

## Frustration-Induced Valence Bond Crystal and Its Melting in $\text{Mo}_3\text{Sb}_7$

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$^{121/123}\text{Sb}$  nuclear quadrupole resonance and muon spin relaxation experiments of  $\text{Mo}_3\text{Sb}_7$  revealed symmetry breakdown to a nonmagnetic state below the transition recently found at  $T_S \approx 50$  K. The transition is characterized by a distinct lattice dynamics suggested from narrowing of nuclear fields. We point out that the Mo sublattice is a unique three-dimensional frustrated lattice where nearest-neighbor and next-nearest-neighbor antiferromagnetic interactions compete, and propose that tetragonal distortion to release the frustration stabilizes long-range order of spin-singlet dimers, i.e., valence bond crystal, which is thermally excited to the dynamic state with cubic symmetry.

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Exotic phenomena induced by the geometric frustration have attracted great interest, and the attempt to find novel phases has been ongoing [1]. In the case of three-dimensional (3D) pyrochlore lattice, the symmetry breakdown to spin-Peierls-like states or to the valence bond crystal with the quenched spin degrees of freedom [2,3] is one of the options to release the frustration; a typical example is found in the case of  $\text{MgTi}_2\text{O}_4$  [4].

A metallic compound  $\text{Mo}_3\text{Sb}_7$ , with the cubic  $\text{Ir}_3\text{Ge}_7$  type structure (space group  $Im\bar{3}m$ ), is a superconductor with a critical temperature  $T_c \approx 2.3$  K [5]. The Mo sublattice (12e), shown in the inset of Fig. 1(a), is a 3D network of Mo-Mo dumbbells formed by nearest neighbors (NN), while next-nearest-neighbor (NNN) bonds form an octahedral cage at the body-centered position (respective interactions are referred to as  $J_1$  and  $J_2$ ). The short NN distance (3.0 Å) compared with the NNN distance (4.6 Å) tends to dimerize the NN pairs. On the other hand, in an extreme case with  $J_1 = 0$  and  $J_2 < 0$ , where the negative sign corresponds to antiferromagnetic (AFM) interaction, the typical 3D frustration emerges in the NNN regular octahedron. These facts make us anticipate unusual competition between intradimer and interdimer interactions. Recently, Candolfi *et al.* [6] regarded  $\text{Mo}_3\text{Sb}_7$  as an itinerant electron system and suggested coexistence of superconductivity and spin fluctuations, which is a rare example in  $d$  electron metals. A broad maximum in the temperature ( $T$ ) dependence of the susceptibility ( $\chi$ ), a large electronic specific heat coefficient, a  $T^2$  dependence of low- $T$  electrical resistivity, the Kawasaki-Wood relation between the specific heat and the resistivity, etc., point to the presence of strong electron correlation. Band structure calculations for cubic  $\text{Mo}_3\text{Sb}_7$  [7,8], showing appreciable contribution of Mo-4d orbitals to the density of states near the Fermi level  $D(E_F)$ , are in agreement with these observations. Although no phase transition other than that at  $T_c$  was known in [6], Tran *et al.* [9] reported recently the presence of another phase transition at  $T^* \approx 50$  K (in this Letter,

referred to as  $T_S$ ), and proposed spin gap formation with the magnitude of 120 K associated with Mo-Mo dimerization. In fact at sufficiently high  $T$ ,  $\chi$  shows a  $S = 1/2$  Curie-Weiss behavior (for  $\text{Mo}^{5+}$ ) with a large negative Weiss temperature, suggesting strong AFM interaction among active Mo spins. Thus the Mo electronic state is of interest as the system with both itinerant and localized characters. Furthermore,  $\text{Mo}_3\text{Sb}_7$  is now recognized as a new material with another phase transition prior to superconductivity; the pairing mechanism is still controversial [5,8–13].

