Pump depletion and hot-electron generation in long-density-scale-length plasma with shock-ignition high-intensity laser

J. Li,¹ S. Zhang¹, C. M. Krauland,² H. Wen,³ F. N. Beg¹, C. Ren,^{4,5,*} and M. S. Wei^{2,†}

¹Center for Energy Research, University of California San Diego, La Jolla, California 92093, USA

²Inertial Fusion Technology, General Atomics, San Diego, California 92121, USA

³Department of Electrical Engineering, University of California, Los Angeles, California 90095, USA

⁴Department of Mechanical Engineering and Laboratory for Laser Energetics, University of Rochester, Rochester, New York 14627, USA

⁵Department of Physics and Astronomy, University of Rochester, Rochester, New York 14627, USA

(Received 10 January 2019; revised manuscript received 16 September 2019; accepted 9 January 2020; published 18 March 2020)

Two-dimensional particle-in-cell simulations for laser plasma interaction with laser intensity of 10^{16} W/cm², plasma density range of $0.01-0.28n_c$, and scale length of $230-330 \ \mu$ m showed significant pump depletion of the laser energy due to stimulated Raman scattering (SRS) and stimulated Brillouin scattering (SBS) in the low-density region ($n_e = 0.01-0.2n_c$). The simulations identified hot electrons generated by SRS in the low-density region with moderate energy and by two-plasmon-decay near $n_e = 0.25n_c$ with higher energy. The overall hot electron temperature (46 keV) and conversion efficiency (3%) were consistent with the experiment's measurements. The simulations also showed artificially reducing SBS would lead to stronger SRS and a softer hot-electron spectrum.

DOI: 10.1103/PhysRevE.101.033206

Shock ignition (SI) [1,2] is a laser-driven inertial confinement fusion scheme which achieves ignition conditions by using a low intensity ($< 10^{15} \text{ W/cm}^2$) laser pulse for fuel compression followed by a high intensity $(10^{\sim 16} \text{ W/cm}^2)$ pulse. This high intensity pulse drives a strong convergent shock in the dense shell to boost pressure and temperature to achieve ignition. It potentially has much higher energy gain and lower risk of hydroinstabilities [1] compared to the conventional center hot spot scheme [3]. The challenge of SI lies in coupling sufficient ignition pulse energy to the target under significant laser plasma instabilities (LPIs) [4], including stimulated Brillouin scattering (SBS) [5,6], stimulated Raman scattering (SRS) [7,8], two-plasmon decay (TPD) [9,10], and filamentation [11]. The LPI can scatter the laser light to reduce the coupling efficiency (SBS and SRS) and generate suprathermal (hot) electrons (SRS and TPD) which can either preheat the fuel or enhance the coupling efficiency depending on their energy distribution [12]. Those hot electrons with energies below 100 keV can significantly boost the shock pressure [13]. Recently Shang et al. showed for laser-hot-electron conversion efficiency of $\eta > 10\%$, ignition can be achieved with 400 kJ compression and 100 kJ ignition pulse energy in what they call *electron shock ignition* [14]. Measuring and understanding LPI and hot-electron generation in SI is critical [15–23].

The existing experiment and simulation results on hotelectron generation are somewhat conflicting. The strong spherical shock experiments on OMEGA measured η up to 4% with overlapped laser beams smoothed by spectral dispersion (SSD) and 9% without SSD [24] for the target density scale length at the quarter-critical surface $L_n =$ $n_e/(dn_e/dx) = 125 \ \mu m$ [25], where n_e is the plasma density along the incident laser direction x. The instantaneous η can be as high as 13-15% [24,25]. Particle-in-cell (PIC) simulations with the experimental conditions and the laser incident from plasma density $n_e = 0.12n_c$ yielded $\eta = 12\%$ [25], where n_c is the critical density of the incident laser. This motivated ignition-scale electron shock ignition design in Ref. [14] with the expectation that η would increase in longer-scale lengths and stronger SRS. The PIC simulations in Ref. [14] with $L_n = 314 \ \mu m$ and laser incident from $n_e = 0.2 n_c$ did show an $\eta = 25\%$. On the other hand, the so-called 40 + 20 experiments on OMEGA using 40 beams for compression and 20 tightly focused nonoverlapping beams as the ignition pulse measured an $\eta = 1.7\%$ [26,27]. PIC simulations for this experiment with $L_n = 170 \ \mu m$ and the laser incident at $n_e = 0.17n_c$ showed η as high as 19%, a clear discrepancy with the experiment. The PIC simulations did not include the lower-density region, which potentially can cause significant SRS and SBS backscattering. Indeed, one-dimensional (1D) PIC [21] and fluid [22] simulations showed significant backscattering (of 40-90%, depending on intensity, of the incident laser energy) once the $n_e = 0.015 - 0.17n_c$ region was included. It is critical to understand the low-density region LPIs since this region is long in ignition-scale targets.

