

Nanoscale mechanical probing of supported lipid bilayers with atomic force microscopy

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We present theory and experiments for the force-distance curve $F(z_0)$ of an atomic force microscope (AFM) tip (radius R) indenting a supported fluid bilayer (thickness $2d$). For realistic conditions the force is dominated by the area compressibility modulus κ_A of the bilayer and, to an excellent approximation, given by $F = \pi\kappa_A R z_0^2 / (2d - z_0)^2$. The experimental AFM force curves from coexisting liquid ordered and liquid disordered domains in three-component lipid bilayers are well described by our model, which provides κ_A in agreement with literature values. The liquid ordered phase has a yieldlike response that we model as due to the breaking of hydrogen bonds.

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I. INTRODUCTION

Atomic force microscopy (AFM) [1] has become a standard tool for imaging surfaces at high resolution and probing local mechanical properties [2]. Force-distance curves for indentation of AFM tips have been used to characterize the mechanical properties of biological membranes [3–5], and the usual approach is to approximate the bilayer as an elastic solid undergoing a Hertzian contact [6–8]. However, at physiological conditions most biological membranes are in a fluid bilayer phase [9], whose free energy is described by a bending modulus κ and the area compressibility modulus κ_A . These are experimentally accessible through, for example, micropipette aspiration experiments [10], which give the average value of the elastic moduli over the whole vesicle. However, biological membranes often have different local compositions, and thus different local mechanical properties and physiological functions.

Despite the growing use of AFM to study lipid bilayers, the flexibility of using it to measure local mechanical properties has not been fully exploited. An AFM tip can bend a freely suspended membrane and compress a supported membrane. In recent work, Steltenkamp *et al.* [11] showed how to extract the bending modulus of lipid bilayers from AFM force-distance curves for bilayers deposited over well-defined sized holes (indentation of “nanodrums”), in which they could safely ignore area compression due to the lack of a supported surface. Another issue neglected in previous AFM studies is the double leaflet form of lipid bilayers, which is known to influence the dynamics of fluctuations [12]. Since an AFM tip induces an asymmetric response in a supported bilayer [13], the distinction between the two leaflets will be important to accurately model the mechanical response.

In this paper we consider the force-distance curves obtained by indenting an AFM tip into a fluid bilayer supported on a solid substrate. The force-distance curves are calculated

from a static analysis of the deformation of the two leaflets and differ from usual Hertzian result of the deformation of elastic bodies. We analyze experiments on a dioleoylphosphatidylcholine (DOPC)–egg sphingomyelin (SM)–cholesterol (CHOL) phase separated supported bilayer, which is a model mixture representative of typical *in vivo* membranes [14]. For certain composition ratios of the components, this system spontaneously phase separates into coexisting liquid ordered (L_o , rich in SM and relatively thick because of strong nematic order in the acyl tails) and liquid disordered (L_d , rich in DOPC and relatively thin because of the more disordered tails) phases. We show how to determine the area compressibility moduli of the coexisting L_o and L_d phases of a single sample and find values in agreement with literature values. Here, the area compressibilities of the two coexisting compositions in fluid bilayers have been extracted directly. This technique should prove invaluable for studying the composition dependence of mechanical properties in lipid bilayers, and can be easily extended to consider more complex interactions between AFM tip and the bilayer.

II. THEORY

We consider a supported fluid lipid bilayer of thickness $2d$ probed by an AFM tip of radius R in contact mode, which measures the force as a function of the depth z_0 from the unperturbed surface of the layer [see Fig. 1(a)]. At typical AFM speeds the viscous forces are negligible. We begin by assuming a hard contact interaction between the tip and the membrane. Electrostatic repulsion from the charged double layers and van der Waals attraction are included later in the paper when comparisons are made with experiments. Since the lipid bilayer is not anchored it remains tension-free. We assume that the volume is conserved at the molecular level: as the tip penetrates the bilayer it occupies a volume δV , so that $\delta N = \delta V / (a_0 d)$ lipids are expelled into the surrounding bilayer. Here, a_0 is the area per lipid in the absence of the AFM tip. The surface area increases by δA , due to the curved spherical surface of the AFM tip, and the increase in area per head group $\delta a \equiv a - a_0$ is given by

