## **Defect-Induced Photoconductivity in Layered Manganese Oxides: A Density Functional Theory Study**

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Enhanced photoconductivity of layered  $Mn(IV)O_2$  containing protonated  $Mn(IV)$  vacancy defects has been recently demonstrated, suggesting new technological possibilities for photoelectric conversion based on visible light harvesting. Using spin-polarized density functional theory, we provide the first direct evidence that such defects can indeed facilitate photoconductivity by (i) reducing the band-gap energy and (ii) separating electron and hole states. Our results thus support the proposition that nanosheet  $MnO<sub>2</sub>$ offers an attractive new material for a variety of photoconductivity applications.

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Manganese oxide nanosheets have emerged recently as interesting new materials for a host of potential applications in energy storage, electrochromism, and catalysis [[1–](#page-3-1) [5](#page-3-2)]. The desirable properties of these materials derive mainly from their nanosheet structure  $[1-6]$  $[1-6]$  $[1-6]$ , which allows inexpensive manufacture, the use of flexible substrates, and facile shaping to suit a variety of devices. An important characteristic of the nanosheets in all materials synthesized thus far is the presence of cation vacancies  $(Mn_{1-x}\square_xO_2)$ , where  $\Box_r$  represents a Mn vacancy) whose negative charge is typically compensated by interlayer metal cations or protons. Vacancies in metal oxides are well known to function as electron donors or acceptors, thereby enhancing material conductivity  $[7–10]$  $[7–10]$  $[7–10]$ , and a similar role of the vacancies in Mn oxide nanosheets is possible.

Sakai et al. [\[6](#page-3-3)] recently reported the first observation of photocurrent generation by a Mn oxide. Protonated nanosheets were exfoliated from a digestion product containing approximately 3 mol% vacancies  $(H_{0.13}[Mn(IV)_{0.97}\square_{0.03}]O_2$ , mean Mn oxidation number 3.87 [[1](#page-3-1)]). A monolayer film produced photocurrents under visible light radiation  $(\lambda \leq 500 \text{ nm})$  without significant structural decomposition [[6\]](#page-3-3). Sakai *et al.* [[6\]](#page-3-3) speculated that the nanoscale thickness (*<*1 nm) of the film facilitated excited electron and hole escape before their recombination could occur.

Understanding electronic structure near the band gap of protonated Mn oxides is clearly essential to developing the full potential of these materials for harvesting visible light. In this Letter, we use spin-polarized density functional theory (DFT) to show that a Mn(IV) vacancy compensated by protons both narrows the energy gap between occupied and unoccupied electronic states of Mn oxides and separates photoinduced charge carriers effectively, thereby enhancing photoconductivity.

Protonated Mn vacancies in Mn(IV) oxides are known in the literature as Ruetschi defects [[11](#page-3-6)]. Balachandran *et al.* [\[12\]](#page-3-7) have reviewed the properties of Ruetschi defects and examined their impact on the structures of a number of MnO2 polymorphs, including a layered variety. Using DFT with electron correlations described by the generalized gradient approximation (GGA), they found that a Ruetschi defect tends to stabilize  $MnO<sub>2</sub>$  polymorphs, especially those having more open structures featuring tunnels formed by chains of edge-sharing octahedra linked by shared corners (e.g., ramsdellite [[13\]](#page-3-8)). A similar type of defect in  $TiO<sub>2</sub>$ , i.e., a  $Ti(IV)$  vacancy charge-compensated with four protons, has been observed and predicted to be a stable entity [[14](#page-3-9)[,15](#page-3-10)].

