Tabletop Creation of Entangled Multi-keV Photon Pairs and the Unruh Effect

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Electrons moving in a strong periodic electromagnetic field (e.g., laser or undulator) may convert quantum vacuum fluctuations into pairs of entangled photons, which can be understood in terms of the Unruh effect. Apart from verifying this striking phenomenon, the considered effect may allow the construction of a tabletop source for entangled photons ("photon pair laser") and the associated quantum-optics applications in the multi-keV regime with near-future facilities.

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The striking discovery that the particle concept in quantum field theory may depend on the inertial state of the observer is one of the main lessons from the Unruh effect [1]. The Minkowski vacuum is the ground state with respect to all stationary and inertial observers moving with a constant velocity. However, an accelerated, i.e., noninertial, observer generally experiences the Minkowski vacuum as an excited quantum state with a nonvanishing content of (Rindler) particles. In case of uniform acceleration a, it corresponds to a thermal bath characterized by the temperature $T_{\text{Unruh}} = \hbar a / (2\pi k_B c)$. Now, considering an accelerated electron, for example, there is a finite probability that a comoving (noninertial) observer witnesses the scattering of a (Rindler) photon out of the thermal bath by the electron due to its nonzero Thomson cross section. Translation of this scattering event observed in the accelerated frame into the (inertial) laboratory frame corresponds to the emission of a pair of real photons [2]. Therefore, accelerated electrons may convert (virtual) quantum vacuum fluctuations into real particle pairs [3] via noninertial scattering-which can be understood in terms of the Unruh effect (similar to moving-mirror radiation [4]). In a previous work [5], we studied the case of electrons under the influence of an approximately constant electric field (corresponding to the case of uniform acceleration) and found that this pair creation effect might be detectable for field strengths not too far below the Schwinger limit [6,7].

In the following, we shall focus on an alternative setup (nonuniform acceleration) and consider electrons that are shot with ultrarelativistic velocities into a strong periodic (e.g., harmonic) electromagnetic field, such as a laser beam or an undulator. In the rest frame of the ultrarelativistic electrons, the (transversal) field strength is strongly boosted and thus the acceleration felt by the electrons is vastly amplified, which facilitates the detection of the effect; cf. [8]. During each acceleration cycle, the electrons emit a small amplitude for photon pair creation and all these amplitudes may add up constructively. In order to demonstrate the main idea, let us assume that the frequency ω (measured in the rest frame of the electrons) of the external electromagnetic field *E* and *B* lies far below the electrons rest mass $m \gg \omega$, and that its normalized amplitude is small $qE \ll m\omega$ and $qB \ll m\omega$ (i.e., large Keldysh parameter). In the natural units used here, $\hbar = c = \varepsilon_0 = \mu_0 = 1$, the electron charge *q* is related to the fine-structure constant α_{QED} via $q = \sqrt{4\pi\alpha_{\text{QED}}}$. In the rest frame of the electrons, their classical quivering motion induced by the external field

$$\boldsymbol{r}_{\rm cl}(t) = \boldsymbol{e}_z \frac{qE}{m\omega^2} \cos(\omega t) \tag{1}$$

is nonrelativistic $\dot{r}_{cl}^2 \ll 1$, and thus the impact of the magnetic field (i.e., photon pressure) can be neglected. Furthermore, the spin of the electrons can be ignored since the spin energy $\mu_e B$ is much smaller than the frequency $\mu_e B \ll \omega$. Hence the dynamics of the electrons under the influence of the (classical plus quantum) electromagnetic field is governed by the Lagrangian

$$L(\dot{\boldsymbol{r}}_e, \boldsymbol{r}_e) = \frac{m}{2} \dot{\boldsymbol{r}}_e^2 - q \dot{\boldsymbol{r}}_e \cdot \boldsymbol{A}(\boldsymbol{r}_e), \qquad (2)$$

