## **Speedy Sound and Cosmic Structure**

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If the speed of sound were vastly larger in the early Universe, a near scale-invariant spectrum of density fluctuations could have been produced even if the Universe did not submit to conventional solutions to the horizon problem. We examine how the mechanism works, presenting full mathematical solutions and their heuristics. We then discuss several concrete models based on scalar fields and hydrodynamical matter that realize this mechanism, but stress that the proposed mechanism is more fundamental and general.

DOI: [10.1103/PhysRevLett.100.231302](http://dx.doi.org/10.1103/PhysRevLett.100.231302) PACS numbers: 98.80.k

*1. Introduction.—*The fact that the large scales we observe today were ''out of touch'' in the early Universe is one of the greatest annoyances of standard cosmology. This ''horizon'' problem prevents a causal explanation for the observed features of our Universe, which have to be added on ''by hand'' as initial conditions. Nowhere is this more unsatisfactory than in relation to the primordial density fluctuations that seed the structures we observe today. We have measured these structures with tremendous accuracy; yet the primordial fluctuations cannot be explained in the standard scenario and remain God-given initial conditions. This weakness has motivated many revisions to the standard big bang picture, notably inflation [\[1](#page-3-0)].

Any explanation for the initial spectrum of fluctuations has to begin with a mechanism for causally connecting vast scales at the cradle. But this is barely the beginning: one then has to suggest a physical mechanism that would render these scales homogeneous but ''not quite.'' In the detail lies the hurdle: the inhomogeneities must be near scale invariant, i.e., look approximately the same on all scales, and have a well-defined amplitude, of the order of a part in 100 000. Herein lies the challenge for any structure formation scenario.

Solutions to the horizon problem rely on either accelerated expansion [\[1](#page-3-0)], a contracting phase followed by a bounce  $[2]$  $[2]$ , or a loitering early phase  $[3]$  $[3]$ . An alternative was supplied by varying speed of light (VSL) theories [[4](#page-3-3)– [7](#page-3-4)]: the idea that the early Universe operated under a much larger maximal speed, causally connecting everything. There are several implementations of this idea and structure formation has been considered in a few [\[8](#page-3-5)]. But in spite of these valiant efforts it is fair to say that VSL scenarios have so far failed to explain the cosmic structures.

In this Letter we use a varying speed of sound as a proxy for VSL. In theories containing two metrics [\[9](#page-3-6)] the speed of massless matter particles and the speed of gravity are different. This defines a frame where gravity is unaffected, but "light" travels much faster. We propose a new mechanism for producing scale-invariant fluctuations, based on a varying speed of sound. The idea mimics that of a varying speed of light. If the sound horizon shrinks, modes that start off oscillating eventually freeze out. The universe is initially homogeneous apart from small quantum or thermal fluctuations. These are left imprinted ''outside the horizon'' after the speed of sound  $c_s$  has decreased suitably.

A varying speed of sound has been considered in other guises before. We nod at  $\kappa$ -essence models, based on (scalar) field theories with nonstandard kinetic terms [\[10\]](#page-3-7). These have been used as inflationary and quintessence models, but can be adapted to implement the varying speed of sound mechanism we advocate. The cuscuton model of [[11](#page-3-8),[12](#page-3-9)] provides a related framework. We can also bypass scalar fields and simply regard the speed of sound  $c_s$  and the equation of state *w* as free phenomeno-logical parameters [\[13](#page-3-10)[,14\]](#page-3-11). Even though VSL is our leading motivation here, we stress that many other approaches may be linked with the conclusions in this Letter. A VSL implementation, however, may be required if additionally one wants to solve the flatness, the entropy, and the other problems of big bang cosmology.

*2. The mechanism.—*We shall first illustrate the mechanism in its simplest realization. Suppose that gravity remains unmodified and that we restrict ourselves to expanding universes with  $w > -1/3$ . This is to avoid confusion with inflation and ekpyrotic scenarios (although constructive alliances should be investigated). The new ingredient, now, is the assumption that the speed of sound is density dependent and diverges with conformal time like  $c_s \propto \eta^{-\alpha}$  (with  $\alpha > 0$ ; note that  $\eta$  is positive and increases from zero). A reparametrization in terms of the density will be examined later (with a striking result) but this is the most suitable expression for a mathematical solution. Concrete models realizing this setup will be presented, but we do not want to wed what follows to any one of them.

