

## Thermal Conductivity Evidence for a $d_{x^2-y^2}$ Pairing Symmetry in the Heavy-Fermion CeIrIn<sub>5</sub> Superconductor

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The phase diagram of the quasi-2D Ce(Ir, Rh)In<sub>5</sub> system contains two distinct superconducting domes. By the thermal transport measurements in rotating magnetic fields  $\mathbf{H}$ , we pinned down the superconducting gap structure of CeIrIn<sub>5</sub> in the second dome, located distant from the first dome in proximity to an antiferromagnetic quantum critical point. Clear fourfold oscillation was observed when  $\mathbf{H}$  is rotated within the  $ab$  plane, while no oscillation was observed within the  $bc$  plane. In sharp contrast to previous reports, our results are most consistent with  $d_{x^2-y^2}$  symmetry, implying that the superconductivity in the second phase is also mediated by antiferromagnetic spin fluctuations.

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The relationship between the magnetism and unconventional superconductivity, whereby the gap function  $\Delta(\mathbf{k})$  has nodes on the Fermi surface where  $\Delta(\mathbf{k}) = 0$ , in heavy-fermion (HF) compounds continues to be a central focus of investigations into strongly correlated electron systems [1]. Many analyses have focused on the superconductivity mediated by magnetic fluctuations, often in proximity to a quantum critical point (QCP), where the magnetic ordering temperature is driven to zero by an external parameter such as pressure or chemical substitution. Indeed, unconventional superconductivity appears in the vicinity of an antiferromagnetic (AF) QCP in most Ce-based HF compounds, including CeIn<sub>3</sub>, CePd<sub>2</sub>Si<sub>2</sub> [2], CeCoIn<sub>5</sub>, [3] and CeRhIn<sub>5</sub> [4], as well as high- $T_c$  cuprates.

Notable counterexamples have been recently reported in two Ce compounds, where two distinct domes of different HF superconducting phases appear as a function of pressure or chemical substitution. The first example is CeCu<sub>2</sub>Si<sub>2</sub>, with one superconducting dome at low pressure around the AF QCP, and another dome emerging at high pressure distant from the QCP [5]. The superconductivity in the low pressure dome is consistent with the magnetically mediated pairing, while Cooper pairing glued by the Ce-*valence* fluctuations was proposed for the high pressure region with no discernible AF fluctuations [5,6].

The second example is a quasi-2D CeIrIn<sub>5</sub> ( $T_c = 0.4$  K) [3], whose phase diagram is shown in the inset of Fig. 1 [7,8]. In this system the Rh substitution for Ir acts as a negative chemical pressure that increases AF correlations. In CeRh<sub>1-x</sub>Ir<sub>x</sub>In<sub>5</sub>, the ground state continuously evolves from AF metal (AFM) ( $x < 0.5$ ) to superconductor ( $x > 0.5$ ).  $T_c$  shows a maximum at  $x \sim 0.7$  and a cusplike minimum at  $x \sim 0.9$ , forming the first dome (SC1). In CeIrIn<sub>5</sub> ( $x = 1$ ),  $T_c$  increases with pressure and exhibits a maximum ( $T_c = 1$  K) at  $P \sim 3$  GPa, forming a second dome (SC2). The strong AF fluctuations associated with

the AF QCP nearby are observed in SC1 [8,9], but are strongly suppressed with pressure, in SC2, away from the AF QCP [8–10]. Moreover, the nature of the AF fluctuations in magnetic fields in CeIrIn<sub>5</sub> is very different from that in CeCoIn<sub>5</sub> and AF CeRhIn<sub>5</sub> [11–13]. Thus superconductivity in CeIrIn<sub>5</sub> at ambient pressure may be distinct from that in CeCoIn<sub>5</sub> and CeRhIn<sub>5</sub>, although all three compounds share similar band structure [14].