In this Letter, to study microscopic and dynamic magnetism in  $\text{Mo}_3\text{Sb}_7$ , particularly to identify the phase between  $T_c$  and  $T_S$ , we present  $^{121/123}\text{Sb}$  nuclear quadrupole resonance (NQR) and muon spin relaxation ( $\mu\text{SR}$ ) results together with low- $T$  x-ray diffraction (XRD) data. We

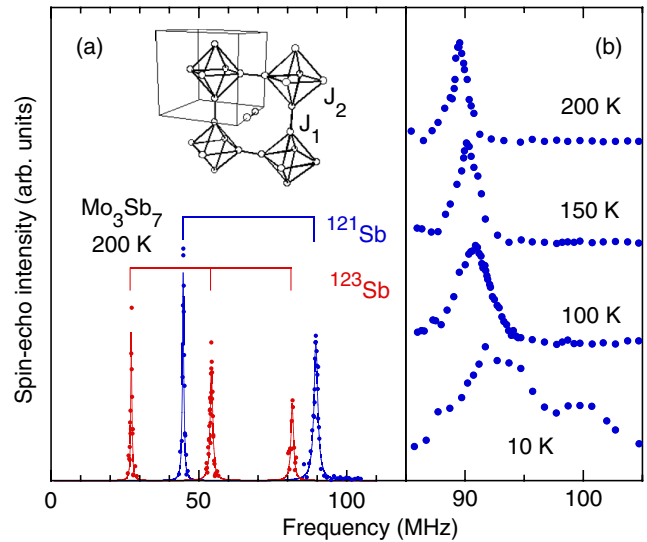


FIG. 1 (color online). (a)  $^{121/123}\text{Sb}$  NQR spectrum of  $\text{Mo}_3\text{Sb}_7$  at 200 K. Inset shows the Mo sublattice. (b)  $T$  variation of  $^{121}\text{Sb}$ - $2\nu_Q$  line.

discuss possible frustration in the Mo sublattice by assuming negative  $J_1$  and  $J_2$ , and propose new exotic states realized due to competing  $J_1$  and  $J_2$ .

Polycrystalline  $\text{Mo}_3\text{Sb}_7$  specimen were prepared via reaction between liquid Sb and solid Mo. NQR spin-echo measurements were carried out using a conventional phase-coherent-type pulse spectrometer at 1.4–200 K. Zero-field (ZF)  $\mu\text{SR}$  measurements were made at the RIKEN-RAL Muon Facility at the Rutherford-Appleton Laboratory using a pulsed positive surface muon beam at 5–250 K. Low- $T$  powder XRD was measured using a conventional diffractometer (MacScience MXP) with  $\text{Cu } K\alpha$  radiation.

NQR probes both static and dynamic local magnetic field as well as electric field gradient (EFG) at the nuclear site. Figure 1(a) shows the  $^{121/123}\text{Sb}$  NQR spectrum of  $\text{Mo}_3\text{Sb}_7$  at 200 K. Antimony has two isotopes  $^{121}\text{Sb}$  (nuclear spin  $I = 5/2$ ) and  $^{123}\text{Sb}$  ( $I = 7/2$ ), which yield two and three quadrupole transition lines, respectively. In cubic  $\text{Mo}_3\text{Sb}_7$ , there are two nonequivalent Sb sites with non-axial and axial symmetries ( $12d$  and  $16f$ , respectively). We have found only five lines at 200 K corresponding to either site. This is probably because the nuclear spin relaxation rate at the unobserved site is enhanced due to fast fluctuations of active Mo electron spins. The frequency intervals between neighboring lines of  $^{121/123}\text{Sb}$  are approximately equal, indicating nearly axial EFG at the observed site.  $^{121/123}\text{Sb}$  quadrupole frequencies are  $^{121/123}\nu_Q \approx 47.7/27.2$  MHz at 200 K.