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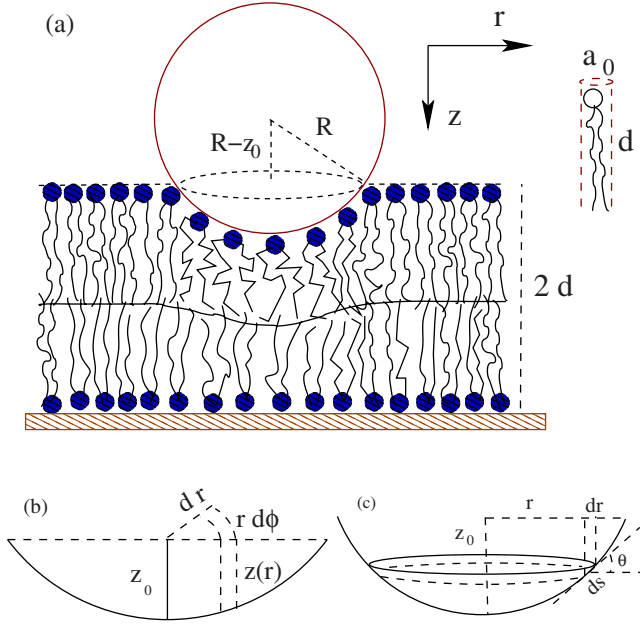


FIG. 1. (Color online) (a) Schematic geometry of an AFM tip of radius R indenting a fluid bilayer of thickness $2d$ by an amount z_0 . The leaflet dividing surface at $h_b(r)$ is shown as a solid line. (b) Cylindrical volume elements of depth $z(r)$ at the distance r from the center of the tip. (c) The area $2\pi r ds$ of such an element in contact with the lipid.

$$\delta a = \frac{A + \delta A}{N - \delta N} - a_0 = a_0 d \left(\frac{A + \delta A}{V - \delta V} \right) - a_0. \quad (1)$$

This increased area induces an elastic cost due to the stretching elasticity of the lipid leaflets. We calculate this not by averaging over the entire spherical cap, but by considering small increases in radius dr and evaluating $\delta a/a_0$ at each r (Fig. 1).

We assume that both leaflets have the same area per lipid a_0 and stretching modulus $\kappa_A/2$ for lipid head groups on a flat surface. This should be valid in the absence of specific interactions of the lipid with the substrate, although experiments have shown that the surface often does have specific interactions [13]. The head groups in the top leaflet are forced to lie on a curved surface below the AFM tip. This affects both the area per lipid and the stretching modulus for the lipids on the top leaflet. We model the local lipid free energy as a sum of a surface energy and a harmonic tail stretching, $g(L) \approx \gamma a_L / \cos \theta + \alpha / a_L^2$, where γ is a surface tension, α penalizes tail stretching, and a_L is the projected area for leaflet thickness L . Here, $\theta(r) = \sin^{-1}(r/R)$ [Fig. 1(c)] is the tilt angle of the lipid surface. Minimizing g at fixed lipid volume $v \approx L a_L$ leads to an effective stretching modulus $\tilde{\kappa}_A/2 \approx \kappa_A/2 \sec^{2/3} \theta$ and an effective area per lipid $a_t^0 = a_0 \cos^{1/3}$ for the top leaflet.