Hence a major outstanding question is the nature of the pairing interaction in CeIrIn<sub>5</sub>. By analogy with CeCu<sub>2</sub>Si<sub>2</sub>, CeIrIn<sub>5</sub> in SC2 was suggested to be a strong candidate for

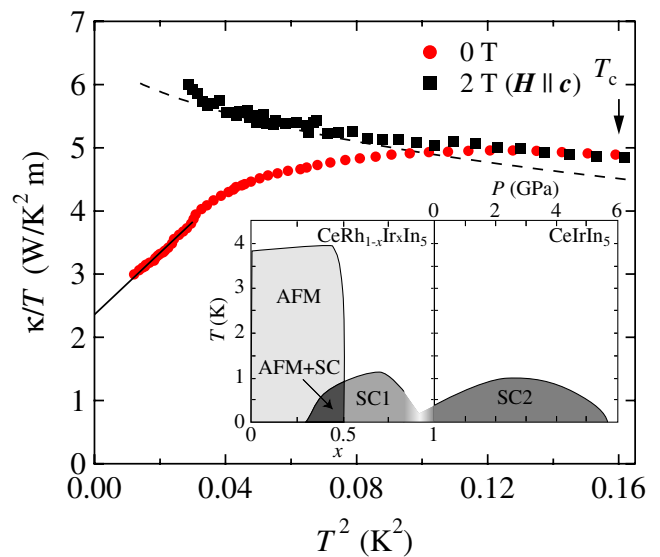


FIG. 1 (color online). Temperature dependence of  $\kappa/T$  as a function of  $T^2$  in zero field and above  $H_{c2}^c$  ( $H = 2$  T). The solid line represents  $\kappa/T = \kappa_{00}/T + AT^2$ ; the dashed line shows  $\kappa/T$  obtained from the resistivity using the Wiedemann-Franz law. Inset: phase diagram of Ce(Ir, Rh)In<sub>5</sub> as a function of Ir concentration and pressure, from Refs. [7,8].

the Ce-valence fluctuation mediated superconductor [6]. To elucidate the pairing symmetry, identification of the superconducting gap structure is of primary importance. Measurements of nuclear quadrupole resonance [9,10], thermal conductivity  $\kappa$  [15,16], and heat capacity [15] revealed that the superconductivity of CeIrIn<sub>5</sub> is unconventional, with line nodes in the gap. Very recently, the interplane and intraplane thermal conductivity in zero field have been reported to have a large residual anisotropy in CeIrIn<sub>5</sub> [16], in contrast to the small anisotropy in CeCoIn<sub>5</sub> [17]. From these results, the gap function of CeIrIn<sub>5</sub> was suggested to be of hybrid type,  $k_z(k_x + ik_y)$ , or  $E_g$  symmetry [16], similar to UPt<sub>3</sub> [18], and in sharp contrast to the  $d_{x^2-y^2}$  gap in CeCoIn<sub>5</sub> (and most likely in CeRhIn<sub>5</sub> under pressure) [19]. However, as pointed out in Ref. [20], the anisotropy of  $\kappa$  alone is not sufficient to establish the hybrid gap, and further experiments aimed at clarifying the shape of the superconducting gap are needed.

Here, to shed light on the pairing mechanism of CeIrIn<sub>5</sub>, we measured the thermal conductivity in a magnetic field  $\mathbf{H}$  rotated relative to the crystal axes. We provide strong evidence of  $d_{x^2-y^2}$  gap symmetry. The results put a constraint on the pairing mechanism in CeIrIn<sub>5</sub>.

Single crystals were grown by the self-flux method. The bulk transition temperature is 0.4 K, and upper critical fields parallel to the  $ab$  plane and the  $c$  axis,  $H_{c2}^{ab}$  and  $H_{c2}^c$ , are 1.0 T and 0.5 T at  $T = 0$  K, respectively. We measured the thermal conductivity  $\kappa$  along the tetragonal  $a$  axis (heat current  $\mathbf{q} \parallel a$ ) on the sample with a rectangular shape ( $2.8 \times 0.45 \times 0.10$  mm<sup>3</sup>). To apply  $\mathbf{H}$  with high accuracy (misalignment of less than 0.05°) relative to the crystal axes, we used a system with two superconducting magnets generating  $\mathbf{H}$  in two mutually orthogonal directions and a dilution refrigerator equipped on a mechanical rotating stage at the top of the Dewar.

Figure 1 shows  $\kappa/T$  as a function of  $T^2$  at  $H = 0$  and above  $H_{c2}^c$ . The overall behavior of  $\kappa/T$  is similar to those reported in Refs. [15,16]. In zero field,  $\kappa/T$  decreases with decreasing  $T$  after showing a broad maximum at  $T_c$ , similar to UPt<sub>3</sub> [21] and CePt<sub>3</sub>Si [22]. The value of  $\kappa/T$  at  $T_c$  is nearly 30% smaller than that reported in Ref. [16] and nearly 3 times larger than that reported in Ref. [15]. The dashed line is  $\kappa/T$  obtained from the Wiedemann-Franz law,  $\kappa/T = L_0/\rho$ , where  $L_0 = \frac{\pi^2}{3}(\frac{k_B}{e})^2$  and  $\rho$  is the normal state resistivity. The observed  $\kappa/T$  is close to  $L_0/\rho$ , indicating the dominant electronic contribution in the heat transport [23].