where A is the vector potential in temporal gauge. Now we split the electromagnetic field $A = A_{cl} + A_{qu}$ into a large classical part A_{cl} plus small quantum fluctuations A_{qu} , e.g., scattered photons. Accordingly, the electron trajectory $\mathbf{r}_e = \mathbf{r}_{cl} + \mathbf{r}_{qu}$ is split up into the classical quivering motion \mathbf{r}_{cl} in Eq. (1) plus small quantum fluctuations \mathbf{r}_{qu} due to coupling to the quantized electromagnetic field A_{qu} . The Euler-Lagrange equations $d[m\dot{\mathbf{r}}_e - qA(\mathbf{r}_e)]/dt = -q\partial[\dot{\mathbf{r}}_e \cdot A(\mathbf{r}_e)]/\partial \mathbf{r}_e$ imply that the canonical momentum $\mathbf{p}_e = m\dot{\mathbf{r}}_e - qA$ is conserved to first order \mathbf{p}_{qu} if the right-hand side vanishes. This is precisely the condition for planar Thomson scattering, which is satisfied if the polarizations are orthogonal or, alternatively, for planar momenta $\mathbf{k}_{qu}, \mathbf{k}_{cl}$

$$A_{\rm qu} \perp A_{\rm cl} \parallel \mathbf{r}_{\rm cl} \perp \mathbf{r}_{\rm qu} \lor \mathbf{k}_{\rm qu} \perp \mathbf{r}_{\rm qu} \parallel A_{\rm qu} \perp \mathbf{k}_{\rm cl}.$$
 (3)

In this case, we get $\dot{\mathbf{r}}_{qu} = q\mathbf{A}_{qu}/m$ (up to an irrelevant constant). The equations of the electromagnetic field depending on the full electron trajectory $\mathbf{r}_e(t)$ read

$$\ddot{A} - \nabla \times (\nabla \times A) = -q\dot{r}_e \delta^3(r_e - r).$$
(4)

(The longitudinal component $\nabla \cdot A$ is nonvanishing in temporal gauge and contains the instantaneous Coulomb field, which does not contribute to the radiation content.) Inserting the split $\mathbf{r}_e = \mathbf{r}_{cl} + \mathbf{r}_{qu}$ into the source term yields the classical Larmor radiation from \mathbf{r}_{cl} plus quantum corrections. There are two lowest-order corrections: variations of the electron position $\delta^3(\mathbf{r}_{cl} + \mathbf{r}_{qu} - \mathbf{r})$ plus the current $\dot{\mathbf{r}}_{qu}$ due to quantum fluctuations. Since the first contribution vanishes for parallel photons $\mathbf{k} \parallel \mathbf{k}'$ (the case we are mostly interested in) and does not generate polarization correlations (which will be used for detection), we shall focus on the quantum current $\dot{\mathbf{r}}_{qu}$. Combining Eq. (4) and $\dot{\mathbf{r}}_{qu} = q\mathbf{A}_{qu}/m$, we obtain the effective interaction Hamiltonian for planar Thomson scattering

$$\hat{H}_{\rm eff}(t) = \frac{q^2}{2m} \hat{A}^2[t, r_{\rm cl}(t)].$$
(5)

(Note that a factor of 2 is missing in [5].) The photon pairs created out of the quantum vacuum by noninertial scattering can now be calculated via time-dependent perturbation theory yielding the two-photon amplitude

$$\mathfrak{A}_{\boldsymbol{k},\boldsymbol{\lambda},\boldsymbol{k}',\boldsymbol{\lambda}'} = \frac{q^2}{4m} \frac{\boldsymbol{e}_{\boldsymbol{k},\boldsymbol{\lambda}} \cdot \boldsymbol{e}_{\boldsymbol{k}',\boldsymbol{\lambda}'}}{V\sqrt{kk'}} \mathcal{F}_{\boldsymbol{k},\boldsymbol{k}'},\tag{6}$$

where V is the quantization volume and $e_{k,\lambda}$, $e_{k',\lambda'}$ denote the (linear) polarization vectors of the two created photons with wave numbers k and k', respectively. The remaining time integral