In the present study, we applied DFT to investigate the impact of a Ruetschi defect on the structure and electronic properties of a  $MnO<sub>2</sub>$  nanosheet bearing 0.033 and 0.125 Mn vacancies per octahedron. Vacancy-free  $Mn(IV)O<sub>2</sub>$ , which has not yet been synthesized in the laboratory, was modeled based on published Mn and O atomic coordinates for a microcrystalline variety of layered  $MnO_2$  (space group *P*6<sub>3</sub>/*mmc*,  $a = b = 2.840 \text{ Å}$ ,  $c =$ 14.031 Å) prepared by thermal decomposition of  $KMnO<sub>4</sub>$ at  $800\text{ °C}$  [[16](#page-3-11)]. The Ruetschi defect was incorporated in  $MnO<sub>2</sub>$  supercells by coordination of one Mn vacancy at the center of each supercell to four H on ''dangling'' O ions around the vacancy. Two different defect concentrations were modeled, with one Mn vacancy placed in either a  $4 \times 4 \times 1$  (32 Mn atoms) or a  $2 \times 2 \times 1$  (8 Mn atoms) supercell, corresponding to the structural formulas,  $H_{0.13}$ [Mn<sub>0.967</sub> $\Box_{0.033}$ ]O<sub>2</sub> and  $H_{0.50}$ [Mn<sub>0.875</sub> $\Box_{0.125}$ ]O<sub>2</sub>, respectively.

All DFT calculations were performed using the CASTEP code [\[17\]](#page-3-12), with either the local spin density approximation (LSDA) or spin-polarized GGA/Perdew, Burke, and Ernzerhof (PBE) functionals [\[18\]](#page-3-13), assuming ferromagnetic ordering among Mn ions [\[19\]](#page-3-14). For Mn and O, ultrasoft pseudopotentials [\[20\]](#page-3-15) were constructed using the onthe-fly pseudopotential generator implemented in CASTEP, with valence electron configurations of  $3s^23p^63d^54s^2$ with a core radius  $(r_c)$  of 2.3  $a_0$  for Mn and  $2s^22p^4$  with  $r_c = 1.3 a_0$  for O. Tests of the pseudopotentials at a 500 eV cutoff energy under LSDA reproduced structure and energy data for MnO calculated with the all-electron method [\[21\]](#page-3-16). For the first Brillouin zone,  $6 \times 6 \times 2$ ,  $5 \times 5 \times 2$ , and  $2 \times 2 \times 1$  *k*-point grids [\[22\]](#page-3-17) were used for a vacancyfree MnO<sub>2</sub>, a  $2 \times 2 \times 1$  defect supercell, and a  $4 \times 4 \times 1$ defect supercell, respectively. Tests of Brillouin zone sampling with the 500 eV cutoff energy showed very high convergence of force  $(0.01 \text{ eV/A})$  or better) and stress (0.01 Gpa or much better). For the Ruetschi-defected supercells, the three unit-cell angles  $(90^\circ, 90^\circ, \text{and}$ 120 $^{\circ}$ ), and the *c*-axis lattice parameters (13.892 A in LSDA and 14.001 A in GGA/PBE) were fixed based on optimized all-relaxed vacancy-free  $MnO<sub>2</sub>$  structures, but the other lattice parameters and all internal ionic positions were relaxed. Residual force and stress for the geometryoptimized structures with a 500 eV cutoff energy were less than  $0.01 \text{ eV/A}$  and  $0.02 \text{ GPa}$ , respectively.

Table [I](#page-1-0) shows that our LSDA and GGA/PBE optimizations closely bracket available experimental lattice parameters and Mn-O bond distances for layered  $MnO<sub>2</sub>$ with defects, in accordance with the usual DFT trend. In Ruetschi-defected  $MnO<sub>2</sub>$ , the four H formed covalent bonds with coordinating O  $(O_H)$  (OH distance 0.984 to 1.001  $\AA$ ) and hydrogen bonds with the O bound to two Mn  $(O_{2Mn})$   $(O-H...O_{2Mn}$  distance 1.96 to 2.17 A) near the vacancy, such that the resulting OH groups were oriented to make a small angle  $(4^{\circ}$  to  $10^{\circ})$  with respect to the  $a-b$ plane. The interatomic distances between H are very short: 1.640 Å (LSDA) and 1.732 Å (GGA/PBE) in the  $2 \times 2 \times 1$ supercells and  $1.773 \text{ Å}$  (LSDA) and  $1.878 \text{ Å}$  (GGA/PBE) in the  $4 \times 4 \times 1$  supercells. Several possible H arrangements were explored by calculating total energies, with H thereby found to coordinate preferentially with  $O_{2Mn}$  (as would be expected from Pauling's rules) and to come into close proximity to one another. Similar structures were reported by Balachandran *et al.* [\[12\]](#page-3-7).