Using the modifications due to the curved surface for the head groups in the top leaflet, the excess free energy due to the increase in the area per lipid during indentation is

$$G(z_0) = \frac{\kappa_A}{4} \int_S d^2 r \left[\sec^{2/3} \theta(r) \left(\frac{\delta a}{a_0} \right)_t^2 + \left(\frac{\delta a}{a_0} \right)_b^2 \right], \quad (2)$$

where t and b refer to the top and bottom leaflets and the integration extends over both leaflets. The lower leaflet will generally deform to accommodate the large energy change due to removing too many lipids from the upper leaflet. We let the lower and upper leaflets have thicknesses $h_b(r)$ and $h_t(r)$, respectively, with $h_b(r) + h_t(r) = 2d - z_0 + R[1 - \cos \theta(r)]$. The area changes at each radius r are given by (Fig. 1)

$$\left(\frac{\delta a}{a_0} \right)_t^2 = \left[\frac{d \sec^{1/3} \theta(r)}{h_t(r)} - 1 \right]^2, \quad (3a)$$

$$\left(\frac{\delta a}{a_0} \right)_b^2 = \left(\frac{d}{h_b(r)} - 1 \right)^2. \quad (3b)$$

The measure is $d^2 r = r dr d\phi$. The dividing surface $h_b(r)$ is determined by minimizing the free energy at each r . For equal stretching moduli in both leaflets, an explicit solution for $h_b(r)$ is possible for small tilt angle,

$$h_b(r) = \frac{2d - z_0 + R[1 - \cos \theta(r)]}{1 + \sec^{1/3} \theta}. \quad (4)$$

For realistic values $z_0 \sim 2$ nm, $d \sim 3$ nm, and $R \sim 10$ nm, this approximation introduces less than 0.1% error in $h_b(r)$ for the entire range of r . We use this approximation in the rest of the paper to derive analytical expressions for the free energy and force.

Using $h_m(r)$ from Eq. (4), the free energy is

$$\frac{2G(z_0)}{\pi \kappa_A R^2} = \int_{1-z_0/R}^1 x(1+x^{-2/3}) \times \left[\frac{(1+x^{1/3})}{x^{1/3} \left[2 - \frac{z_0}{d} + \frac{R}{d}(1-x) \right]} - 1 \right]^2 dx, \quad (5)$$

and the force on the AFM tip is given by $F = \partial G / \partial z_0$. We use the numerical force derived from Eq. (2) when performing fits to the data. For small penetrations z_0 the force can be written as

$$F \approx \frac{\pi \kappa_A R}{4} \left[1 + \frac{d}{3R} + \left(\frac{d}{3R} \right)^2 \right] \left(\frac{z_0}{d} \right)^2 + \mathcal{O}(z_0^3) \dots \quad (6)$$

A surprisingly simple function that fits the entire experimental range of forces, correct to within a few percent for $R = 3d$ and much better for larger R , is

$$F = \frac{\pi \kappa_A R}{4} \left(\frac{2z_0}{2d - z_0} \right)^2. \quad (7)$$

The force diverges as z_0 approaches $2d$ because the area per lipid diverges in order to preserve molecular volume. The quadratic free energy [Eq. (2)] is no longer valid there. Experimentally this divergence is pre-empted by pore formation (see below).

For comparison, the contact force between two solid (elastic) bodies much larger than the radius of contact (Hert-

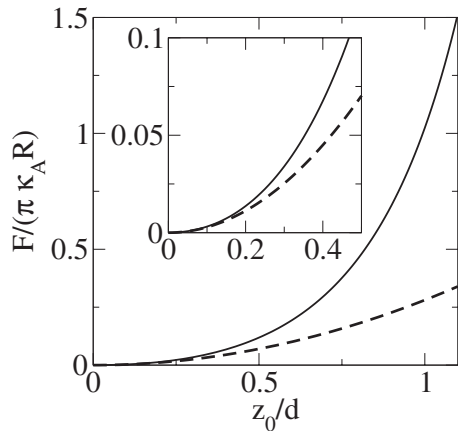


FIG. 2. Scaled force $F/(\pi\kappa_A R)$ as a function of tip depth z_0/d (solid line) for tip radius $R/d=3$, according to Eq. (5). The dashed line shows only the leading quadratic term in z_0/d [Eq. (6)]. Inset: behavior at small z_0/d . On this scale the approximation of Eq. (7) is indistinguishable from the numerical solution of Eq. (5).