<span id="page-0-0"></span>Whether we employ a fluid or a scalar field, the density fluctuations are described by a modified harmonic oscillator equation. This can be written in terms of variables related to the Newtonian potential  $\Phi$  or the curvature perturbation  $\zeta$ , the so-called "*u*" and "*v*." The equation for *v* is  $[15-17]$  $[15-17]$  $[15-17]$ 

$$
v'' + \left[c_s^2 k^2 - \frac{z''}{z}\right]v = 0,\tag{1}
$$

where  $z \propto a/c_s$ . Thus  $c_s$  appears in two places: in the  $k^2$ term responsible for subhorizon oscillations and in the variable mass term in  $z''/z$ . The equivalent equation for *u* has a variable mass term that does not contain  $c_s$ .

As with inflation this equation can be exactly solved with Bessel functions, but we will first examine a WKB solution in order to establish the initial conditions. With  $\alpha$  > 1 modes start inside the sound horizon but eventually leave it (the horizon scale is set by  $c_s k \eta \sim 1$ , i.e.,  $k \propto$  $\eta^{1-\alpha}$ ). We can therefore initially ignore the term in  $z''/z$ . Even though the frequency  $\omega = c_s k$  is changing, the WKB condition  $\omega' \ll \omega^2$  translates into  $c_s k \eta \gg |\alpha|$ , which is always satisfied early on. This amounts to preserving the adiabatic invariants; i.e., the number of quanta in a given mode is kept fixed but not the total energy in that mode, which changes proportionally to the frequency. The appropriately normalized WKB solution is therefore

$$
v \sim \frac{e^{ik} \int c_s d\eta}{\sqrt{c_s k}} \sim \frac{e^{-\beta c_s k \eta}}{\sqrt{c_s k}},
$$
 (2)

<span id="page-1-0"></span>where  $\beta = 1/(\alpha - 1) > 0$  and in the last  $\sim$  we neglected a phase. We can also consider scenarios where  $c_s$  is initially constant, then drops like a power law. The standard boundary condition may then be imposed in the constant  $c_s$  phase and propagated using the WKB solution, with the same result.

As with the equivalent calculation in inflation, Eq. [\(1\)](#page-0-0) can be transformed into a Bessel equation, with solutions

$$
v = \sqrt{\beta \eta} [AJ_{\nu}(\beta c_s k \eta) + BJ_{-\nu}(\beta c_s k \eta)].
$$
 (3)

The order *v* is given by  $\nu = \beta(\alpha - \frac{3(1-w)}{2(1+3w)})$  and *A* and *B* are *k*-independent numbers of order 1, so that the boundary condition ([2\)](#page-1-0) is satisfied. The spectrum left outside the horizon is now easy to find. Since  $c_s \eta$  is a decreasing function of time, the negative order solution is the growing mode, so that asymptotically we have

$$
v \sim \frac{\sqrt{\beta \eta}}{(c_s k \eta)^{\nu}}.\tag{4}
$$

<span id="page-1-4"></span><span id="page-1-2"></span>Since the curvature fluctuation is related to *v* by  $\zeta = v/z$ , its scale invariance ( $k^3 \zeta^2$  = const) requires  $\nu = 3/2$ , i.e.,

$$
\alpha = \alpha_0 = 6 \frac{1+w}{1+3w}.\tag{5}
$$

<span id="page-1-3"></span>If we rephrase this requirement by writing  $c_s$  in terms of the density  $\rho$ , we conclude, interestingly, that  $c_s \propto \rho$  for all *w*. The spectrum can also be made red or blue depending on whether  $\alpha < \alpha_0$  or  $\alpha > \alpha_0$ , specifically

$$
n_S - 1 = \beta(\alpha - \alpha_0). \tag{6}
$$

We note that an infinitely fast transition ( $\alpha \gg 1$ ) implies  $n<sub>S</sub> = 2$  for all *w*. All of these considerations depend on the subhorizon normalization, here chosen to match a vacuum quantum state.

We can also work out the fluctuations' amplitude for near scale-invariant spectra. Considering the curvature  $\zeta$ , which "freezes-in" (i.e., is time independent outside the horizon, even with a variable  $c<sub>s</sub>$ ), it is found [\[17\]](#page-3-13) after straightforward algebra:

$$
k^3 \zeta^2 \sim \frac{(5+3w)^2}{1+w} \frac{\rho}{M_{\rm Pl}^4 c_s}.\tag{7}
$$

<span id="page-1-5"></span>Those acquainted with this expression (say, from inflation) will find here a good explanation for why  $c_s \propto \rho$  leads to scale invariance, even without inflation. If we refine the *cs* law to  $c_s = c_0(1 + \rho/\rho_\star)$  (where  $c_s \approx c_0$  at low energy and  $\rho_{\star}$  is the density that triggers its divergence), we find

$$
k^3 \zeta^2 \sim \frac{(5+3w)^2}{1+w} \frac{\rho_\star}{M_{\rm Pl}^4} \sim 10^{-10}.\tag{8}
$$

<span id="page-1-1"></span>This forces the energy scale of the varying speed of sound phenomenon to be a couple of orders of magnitude below the Planck scale, unless  $w \gg 1$  in which case it can be significantly lower.