Figure [1](#page-2-0) compares the electronic density of states (DOS) of vacancy-free  $MnO<sub>2</sub>$  with Ruetschi-defected  $MnO<sub>2</sub>$ . Incorporation of a Ruetschi defect significantly reduced the band-gap energy, from 1.3 eV to 0.9 eV in the  $4 \times 4 \times$ 1 supercell and from 1.3 eV to 0.3 eV in the  $2 \times 2 \times 1$ supercell (GGA/PBE). Sakai *et al.* [\[6](#page-3-3)] reported an indirect band-gap energy of 2.23 eV for the Mn oxide nanosheets they prepared, based on a relationship between the incident photon energy and the incident photon-to-current efficiency. It is well known that LDA and GGA generally underestimate band gaps of semiconductors. However, for insulating and semiconducting systems, the primary effect of this DFT underestimation is a uniform downward shift of all conduction bands. Our calculations demonstrate additional valence levels for systems containing Ruetschi defects, so the band-gap shift is modeled fairly reliably even though the absolute value is not. Improved band-gap energy estimates may be obtained with the DFT  $+$  U approach [[24](#page-3-18)] or the screened exchange method [[25](#page-3-19)].

The substantial reduction in band-gap energy we observed is due to the introduction of states at the top of the valence band (VB) (arrows in Fig. [1](#page-2-0)) by the Ruetschi defect. Detailed orbital analysis revealed that these newly introduced states around  $-1$  to 0 eV are contributed almost entirely by nearest-neighbor Mn and O ions around the cation vacancy. In particular, the localized states were mostly Mn-3*d* states and  $O_{2Mn}$ -*p* states around the Ruetschi defect. The  $O_{2Mn}$ -*p* states were oriented parallel to the axial Mn-O bonds in the  $MnO<sub>6</sub>$  octahedra and are a consequence of Mn-O bonds lost by removal of  $Mn^{4+}$ , which results in dangling states that are analogous to nonbonding states compared to  $O_H$  (at around  $-8$  eV in Fig. [1\)](#page-2-0) or to saturated O bound to three Mn atoms  $(O_{3Mn})$ . The  $O<sub>2Mn</sub>$  states are reflected also in the noticeable induction of spin polarization on the  $O_{2Mn}$ ; the magnetic moment increases from  $-0.04\mu$ <sub>B</sub> on O<sub>3Mn</sub> in vacancy-free MnO<sub>2</sub> to between  $+0.12\mu_B$  and  $+0.14\mu_B$  on the O<sub>2Mn</sub> (GGA/PBE).

According to our DFT calculations, the Mn-3*s* states were strongly polarized, leading to significant energy splitting  $(\Delta E_{Mn3s})$  between the spin-up and spin-down states of Mn-3*s*. Our values of  $\Delta E_{\text{Mn3s}}$  can be compared to the

	<b>LSDA</b>			<b>GGA/PBE</b>			Experimental			
Distance $(A)$	$\theta$	0.033	0.125	$\Omega$	0.033	0.125	$0.03^{\rm a}$	$0.03^{p}$	0.06 <sup>c</sup>	$0.12^d$
$Mnlayer - Mnlayer$	2.827	$2.756 - 2.888$ (2.825)	2.815	2.897	$2.820 - 2.943$ (2.895)	2.895	2.85	2.86	2.88	2.840
$Mnlayer - Olayer$	1.883	1.833-1.929 (1.882)	1.854–1.929 (1.882)	1.925	$1.852 - 2.002$ (1.928)	1.887-1.979 (1.931)	1.91	1.89	1.90	1.914
Mn sheet thickness	1.88	1.91	l.98	1.91	1.94	2.02				1.96

<span id="page-1-0"></span>TABLE I. Interatomic distances in vacancy-free and Ruetschi-defected MnO<sub>2</sub> optimized with spin-polarized DFT. Vacancy rate per octahedron indicated at the top of each column of data. Values in parentheses are averages of calculated interatomic distances.