The  $T$  dependence of the  $^{121}\text{Sb}$ - $2\nu_Q$  line (transitions of  $|\pm 3/2\rangle \leftrightarrow |\pm 5/2\rangle$ ) is shown in Fig. 1(b). The line is shifted to the high frequency side and gradually broadened on cooling towards  $T_S$ . At  $\sim T_S$ , the line loses intensity and disappears due to highly enhanced spin-echo decay rate  $1/T_2$  (see the inset of Fig. 2, which will be recalled below). Below 20 K the signal reappears with complicated struc-

tures [see the data at 10 K in Fig. 1(b)]. Actually, ZF nuclear resonance signal was continuously observed in almost the whole frequency range below 110 MHz with a number of peaks. This indicates clearly symmetry breakdown below  $T_S$ . The origin is either appearance of the internal field (due to magnetic order), separation of crystallographic Sb sites (due to structural deformation), or both. Unfortunately, the spectrum at low  $T$  is too complicated and unresolved to conclude this issue because of line split together with broadening, as well as the possible emergence of the signal from another Sb site. An early  $^{121}\text{Sb}$  Mössbauer study was not conclusive either [14]. Hence, to determine the magnetic ground state, we employ another microscopic probe,  $\mu\text{SR}$ ; the result will be presented later.

The nuclear spin-lattice relaxation rate  $1/T_1$ , giving information on electron spin fluctuations via hyperfine coupling, was measured for both  $^{121}\text{Sb}$ - and  $^{123}\text{Sb}$ - $2\nu_Q$  transitions. The ratio of relaxation rates for the different isotopes is  $^{123}T_1/^{121}T_1 \approx 3.5$  at  $T > T_S$ , being close to the squared gyromagnetic ratios  $^{121}\gamma_n^2/^{123}\gamma_n^2 \approx 3.4$ . This confirms that the relaxation process is not by fluctuations of EFG but by those of the internal magnetic field at least above  $T_S$ . The  $T$  dependence of  $1/T_1$  measured for  $^{121}\text{Sb}$  is plotted in the form of  $1/(T_1T)$  vs  $T$  in Fig. 2 [15]. The divergent behavior was observed at  $\sim T_S$ , although reliable values of  $1/T_1$  could not be obtained near  $T_S$  due to poor signal-to-noise ratio. In fact, the transition at  $T_S$  is characterized by the stronger  $T$  dependence of  $1/T_2$  (the inset of Fig. 2):  $1/T_2 \sim 10\text{--}10^3(1/T_1)$ . This implies the presence of anomaly in the nuclear spin-spin coupling, being rare in the electronic spin transition. Below  $T_S$ ,  $1/(T_1T)$  decreases rapidly with decreasing  $T$ , being consistent with the possible existence of spin gap [9], but turns to show a  $T_1T = \text{const}$  Korringa behavior below  $\sim 10$  K, indicating the presence of residual  $D(E_F)$ .  $1/T_1$  is enhanced just below  $T_c$ , which is known as a coherence peak for the conventional BCS superconductor with an isotropic gap [16].

Now we shift to  $\mu\text{SR}$  results. Being different from NQR,  $\mu\text{SR}$  probes only the magnetic field, and is very sensitive to the appearance and variation of the internal field. Typical examples of ZF- $\mu\text{SR}$  spectra are shown in the inset of Fig. 3. Even at the lowest  $T$  (5 K), no straightforward evidence of magnetic order such as muon spin precession was observed. At all  $T$ , the feature of relaxation is essentially the same and shows Gaussian-like depolarization. The commonly used damped Kubo-Toyabe (KT) function  $P_\mu(t) = \exp(-\Lambda t)G_z^{\text{KT}}(\Delta, t)$  with  $G_z^{\text{KT}}(\Delta, t) = \frac{1}{3} + \frac{2}{3}(1 - \Delta^2 t^2) \exp(-\frac{1}{2}\Delta^2 t^2)$  was fit to the data, where  $\Delta/\gamma_\mu$  is the width of the static field distribution ( $\gamma_\mu$  the muon gyromagnetic ratio), and  $\Lambda$  is the damping rate associated with an additional relaxation process. As seen below, the KT term is dominated by the nuclear dipolar field  $H_n$  and the damping part reflects the Mo electronic system. Figure 3 shows the  $T$  dependence of  $\Delta$ . First, let us see the  $T$ -independent part in the intermediate  $T$  range of