Recently, a new SI experiment on OMEGA extended performance (EP) using planar targets to achieve long-scale

^{*}chuang.ren@rochester.edu

[†]Current address: Laboratory for Laser Energetics, University of Rochester, Rochester, New York 14623; mingsheng.wei@rochester.edu

TABLE I. The density ranges and laser types for three PIC simulations.

Index	Density range (n_c)	Laser type
(i) (long)	0.01-0.28	Plane wave
(ii) (short)	0.14-0.28	Plane wave
(iii) (speckle)	0.14-0.28	Speckle

lengths ($L_n = 230-330 \ \mu \text{m}$) measured $\eta = 2 \pm 1\%$ with a hot-electron temperature of $T_h \sim 45$ keV [20]. The backscattered SRS light spectra and the 4ω probe diagnostic measuring laser front movement indicated strong pump depletion (pd) in the region of $n_e < 0.2n_c$ [28]. In this paper, we present twodimensional (2D) fully relativistic PIC simulations with physical conditions relevant to this experiment. This was the planar multi-picosecond 2D PIC simulations of LPI at SI intensity in millimeter long-scale plasmas with $n_e = 0.01 - 0.28 n_c$. Our simulation results show strong pump depletion dominated by SBS and $\eta = 3\%$ and $T_h = 46$ keV that were in excellent agreement with the experimental results. The observed hotelectron properties were profoundly linked to SBS in the low-density region, which can affect the location and saturation level of the most significant SRS modes through pump depletion. This new physics is unique to long-scale-length plasmas and a SI high intensity laser for which the SBS seeds in the low-density region can be amplified to the pump level and cause significant energy loss. Our results raise the concern of LPI-induced pump depletion in ignition-scale design for SI.

Our 2D PIC simulations with the OSIRIS code [29] are listed in Table I. The initial physical conditions of the simulations were relevant to the OMEGA EP experiment [20] and obtained from hydrosimulations with the FLASH code [30]. As shown in Fig. 1(a), the plasma density n_e for Simulation (i) (long), the main focus of this paper, ranged from $0.01n_c$ to $0.28n_c$ with $L_n \sim 230 \ \mu m$ for $n_e > 0.2n_c$ and $L_n \sim 330 \ \mu m$ for $n_e < 0.2 n_c$. This density profile had been validated in the experiment. The initial plasma fluid velocity gradient was $1.5 \times 10^{-7} \omega_0$, where ω_0 is the laser frequency. The incident plane-wave ultraviolet (UV) laser (wavelength = 0.351 μ m) was linearly polarized on the simulation plane with an intensity of $I_0 = 1 \times 10^{16} \text{ W/cm}^2$. It was launched at the left boundary of the simulation domain with a short rising time of $10\omega_0^{-1}$ (~1.9 fs). The plasma consisted of electrons with temperatures of $T_e = 1.6$ keV, carbon and hydrogen ions with temperatures of $T_i = 1$ keV. The simulation was performed for 10 ps to demonstrate the time evolution and competition of different LPI modes. The simulation domain was 16 000 c/ω_0 (~900 μ m) (in longitudinal x) by $200c/\omega_0$ $(\sim 11 \ \mu m)$ (in transverse y) with the grid sizes of $\Delta x = \Delta y =$ $0.2c/\omega_0$ (~0.01 μ m), where c is the light speed. The initial numbers of particles per cell were 100 for electrons and 50 for each ion species. The boundary conditions were periodic in the y direction. In x, the boundary conditions were thermal for particles and open for electromagnetic fields.