This is not to say that this scenario is protected from the super-Planckian "problem" (cf. [\[18\]](#page-3-14) for a similar affliction). Indeed, choosing  $w = 1/3$  to fix ideas, and taking into account the amplitude ([8](#page-1-1)), straightforward algebra shows that the current Hubble scale left the sound horizon when  $H_0^{-1} = H^{-1}(\rho)c_s(\rho)a_0/a(\rho)$ , translating into  $\rho/M_{\text{Pl}} \sim 10^{24}$ , or  $E \sim 10^6 M_{\text{Pl}}$ . This can only be evaded with a very large  $w \gg 1$ , leading to  $E_{\star} < 10^{-10} M_{\text{Pl}}$  so that the current Hubble scale does freeze-in for  $E \leq M_{\text{Pl}}$ ; however, for the normalization to be correct one would then need  $w > 10^{30}$ . We would not discount more standard scenarios (with *w* of order 1), as this problem might be quite fictitious: it could well be that there is never a Planckian quantum gravity phase.

Perhaps more interesting is the possibility that the initial conditions are ''thermal'' rather than quantum vacuum fluctuations as assumed above [\[19\]](#page-3-15). The subhorizon modes then have a spectrum obtained from the above by a multiplicative factor of  $T_c/k$  (where  $T_c = Ta/c_s$  is a constant). This reflects the Rayleigh-Jeans limit of the thermal occupation number  $n(k)$  and implies a subhorizon white-noise spectrum. This then propagates to the final result [Eqs.  $(4)$ ] or [\(6](#page-1-3))] leading to the prediction

$$
n_S - 1 = -\frac{\alpha_0 - 1}{\alpha - 1}.
$$
 (9)

Scale invariance is now ensured by a very fast phase transition ( $\alpha \gg \alpha_0$ , i.e., something close to a step function). The spectrum is always red but can also be made arbitrarily close to flat. The amplitude, if departures from scale invariance are small, can be found following some simple algebra, keeping track of all significant multiplicative constants, and is  $A^2 = \alpha (T_{\star}/M_{\rm Pl})^3 \sim 10^{-10}$ . Thus these models do not suffer from a trans-Planckian problem. With  $\alpha \sim 100$  we have  $\rho_{\star}/M_{\text{Pl}}^4 \sim 10^{-16}$ , and the current horizon scale leaves the horizon at a density barely an order of magnitude higher than this. If anything, these scenarios may have the opposite problem: they push  $E_{\star}$ very low if the transition is extremely steep. For example, with  $\alpha \sim 10^{50}$  the appropriate normalization would require  $T_{\star} \sim 1$  GeV, with the current horizon scale leaving the horizon at around the same energy scale. This might bring these scenarios within the reach of a direct experimental test. Perhaps the study of high energy thermal plasmas [\[20\]](#page-3-16) could provide a direct measurement of *cs*, placing the model under laboratory test.

To conclude our presentation of the mechanism, we note that in general one might have both thermal and quantum contributions. In the absence of the usual inflationary justification for a vacuum state, the thermal argument may make more sense. Also notice that in these scenarios the curvature  $\zeta$  and the potential  $\Phi$  both freeze outside the horizon and have the same spectrum and normalization (within factors of order 1). This is to be contrasted with the pathologies known to plague some scenarios [\[21\]](#page-3-17).

*3. Models.—*So far we have concentrated on investigating a new *mechanism* for producing scale invariance and on its phenomenology. We specifically avoided wedding it to any ''model'' (although this has to be done to solve the flatness and other big bang problems). However, we will happily exhibit some possible models realizing this mechanism. These should be merely seen as proof of concept.