First, let us consider the thermal conductivity at  $H = 0$ . As shown in Fig. 1,  $\kappa/T$  at low  $T$  is well fitted by  $\kappa/T = \kappa_{00}/T + AT^2$ , with the clearly resolved residual term  $\kappa_{00}/T$  as  $T \rightarrow 0$  K. This indicates the existence of a residual normal fluid, expected for nodal superconductors with impurities. For a gap with line nodes, the magnitude of  $\kappa_{00}/T$  is independent of impurity concentration [24]. Our value of  $\kappa_{00}/T = 2.3 \pm 0.2$  W/K<sup>2</sup> m agrees, within error

bars, with that reported in Ref. [16] ( $\kappa_{00}/T = 2.1 \pm 0.2$  W/K<sup>2</sup> m) and is consistent with the theoretical estimate for a superconductor with line node.

The next question is the nodal topology. Thermal conductivity is a powerful directional probe of the nodal structure: Recent measurements of both  $\kappa$  and the heat capacity with  $\mathbf{H}$  applied at varying orientation relative to the crystal axes established the superconducting gap structure in several systems [19,25,26]. In nodal superconductors the heat transport is dominated by delocalized near-nodal quasiparticles (QPs). The applied field creates a circulating supercurrent flow  $\mathbf{v}_s(\mathbf{r})$  associated with vortices. The Doppler shift of the energy of a quasiparticle with momentum  $\mathbf{p}$ ,  $E(\mathbf{p}) \rightarrow E(\mathbf{p}) - \mathbf{v}_s \cdot \mathbf{p}$ , is important near the nodes, where the local energy gap is small,  $\Delta(\hat{\mathbf{p}}) < |\mathbf{v}_s \cdot \mathbf{p}|$ . Consequently the density of states (DOS) depends sensitively on the angle between  $\mathbf{H}$  and the nodal directions [27]. Clear twofold or fourfold oscillations of thermal conductivity and heat capacity due to nodes have been observed in UPd<sub>2</sub>Al<sub>3</sub> [28], YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7</sub> [29], CeCoIn<sub>5</sub> [26,30], and  $\kappa$ -(BEDT-TTF)<sub>2</sub>Cu(NCS)<sub>2</sub> [31] when  $\mathbf{H}$  is rotated relative to the crystal axes.

Figures 2(a) and 2(b) show the angular variation of the thermal conductivity at 200 mK ( $k_B T/\Delta \sim 0.2$ ) as  $\mathbf{H}$  is rotated within the  $bc$  plane at  $|\mathbf{H}| = 0.05$  T [ $H/H_{c2}^c(T) \approx 0.14$ ] and at  $|\mathbf{H}| = 0.1$  T [ $H/H_{c2}^{ab}(T) \approx 0.14$ ], and within the 2D  $ab$  plane at  $|\mathbf{H}| = 0.1$  T [ $H/H_{c2}^{ab}(T) \approx 0.14$ ], respectively. Here  $\theta = (\mathbf{H}, c)$  and  $\phi = (\mathbf{H}, a)$  are the polar and azimuthal angles, respectively. For the field rotated

