Influence of cap weight on the motion of a Janus particle very near a wall

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The dynamics of anisotropic nano- to micro scale colloidal particles in confined environments, either near neighboring particles or boundaries, is relevant to a wide range of applications. We utilized Brownian dynamics simulations to predict the translational and rotational fluctuations of a Janus sphere with a cap of nonmatching density near a boundary. The presence of the cap significantly impacted the rotational dynamics of the particle as a consequence of gravitational torque at experimentally relevant conditions. Gravitational torque dominated stochastic torque for a particle $>1 \mu m$ in diameter and with a 20-nm-thick gold cap. Janus particles at these conditions sampled mostly cap-down or "quenched" orientations. Although the results summarized herein showed that particles of smaller diameter ($\lt 1 \mu m$) with a thin gold coating ($\lt 5 \text{ nm}$) behave similarly to an isotropic particle, small increases in either particle diameter or coating thickness quenched the polar rotation of the particle. Histogram landscapes of the separation distance from the boundary and orientation observations of particles with larger diameters or thicker gold coatings were mostly populated with quenched configurations. Finally, the histogram landscapes were inverted to obtain the potential energy landscapes, providing a road map for experimental data to be interpreted.

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I. INTRODUCTION

Colloidal particles dispersed in a liquid interact via surface forces that play a critical role in dictating the properties and performance of complex fluids. Over the past decade, the dynamics and interactions of anisotropic colloidal particles have gained attention [\[1\]](#page-7-0) because of potential applications in various fields such as optical displays [\[2\]](#page-7-0), magnetorheological systems [\[3\]](#page-7-0), controlling interfacial microstructure [\[4\]](#page-7-0), selfassembly [\[5,6\]](#page-7-0), microfluidic devices [\[7\]](#page-7-0), tuning interparticle interactions $[8,9]$, and biomaterials or drug delivery $[10]$. Supporting these efforts have been a variety of new techniques for the synthesis of anisotropic colloidal particles [\[5,10–21\]](#page-7-0). Newly developed fabrication techniques provided the ability to tune the shape and the surface properties of these materials. Janus particles are one class of anisotropic colloid, typically with some property difference between the two hemispheres. Each hemispherical domain of a Janus particle may have its own surface chemistry, shape, or other property [\[22\]](#page-7-0).

Predicting the dynamics of anisotropic colloids is important for applications in real systems, for example, during processing when complex fluids are often not at equilibrium [\[23,24\]](#page-7-0). Various parameters influence the dynamics of anisotropic colloids [\[25–28\]](#page-7-0). Particle confinement will impact the hydrodynamic interactions between the colloid and boundary, thereby influencing particle mobility. Brownian motion and conservative (i.e., *path independent*) forces, such as electrostatic double layer repulsion and gravity, will also impact the dynamics of a confined spherical Janus particle. Although not dependent on orientation for an isotropic particle, each

of these phenomena will likely depend on the orientation of an anisotropic particle. For example, a Janus particle with anisotropy in zeta potential will experience an electrostatic interaction that depends upon orientation with respect to the boundary [\[29\]](#page-8-0). Rotation of the Janus particle at a constant separation distance from a boundary induces an effective change in an interaction, which then alters the probability density at that particle's position.

Janus particles are fabricated by coating one hemisphere of a spherical colloidal particle with another material, usually a metal such as gold [\[30,31\]](#page-8-0). The cap typically has some nominal thickness from a few to tens of nanometers, but direct measurement of the coating thickness has shown the cap to be nonuniform across the contour of the particle [\[32\]](#page-8-0). Tracking translational and rotational displacement of Janus particles at various boundary, physiochemical, and rheological conditions will assist in understanding the dynamics of these particles [\[33–36\]](#page-8-0). Various studies have focused on the rotation of isotropic [\[37,38\]](#page-8-0) and anisotropic colloids [\[39,40\]](#page-8-0). There has been some work on the translational and rotational dynamics of Janus particles near a boundary [\[41,42\]](#page-8-0), on the effect of mass-anisotropic coating on the dynamics of active particles away from a boundary [\[43–45\]](#page-8-0), and on the dynamics of Janus microswimmers which have bottom heaviness near surfaces [\[46\]](#page-8-0). Experimental techniques such as confocal microscopy [\[47,48\]](#page-8-0), evanescent wave scattering [\[49\]](#page-8-0), videomicroscopy [\[50\]](#page-8-0), and holographic microscopy [\[51–53\]](#page-8-0) were used to measure the rotational diffusion coefficient. Surface roughness [\[54\]](#page-8-0), particle shape [\[55\]](#page-8-0), external fields [\[56\]](#page-8-0), and the presence of motility (i.e., *for active particles*) [\[57–63\]](#page-8-0) were found to influence the rotation of Janus particles. Despite the significant recent work in this area, there has not yet been a detailed