For example, one can appeal to a scalar field  $\phi$  endowed with nontrivial kinetic terms  $[10,22-24]$  $[10,22-24]$  $[10,22-24]$ , a suitable potential to recreate constant *w* (i.e., a scaling solution), and a varying  $c_s$ . The Lagrangian for such models has the form  $\mathcal{L}_0 = K(X) - V(\phi)$  (with  $X = \frac{1}{2} \partial_\mu \phi \partial^\mu \phi$ ). From the stress energy tensor we find that  $p = K - V$  and  $\rho =$  $2XK_{,X} - K + V$ ; i.e., *w* depends on both *K* and *V*. In contrast, the speed of sound is given by

$$
c_s^2 = \frac{K_{,X}}{K_{,X} + 2XK_{,XX}};
$$
\n(10)

<span id="page-2-0"></span>i.e., it depends only on *K*. For any power-law function  $K(X)$  we can always find a power-law potential  $V(\phi)$  that ensures a constant *w* (scaling) solution. An example is

$$
\mathcal{L}_0 = \sqrt{|X|X_{\star} - m^2 \phi^2},\tag{11}
$$

for which one can find a consistency relation between parameters  $X_{\star}$  and *m*, as well as initial conditions so that constant *w* solutions, for any *w*, can be generated. As is well known, this model has an infinite speed of sound  $c_s$ [cf. Eq.  $(10)$  $(10)$  $(10)$ ]: it is the so-called cuscuton field  $[11,12]$  $[11,12]$  $[11,12]$  $[11,12]$  $[11,12]$ . But if we now add to  $\mathcal{L}_0$  a new term  $\mathcal{L}_1 = X(X/X_\star)^{n-1}$  with  $n < 1/2$ , this term will be subdominant when  $\rho \gg X_{\star}$ , so that the initial, constant *w* solution is still valid in this regime. However,  $c_s$  will no longer be infinite, and using Eq. [\(10\)](#page-2-0) we find  $c_s^2 \propto X^{(1/2)-n} \propto \rho^{1-2n}$ . Thus for  $n =$  $-1/2$  we have  $c_s \propto \rho$ , as required for scale invariance. Under thermal initial conditions the more extreme  $\alpha \rightarrow$  $-\infty$  limit would have to be considered. Note that the theory has to contain a cutoff at low *X* ensuring that the kinetic term becomes linear in *X* at low *X* (or else the field should decay into normal matter).

This is only an illustration, but it highlights the limitations of standard thermodynamical arguments relating  $c_s$ and *w*. For hydrodynamical matter  $w = p/\rho$ , whereas  $c_s^2 = \frac{\delta p}{\delta \rho}$ . If the  $\delta$  in this expression is an adiabatic partial derivative and the background also evolves adiabati-cally [[13,](#page-3-10)[25](#page-3-20)], we must have  $w = -3\frac{\dot{a}}{a}(1 + w)(c_s^2 - w)$ , which results from  $w_{,\rho} = (c_s^2 - w)/\rho$ , itself a simple rearrangement of

$$
c_s^2 = \frac{d}{d\rho}(w\rho). \tag{12}
$$

<span id="page-2-1"></span>These relations contradict the assumptions in our perturbation calculation (*w* cannot be constant); however, they are blatantly violated by scalar fields endowed with a potential, as in the example just presented, or more prosaically in the cases of inflation or quintessence (for which  $c_s = 1$  but *w* can be anything).

Once this is noted, there is no reason not to consider general forms of matter with  $c_s$  and  $w$  regarded as independent variables [\[14\]](#page-3-11). Even with thermalized matter the evolution may be nonadiabatic  $[13]$  for the fluctuations, the background, or both, thereby violating ([12](#page-2-1)). If the background evolves adiabatically there must be entropy production  $p\Gamma = \delta p - c_{ad}^2 \delta \rho$  in order to have a constant *w* and a varying *cs*. Specifically, the conditions of our calculation are met if  $\Gamma = (\rho/\rho_*)^2 \delta$ , which can be seen as the appropriate ''nonadiabatic condition.''

It is also possible that a more complicated solution to [\(1\)](#page-0-0), allowing for a varying *w* satisfying ([12](#page-2-1)) and using the proposed varying  $c_s$  mechanism, still finds a niche for scale invariance. This possibility is currently under consideration, for example, in the context of adaptations of the Chaplygin gas [[26](#page-3-21)] (or generalizations of the work in [\[27](#page-3-22)[,28\]](#page-3-23)). The mathematics of such models is considerably less straightforward, but there is one case where a simple solution may be found. If the initial conditions are thermal, as discussed above, then we should have a step function in  $c_s$  in order to obtain scale invariance (or require  $\alpha \gg 1$ ). Let this step in  $c_s(\rho)$  happen at  $\rho = \rho_*$  and take  $c_s = c_-$ (for  $\rho < \rho_\star$ ) into  $c_s = c_+ \gg c_-$  (for  $\rho > \rho_\star$ ). Integration of Eq. [\(12\)](#page-2-1) leads to  $w = c_+^2 + (c_-^2 - c_+^2)\rho/\rho_\star \approx c_+^2(1 \rho/\rho_\star$ ) (for  $\rho \ge \rho_\star$ ) showing that in this case we can ignore variations in *w* while  $c_s$  is changing, enforcing the conditions for our calculation while complying with [\(12\)](#page-2-1). Thus the calculations presented do not need to be modified if thermal initial conditions are used to obtain scale invariance, in contrast with quantum initial conditions (and  $c_s \propto$  $\rho$ ), for which Eq. [\(12\)](#page-2-1) implies  $w \approx c_s^2/3$ , so that a whole new calculation is warranted.