zian contact) is $F \sim z_0^{3/2}$ [15]. More relevant for AFM experiments, the force to indent a finite elastic layer scales as $F \sim R^2 z_0^3/d^3$ if the layer is bonded to the substrate and $F \sim R z_0^2/d$ if the layer can slip [7]. The response of fluid bilayers in Eq. (6) scales differently than all of these scenarios, and force is proportional to the area compressibility modulus instead of Young's modulus. For realistic experimental values the region of validity for this quadratic behavior is limited, as shown in Fig. 2.

III. EXPERIMENTS

To test the theory we performed experiments on a supported bilayer comprising DOPC, SM, and CHOL at overall molar ratios DOPC:SM:CHOL=40:40:20. At room temperature this system phase separates into coexisting DOPC rich liquid disordered and SM rich liquid ordered domains (Fig. 3). The hydrocarbon tails have large nematic order in the L_o phase, leading to a thicker bilayer and higher area compressibility modulus. In contrast, the tails have lower nematic order in the L_d phase with concomitant smaller thickness and lower moduli. DOPC, CHOL (purchased from Sigma), and egg SM (purchased from Avanti) were dissolved in chloroform, dried under a stream of argon for 30 min, and then vacuum desiccated for 30 min. The lipid was resuspended in phosphate buffered saline (PBS) buffer at a pH of 7.4 to a concentration of 1 mg/ml by vortexing. To make small single unilamellar vesicles (SUVs), the cloudy lipid suspension was tip sonicated (IKA, U50) at less than 5 °C for 25 min (until the solution became clear). The mica (Agar Scientific Ltd.) surface was incubated with the SUVs at 50 °C and cooled down to room temperature in an incubator over 15 min. After 1 h, the sample was gently rinsed with PBS buffer to remove any excess vesicles.

Force measurements were performed at 27 °C in PBS buffer using a Nanoscope IV Multimode AFM (Veeco) equipped with a temperature control stage, using cantilevers (NP, Veeco) with nominal spring constants of 0.12 N/m.

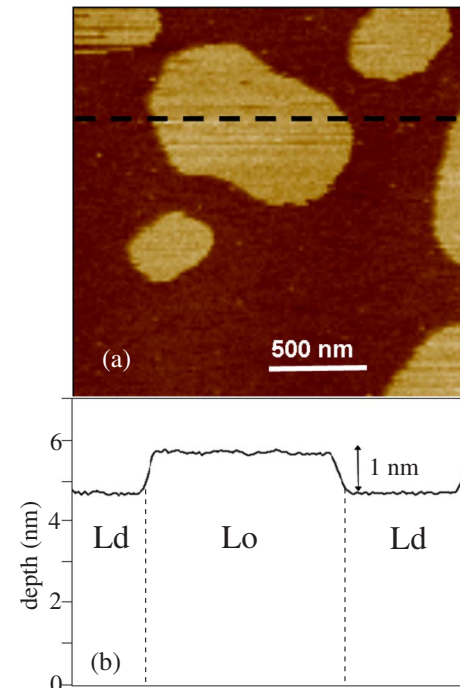


FIG. 3. (Color online) Phase separated lipid bilayer with liquid ordered and liquid disordered domains. (a) Tapping mode AFM image showing the height profile of the bilayer. (b) One-dimensional section along the dashed line in (a).

Spring constants were measured using the thermal noise method [16] in air, and optical lever sensitivity was determined against a clean mica surface. The force curves analyzed in this paper were all taken from a single force-volume map of the phase separated bilayer shown in Fig. 4 and exported using NANSOPE software v5.12r30.