FIG. 1. (a) Schematic of a Janus particle with one hemisphere coated by a metallic cap. (b) Schematic representation of θ orientation. (c) Alpha (α) definition for the center of mass calculation.

quantitative analysis of the dynamics of a Janus particle with a cap of nonmatching density near a boundary.

Herein, we conducted Brownian dynamics simulations to predict the behavior of a Janus particle with a cap of density not matching that of the native particle. This technique has been previously used to study the dynamic behavior of other colloidal systems [\[64–67\]](#page-8-0). Our results show the importance of the particle's surface properties, in particular, the weight of the cap, on the dynamics of a particle close to a wall. We systematically altered coating thickness and particle size to test their impact on rotational and translational dynamics, probability distribution, and potential energy landscape. Our findings illustrate the importance of non-negligible gravitational torque on the rotational and translational trajectories of a Janus particle. Notably, the aforementioned torque influenced the behavior of Janus particles at conditions relevant to experimental studies.

II. THEORY

Near-boundary forces and torques on a Janus particle. A colloidal particle dispersed in a fluid near a boundary experiences conservative, dissipative, and stochastic forces. Conservative forces experienced by a nondensity matched particle in low concentration electrolyte with bound surface charges are primarily due to electrostatic double layer repulsion and gravity. Strong electrostatic forces help to keep the particle levitated close to the substrate. van der Waals attraction may also play a role at sufficiently small separation distances $(h < 100 \text{ nm})$, but is neglected herein [\[68,69\]](#page-8-0). Further support for neglecting van der Waals attraction at these conditions is included in Appendix [A.](#page-6-0) A charged spherical colloidal particle with radius *a* and separation distance *h* [see Fig. 1(a)] will experience an electrostatic force that depends upon the size of the particle, the solution Debye length κ^{-1} , and Stern potential of the particle and the substrate. The conservative force F_c is calculated by

$$
F_c = -\frac{d\phi_c(h)}{dh} = \underbrace{\kappa B \exp(-\kappa h)}_{\text{Electrostatic}} - \underbrace{\frac{4}{3}\pi a^3 (\rho_p - \rho_f)g}_{\text{Covitation}} , \quad (1)
$$

$$
B = 64\pi \varepsilon_0 \varepsilon_f a \left(\frac{kT}{e}\right)^2 \tan h \left(\frac{e\zeta_s}{4kT}\right) \tan h \left(\frac{e\zeta_p}{4kT}\right), \quad (2)
$$

$$
\kappa = \sqrt{\frac{2e^2C_{\infty}}{\varepsilon_0\varepsilon_f kT}},\tag{3}
$$

where *B* is the electrostatic charge parameter; ρ_p and ρ_f are density of the particle and fluid respectively; *g* is gravitational acceleration; ε_0 is the electric permittivity of vacuum, ε_f is the relative permittivity of water; *e* is the charge of an electron; ζ_s and ζ_p are the zeta potentials of the surface (boundary) and particle, respectively (equated with the Stern potential); *k* is the Boltzmann's constant; *T* is temperature; and C_{∞} is electrolyte concentration in the bulk. This expression is applicable to an isotropic particle with uniform surface chemistry. A meshing method was previously developed to account for these forces on a chemically anisotropic particle with a nonuniform zeta potential [\[29\]](#page-8-0).

A Janus particle will experience stochastic torque, just as an isotropic particle will, but will additionally experience deterministic torque due to the asymmetry in both the gravitational and electrostatic interaction. For instance, a mismatch in the electrostatic charge on the surface of a particle induces an electrostatic torque relevant only when the boundary between the hemispheres of the Janus particle is near perpendicular to the wall. Similar to accounting for variations in surface chemistry in calculating translational displacements as mentioned above, a meshing method was used to calculate the electrostatic torque on a Janus particle. For each mesh point, the torque $[T_{dL}(i)]$ was equated to the product of the electrostatic force $[F_{dL}(i)]$ and the distance of the projected mesh point from the center of the particle (*d*) [Fig. 1(b)]:

$$
P_{dL}(i) = 64C_{\infty}kT \tanh\left(\frac{e\zeta_s}{4kT}\right) \tanh\left[\frac{e\zeta_{mp}(i)}{4kT}\right] \times \exp\left[-h_{dL}(i)\right],\tag{4}
$$

$$
T_{dL}(i) = P_{dL}(i)A(i)d,
$$
\n(5)

where P_{dL} is the electrostatic double layer repulsion pressure of the substrate and projection of curved mesh area [*A*(*i*)], ζ*mp* is the zeta potential of the flat projected surface of a mesh point, and h_{dL} is equal to the substrate distance from the midpoint of the curved meshed surface $(h_{dL} = h_p + L/2)$. The total torque was calculated by summing contributions from each projected flat surface area. The sum of clockwise and counterclockwise torques at each time step provided the electrostatic torque on the Janus particle:

$$
T_{dL-\text{total}} = \sum T_{dL}(i),\tag{6}
$$

where $T_{dL_{\text{total}}}$ is the electrostatic torque between the Janus particle and the substrate.

The gravitational torque on a Janus particle originates from the density distribution mismatch between the cap and native particle. Although gravitational deterministic torque affects the rotation of the particle about an axis parallel to the substrate, there is no impact on the rotation of the particle about the *z* axis (see Fig. 1) because of the particle's axisymmetric geometry. Note that for the work summarized herein, we assumed the coating thickness distribution to be uniform over the contour of the particle. The weight of right and left hemispheres of the Janus particle was calculated at each time step with respect to a dynamic spherical coordinate system and a vertical plate that passes through the particle center. The gravitational torque was calculated:

$$
T_{G_{\text{total}}} = (\text{weight_Cap}_{\text{right}} - \text{weight_Cap}_{\text{left}}) w_{\text{CoM}}, \quad (7)
$$

weight_Cap_{right} = Total cap weight ×
$$
\frac{2\theta + \pi}{2\pi}
$$
, (8)

weight_Cap_{left} = Total cap weight – weight_Cap_{right}, (9)

$$
w_{\text{CoM}} = \frac{2a}{\pi \sin(\alpha)} \left[\frac{\alpha}{2} + \frac{\sin(2\alpha)}{4} \right],\tag{10}
$$

where w_{CoM} is the center of mass [Fig. [1\(b\)\]](#page-1-0) and α is half of the angle swept out by the noncanceled portion of the cap [Figs. $1(b)$ $1(b)$, $1(c)$, and 8]. Note from Fig. 1 and equations (7) – (10) that particle symmetry was utilized to calculate torque. The portion of the noncanceled cap, swept out by the angle 2α , was the body contributing to gravitational torque, while the remaining cap and hemispheres of the native particle canceled. Additional details regarding center of mass calculations for the cap are found in Appendix \overline{B} \overline{B} \overline{B} at the end of the paper.

Near-boundary diffusion coefficients. Although hydrodynamic hindrance from the nearby boundary will occur in all translational (x, y, z) and orientational (θ, ϕ) directions (see Fig. [1\)](#page-1-0), we are primarily concerned with hindrance in the polar rotational (θ) and translational direction normal to the substrate (*z*). A solution of the Stokes equation is necessary to account for the bounding effect of the wall on hydrodynamic interactions. Goldman *et al.* [\[70\]](#page-8-0) provided an infinite-series solution for this equation. The normal translational diffusion coefficient of a spherical particle can be computed by an approximation of the Goldman infinite-series solution by a regression [\[71\]](#page-8-0):

$$
D_z = \frac{kT}{f_{\infty}}q(h) = \frac{kT}{6\pi\eta a}q(h),\tag{11}
$$

$$
q(h) = \frac{6h^2 + 2ha}{6h^2 + 9ha + 2a^2},
$$
\n(12)

where *T* is temperature, *k* is the Boltzmann constant, η is the fluid viscosity, f_{∞} is the friction coefficient ($f_{\infty} = 6\pi \eta a$), and *q*(*h*) is the wall correction factor.