We note that causality complaints [\[11,](#page-3-8)[29\]](#page-3-24) are bound to be model dependent. They do not affect bimetric and cuscuton models (see discussions in [\[11,](#page-3-8)[29,](#page-3-24)[30](#page-3-25)]), or more general  $\kappa$ -essence models if they are seen as bimetric theories [\[30\]](#page-3-25). It *may* be that one generally needs to embed  $c_s$  > 1 in bimetric VSL in order to prevent causality violations, but the instantaneous change required in thermal scenarios could open up other possibilities.

*4. Conclusions.—*In summary, we have revisited VSL scenarios with reference to structure formation [\[4](#page-3-3)] in the context of what we hope is a simpler framework: a varying speed of sound. In VSL's initial formulation [\[5,](#page-3-26)[6](#page-3-27)] the idea was to have increased symmetry as the Universe cooled down, transitioning from a Galilean universe (with infinite speed of light) to the near Lorentzian universe we see today. Obtaining a well-defined formulation of such scenarios proved challenging, particularly under hard breaking of Lorentz invariance (for instance, the issue of gauge choice became a physical one, and arbitrariness ruled). Machian scenarios, where the constants of nature evolve along with the Universe, as a power of *a* were also con-sidered [\[7](#page-3-4),[31](#page-3-28)]. It is ironic that, as shown in this Letter, thermal and quantum initial conditions provide room for a phase transition [[5,](#page-3-26)[6\]](#page-3-27) and a Machian scenario [[7\]](#page-3-4), respectively.

How can we understand our results heuristically? In inflation a suitable heuristic can be obtained by noting that the curvature  $\zeta = v/z$  freezes outside the horizon and that inside the horizon *v* becomes a regular Minkowski scalar field. The same is true in our scenario. In inflation one has to match free oscillating modes of the In inflation one has to match free oscillating modes of the<br>form  $v \sim e^{ik\eta}/\sqrt{2k}$  inside the horizon with  $\zeta = F(k) \propto$  $k^{-3/2}$  outside the horizon. The matching is done when  $k\eta \sim 1$  and therefore requires  $z \propto 1/|\eta|$  for scale invariance: a near de Sitter background. Here a similar argument can be made, but now inside the horizon modes have the well-known WKB form  $v \sim e^{ik \int c_s / \sqrt{c_s k}}$ , resulting from the variation in their frequency  $\omega = c_s k$ . These have to be matched with  $\zeta = F(k) \propto k^{-3/2}$  outside the *sound* horizon, and the matching done when  $c_s k \eta \sim 1$ . Thus we should have  $a\sqrt{c_s} \propto 1/\eta$ , resulting in the general condition ([5\)](#page-1-4). In both cases study of the two extreme regimes (large and small) followed by suitable matching is enough to infer the final result. (Those conversant with Eq.  $(7)$  $(7)$  $(7)$ —say, from inflation, or  $\kappa$  essence—will also quickly see why  $c_s \propto$  $\rho$  leads to scale invariance.)

Are there any striking observational differences between this mechanism and inflation? Deviations from  $n<sub>s</sub> = 1$  can be easily obtained in this scenario, so we do not expect striking differences in terms of scalar fluctuations. However, in the simple models we have considered the horizon problem remains unsolved for gravitational waves, and so we do not expect any tensor modes. This is to be contrasted with inflationary models with  $c_s > 1$  where the tensor to scalar ratio is actually enhanced [\[23\]](#page-3-29). This feature may be bypassed, say, in more complex bimetric theories, a matter we are currently investigating. Concrete implementations, such as the bimetric VSL theory, also have to be considered if one wants to address the other problems of big bang cosmology.

I would like to thank C. Armendariz-Picon, C. Contaldi, R. Brandenberger, P. Ferreira, A. Liddle, Y. Piao, and A. Vikman for helpful comments.

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