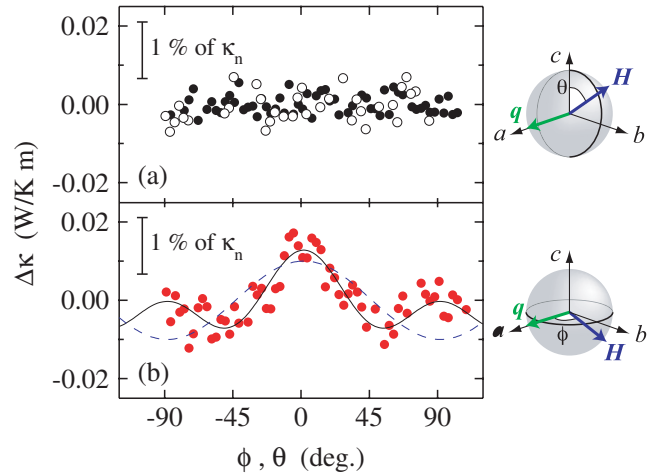


FIG. 2 (color online). Angular variation of the thermal conductivity  $\Delta\kappa \equiv \kappa - \kappa_0$  at  $T = 200$  mK with rotating  $\mathbf{H}$  (a) within the  $bc$  plane as a function of polar angle  $\theta$  for  $|\mathbf{H}| = 0.05$  T (filled circles) and  $0.10$  T (open circles) and (b) within the 2D  $ab$  plane as a function of azimuthal angle  $\phi$  for  $|\mathbf{H}| = 0.10$  T. Here  $\kappa_0$  is the angular average of  $\kappa$ . The thermal current  $\mathbf{q}$  is applied parallel to the  $a$  axis. The dashed line shows the twofold ( $\cos 2\phi$ ) variation. The solid line is the fit by  $\kappa(\phi) = \kappa_0 + C_{2\phi} \cos 2\phi + C_{4\phi} \cos 4\phi$ , where  $C_{2\phi}$ , and  $C_{4\phi}$  are constants.

within the  $ab$  plane ( $\theta = 90^\circ$ )  $\kappa(\phi)$  exhibits a distinct oscillation as a function of  $\phi$ , which is characterized by peaks at  $\phi = 0^\circ$  and  $\pm 90^\circ$  and minima at around  $\pm 45^\circ$ . As shown by the solid line,  $\kappa(\phi)$  can be decomposed into three terms,  $\kappa(\phi) = \kappa_0 + \kappa_{2\phi} + \kappa_{4\phi}$ , where  $\kappa_{2\phi} = C_{2\phi} \cos 2\phi$  and  $\kappa_{4\phi} = C_{4\phi} \cos 4\phi$  have the two- and four-fold symmetry with respect to  $\phi$ , respectively. We note that, as shown by the dashed line,  $\kappa(\phi)$  with minima at  $\pm 45^\circ$  and peaks at  $\pm 90^\circ$  cannot be fitted only by the  $\kappa_{2\phi}$  term, indicating the presence of the fourfold term. In sharp contrast to  $\mathbf{H}$  rotating within the  $ab$  plane, no oscillation is observed when rotating  $\mathbf{H}$  within the  $bc$  plane; the amplitude of the oscillation is less than 0.2% (0.3%) of  $\kappa_n$  for  $|\mathbf{H}| = 0.05$  T (0.1 T) if it exists, where  $\kappa_n$  is the normal state thermal conductivity measured above  $H_{c2}$ . The  $\kappa_{2\phi}$  term arises from the difference between transport parallel and perpendicular to the vortices. Since for  $\mathbf{H}$  within the  $bc$  plane the field is always normal to  $\mathbf{q}$ , the  $\kappa_{2\phi}$  term is absent for this geometry.

We address the origin of the fourfold oscillation. Figures 3(a)–3(d) display  $\kappa_{4\phi}$  normalized by  $\kappa_n$  at 200 mK below  $H_{c2}^{ab}(T)$  ( $\approx 0.7$  T). In the normal state above  $H_{c2}^{ab}$ , no discernible oscillation was observed (not shown). At 0.69 T just below  $H_{c2}^{ab}(T)$ ,  $\kappa_{4\phi}$  exhibits a minimum at  $\phi = 0^\circ$  ( $C_{4\phi} < 0$ ). At  $H = 0.5$  T,  $\kappa_{4\phi}$  oscillation vanishes. Further decrease of  $H$  leads to the appearance of distinct  $\kappa_{4\phi}$  oscillation with a maximum at  $\phi = 0^\circ$  ( $C_{4\phi} > 0$ ) at  $H = 0.1$  and 0.25 T. Figure 3(e) shows the  $H$  depen-