Dean and O'Neill [\[72\]](#page-8-0) considered the polar rotation of a bounded sphere about an axis parallel to the planar surface. Goldman [\[70,73,74\]](#page-8-0) updated the Dean and O'Neill solution and numerically computed the solution in the form of dimensionless force and torque on a rotating sphere. We previously fit several gap ranges to implement the corrected Dean and O'Neill expression based on the numerical fit from Goldman. [\[29\]](#page-8-0) The comprehensive polar rotational diffusion coefficients are as follows:

$$
D_{r,\theta} = \frac{kT}{f_{r,\infty}} \Bigg/ q^{\theta}(h) = \frac{kT}{8\pi \eta a^3} \Bigg/ q^{\theta}(h), \tag{13}
$$

$$
q^{\theta}(h) = 0.9641 \left(\frac{h}{a}\right)^{-0.1815} \frac{h}{a} \leq 0.6, \quad (14)
$$

$$
q^{\theta}(h) = 1.056 \left(\frac{h}{a}\right)^{-0.07286} \quad 0.6 \leq \frac{h}{a} \leq 2, \tag{15}
$$

$$
q^{\theta}(h) = 1 \frac{h}{a} > 2.
$$
 (16)

Brownian dynamics simulation (BDS). We carried out Brownian dynamics simulations to track rotational and *z*axis translational motion of a Janus particle. The Langevin equation with a thermal fluctuating force, conservative forces, and hydrodynamic forces, as well as torques, was used to formulate a stepping algorithm for the Janus particle. A well-known inertialess numerical solution was obtained by Ermak and McCammon [\[75\]](#page-8-0) to solve the Langevin equation at small Reynolds numbers. This numerical solution was used to predict the dynamic behavior of a single particle and consequently track the position of the particle at consecutive time steps. The *z*-axis translational and polar rotational trajectories of a single particle were predicted via the Ermak and MaCammon stepping algorithm:

$$
h(t + \Delta t) = h(t) + \frac{dD_z}{dh} \Delta t + \frac{D_z}{kT} F \Delta t + H(\Delta t), \quad (17)
$$

$$
\theta(t + \Delta t) = \theta(t) + \frac{D_{r,\theta}T_{\text{det}}\Delta t}{kT} + G(\Delta t). \tag{18}
$$

These stepping algorithms are valid when the time step (Δt) is longer than the momentum relaxation time of the particle and is short enough such that the system properties are constant. The momentum relaxation times for the colloidal particles in the range of particles we use in our simulation are on the order of 10−⁶ s [\[76\]](#page-8-0). In the *z*-axis translational algorithm, *F* represents conservative forces on the particle and *H*, which has $\langle H^2 \rangle = 2D_z \Delta t$ variance, is the Gaussian random fluctuation due to Brownian motion. The total force *F* was the sum of the double layer repulsion and gravity. In the polar rotational algorithm, T_{det} is the deterministic torque, which may include contributions from a mismatch in electrostatic forces near the Janus boundary and gravitational force due to a mismatch in the density of the cap and particle. $G(\Delta t)$, which has $\langle G^2 \rangle = 2D_{r,\theta} \Delta t$ variance, is Gaussian random rotation due to the stochastic torque. Electrostatic torque results from the asymmetry in electrostatic force arising when the Janus boundary separating the two hemispheres of different properties rotates toward the wall ($\theta = 90^{\circ}$). The gravitational torque depends on the polar orientation of the particle and the weight of the cap, which in turn depends on the thickness, total size, and cap material. Note that although the stepping algorithms are uncoupled, height $[Eq. (17)]$ and rotation $[Eq. (18)]$ may have synergistic effects. The height of the particle will impact rotation by affecting the rotational diffusion coefficient, and electrostatic and rotational stochastic torques. Also, the orientational position of the particle will impact *z*-axis translation by affecting the electrostatic force between the particle and the substrate.

A MATLAB code was developed to implement the Brownian dynamics simulation for our system. The zeta potential is a key factor in calculating electrostatic double layer repulsion force between colloidal particles and surrounding media. We addressed the challenge of accounting for variations in zeta potential with an existing meshing method [\[29\]](#page-8-0) in which the sphere was divided into small parts in both the azimuth (φ) and polar (θ') angles. Each small meshed region has its own value of zeta potential; the small curved area was projected parallel to the boundary. The electrostatic force was calculated between each small projected flat surface and the substrate. The sum of the electrostatic interactions

TABLE I. Simulation conditions and particle properties used in the study.

