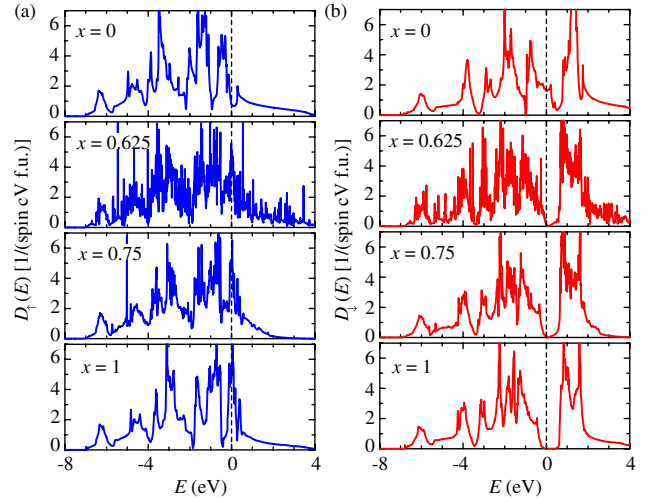


FIG. 3 (color online). Densities of states for (a) spin-up ( $\uparrow$ ) and (b) spin-down ( $\downarrow$ ) states of cubic  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  for  $x = 0, 0.625, 0.75$ , and  $1$ . The Fermi level is chosen as the origin of energy.

worth noting that the magnetic moment obtained for the half-metallic state ( $0.75 \leq x \leq 1.5$ ) is well explained by the Slater-Pauling behavior of the full Heusler alloys [23].

We also investigated theoretically how the electronic structure of  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  is affected by lattice distortion under biaxial compressive or tensile strain. Assuming (001) stacking and a constant volume of the unit cell, we introduce a tetragonal distortion,  $a^2c = a_0^3$ , where  $a$  and  $c$  are in-plane and out-of-plane lattice constants, respectively. Figure 4 shows a contour plot of  $P$  obtained for various  $x$  and  $c/a$ . It is clear that  $P$  gradually decreases with increasing lattice distortion. For the half-metallicity of  $X_2\text{MnZ}$  Heusler compounds, it is known that the energy level splitting between the  $t_{2g}$  and  $e_g$  orbitals of the  $X$  ions due to the crystal field in cubic symmetry is a crucial factor [23]. As the crystal lattice deviates from cubic (i.e.,  $c/a$  deviates from 1), the energy splitting shrinks and then the half-metallicity is lost, causing a decrease in  $P$ . However, we find that the half-metallicity is stable in a relatively wide range of  $x$  and  $c/a$  for the  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  systems considered here. In experiments, although the bulk lattice

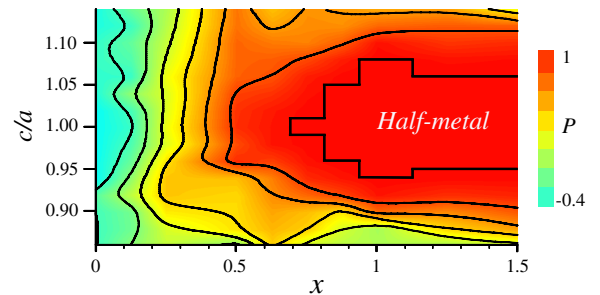


FIG. 4 (color online). Contour plot of spin polarization  $P$  as functions of  $x$  and  $c/a$ , where the contour lines are drawn at intervals of  $|P| = 0.2$ .



constant of  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  ( $x \approx 1$ ) has been reported to be  $0.5665 \sim 0.5672$  nm [15–17,19], that of our epilayer shown in Fig. 1(b) becomes  $\sim 0.5654$  nm, slightly smaller than the bulk value. It can be considered that the estimated lattice constant of the MBE-grown epilayer includes an effect due to lattice distortion. Hence, it is important for a full description of epitaxial Heusler compounds to understand the influence of lattice distortion on the half-metallicity. We note that the lattice distortion for  $x \approx 0.6$  is quite small,  $\sim 0.7\%$ , where the converted  $c/a$  is in the range  $0.98 \leq c/a \leq 1.02$ . Therefore, we can expect that room-temperature ferromagnetic  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}/\text{Ge}$  epilayers with  $x \approx 0.6$  maintain a high spin polarization of  $P \geq 0.9$ , and this material can be used as spin injector and detector in Ge-based spintronic devices.

Because of interdiffusive solid-phase reactions [24] at the  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}/\text{Ge}$  interface, we could not utilize high-temperature processes ( $\geq 500^\circ\text{C}$ ) to fabricate the magnetic tunnel junctions with Ge or MgO high-quality tunnel barriers. Thus, we cannot estimate the spin polarization of the  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  epilayers experimentally. To advance the next step for group-IV-semiconductor spintronics, we should further explore a method for the thermal stabilization of the Heusler compounds/Ge interfaces.

In summary, we have explored control of ferromagnetism and electronic structure of Heusler compounds  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}/\text{Ge}$  epitaxially grown on a group-IV semiconductor Ge. By tuning the Mn composition  $x$  during LT-MBE growth, the saturation magnetization and Curie temperature can be controlled and we can fabricate  $L2_1$ -ordered structures, even for nonstoichiometric atomic compositions. We demonstrated that for a composition of  $x \approx 0.6$ , the Curie temperature exceeds 300 K. Theoretical calculations suggest that  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}$  alloys with nonstoichiometric compositions in the range  $0.75 \leq x \leq 1.5$  have a half-metallic electronic structure. The effect of lattice distortion on the spin polarization  $P$  was also examined. It is expected that room-temperature ferromagnetic  $\text{Fe}_{3-x}\text{Mn}_x\text{Si}/\text{Ge}$  epilayers maintain a high spin polarization of  $P \geq 0.9$ .

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