<sup>a</sup>Mn *K*-edge EXAFS analysis ( $\pm 0.01$  Å) of protonated nanosheet MnO<sub>2</sub>, H<sub>0.13</sub>[Mn(IV)<sub>0.87</sub> $\Box_{0.03}$ ]O<sub>2</sub>  $\cdot$  0.7H<sub>2</sub>O [\[2\]](#page-3-20). The Mn-Mn distance is 2.842  $\AA$  by x-ray diffraction (XRD) analysis.

<sup>b</sup>Mn *K*-edge EXAFS analysis of protonated nanosheet MnO<sub>2</sub> [[3\]](#page-3-21).

Mn *K*-edge EXAFS analysis ( $\pm 0.02$  Å) of nanoparticle  $\delta$ -MnO<sub>2</sub>, Na<sub>0.24</sub>[Mn(IV)<sub>0.94</sub> $\Box$ <sub>0.06</sub>]O<sub>2</sub> · 0.72H<sub>2</sub>O [[23](#page-3-22)]. The Mn-O distance is 1.92 A by XRD analysis.

 $XRD$  analysis of microcrystalline layered K-MnO<sub>2</sub>,  $K_{0.231}Mn(III)_{0.077}[Mn(IV)_{0.885}\Box_{0.115}]O_2 \cdot 0.60H_2O$  [\[16\]](#page-3-11). The Mn-Mn distance for a powder sample was 2.845 A˚ by XRD analysis and 2.87 A˚ by Mn *K*-edge EXAFS analysis.



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FIG. 1 (color online). Density of states (DOS) of vacancy-free  $MnO<sub>2</sub>$  and Ruetschi-defected  $MnO<sub>2</sub>$  in (a) the 4  $\times$  4  $\times$  1 supercell and (b) the  $2 \times 2 \times 1$  supercell for spin-up (1) and spindown ( $\downarrow$ ) states. The Fermi energy of Ruetschi-defected MnO<sub>2</sub> was set equal to zero. The conduction band minimum (CBM) of vacancy-free  $MnO<sub>2</sub>$  was aligned at the CBM of Ruetschidefected MnO<sub>2</sub>. The slight occupation above  $E_F$  in the 2  $\times$  2  $\times$ 1 supercell is due to Gaussian smearing of the DOS over the 0.05 eV width.

Mn-3*s* spectral splitting as measured by x-ray photoelectron spectroscopy, which has been used to identify formal Mn valence states [\[26](#page-3-23)[,27\]](#page-3-24). The GGA/PBE results underestimate  $\Delta E_{\text{Mn3s}}$ , but they do so in a systematic way (Fig. [2\)](#page-2-1) when compared to experimental Mn-3*s* splittings [\[26](#page-3-23)[–28\]](#page-3-25). The calculated  $\Delta E_{\text{Mn3s}}$  values are 3.9 eV for vacancy-free  $MnO<sub>2</sub>$  and 3.8 to 4.0 eV for Ruetschi-defected  $MnO<sub>2</sub>$ . This very slight change indicates that the influence of Ruetschi defects on the magnetic moments of the Mn atoms around the defect sites is quite minor, so a formal high-spin Mn (IV) state can be assigned to the Mn ions in both vacancy-free and Ruetschi-defected  $MnO<sub>2</sub>$ .