Property name	Value
Particle diameter	$1-6 \mu m$
Particle material	Polystyrene
Polystyrene density	1.055 g ¹ cm ⁻³
Gold coating thickness	$2 - 20$ nm
Gold density	$19.32 \text{ g}^1 \text{ cm}^{-3}$
Titanium density	$4.5 g1 cm-3$
Temperature	298.15 K
Electrolyte concentration	1 m M
Debye length	9.6 nm
Time step	5 ms
Initial orientation position	$\pi/2$
Number of time steps	4.8×10^{6}
Surface zeta value	-50 mV
Particle coated side zeta value	-5 mV
Particle uncoated side zeta value	-50 mV
Number of iterations for each simulated condition	Ten

between the small projected area and the substrate is the double layer electrostatic force between the particle and the substrate. At each time step, this force was calculated as one of the conservative forces (F) in Eq. (17) . Finally, the time step for each simulation was set as $\Delta t = 5$ ms. For all the system conditions studied here, the stepping algorithms were run ten times each for 4.8×10^6 time steps. The number of observations at each separation height or orientation is the average of ten sets of simulations. In all simulations the Janus particle cap includes a 2.5-nm titanium layer as a sublayer in addition to the reported gold layer thickness. Experiments regularly include a thin layer of titanium to increase adhesion of a gold coating on a polystyrene (PS) particle. A summary of simulation conditions and particle properties is provided in Table I.

III. RESULTS AND DISCUSSION

Influence of deterministic torque on particle rotation dynamics. We defined a dimensionless rotation number (DRN, $\hat{\theta}$) that balances the deterministic and stochastic torques:

$$
\hat{\boldsymbol{\theta}} = \frac{\Delta \theta_{\text{det}}}{\Delta \theta_{sto}},\tag{19}
$$

where $\Delta\theta_{\text{det}}$ and $\Delta\theta_{\text{sto}}$ are the rotational displacements of the Janus particle in the polar direction due to deterministic and stochastic torques, respectively. This dimensionless number furnished a direct quantitative measure of the relative influence of deterministic torque as compared to stochastic torque on the particle. Note also that the DRN is a dynamic quantity, in that it will depend upon the time step. Thus, the proceeding comparison is applicable to the time step conditions we tested herein.

Stochastic rotational fluctuations dominate at small values of DRN, while deterministic fluctuations become more relevant at large values of DRN. We calculated the DRN to compare fluctuations from gravitational and stochastic torque absent of hydrodynamic hindrance as a function of particle size. The expression for calculating the deterministic rotational displacement is

$$
\Delta \theta_{\det}(\Delta t) = \frac{D_{r,\theta \text{.Bulk}} \langle T_{\det} \rangle \Delta t}{kT} \,, \tag{20}
$$

where $\langle T_{\text{det}} \rangle$ is the average deterministic torque over 180 orientations and $D_{r, \theta_{\text{Bulk}}}$ is the rotational diffusion coefficient in the bulk, ensuring that this DRN will be height independent. Torque, $\langle T_{\text{det}} \rangle$, was obtained by uniform averaging over 180° in the (clockwise) orientation according to Eq. [\(7\)](#page-2-0). We used the standard deviation $\sqrt{\langle G^2 \rangle} = \sqrt{2D_{r,\theta}\Delta t}$ for calculating the random torque on the rotation of the Janus particle [Eq. [\(18\)](#page-2-0)] as the stochastic contribution. Further, DRN was developed to approximate the impact of gravitational force, thereby neglecting electrostatic torque. However, the latter effect was included in all subsequent calculations found in this paper, although previous work has shown electrostatic torque to be small [\[29\]](#page-8-0).

Figure $2(a)$ shows the impact of stochastic torque embodied in the rotational displacement experienced by a Janus particle as a function of diameter and with a gold cap thickness of 20 nm. Increasing the diameter of the particle induced a decrease in the fluctuations arising from stochastic torque because of the correlation between the diameter of the Janus

FIG. 2. Calculations for the fluctuations arising from (a) stochastic torque, (b) deterministic torque, and (c) the balance of these two torques via the dimensionless rotation number (DRN) on a Janus particle with a cap of 2.5 nm titanium and 20 nm gold. The reader should note the difference in the *y*-axis range of (a) and (b) panels. These data show that although both fluctuations arising from stochastic and deterministic torque decreased with increasing diameter, fluctuations from deterministic torque decreased more slowly as a function of diameter. Deterministic torque, which induces rotational quenching of the Janus particle, became more important as particle size increased.

FIG. 3. Angular motion of the spherical particles with and without a cap. The MSAD analysis results for capped and noncapped particles can be differentiated by their color. The evaluated particles are 1, 3, and 6 μ m. The τ parameter refers to lag time.

particle and rotational diffusion coefficient [see $G(\Delta t)$ term of Eq. (18)]. The characteristic fluctuations arising from deterministic torque were calculated for the same conditions. Deterministic torque had a qualitatively similar impact on rotation as stochastic torque [see Fig. $2(b)$]; the magnitude of rotation decreased with increasing particle diameter at fixed cap thickness. However, deterministic torque decreased more slowly with increasing diameter as compared with stochastic torque. The origin of this trend for deterministic torque is in the competing effects of diameter on rotational displacements.