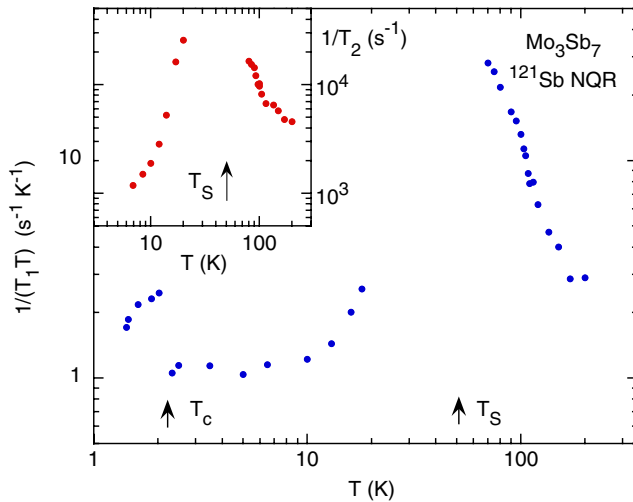


FIG. 2 (color online).  $T$  dependence of  $^{121}\text{Sb}$ - $1/(T_1T)$  and  $1/T_2$  (inset) for  $\text{Mo}_3\text{Sb}_7$ .

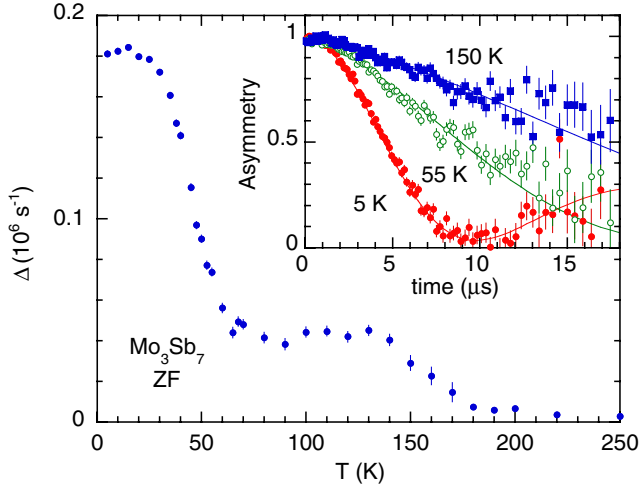


FIG. 3 (color online).  $T$  dependence of the ZF Kubo-Toyabe relaxation rate  $\Delta$  in  $\text{Mo}_3\text{Sb}_7$ . Inset shows typical examples of ZF- $\mu\text{SR}$  spectra (at 5, 55, and 150 K). Solid curves indicate the fit by the damped KT function.

$\sim 70$ – $140$  K with  $\Delta/\gamma_\mu \approx 0.5$  G. This tiny field is most probably due to dipolar fields coming from randomly oriented nuclear spins. Above  $\sim 140$  K,  $\Delta$  is reduced markedly. As shown in Fig. 4,  $\ln\Delta$  is in proportion to  $1/T$  in the  $T$  range, suggesting a motional narrowing process caused by muon hopping among different sites, that is frequently observed at high  $T$ . With decreasing  $T$  passing through  $T_S$ ,  $\Delta$  is enhanced strongly as seen in Fig. 3. The origin of the additional internal field below  $T_S$  is the most essential point in this experiment. The Gaussian-type random distribution with small  $\Delta/\gamma_\mu \approx 2.1$  G even at the lowest  $T$  is hardly attributed to the electron spin freezing but is reasonably explained as due to the change in  $H_n$  associated with the

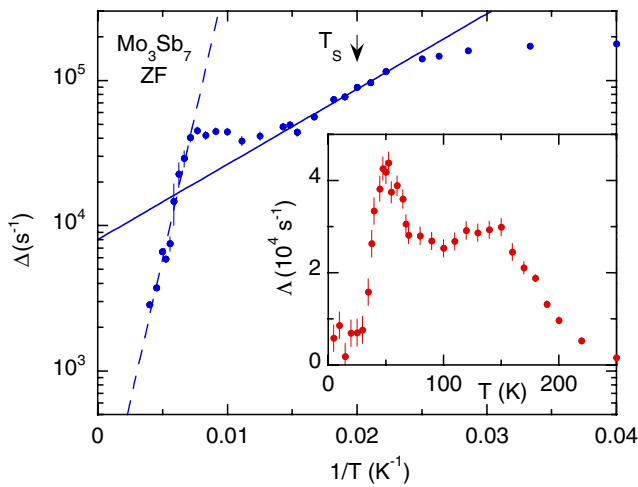


FIG. 4 (color online). ZF Kubo-Toyabe relaxation rate  $\Delta$  in  $\text{Mo}_3\text{Sb}_7$  plotted against  $1/T$ . Activation energies for two different thermal excitation processes are estimated to be 120 and 910 K from the solid line and broken line, respectively. Inset shows  $T$  dependence of the relaxation rate  $\Delta$ .