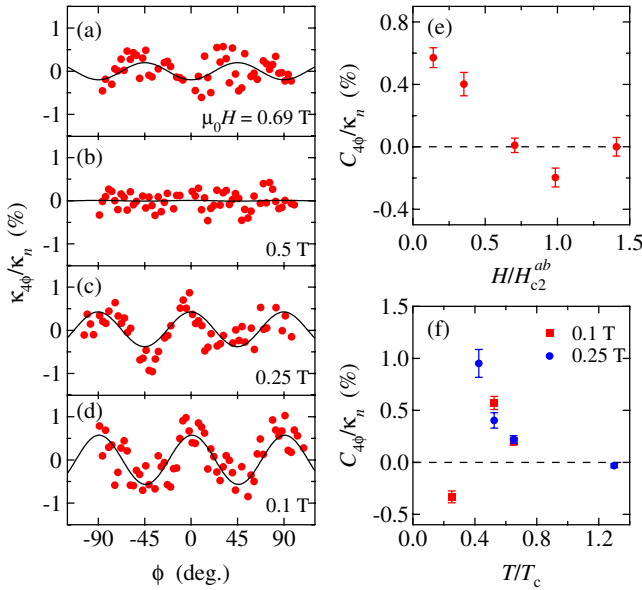


FIG. 3 (color online). (a)–(d) The fourfold component  $\kappa_{4\phi}$  normalized by  $\kappa_n$  with  $\mathbf{H}$  rotated in the  $ab$  plane at  $T = 200$  mK at  $|\mathbf{H}| = 0.69, 0.5, 0.25,$  and  $0.1$  T, respectively. The upper critical field is  $H_{c2}^{ab} \approx 0.7$  T at this temperature. The solid lines represent the fit by  $C_{4\phi} \cos 4\phi$ . (e)  $C_{4\phi}/\kappa_n$  at  $T = 200$  mK as a function of  $H/H_{c2}^{ab}$ . (f)  $C_{4\phi}/\kappa_n$  at  $H = 0.1$  and  $0.25$  T as a function of  $T/T_c$ .

dence of  $C_{4\phi}/\kappa_n$ . Fourfold oscillation may originate from (i) the nodal structure and (ii) in-plane anisotropy of the Fermi surface and  $H_{c2}^{ab}$ . It should be stressed that the sign of  $C_{4\phi}$  just below  $H_{c2}^{ab}$  is the same as that expected from the in-plane anisotropy of  $H_{c2}^{ab}$  [ $H_{c2} \parallel (100) > H_{c2} \parallel (110)$ ] [32], whereas its sign at low fields is opposite. This immediately indicates that the origin of the fourfold symmetry at low fields is not due to the anisotropy of the Fermi surface or  $H_{c2}^{ab}$ . A rough estimate of the amplitude of the fourfold term in layered  $d$  wave superconductors yields  $C_{4\phi}/\kappa_n = 0.082 \frac{v_F v'_F e H}{3\pi \Gamma \Delta} \ln(\sqrt{32\Delta}/\pi \hbar \Gamma)$ , where  $\Delta$  is the superconducting gap,  $\Gamma$  is the QP relaxation rate,  $v_F$  and  $v'_F$  are the in-plane and out-of-plane Fermi velocities [33]. Using  $\Gamma \sim 1.3 \times 10^{11} \text{ s}^{-1}$ ,  $2\Delta/k_B T_c \sim 5$ ,  $v_F \sim 1 \times 10^4 \text{ m/s}$ , and  $v'_F \sim 5 \times 10^3 \text{ m/s}$  [9,30] gives  $C_{4\phi}/\kappa_n \sim 2\%$ , of the same order as the data. These results lead us to conclude that the fourfold symmetry at low fields originates from the nodal structure.

The distinct fourfold oscillation within the  $ab$  plane, together with the absence of the oscillation within the  $bc$  plane, definitely indicates the vertical line nodes perpendicular to the  $ab$  plane, and excludes a horizontal line of nodes at least in the dominant heavy electron bands. Recall that in  $\text{UPd}_2\text{Al}_3$  with horizontal line node, clear oscillations of  $\kappa(\theta)$  are observed when rotating  $\mathbf{H}$  within the  $ac$  plane [28]. One could argue that the absence of oscillations within the  $bc$  plane shown in Fig. 2(a) is due to relatively high temperature ( $k_B T/\Delta \sim 0.2$ ), but the simultaneous observation of the fourfold oscillation within the  $ab$  plane at the same  $T$  rules out such a possibility.