Significant pump depletion of the incident laser was observed from the y-averaged Poynting vector P_x plot [Fig. 1(b)]. Strong negative P_x bursts (blue color in the two black ellipses) correspond to significant backscattered light from SRS and SBS below $0.1n_c$. The components of the bursts can



FIG. 1. (a) The initial density and fluid velocity profiles of the PIC simulations. (b) The space and time evolution of the longitudinal Poynting vector P_x . (c) The instantaneous reflectivities of SRS and SBS. (d) The calculated Λ_{SBS} and Λ_{SRS} at different densities. The horizontal purple dashed and green dashed-circle lines refer to the Λ_{pd} for the Thomson scattering seed and PIC seed, respectively. (e) The distribution functions of electron momentum near $0.1n_c$ at different times. The vertical dashed line marks the phase velocity of the resonant plasma wave of the SRS modes. (f) The space profiles of the reflected SRS light with a frequency of $0.651\omega_0$ at 2.25 ps (black solid line, lower), 2.35 ps (red dashed line, middle), and 2.45 ps (green dot-dashed line, upper).

be distinguished by the longitudinal wave number k_x of the reflected lights near the left boundary with $n_e = 0.01n_c$. Here, the SRS reflected lights had $0.5k_0 < k_x < 0.8k_0$, where k_0 is the incident laser wave number in vacuum. By comparison, the reflected lights from SBS had $k_x \sim k_0$. The SRS and SBS reflectivities are plotted in Fig. 1(c). At ~4 ps, the instantaneous SRS reflectivity (~75%) was comparable to SBS in the first burst, but SBS (66% on average) strongly suppressed SRS (8% on average) after 6 ps.

The strong laser pump depletion was due to the large convective gains of SRS and especially SBS. In an inhomogeneous plasma, the linear convective gain [9] $\Lambda = \gamma_{\text{eff}}^2/|\kappa' V_1 V_2|$ describes how much SRS and SBS can grow from an initial δ -function seed. Here, γ_{eff} is approximated by $\sqrt{(\gamma_0 - \nu_1)(\gamma_0 - \nu_2)}$, where γ_0 is the temporal growth rates of SRS or SBS in a homogeneous plasma without any damping, V_1 , V_2 , ν_1 , and ν_2 are the group velocities and total damping rates on the two daughter waves. We consider both Landau damping and collisional damping [4]. The Landau damping only applies to the plasma wave for SRS and the ion acoustic wave for SBS [31], and the collisional damping affects both daughter waves for SRS and SBS. The gradient of the wave number mismatch is $\kappa' = d(k_{pump} - k_1 - k_2)/dx$, where k_{pump} , k_1 , and k_2 are the wave numbers of the pump and two daughter waves. Large I_0 ($I_0 \propto \gamma_0^2$) and L_n ($L_n \propto 1/\kappa'$) lead to large Λ . Since the scattered light intensity $I_{\text{scatter}} \approx$ $\exp(2\pi\Lambda)I_{\text{seed}}$ (I_{seed} is the seed intensity), one can reasonably estimate that strong pump depletion occurs when I_{scatter} becomes comparable to the incident laser intensity I_0 . For the actual $I_{\text{seed}} \approx (1-8) \times 10^{-10}I_0$ (based on the Thomson scattering model [21,32] for SBS), the critical gain above which pump depletion by SBS becomes important was $\Lambda_{\text{pd}}^{(\text{SBS})} =$ $(2\pi)^{-1} \ln(I_0/I_{\text{seed}}) = 3.4$. [The SRS seed level was lower than $I_{\text{seed}} \approx (5 \text{ to } 6) \times 10^{-11}I_0$.]

We plot Λ for SRS and SBS in Fig. 1(d). The results show that SBS gain factor Λ_{SBS} was above $\Lambda_{pd}^{(SBS)}$ for $n > 0.06n_c$ whereas the gain factor for SRS Λ_{SRS} stayed at ~2. This suggests that SBS, not SRS, can cause significant pump depletion for $n_e < 0.1n_c$. Both gains significantly decreased at lower densities due to strong Landau damping. We did observe flattening of the electron velocity distribution [Fig. 1(e)] which can cause decreasing in Landau damping. Neglecting all the damping effects $\Lambda_{SRS} = 2.7$ which was still much lower than Λ_{SBS} . This was consistent with the observed suppression of SRS caused by SBS in the region near $0.1n_c$ [Figs. 1(b) and 1(c)].