FIG. 4. (a) Impact of particle size on the number of observations for a particle with cap oriented downward (BDS, coating thickness is 20 nm gold and 2.5 nm titanium). (b) Coating thickness impact on the number of observations for a particle with cap oriented downward (BDS, $6 \mu m$). (c) Coating thickness impact on the number of observations for a particle with cap oriented downward (BDS, 3μ m). (d) Number of observations at different orientations for various particle sizes and same coating thickness (4 800 000 iterations, BDS, coating thickness is 20 nm gold and 2.5 nm titanium). "B" refers to the uncoated side. The angle bin size is the number of observation evaluation is 1°.

The rotational diffusion coefficient [see Eq. [\(20\)](#page-3-0)] decreased with increasing diameter, but the magnitude of deterministic torque increased with increasing diameter due to both the growth of cap weight and displacing this weight further from the center. Figure $2(c)$ shows the DRN, which is the quotient of values summarized in Figs. $2(a)$ and $2(b)$. The positive slope of DRN as a function of diameter indicates that deterministic torque had an increased influence as the diameter of the particle increased.

We measured mean squared angular displacement (MSAD) from our Brownian dynamics simulations to track the influence of the cap on a quantity now regularly obtained from experiments. The MSAD can be calculated by the $\langle \Delta \theta^2(t) \rangle$ = $\langle [\theta(t+dt) - \theta(t)]^2 \rangle$ relation [\[54,77,78\]](#page-8-0). The MSAD results for Brownian dynamics simulation data for particles with and without cap are shown in Fig. 3**.** First, for both coated and noncoated particles, increases in the size of particles caused a shift in the magnitude of the MSAD to lower values. However, the shape of the MSAD was significantly different for coated and noncoated particles. The MSAD is a straight line on the log-log plot shown in Fig. 3 for noncapped particles. However, the MSAD for capped particles has a shoulder indicative of "quenched" rotation. Also, the size of the particle affects the start location of the shoulder. The start points shift to lower scaled lag time as the size of the particle increases.

Probability and potential energy landscapes for a Janus particle with cap of nonmatching density. Data summarized in the previous section suggest that deterministic torque is relevant to the dynamics of a Janus particle near a boundary. The outcome of such relevance is that the probability of finding a Janus particle at a given state will be altered by the deterministic torque. The probability density of translational and orientation states was obtained to assemble a histogram and subsequently calculate the effective interaction landscape experienced by the Janus particle under various conditions. Figures $4(a) - 4(c)$ summarize data showing the

FIG. 5. (a) Histogram landscape for non-Janus $6-\mu m$ colloid particle, and histogram landscape for Janus particles with 2.5-nm titanium and 20-nm gold coatings at different diameters: (b) 1 μ m, (c) 3 μ m, (d) 6 μ m. The height here refers to the separation distance between the particle and the substrate. The reader should note the difference in the *y*-axis scale.

FIG. 6. (a) Potential energy landscape of $1-\mu m$ particle with 2.5-nm titanium and 20-nm gold cap. (b) Potential energy landscape of $3-\mu m$ particle with 2.5-nm titanium and 20-nm gold cap. (c) Potential energy landscape of 6-μm particle with 2.5-nm titanium and 20-nm gold cap.

impact of various parameters on the polar orientation of a Janus particle. The number of observations reported in these figures is that of a cap-down orientation, which corresponds to the quenched state. Stronger quenching is associated with a larger number of observations at $\theta = 180^\circ$. As shown in the previous section, the particle diameter at a fixed cap thickness had a strong effect on rotational quenching [see Fig. $4(a)$]. The number of observations at $\theta = 180^\circ$ increased as the diameter was increased. Increasing the coating thickness increased the number of observations at $\theta = 180^\circ$ [see Figs. [4\(b\)](#page-4-0) and [4\(c\)\]](#page-4-0). Both figures demonstrate the critical importance of changes in cap weight to rotational quenching of a Janus particle. Larger particle diameters and thicker caps enhance the influence of deterministic torque, thereby increasing the probability of a rotationally quenched Janus particle.