Figure [3](#page-3-26) shows that Ruetschi defects reduce the bandgap energy effectively both for the yield in electron-hole pair formation and for charge carrier mobility under photon illumination. In vacancy-free  $MnO<sub>2</sub>$ , the fundamental band gap is indirect [Fig.  $3(a)$ ], and light absorption would

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FIG. 2 (color online). Calculated Mn-3*s* splitting  $(\Delta E_{Mn3s})$  for Mn ions in MnO,  $LiMnO<sub>2</sub>$ , vacancy-free MnO<sub>2</sub>, and Ruetschidefected  $MnO_2$ . Experimental data are for  $MnO_1$ ,  $Mn<sub>2</sub>O_3$ , and  $\beta$ -MnO<sub>2</sub> (Refs. [\[26,](#page-3-23)[28](#page-3-25)]) and MnO, Mn<sub>3</sub>O<sub>4</sub>, LiMnO<sub>2</sub>, and  $Li<sub>2</sub>MnO<sub>3</sub>$  (Ref. [\[27](#page-3-24)]). Cubic MnO and monoclinic  $LiMnO<sub>2</sub>$ splittings were also calculated with spin-polarized GGA/PBE and ferromagnetic ordering among Mn ions. Solid and dash lines guide the data trends.

typically be weak. Introduction of a direct excitation at  $\Gamma$ by the Ruetschi defect  $[Fig. 3(b)]$  $[Fig. 3(b)]$  $[Fig. 3(b)]$  should enhance light absorption compared to vacancy-free  $MnO<sub>2</sub>$ . On the other hand, band-gap-reducing states often diminish the photoactivity of materials because, localized deep inside the band gap, they often function as recombination centers, or traps, of photogenerated electrons and holes (e.g., *d* states of transition metals doped into  $TiO<sub>2</sub>$ ) [[29\]](#page-3-28). In the design of solar cell applications of semiconductors, efficient separation of photoinduced charge carriers has been a principal goal [\[30\]](#page-3-29). The states introduced in Ruetschidefected  $MnO<sub>2</sub>$  have a finite bandwidth overlapping the band states of  $MnO<sub>2</sub>$ , and the change in the conduction band (CB) from the defect is negligible [Figs.  $3(a)$  and [3\(b\)](#page-3-27)]. Therefore, band-gap reduction by Ruetschi defects would not lower the mobility of the photoproduced charge carriers. This point is seen clearly in comparing the charge distribution (orbitals) at the valence band maximum (VBM) and the conduction band minimum (CBM) for vacancy-free  $MnO<sub>2</sub>$  and Ruetschi-defected  $MnO<sub>2</sub>$ [Figs.  $3(c)$  and  $3(d)$ ]. In the vacancy-free MnO<sub>2</sub>, most of electron and hole states are overlapping, whereas in the Ruetschi-defected  $MnO<sub>2</sub>$ , the electron and hole states are well separated. The VBM hole states are near the vacancy site, and the CBM electron states are mostly in a neighboring sheet well away from the VBM hole states. The lowest CB electron states near the vacancy site are found at *ca*. 0.2 eV (4  $\times$  4  $\times$  1 supercell) and 0.3 eV (2  $\times$  2  $\times$  1 supercell) above the CBM at  $\Gamma$  of the Ruetschi-defected MnO<sub>2</sub>.

In summary, the results presented here show that a Ruetschi defect in nanosheet  $MnO<sub>2</sub>$  effectively reduces

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<span id="page-3-27"></span>FIG. 3 (color online). [H: white, Mn: purple (or dark gray), O: red (or lightest gray)] Band structures of (a) vacancy-free  $MnO<sub>2</sub>$ and (b) Ruetschi-defected MnO<sub>2</sub> ( $2 \times 2 \times 1$  supercell). Views of charge distributions of valence band maximum (VBM) hole states [orange (or light gray)] and conduction band minimum (CBM) electron states [blue (or gray)] in (c) vacancy-free  $MnO<sub>2</sub>$ and (d) its Ruetschi-defected MnO<sub>2</sub> ( $4 \times 4 \times 1$  supercell). The Fermi energy was set equal to zero. Isosurfaces represent  $0.001 \text{ e}^{-}/\text{\AA}^{3}$ .

the band-gap energy between occupied and unoccupied electronic states relative to a defect-free layered Mn oxide. Our finding of enhanced photoconductivity by introducing Ruetschi defects suggests that photoinduced electronic transitions by nanosheet  $MnO<sub>2</sub>$  can be optimized by control of defect formation rates during the synthesis of these self-doped materials.

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