$$\mathcal{F}_{\boldsymbol{k},\boldsymbol{k}'} = i \int dt \exp\{i(\boldsymbol{k} + \boldsymbol{k}')t - i(\boldsymbol{k} + \boldsymbol{k}') \cdot \boldsymbol{r}_{\rm cl}(t)\} \quad (7)$$

can be Taylor expanded for small oscillation amplitudes $\mathcal{F}_{k,k'} \approx \int dt e^{i(k+k')t} (\mathbf{k} + \mathbf{k}') \cdot \mathbf{r}_{cl}(t)$ and just yields the Fourier transform $(\mathbf{k} + \mathbf{k}') \cdot \tilde{\mathbf{r}}_{cl}(k + k')$ of the quivering motion evaluated at a frequency of k + k' and projected onto $\mathbf{k} + \mathbf{k}'$. The resonance condition (energy conservation) reads $k + k' = \omega$, and at resonance, we get

$$\mathfrak{A}_{\boldsymbol{k},\boldsymbol{\lambda},\boldsymbol{k}',\boldsymbol{\lambda}'} = \frac{q^{3}E}{8m^{2}} \frac{\boldsymbol{e}_{\boldsymbol{k},\boldsymbol{\lambda}} \cdot \boldsymbol{e}_{\boldsymbol{k}',\boldsymbol{\lambda}'}}{\omega^{3}V} \frac{k_{z} + k_{z}'}{\sqrt{kk'}} \,\omega T, \qquad (8)$$

where ωT counts the number of laser cycles experienced by the electrons. The probability of emitting a pair of photons in resonance band $k + k' = \omega \pm \mathcal{O}(1/T)$ can be estimated via $\sum_{\lambda,\lambda'} (\mathbf{e}_{\mathbf{k},\lambda} \cdot \mathbf{e}_{\mathbf{k}',\lambda'})^2 = 1 + (\mathbf{e}_{\mathbf{k}} \cdot \mathbf{e}_{\mathbf{k}'})^2 \ge 1$

$$\mathfrak{P}_{\text{Unruh}} = \frac{\alpha_{\text{QED}}^2}{4\pi} \left[\frac{E}{E_s}\right]^2 \mathcal{O}\left(\frac{\omega T}{30}\right) \ll 1, \qquad (9)$$

where $E_s = m^2/q$ denotes the Schwinger limit [6] and the exact prefactor depends on the pulse shape etc. [9].

Of course, the electron does not just act as a scatterer, but also possesses a charge—and, as every accelerated charge, emits Larmor radiation. This classical radiation corresponds to a coherent state and can fully be described by the associated one-photon amplitudes

$$\alpha_{\boldsymbol{k},\lambda} = q \int dt \frac{\boldsymbol{e}_{\boldsymbol{k},\lambda} \cdot \dot{\boldsymbol{r}}_{\rm cl}(t)}{\sqrt{2Vk}} \exp\{ikt - i\boldsymbol{k} \cdot \boldsymbol{r}_{\rm cl}(t)\}.$$
 (10)

From the scalar product $e_{k,\lambda} \cdot \dot{r}_{cl}$, one may read off the well-known blind spot and the fixed polarization. Similar to the above estimate (9), the one-photon probability of this classical counterpart yields (see also [10])

$$\mathfrak{P}_{\text{Larmor}}^{(1)} = \alpha_{\text{QED}} \left[\frac{qE}{m\omega} \right]^2 \mathcal{O} \left(\frac{\omega T}{2} \right). \tag{11}$$

In view of $\omega \ll m$, the total classical probability above exceeds the probability $\mathfrak{P}_{\text{Unruh}}$ of quantum radiation. However, as one may infer from Eq. (10), the classical resonance condition reads $k = \omega$; i.e., the Larmor photons are predominantly monochromatic (in the electron frame). In contrast, the photon pairs created via the Unruh effect occur at different frequencies, as long as they satisfy $k + k' = \omega$; i.e., these pairs are correlated in energy and polarization [11] (whereas the Larmor radiation has a fixed polarization and a blind spot in the *z* direction). Note that the ratio of the probabilities in Eqs. (9) and (11) is roughly independent of the field strength *E*

$$\frac{\mathfrak{B}_{\text{Unruh}}}{\mathfrak{B}_{\text{Larmor}}^{(1)}} = \mathcal{O}\left(\frac{\alpha_{\text{QED}}}{60\pi} \frac{\omega^2}{m^2}\right).$$
(12)