Figure [5](#page-4-0) shows a histogram landscape of observations in separation distance and orientation. Note the significant change in probability density for variation in particle size from 1 μ m [Fig. [5\(a\)\]](#page-4-0) to 6 μ m [Fig. [5\(c\)\]](#page-4-0) with the same coating thickness. The distribution of states spreads across all orientations for a Janus particle of 1 μ m diameter and 20 nm cap thickness, meaning the Janus particle is only weakly quenched at these conditions. However, merely increasing the particle diameter to 3 μ m and then 6 μ m induces orientational states that are highly populated around $\theta = 180^\circ$. Deterministic torque became increasingly important at larger diameters due to the mismatch in the cap and particle core densities. This behavior is in contrast with the $1-\mu$ m-diameter particle, which

experienced random rotation such that orientational states are distributed across all available θ .

As was done previously for separation distance observations of isotropic spheres [\[66\]](#page-8-0), observations of position and orientation were used to calculate the potential energy landscape for a Janus particle. Histogram landscapes shown in the previous section were interpreted to obtain the potential energy of interaction for a Janus particle with a cap of nonmatching density. In the BDS, we used a noncoupled translational-rotational Langevin equation to solve BDS. The single spherical particle of our model system allows us to neglect translational and rotational coupling motion. As the translation and rotation are not coupled so the probability of finding a Janus particle at a particular separation distance and orientation can be independent.

The probability is equal to the product of separation distance and orientation individual probabilities:

$$
p(h,\theta) = \underbrace{A_h e^{-\phi_h/kT}}_{p_h} \underbrace{A_\theta e^{-\phi_\theta/kT}}_{p_\theta} = A e^{-\phi_c/kT}, \qquad (21)
$$

where ϕ_h is the potential energy associated with changes in separation distance, ϕ_{θ} is the potential energy associated with changes in orientation, ϕ_c is the total colloidal potential energy ($\phi_c = \phi_h + \phi_\theta$), and *A* is a normalization constant chosen such that the cumulative probability summed over all states equals 1. Equation (21) can be rearranged and the normalization constant eliminated by subtracting the potential

FIG. 7. (a) Two-dimensional cutaway panel of BDS potential energy landscape of 1-μm PS with 2.5-nm titanium and 20-nm gold cap. (b) 2D cutaway panel of BDS Potential Energy landscape of 3-μm PS with 2.5-nm titanium and 20-nm gold cap. (c) 2D cutaway panel of BDS Potential Energy landscape of 2.5-nm titanium and $6-\mu$ m PS with 20-nm gold cap.

energy of the most probable state $\phi_c(h_m, \theta_m)$, where h_m and θ*^m* are the most probable separation distance *and* orientation corresponding to a maximum in the probability density landscape. Thus, the potential energy landscape was calculated by

$$
\frac{\phi_c(h,\theta) - \phi_c(h_m,\theta_m)}{kT} = \ln \frac{n(h_m,\theta_m)}{n(h,\theta)},\tag{22}
$$

where $n(h_m, \theta_m)$ is the maximum number of particle observations among all heights and orientations, $\phi_c(h_m, \theta_m)$ is the potential energy at the "most probable" position and orientation, and $n(h, \theta)$ and $\phi_c(h, \theta)$ are the number of particle observations and potential energy, respectively, at some specific height and polar orientation.

Figure [6](#page-5-0) shows the potential energy landscape for a Janus sphere of varying diameter and 20-nm gold cap. In Figs. $6(b)$ and $6(c)$, there is a minimum potential energy configuration belonging to the location of maximum observations among all orientations, corresponding to the coated side facing the wall. Comparing these three profiles, from a particle with a diameter of 1 μ m to one with a diameter 6 of μ m, illustrates the impact of a cap on conservative interactions. The potential energy landscape for a particle of 1 μ m diameter nearly matches that of a Janus particle with a density matching cap. Larger particle diameters with correspondingly larger gravitational torques have landscapes with a clear minimum. A colloidal particle will typically only sample states of a few kT. The projected two-dimensional view of the energy landscapes then shows how the presence of a cap will restrict the sampled states of a Janus particle. Increasing particle diameter at constant cap thickness severely limited the available orientations of the particle for a fixed energy state (see Fig. [7\)](#page-5-0). Although a 1- μ m particle with a 20-nm-thick cap will sample most orientations, a $6-\mu m$ particle with the same cap thickness will sample only a fraction of possible orientations. Variations of potential energy landscapes for Janus particles of different particle size will help to explain observations of stable and unstable positions for a coated particle.

