⁶S. J. Lindenbaum, W. A. Love, J. A. Neiderer, S. Ozaki, J. J. Russell, and L. C. L. Yuan, Phys. Rev. Letters <u>7</u>, 184,352 (1961); G. von Dardel,

D. Dekkers, R. Mermod, M. Vivargent, G. Weber, and K. Winter, Phys. Rev. Letters 8, 173 (1962).

⁷A. N. Diddens, E. Lillethun, G. Manning, A. E. Taylor, T. G. Walker, and A. M. Wetherell, Phys. Rev. Letters <u>9</u>, 108 (1962).

⁸Our argument to justify the use of the Schrödinger equation coincides with that of J. M. Cornwall and M. A. Ruderman, Phys. Rev. <u>128</u>, 1474 (1962). We note especially that the Klein-Gordon and Dirac equations can always be cast into the form of (6) where k^2 is the square of the incident momentum. As long as k^2 has this meaning, (6) describes correctly the asymptotic behavior of scattering. Note that k^2 is essentially s of this note.

⁹R. J. Glauber, <u>Lectures Delivered at the Summer</u> <u>Institute for Theoretical Physics</u>, <u>University of Colora-</u> do 1958-59, edited by W. E. Brittin and L. G. Dunham (Interscience Publishers, Inc., New York, 1959), Vol. 1, p. 315.

¹⁰The physical reason for this analyticity is the microscopic causality as is explained by Cornwall and Ruderman in reference 8. See, also, H. Feshbach, Ann. Phys. (N.Y.) 5, 357 (1958).

¹¹This does not necessarily mean that R is energy independent.

¹²The proof by Cornwall and Ruderman in reference 8 assumes that $V(r, k^2)$ is bounded everywhere in the k^2 plane. This, however, does not seem to be crucial in their proof according to M. A. Ruderman (private communication).

¹³Y. Nambu and M. Sugawara (to be published). We are unable to confirm if the condition $\alpha(t) = 1$ is compatible with the unitarity condition. According to V. N. Gribov, Nucl. Phys. <u>22</u>, 249 (1961), the condition $\alpha(t) = 1$ is not consistent with the analyticity and unitarity conditions. As far as we could see, however, his argument is not conclusive.

EXAMPLE OF $\Sigma^+ \rightarrow p + \gamma$ IN A HYDROGEN BUBBLE CHAMBER*

R. A. Burnstein, T. B. Day, F. Martin, and M. Sakitt[†] University of Maryland, College Park, Maryland

and

R. G. Glasser, N. Seeman, and A. J. Herz U. S. Naval Research Laboratory, Washington, D. C. (Received 13 February 1963)

Several searches have been made for the decay $\Sigma^+ \rightarrow p + \gamma$ of which two^{1,2} claim negative results and two^{3,4} claim positive results. All of the previous attempts were done in emulsions. In this Letter we present evidence of a $\Sigma^+ \rightarrow p + \gamma$ decay where the Σ^+ hyperon was produced by a K^- meson at rest in a hydrogen bubble chamber.

As part of our study of stopping K^- mesons in the Alvarez 15-in. hydrogen bubble chamber, we have measured all Σ^+ hyperons which were produced and did not decay into a light track. The events were found by a double general scan in which all K^- mesons entering a specified fiducial region were followed. The events were processed through a combined program of PANG and KICK called PACKAGE, and then the output was sorted by an EXAMIN program.

In our event, the K^- came to rest and produced a Σ^+ which decayed in flight. The proton came off backwards and stopped in the chamber. This type of configuration could be due to either

$$K^{-} + p \rightarrow \Sigma^{+} + \pi^{-}$$

$$\downarrow p + \gamma \qquad (1)$$

or

$$K^{-} + p - \Sigma^{+} + \pi^{-}$$

$$p + \pi^{0}.$$
(2)

The unfitted data for the tracks are shown in Table I.