Thus the superconducting symmetry of  $\text{CeIrIn}_5$  is narrowed down to either  $d_{x^2-y^2}$  or  $d_{xy}$ . Further identification relies on the evolution of the oscillations with temperature

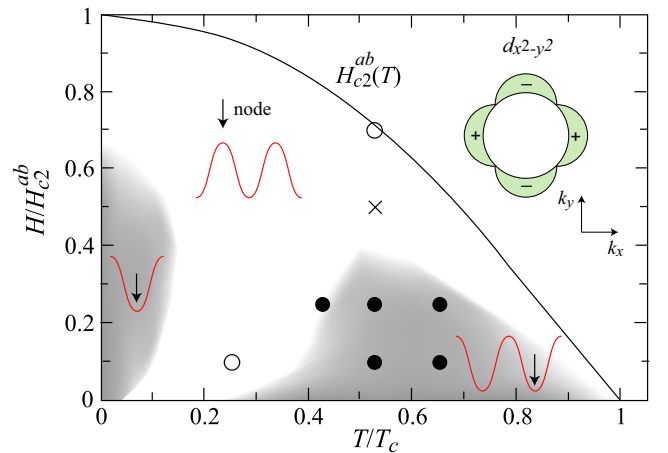


FIG. 4 (color online).  $H$ - $T$  phase diagram for the fourfold term  $\kappa_{4\phi}$  in  $\mathbf{H}$  rotated within the  $ab$  plane. Solid (open) circles indicate points with maxima (minima) of  $\kappa_{4\phi}$  at  $\phi = 0^\circ$ . The shaded (unshaded) regions correspond to minima (maxima) of  $\kappa_{4\phi}$  for  $\mathbf{H}$  along the nodal directions [35].

and field. In the low- $T$ , low- $H$  limit, the Doppler shifted DOS shows a maximum (minimum) when  $\mathbf{H}$  is along the antinodal (nodal) directions. However, according to recent microscopic calculations, the pattern is inverted at higher  $T$ ,  $H$  due to vortex scattering, and the fourfold components of the specific heat and of the thermal conductivity have similar behavior across the phase diagram [34,35]. In Fig. 3(f) we plot  $C_{4\phi}/\kappa_n$  as a function of temperature. At  $H = 0.1$  T, the sign change indeed occurs at  $T/T_c \simeq 0.25$ . Figure 4 displays the  $H$ - $T$  phase diagram for the fourfold component. The solid (open) circles represent the points at which observed  $\kappa_{4\phi}$  exhibits a maximum (minimum) at  $\phi = 0^\circ$ , and the shading indicates the calculated anisotropy of the thermal conductivity for a  $d$ -wave superconductor from Ref. [35]. The shaded (unshaded) regions correspond to the region where  $\kappa_{4\phi}$  has a minimum (maximum) for the field in the nodal direction. The calculation is for a corrugated cylindrical Fermi surface, similar to that of the main Fermi surface sheet of CeIrIn<sub>5</sub>, and the results well reproduce the observed sign change of  $\kappa_{4\phi}$ . Ref. [20] showed that small deviations from cylindrical symmetry are sufficient to reconcile the vertical lines of nodes with the results of Ref. [16]. We assume that these small deviations weakly affect the phase diagram of Fig. 4. Since the minimum (maximum) of  $\kappa_{4\phi}$  occurs at  $\phi = 45^\circ$  inside (outside) the shaded region, the nodes are located at  $\pm 45^\circ$ . We thus conclude that the gap symmetry of CeIrIn<sub>5</sub> is  $d_{x^2-y^2}$ .

The  $d_{x^2-y^2}$  symmetry implies that the superconductivity is most likely to be mediated by the AF spin fluctuations, not by the Ce-valence fluctuations [36]. Our result is also at odds with the hybrid gap function with horizontal node proposed in Ref. [16]. Recent study of CeCo(In<sub>1-x</sub>Cd<sub>x</sub>)<sub>5</sub> revealed that the superconductivity in CeCoIn<sub>5</sub> occurs in the proximity to the AF ordered phase [37]. Therefore it is natural to consider that the symmetry of the SC1 phase is  $d_{x^2-y^2}$ , the same as CeCoIn<sub>5</sub> [19]. It is then intriguing that the superconductivity in the SC1 and SC2 phases has the same gap symmetry.

In conclusion, the measurements of the thermal conductivity under rotated magnetic fields provide strong evidence that the superconducting gap of CeIrIn<sub>5</sub> at ambient pressure has vertical line nodes, and is of  $d_{x^2-y^2}$  symmetry. This indicates that two distinct domes of HF superconducting phases possess the same superconducting symmetry, in which AF fluctuations appear to play an important role. The determined gap symmetry in CeIrIn<sub>5</sub> which is located in the second superconducting phase, further restricts theories of the pairing mechanism.

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