Let us insert a set of parameters that are potentially realizable with present or near-future technology [12]. Assuming an optical laser beam with a photon energy of 2.5 eV (in the laboratory frame) and a boost factor of $\gamma =$ 300, the photon energy in the rest frame of the electrons $\omega = 1.5$ keV is still much smaller than the electron mass. With a laser intensity of order 10^{18} W/cm² in the laboratory frame, the electric field E lies a factor of 1000 below the Schwinger limit E_S in the rest frame of the electrons and their transversal quivering motion $\dot{r}_{cl}^2 \approx 1/9$ is still approximately nonrelativistic. After 100 laser cycles (width of a Gaussian pulse), we obtain a two-photon probability around 4×10^{-11} from one electron. Depending on their direction, the sum of the energies of the created photons in the laboratory frame is then around 500 keV [13]. The total probability for the competing classical counterpart (Larmor radiation) is much higher $\mathcal{O}(10^{-1})$. Fortunately, the monochromatic character (rest frame of electrons) of the Larmor radiation (which just corresponds to Thomson scattering of the laser photons) in our setup ensures that the phase-space regions of the two effects are very different. In the laboratory frame, the phase space is quite distorted after the boost (see Fig. 1), but it is (at least in principle) still possible to discriminate the two effects via suitable apertures and energy filters, etc.

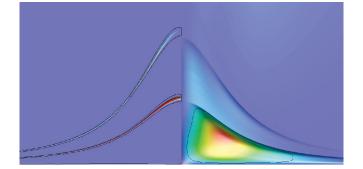


FIG. 1 (color). $E \cdot \vartheta$ plot of the one-photon probability of classical (Larmor, left half of image) and quantum (Unruh, right) radiation in the laboratory frame (averaged over rotations around beam axis). An electron with a boost factor of $\gamma = 300$ hits a counterpropagating optical Gaussian laser pulse with an intensity of 10^{18} W/cm² and a width of 100 cycles. The photon energy E ranges from zero (bottom) to 2 MeV (top) and ϑ varies from zero (middle) to 1/100 (left and right boundary). In the chosen color coding (not the same in the two images), red indicates a large and dark blue a vanishing probability. The black isolines denote the same values in both pictures and show that the quantum radiation dominates in certain phase-space regions (which could be extracted with apertures and energy filters). As one may infer from the visibility of the second harmonic, relativistic effects already start to play a role for this set of parameters ($\dot{r}_{cl}^2 \approx 1/9$). Therefore, we numerically calculated the full electron trajectory (including the impact of the magnetic field) and inserted it into Eqs. (6), (7), and (10), respectively.

So far, we considered the case of single electrons only. For many electrons, their space-time distribution and the resulting spatial interference becomes important (in addition to the temporal interference, which yields the resonance conditions $k = \omega$ and $k + k' = \omega$). For both classical and quantum radiation, one should distinguish two major limiting cases: incoherent or coherent superposition. If the electrons are randomly distributed and their typical distance is much larger than $1/\omega$, we have an incoherent superposition (addition of probabilities). For example, sending such a pulse of $N_e = 6 \times 10^9$ independent electrons [12] into a laser beam with the values discussed above, we obtain around one Unruh event in four shots. One option to suppress the competing Larmor radiation could be to detect photons from a small cone $\Delta \vartheta$ around the blind spot at $e_{k,\lambda} \cdot \dot{r}_{cl} = 0$ only; cf. Eq. (10). For the values $E = 10^{-4}E_s$ and $\Delta \vartheta = 10^{-2}$, the Larmor probability is suppressed to 4×10^{-12} . For example, for $N_e = 6 \times 10^9$ electrons and 10^4 laser cycles, we get a few Larmor photons per shot. But now the Unruh-Larmor ratio is strongly enhanced to 7×10^{-6} and a repetition rate of a few Hz (up to 1 kHz [12]) would result in a couple of Unruh events per day (down to a few minutes).