The near colinearity of the Σ^+ and π^- , and the close agreement of the beginning momentum of the K^- with the value of momentum obtained by range, strongly suggest that one should try to fit the production of the Σ^+ assuming the K^- stops. This fit is a 3-constraint fit since the magnitude of the Σ^+ momentum, from curvature, is too poorly determined to be used in the fitting. After propagating the Σ^+ to the decay vertex, we did a 1-constraint fit. The results for our three measurements are shown in Table II. As an additional check, we tried fitting the over-all event as a 4-constraint fit on another measurement and obtained

 $\chi^2(\Sigma^+ + p + \pi^0) = 147.54, \quad \chi^2(\Sigma^+ - p + \gamma) = 0.59.$

We now consider various interpretations of the event as a $\Sigma^+ \rightarrow p + \pi^0$ decay which would give

	P	Phi	Dip
	(MeV/c)	(degrees)	(degrees)
	Produ	ction Vertex	
K ⁻	221.8 ± 13.3 at beginning,	250.55 ± 0.51	7.42 ± 0.75
	from curvature		
	213.2 ± 1.1 from range		
π-	181.7 \pm 7.3 from curvature	178.35 ± 0.23	23.39 ± 0.35
Σ^+	136.3 ± 1.9 from range	358.44 ± 4.29	-20.95 ± 4.09
	Dec	ay Vertex	
Σ^+	5 mm length	1.55 ± 4.29	-20.93 ± 4.09
Þ	137.0 ± 1.0 from range	104.09 ± 2.24	29.41 ± 2.19

Table II. Vertex fits (chi-squares).

	N		
	1	2	3
$\overline{K^- + p \rightarrow \Sigma^+ + \pi^-}$	0.35	0.77	0.88
$\Sigma^+ \rightarrow p + \pi^0$	92.85	829.35 (first step)	96.48
$\Sigma^+ \rightarrow p + \gamma$	5.08	0.09	3.66

rise to a poor fit, if they were possible.

(a) The Σ^+ could have decayed within 1 mm of the production vertex, and what we see is really a proton which then scatters. This is impossible since the proton would have to backscatter in the laboratory system.

(b) The proton could have scattered as it came out of the decay vertex. If it came from the Σ^+ decay, the track of the minimum recoil proton, such that the decay proton ends up in its observed final state, is greater than 2 mm. This recoil should be quite visible and cannot be hidden under the decay proton or Σ^+ . We see no such recoil.

(c) The Σ^+ could have scattered just before decaying without giving rise to a visible recoil. If the hyperon has to decay with the proton ending up in the observed final state, the minimum recoil is 1.3 mm. This recoil should be quite visible and cannot be hidden under the decay proton

or Σ^+ hyperon. We see no such recoil.

(d)The production vertex could have been slightly in flight. This could not explain the observed decay, since the unfitted data allows very little K^{-} momentum.

Our conclusion is that this event is, indeed, an example of the decay $\Sigma^+ - p + \gamma$. It was found in a sample of 237 $\Sigma^+ \rightarrow p + \pi^0$ events with a confidence level of at least 1%, giving a branching ratio on the order of 0.4%.

We would like to express our deep appreciation of the help given us by the Alvarez group, especially Dr. Humphrey and Dr. Ross, in sending us the film and the original versions of the programs. We are particularly indebted to Professor G. A. Snow for his continual guidance throughout this work.

³G. Quareni, A. Quareni Vignudelli, G. Dasida, and S. Mora, Nuovo Cimento 14, 1179 (1959).

^{*}Work supported by U. S. Atomic Energy Commission.

[†]U. S. Steel Fellow.

¹S. C. Freden, H. N. Kernblum, and R. S. White, Nuovo Cimento 16, 611 (1960).

²R. G. Glasser, N. Seeman, Y. Prakash, G. A. Snow, and P. Steinberg, Nuovo Cimento 19, 1058 (1961).

⁴J. Schneps and Y. W. Kang, Nuovo Cimento 19, 1218 (1961).