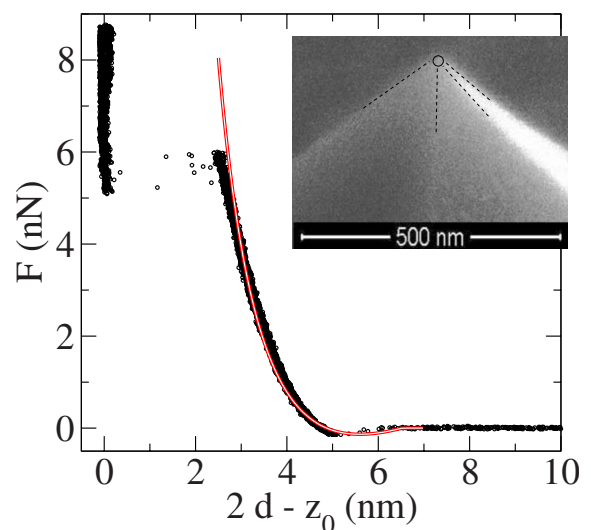


FIG. 4. (Color online) Force-distance curve for a DOPC rich bilayer in the liquid disordered phase. The data points are from AFM experiments and the line is a fit for the theoretical prediction with $\kappa_A=0.12$ N/m. Inset: SEM image of the tip to measure the tip radius. The dashed lines are along the pyramidal face edges. The circle drawn at the end of the tip has a radius of 10 nm.

Scanning electron microscopy (SEM) (Camscan series III, FEG-SEM operating at 5 kV with magnification of 160 k) was used to measure the tip radius. The inset of Fig. 4 shows the tip image with dashed lines along the edges of the four pyramidal faces. The end of the tip can be approximated as spherical. The drawn circle (Fig. 4, inset) has a radius of 10 nm. The contrast of the image is poor. Consequently the uncertainty of the exact value of the radius is large. In our analysis we consider the tip radius to be $R=10 \pm 5$ nm.

Figure 3 shows a tapping mode image of the bilayer along with a one-dimensional cross section. There is a ~ 5 -nm-thick L_d matrix enclosing ~ 6 -nm-thick L_o domains (the heights reported here include the thickness of any water layer between the bilayer and the mica surface). The composition of the two phases was determined by following the tie lines on the ternary phase diagram, which were determined using AFM [17]:

$$L_d:(\text{DOPC}:\text{SM}:\text{CHOL}) = (68:27:5), \quad (8a)$$

$$L_o:(\text{DOPC}:\text{SM}:\text{CHOL}) = (3:71:26). \quad (8b)$$

Phase diagrams on similar ternary mixtures have been calculated using NMR, and the compositions of the liquid disordered and liquid ordered phases are similar [18]. The uncertainty in the compositions from placement of the tie lines is estimated to be less than 2% of the quoted values. For both L_o and L_d phases, force curves from contact mode AFM were used from at least ten different measurements from different points within different regions (“patches,” as in Fig. 3) of the sample.

Figure 4 (symbols) shows the force curve for the DOPC rich bilayer in the liquid disordered phase. Besides the stretching contribution considered so far, the tip experiences an attractive force due to van der Waals interaction and a short-range repulsive force due to the electric double layers on the tip surface and the membrane top surface. In principle the van der Waals interaction can be calculated from a knowledge of the dielectric constants of the tip, membrane, and the PBS buffer [19]. Similarly, the repulsive interaction can be estimated by knowing the detailed charge distribution and solving Poisson-Boltzmann equation. Phenomenologically, we model the van der Waals attraction as an interaction energy of the form $-A/\xi^6$ between volume elements of the tip and the membrane separated by a distance ξ .