Of course, a coherent superposition (constructive interference of amplitudes) would be much more effective. It is probably hard to achieve the necessary phase coherence (e.g., to confine all the electrons to within half a wavelength π/ω) for optical lasers, but in undulators for freeelectron lasers (FEL), this is already state of the art. Because of the backreaction of the created Larmor radiation, the original electron pulse is split up into many nearly equidistant microbunches. The amplitudes generated by the zigzag motion of these microbunches interfere constructively in forward (i.e., electron beam) direction leading to the amplification of Larmor radiation (in the ideal case $\propto N_e^2$ instead of $\propto N_e$). Comparing Eqs. (7) and (10), we see that the quantum (two-photon) amplitudes (8) do also interfere constructively if both photons (with $k + k' = \omega$) are emitted in forward direction.

In this setup, the laser wavelength should be replaced by the undulator period of order ten millimeters, which corresponds to a frequency $\omega = \mathcal{O}(1 \text{ eV})$ in the electron frame for a boost factor of $\gamma = 4000$. In the laboratory frame, the monochromatic Larmor photons would have an energy around 8 keV and could be filtered out via multiple Bragg scattering. In order to eliminate further background, it might be useful to send the microbunches shaped in one undulator into a second one (and to get rid of the photons from the first undulator) and to switch on and off the undulator field smoothly, i.e., with a Gaussian instead of a rectangular envelope. If the period of the second undulator is slightly different from the first one (generating the microbunches), we may even send the Larmor and the Unruh photons into different spatial directions: For Larmor radiation, the phase matching conditions (in the electron frame) read $k = \omega$ and $\mathbf{k} \cdot \mathbf{n} = \kappa_{\text{micro}} \pm \kappa_{\text{und}}$, where *n* is the beam axis and κ_{micro} as well as κ_{und} denote the inverse length scales of the microbunches and the undulator, respectively. Hence the angle ϑ between the beam axis and Larmor radiation is fixed. For an Unruh pair, on the other hand, the phase matching conditions read $k + k' = \omega$ and $(\mathbf{k} + \mathbf{k}') \cdot \mathbf{n} = \kappa_{\text{micro}} \pm \kappa_{\text{und}}$; i.e., the two photons will be emitted at angles ϑ and ϑ' away from the Larmor cone in general. The quantum numbers of the two photons are entangled; i.e., if one photon (k, λ, ϑ) of the pair is detected, the energy k', the polarization λ' , and the angle ϑ' of the other one are fixed.

By adding up the amplitudes generated by many electrons coherently, it might even be possible to reach the nonperturbative regime, where multiphoton effects become important. In this regime, there is a crucial difference between quantum and classical radiation: Classical radiation can be described by a coherent state $|\alpha\rangle = \exp\{\alpha \hat{a}^{\dagger} - \alpha \hat{a}^{\dagger}\}$ $\alpha^* \hat{a} |0\rangle$. In this case, the photon number $\langle \alpha | \hat{n} | \alpha \rangle = |\alpha|^2$ scales quadratically with the number of electrons $\alpha \propto N_{e}$ (constructive interference). Quantum radiation, on the other hand, corresponds to a (multimode) squeezed state $|\xi\rangle = \exp\{\xi \hat{a}_1^{\dagger} \hat{a}_2^{\dagger} - \xi^* \hat{a}_1 \hat{a}_2\}|0\rangle$, where we consider two modes \hat{a}_1 and \hat{a}_2 for simplicity. For small amplitudes $\xi \ll$ 1, the photon number $\langle \xi | \hat{n}_1 | \xi \rangle = \sinh^2(|\xi|)$ also scales quadratically with the number of electrons $\xi \propto N_e$, but after a certain threshold $\xi = \mathcal{O}(1)$ is reached, it grows exponentially [14]. Ignoring all geometrical factors, the threshold can be estimated from Eq. (8): after passing $N_e = O(\alpha_{\text{QED}}^{-1} E_S / E)$ electrons (in the oscillating microbunches), the two-photon wave packets start to grow exponentially (until their growth is limited by backreaction, etc.). Reaching this threshold is a quite ambitious goal, but may become within reach with the next generation of FEL.