structural deformation mentioned below. The  $T$  dependence of  $\Delta$  at  $\sim T_S$  is again explained as a thermal excitation process with activation energy of  $E_a/k_B \approx 120$  K. This  $T$  variation, without critical divergence, implies that a principal part of field fluctuations is dominated by *dynamic* process of nuclear spins, i.e., of lattice. In other words, electron spin fluctuations, which should show a critical behavior at  $T_S$ , is relatively less enhanced at the muon site. This result gives very fruitful information on the nature of the transition at  $T_S$ , as discussed below.

The  $T$  dependence of  $\Delta$ , which also gives information on the Mo electronic spin fluctuations as  $\text{NQR}-1/T_1$ , is shown in the inset of Fig. 4. The decrease above  $\sim 150$  K would be an analytical artifact due to the evolution of the relaxation process associated with the dynamic muon hopping.  $\Delta$  has a sharp peak at  $T_S$  and decreases rapidly below  $T_S$ . This behavior is qualitatively the same as that of  $\text{NQR}-1/T_1$ . The quantitative difference in  $\text{NQR}-1/T_1$  and  $\mu\text{SR}-\Delta$  is most probably due to the difference in the coupling mechanism; the interaction between Sb nuclei and Mo electrons is probably dominated by the direct hyperfine coupling, while fields from Mo electrons to the muon site are by the dipolar mechanism. Different time windows of the measurements would also be appreciable. Furthermore, the muon stopping site may be a high symmetric position, say the center of the Mo cage, where the fields from Mo electron spins would mostly be canceled.

To get information on the lattice symmetry below  $T_S$ , we made conventional XRD analyses at low  $T$  and found appreciable difference in the patterns below and above  $T_S$ . To see the change efficiently, we particularly show (600) diffraction peaks at 70 and 15 K in Fig. 5(a) [17]. A high- $T$  singlet splits into double peaks with the intensity ratio of  $\sim 2:1$  by crossing  $T_S$ , suggesting structural deformation from cubic to tetragonal (space group  $I4/mmm$ ) as

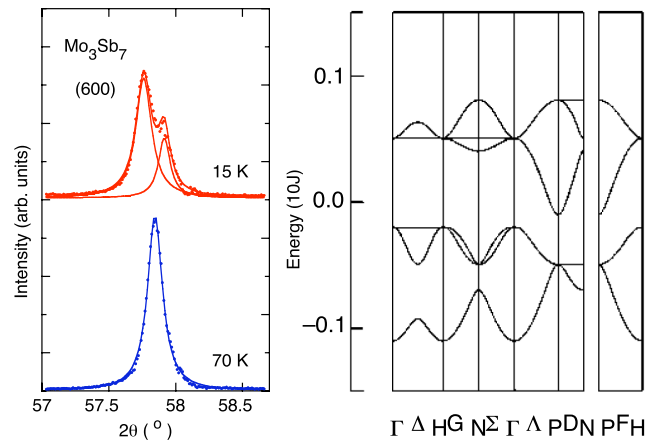


FIG. 5 (color online). (a) X-ray (600) peak of  $\text{Mo}_3\text{Sb}_7$  at 70 K and its split pattern at 15 K [17]. The  $K\alpha_2$  contribution is subtracted by profile fitting. (b) Dispersion curves of the exchange integral  $J(q)$  of the Mo sublattice assuming negative  $J_1$  and  $J_2$ .  $J_1 = -0.05$  and  $J_2 = 0.3J_1$  were used arbitrarily.

the simplest possibility; the lattice parameter  $a$  is larger than  $c$  by  $\sim 0.2\%$  at 15 K.