Since these forces are short ranged, we consider the tip as a sphere, and for the volume integration consider the membrane as infinitely thick. We further assume that the repulsive interaction is strong enough to avoid adsorption. As the tip approaches the bilayer, the bilayer deforms. The extent of the deformation is governed by the minimum of the stretching free energy and the long-range interactions (van der Waals and screened Coulomb). We assume that the deformation can be modeled as hard interaction from a tip with radius R_c larger than the physical tip radius R . Although A is poorly known and depends on the detailed dielectric properties of the membrane, its precise value only changes R_c and controls the details of the force near contact. For deeper contact the force is overwhelmingly dominated by the stretching modu-

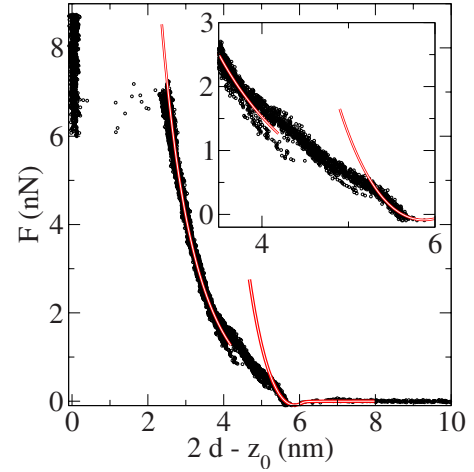


FIG. 5. (Color online) Force-distance curve from AFM (symbols) in the SM rich liquid ordered phase superposed with two separate theoretical fits [lines, using Eq. (5)] involving two different κ_A 's at small and large tip penetrations z_0 . Inset: closeup of the crossover region.

lus κ_A , so that the force-distance curves yield the same κ_A , independent of A .

The drawn line in Fig. 4 shows the fit from our theoretical analysis, using a downhill simplex method [20] to minimize the mean-square fractional deviation of the prediction from the experimental data over the fitted range. The best fit for the compressibility modulus for $R=10$ nm is $\kappa_A=0.12$ N/m. Because of the uncertainty in the tip radius, the range of κ_A for R between 5 and 10 nm is between 0.25 and 0.08 N/m, respectively. Our estimate compares well with the literature values $\kappa_A=0.13-0.6$ N/m from osmotic pressure measurements [21] and $\kappa_A=0.18 \pm 0.04$ N/m from micropipette aspiration of giant unilamellar vesicles (GUVs) [22] made of pure DOPC. Our model provides an excellent fit until $2d-z_0 \approx 2.5$ nm, at which point the elastic energy of the deformed bilayer overcomes the cost of forming a hole [23] and the tip abruptly penetrates the full bilayer.

IV. RESPONSE OF LIQUID ORDERED DOMAINS

The AFM force curves for the SM rich liquid ordered phase are qualitatively different from those in the coexisting liquid disordered phase (Fig. 5). The initial deformation ($5 \text{ nm} \leq 2d-z_0 \leq 6 \text{ nm}$) shows a high modulus consistent with the tightly packed character of the L_o phase. Around $2d-z_0 \approx 5$ nm the response shows a crossover to a much lower modulus. The symbols in Fig. 5 are from 12 separate force-distance measurements. While the experimental data fall on the same curves away from the crossover region, the transition from stiff to soft behavior occurs at different values of z_0 , which may be due to either the stochastic behavior of an activated event or fluctuations in composition from region to region.

We first attempt to model these force curves as due to an effective stretching modulus that differs for small and large penetrations far from the crossover region. Hence, we fit the data at small penetration ($2d-z_0 > 5.3$ nm) and large pen-

etration ($2d - z_0 < 3.5$ nm), with effective stretching moduli according to Eq. (5). For $R=10$ nm, the small z_0 fit gives $\kappa_A = 1.1$ N/m. Recent experiments on a bovine brain SM and CHOL equimolar mixture found $\kappa_A = 2.1 \pm 0.2$ N/m [24]. Since egg SM (16:0 SM) has shorter fatty acid chains than does bovine SM (18:0 SM), and the current composition has comparatively smaller amounts of CHOL, we expect the membrane to be softer (smaller κ_A), as found.