IV. CONCLUSION

Brownian dynamics simulations were used to predict the rotational and translational displacements of a Janus particle with a cap of nonmatching density. These simulated data provided evidence that gold caps of thickness 5–20 nm on particles of diameter 1–6 μ m may strongly influence the rotational dynamics of the particle. Cap-down or "quenched" orientations arise when the balance of deterministic and stochastic torque is dominated by the former. Deterministic torque arising from the weight of the cap depended on particle size and cap thickness. Our parametric variation found that at experimentally relevant particle sizes $(>1 \mu m)$ or cap thicknesses (55 nm) , the particle was strongly quenched such that most observations of orientation were in the cap-down state. Further, histogram landscapes were inverted to calculate the potential energy landscape for Janus particles. The energy landscapes showed that Janus particles of typical size and coating thickness will sample only a limited number of orientation states. These simulations and associated analysis revealed the importance of considering the cap weight of a

FIG. 8. Histogram landscape for $6-\mu m$ Janus particles with 2.5-nm titanium and 20-nm gold coatings at different diameters. The coating thickness is 20 nm gold and 2.5 nm titanium. In the left panel the vdW force is included, but in the right panel the vdW force is not included.

Janus particle, especially when designing new materials and developing new applications that rely on particle dynamics or transport. Further, Janus particles have also been suggested as probes of local rheology and mechanics of a material. The phenomena described herein should be taken into account when utilizing Janus particles in this manner.

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APPENDIX A: VAN DER WAALS ATTRACTION FORCE EFFECT ON THE SYSTEM

Additional Brownian dynamics simulations were conducted by adding the force resulting from the van der Waals interactions. A known potential energy expression obtained from experiments on isotropic 6-μm PS particles in 0.95 m*M* NaCl electrolyte was used [\[79\]](#page-8-0):

$$
E_{\text{vdW}}(h) = -3kT \exp\left(-\frac{h}{\delta}\right),\tag{A1}
$$

$$
F_{\text{vdW}}(h) = -\frac{3kT}{\delta} \exp\left(-\frac{h}{\delta}\right),\tag{A2}
$$

where $\delta = 40$ nm. Figure 8 compares the number of observations at different orientations between BDS with and without van der Waals (vdW) force and Fig. [9](#page-7-0) illustrates the number of observations at different heights and orientations. In summary, these results show the vdW force for a $6-\mu m$ PS isotropic particle is negligible as compared to the other forces at these electrolyte conditions. Particles of smaller diameter will sample larger separation distances, thereby further reducing the relative impact of the vdW force. Note, however, this expression is for an isotropic particle and that work is ongoing to develop a vdW expression for a Janus particle. Also note that at conditions in which the electrolyte concentration is larger, a particle will sample smaller separation distances and the vdW force is likely to have a more significant impact.

FIG. 9. Number of observations for a particle with cap oriented downward. The coating thickness is 20 nm gold and 2.5 nm titanium.

APPENDIX B: CENTER OF MASS CALCULATION

The geometry required for the center of mass in the torque calculation was that of a semihollow hemisphere (Fig. 10). The axisymmetric nature of the relevant geometry allowed for the center of mass to be obtained at some position along the *x* axis. A cut of the cap was required to account for the noncanceled torque of the Janus particle when rotated away from $\theta = 0^\circ$ or $\theta = 180^\circ$. Finally, the cap thickness was small enough as compared to the particle radius that it was neglected in center of mass calculations. The center of mass was calculated by

$$
w_{\text{CoM}} = \frac{\int x dm}{M} = \frac{\int x dA}{\int dA},\tag{B1}
$$

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FIG. 10. A schematic of a semihollow hemisphere.

where *dm* is a differential mass element, *M* is total mass, *dA* is a differential surface area element, and *A* is the total surface area. By replacing *x* and *dA* values with the expressions found in Fig. 10 , w_{CoM} was calculated:

$$
\frac{\int_0^{\alpha} \int_0^{\pi} a \cos \psi \sin \varphi \, d\psi \, a \cos \psi d\varphi}{\int_0^{\alpha} \int_0^{\pi} a d\psi \, a \cos \psi d\varphi}.
$$
 (B2)

The result following integration is the center of mass:

$$
w_{\text{CoM}} = \frac{2a}{\pi \sin(\alpha)} \left[\frac{\alpha}{2} + \frac{\sin(2\alpha)}{4} \right].
$$
 (B3)

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