The signatures of the Unruh effect discussed above bear strong similarities to (spontaneous) parametric downconversion [15] known from quantum optics: The external periodic electromagnetic field corresponds to the pump beam, and the electrons are analogous to the nonlinear dielectric medium. In both cases, the scattering properties (refractive index) of the medium are varied periodically (frequency ω) by the multiphoton pump beam and thereby the quantum vacuum fluctuations of the electromagnetic field are converted into (a small number of) pairs of entangled photons (signal and idler) whose energies add up to the pump frequency $k + k' = \omega$. In quantum optics, this mechanism is the main source for entangled photon pairs, which have a wide range of applications including concepts known from quantum information theory (e.g., tests of Bell's inequality, quantum cryptography, or teleportation), two-photon interferometry, photonic Fock states (i.e., states with a well-defined photon number, which could be used for counting excitations, for example), heralded photon emission, and coincidence experiments, etc. Since the quantum radiation discussed here consists of entangled photon pairs with much higher energies (which are typically more robust, less noisy, and offer higher interaction rates), it may help to transfer these quantumoptics applications into the multi-keV regime [16].

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A. Roura, *ibid.* **93**, 129301 (2004); M. O. Scully *et al.*, *ibid.* **93**, 129302 (2004); A. Belyanin *et al.*, Phys. Rev. A **74**, 023807 (2006); and similar ideas, where the predicted enhancement of acceleration radiation is caused by non-adiabatic switching effects (at the entrance and the exit of the cavity), the mechanism considered in the present Letter is a consequence of the real acceleration a = qE/m felt by the electrons.

- [9] Note that, after reaching the relativistic limit $qE = \omega m$, the probability $\mathfrak{P}_{\text{Unruh}}$ scales with ω^2/m^2 ; i.e., further increasing *E* basically does not enhance the probability $\mathfrak{P}_{\text{Unruh}}$ for the lowest resonance anymore, merely the higher harmonics grow.
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- [13] The photons could be detected with Ge strip detectors (based on Compton scattering), which provide a good energy resolution (of order keV) in the range between 100 and 500 keV and are even sensitive to the polarization. A typical segmentation size of order millimeter results in an angular resolution of $\delta \vartheta = \mathcal{O}(10^{-4})$ after a distance of order ten meters, which should be sufficient for a boost factor of $\gamma = 300$; see Fig. 1.
- [14] It is interesting to note that the single-photon distribution is thermal; i.e., the reduced density matrix $\hat{\varrho}_1$ of one photon obtained after averaging the (entangled) quantum state over the other photon $\hat{\varrho}_1 = \text{Tr}_2\{|\xi\rangle\langle\xi|\}$ exactly corresponds to the canonical ensemble. The associated temperature, however, is not constant but depends on ξ , i.e., the quantum numbers of the photon.
- [15] It should be mentioned here that x-ray down-conversion (in crystals, for example), which has already been observed in the laboratory [I. Freund and B. F. Levine, Phys. Rev. Lett. 23, 854 (1969); P. Eisenberger and S. L. McCall, *ibid.* 26, 684 (1971); Y. Yoda *et al.*, J. Synchrotron Radiat. 5, 980 (1998); B. Adams et al., ibid. 7, 81 (2000)], could in principle also be interpreted as a signature of the Unruh effect (in the weak-field limit), since the involved electrons in the crystal can be considered quasifree. However, the setup discussed here offers more options for tuning (e.g., tapering of the undulator) and can be applied to a wider range of parameters. For instance, it involves much stronger fields (i.e., many laser photons interact coherently with the electrons) and one can reach higher energies (increasing γ and using an optical laser instead of an undulator, etc.). Moreover, the efficiency is much larger, e.g., the considerations above show that it might even be possible to reach the (nonperturbative) regime where many photon pairs are created coherently ("photon pair laser").
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