The large penetration (z_0) region has a stretching modulus $\kappa_A = 0.05$ N/m, which is much closer to that of the L_d phase shown in Fig. 4 than the unperturbed L_o phase. The AFM tip forces the bilayer immediately below it to decrease in thickness, which thus destroys the strong nematic order of the L_o phase and induces a yielding or phase transition of the L_o phase into an L_d phase. It is likely that the composition of this induced L_d phase differs from that of the L_d phase that characterizes equilibrium coexistence far from the AFM tip [Eq. (8a)], because of slow kinetics of composition changes under the AFM tip. Our separate fits to extract κ_A suffer from narrow available fit window (~ 0.3 nm) for small z_0 and the lack of small force data for the large z_0 fit. Also, this procedure does not elucidate the reason for two distinct elastic regions separated by a crossover.

To understand the qualitatively difference force responses of the L_o and L_d phases, we propose a microscopically motivated model. SM has both hydrogen bond donor and acceptor groups and is known to form inter-SM hydrogen bonds [25,26]. The free energy in the L_d phase, as represented in Eq. (2), is dominated by solvent and tail packing entropies. Hence, to describe the L_o phase we separately include the short-range energy of hydrogen bond breaking through a simple Morse potential: $U(b) = E_D \{1 - \exp[-(b - b_0)/\lambda_m]\}^2$, where b is the separation between the donor and acceptor group and b_0 is the equilibrium separation. For typical hydrogen bonds the dissociation energy $E_D \sim 2-7$ kcal/mol and the range $\lambda_m \sim 0.02-0.07$ nm [27,28]. For small changes in area per lipid and affine deformation the contribution to the free energy from distortion of hydrogen bonds is approximately

$$G_{\text{HB}}(z_0) = e_{\text{HB}} \int d^2r \left\{ \frac{h_t(r)}{d} [1 - e^{-(1/\lambda)(\delta a/a_0)_t}]^2 + \frac{h_b(r)}{d} [1 - e^{-(1/\lambda)(\delta a/a_0)_b}]^2 \right\}. \quad (9)$$

Here, e_{HB} is the interlipid hydrogen bond dissociation energy per area and $\lambda \sim 3^{1/4} \lambda_m / \sqrt{a_0}$ for hexagonal arrangement of the lipids. As before, the total free energy, now comprising contributions from Eqs. (5) and (9), is minimized at each r to find the dividing surface between the leaflets, and the force is calculated from $F = \partial G / \partial z_0$.

In the limit of small penetrations this model gives an effective stretching modulus κ_A^{eff} in the L_o phase of

$$\kappa_A^{\text{eff}} = \kappa_A + 4 \frac{e_{\text{HB}}}{\lambda^2}, \quad (10)$$

where κ_A is thus the stretching modulus of the L_d phase that is left after the L_o phase has been destabilized and there is no

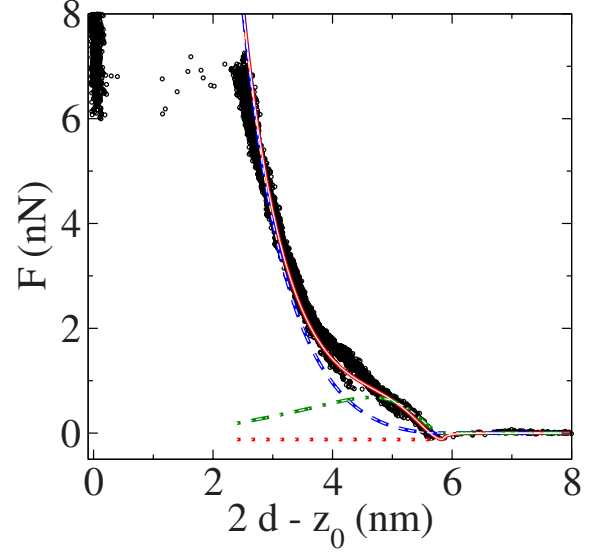


FIG. 6. (Color online) Force-distance curve from AFM (symbols) in the SM rich liquid ordered phase superposed with a microscopically motivated fit that accounts for a separate energetic contribution from hydrogen bond breaking [solid line, based on Eq. (9)]. Also shown are the separate contributions from the van der Waals interaction (dotted line), from the hydrogen bonds (dotted-dashed line), and the area compressibility term (dashed line).

remaining hydrogen bond contribution. The fit to the data is shown in Fig. 6. The stochastic nature of the force curves near the rupture point ($2d - z_0 \approx 5.7$) limits the ability to obtain excellent fits. Our fit gives $\kappa_A = 0.13$ N/m, $e_{\text{HB}} = 0.006$ N/m, and $\lambda = 0.1$.