Although  $\text{Mo}_3\text{Sb}_7$  is a metallic magnet, here we focus on the local nature of the Mo electron. Taking a look at the Mo sublattice, if  $J_1$  is dominant, no substantial symmetry breakdown is necessary to form dimers since Mo-Mo dumbbells run along [100], [010], and [001] equally. Therefore in discussing the mechanism of the transition, the low- $T$  lattice symmetry is essential and  $J_2$  should be taken into account. Note that positive  $J_2$  as suggested in [9] does not destabilize the cubic state. Here assuming negative  $J_1$  and  $J_2$ , we calculated eigenvalues of their Fourier transform  $J(q)$  for the cubic state in the scheme of the linear combination of atomic orbitals approximation; see Fig. 5(b). A flat dispersion of  $J(q)$  found along the highest  $P$ -( $D$ )- $N$  branch indicates macroscopic degeneracies of AFM ground states [18]; the Mo sublattice is not fully frustrated like pyrochlore but is frustrated for all AFM states with  $\mathbf{q} = (\frac{1}{2} \frac{1}{2} \xi)$  with arbitrary  $\xi$ . We also confirmed that the suggested tetragonal deformation lifts the degeneracies. Thus we conclude that the cubic structure is unstable for negative  $J_2$ . The lattice deformation may be spin-frustration-driven symmetry breakdown like the spin Jahn-Teller (JT) effect [2]. The strong  $T$  dependence of  $1/T_1$  at  $\sim T_S$ , being unlikely for a classical JT transition, suggests enhanced spin fluctuations and the spin-driven mechanism. In  $\text{Mo}_3\text{Sb}_7$ , the spin frustration triggers the tetragonal deformation to decouple the 3D isotropic AFM interaction, and stabilizes spatial long-range order of spin-singlet dimers, i.e., the valence bond crystal. As the reduced  $\chi$  from higher  $T$  ( $\gg T_S$ ) and the considerably broadened specific heat ( $C$ ) anomaly were reported [9], this state is realized instead of long-range AFM order due to strong intradimer coupling already developed from sufficiently high  $T$ .

Taking account of the motional narrowing of  $H_n$  observed by  $\mu\text{SR}$  at  $\sim T_S$ , and structural characteristics of the low- $T$  phase, we propose a scenario for the transition. First, note that the deformed states along the [100], [010], and [001] directions are degenerate; we refer to the corresponding Mo electronic states as  $\psi_x$ ,  $\psi_y$ , and  $\psi_z$ . We expect that the high- $T$  cubic state is the dynamic mixing of the three states, i.e.,  $(\psi_x + \psi_y + \psi_z)/\sqrt{3}$ , just like the vibronic dynamic JT state. In other words, harmonic oscillations of the valence bonds keeping strong intradimer interaction are thermally induced. The narrowing of  $\mu\text{SR}-\Delta$ , which reflects a relatively high-energy part of the dynamics, is explained naturally; at sufficiently low  $T$ , muons sense well-defined  $H_n$  from the deformed Mo sublattice, which are averaged by the dynamic atomic motion with increasing  $T$ . NQR- $1/T_2$  above  $T_S$ , which nearly follows  $\mu\text{SR}-\Delta$ , is explained by the same mechanism, while the damping below  $T_S$  is ascribed to the decoupling of the nuclear spin-spin interaction, i.e., the reduction of Sb-like nuclei due to the separation of the Sb sites in the distorted state.

In conclusion, NQR and  $\mu\text{SR}$  experiments revealed symmetry breakdown to a nonmagnetic state below  $T_S \approx 50$  K, with most probably tetragonal lattice distortion. Assuming negative  $J_1$  and  $J_2$  in the Mo sublattice, we pointed out possible frustration and proposed long-range order of spin-singlet dimers to the valence bond crystal, which transfers to the characteristic dynamic state with the cubic symmetry above  $T_S$ . The electron itinerancy and the present description focusing on the local nature should be reconciled in further studies, similarly to in other geometrically frustrated metals [19].

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