Assuming an area per lipid $a_0 \sim 0.6$ nm², the fitted value λ implies that the range of the Morse potential is $\lambda_m \sim 0.06$ nm. Simulations show about 0.5 hydrogen bond per lipid in SM bilayers [25]. Assuming an average hydrogen bond energy of 3.5 kcal/mol, our value for e_{HB} gives 0.4 hydrogen bond broken per lipid. The initial deformation is dominated by the contribution from the hydrogen bonds, and the corresponding force curve leads to an area compressibility modulus $\kappa_A^{\text{eff}} \approx 2.7$ N/m.

V. DISCUSSION

We have assumed a static force response, despite typical tip velocities $v_{\text{tip}} \approx 10^2$ nm/s. We can estimate the correction due to finite tip velocity by considering the dissipation from two-dimensional viscosity η of the lipid layer. The dissipative force is found to be

$$F_D(z_0) = \frac{\eta \pi z_0 (2R - z_0)}{2d^2} v_{\text{tip}}. \quad (11)$$

The two-dimensional shear viscosity for fluid bilayers is expected to be on the order of 10^{-10} N s/m [29], leading to $F_D \approx 10^{-8}$ nN, much smaller than the elastic contributions. Hence, our static approach is sufficient to describe the AFM force-distance curves on fluid lipid layers.

In our calculations we have assumed that the two leaflets have the same area compressibility and preferred area per

head group. This may not always be the case, because of surface interactions [13]; for example, supported bilayers often have different melting temperatures than their counterparts in giant unilamellar vesicles. Incorporation of asymmetric membranes into the model is straightforward, although more complex. We have also neglected splay or bending energies. Part of the elastic cost of this is already included in the increased area per lipid against the curved surface, in Eq. (2), but there may also be an additional negligible free energy cost due to the splay of the lipid tails, through the bending modulus of each leaflet.

In our analysis, the initial deformation for the L_o phase is described in terms of the stretching of hydrogen bonds. This can be explicitly tested by performing experiments with varying concentrations of SM or using chemicals that disrupt hydrogen bonds. However, this is beyond the scope of the present work.

Evidently, local applied pressure can melt the liquid ordered phase into the thinner L_d phase, which is not surprising. We have proposed an explicit microscopic mechanism in terms of breaking hydrogen bonds that are implicated in stabilizing L_o phase. An alternative and more general description could include a Landau theory for the free energy of the L_o - L_d phase transition, with local pressure p added as an external field to destabilize the L_o phase, $\Delta G \sim p\psi$, where ψ is an order parameter proportional to thickness whose value decreases upon a transformation to the L_d phase [30]. The

phase transformation would then occur first at constant composition, and then one may expect the composition to change slowly as the external force changes the local preference for the different lipid species. The subject of kinetics and composition as functions of the applied pressure is interesting and important, and we leave this for further work.

In summary, we have presented, and validated by experiments, a theory for describing the force-distance $F(z_0)$ relationship for AFM experiments on fluid bilayers, which leads to a remarkably simple expression for $F(z_0)$ [Eq. (7)]. This provides a method for finding the area compressibility modulus and the amount of interlipid hydrogen bonds of fluid bilayers. The agreement with the existing literature values for the area compressibility is excellent. The main uncertainty in our prediction is due to the uncertainty in the tip radius R . However, the simple linear dependence on R means that relative measurements taken with the same tip can be compared very accurately.

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