However, previous theory predicted SRS may turn from convective to absolute at shock ignition intensities [23] by density modulations [33-36], potentially growing SRS beyond the convective limit. According to Ref. [23], the density modulation threshold for this transition is low, $\Delta n/n \sim 10^{-5}$ for a characteristic modulation length of $\sqrt{V_1V_2}/\gamma_0 = 25c/\omega_0$. This is well below the typical 2% in our simulations and measured in experiments with similar parameters [37]. Here, we present evidence that SRS may have turned absolute in our PIC simulations. At $0.1n_c$, the resonant mode of the SRS backscattered light had a frequency of $\omega_{SRS} = 0.651\omega_0$. The wave numbers of this mode can be calculated at different densities, enabling the extraction of this mode amplitude in space. Figure 1(f) shows the space profiles of this mode at 2.25, 2.35, and 2.45 ps near $0.1n_c$ ($x = 10500c/\omega_0$). The chosen time frames were right after the laser reached $0.1n_c$ at 2 ps but before strong pump depletion due to SBS reduces the laser intensity by half at 2.5 ps. The left peaks near x = $8000c/\omega_0$ displayed signatures of convective growth, growing in amplitude and moving to the left. In contrast, the right peak in the resonant region near $x = 10\,000c/\omega_0$ kept growing at the same location, showing the signatures of absolute instability. Its growth eventually was interrupted by SBS-induced pump depletion that lowers the local pump intensity. This illustrates the importance of LPI coupling in this region.

Pump depletion due to SBS and SRS reduced the laser intensity near $n_c/4$ to $\sim 8 \times 10^{14}$ W/cm², only $\sim 8\% I_0$. But this intensity was still well above the threshold for absolute TPD (1.6×10^{14} W/cm²) [10]. TPD signals are presented in Fig. 2. Near $n_c/4$, significant plasma waves were observed [Fig. 2(a)], and the Fourier transform of these modes showed that they overlapped with the theoretical curve of TPD instability [Fig. 2(b)] above $0.2n_c$. Note that the strong signals near



FIG. 2. (a) The space and time evolution of longitudinal electric field energy $\langle E_x^2 \rangle$. (b) The $k_x - x$ spectrum of E_x at 10 ps. The white curves represent k_x corresponding to the maximum TPD growth rate at different densities. (c) The density of hot electrons with energy above 50 keV in the phase space of x and time. The white arrow shows the hot electrons move to the higher-density region with time. (d) The energy spectra of accumulated hot electrons from Simulations (i)–(iii) (denoted by long, short, and speckle, respectively, in the legend). In (a)–(c), the left boundaries correspond to the plasma density $0.1n_c$.

 $k_x \sim 0.9\omega_0/c$ in Fig. 2(b) corresponded to the electric fields of both the incident laser and the SBS side scattered light.

The space-time information of hot electrons (with energy above 50 keV) is presented in Fig. 2(c) and shows that most hot electrons were generated in $n_e = 0.2-0.25n_c$ and TPD may be the main cause. However, in $n_e = 0.1-0.2n_c$, SRSgenerated hot electrons were also observed at 4 and 8 ps. The SRS hot electrons may continue to be accelerated by TPD [Fig. 2(c)]. This was where both the SRS and the TPD hot electrons were identified by their origins in one simulation. The time-averaged η was 3% with a temperature of $T_h \sim$ 46 keV [Fig. 2(d) (long)].

The high SBS reflectivity was not due to elevated seed level in the simulation. In the simulation, the SBS seed was dominated by the electromagnetic noise, which was about 10³ times higher than electrostatic noise. The PIC SBS seed level was higher than the actual seed level $I_{\text{seed}}^{(\text{PIC})} \approx 10^{-4 \text{ to} -5} I_0 \approx 10^5 I_{\text{seed}}$. However, the critical gain $\Lambda_{\text{pd}}^{(\text{SBS})}$ depends *insensitively* on the seed level and would decrease from 3.4 to 1.7. This did not expand significantly the density region of strong SBS pump depletion [Fig. 1(d)]. This was further supported by two 1D PIC simulations with the same physical parameters but different number of particles per cell (PPC) = 200 and 20000, which showed similar average SBS reflectivity [Fig. 3(a)]. We believe, here, physics depended more on strong pump depletion and not sensitive to the seed level [38].

The experiment found strong pump depletion but did not have direct SBS measurement [20]. To study possible situations when SBS was not as high below $0.1n_c$ and a higher laser intensity can reach $n_e > 0.1n_c$, we performed two more 2D PIC Simulations (ii) and (iii) (Table I) with the same



FIG. 3. (a) The SBS reflectivities in 1D PIC simulations with numbers of PPC = 200 and 20 000. The time-averaged reflectivities are given in the legend. (b) The reflectivities of SRS and SBS in Simulations (ii) and (iii) denoted by short and speckle. (c) The density of hot electrons with energy above 50 keV in the phase space of *x* and time. (d) The instantaneous η for Simulations (i)–(iii).

initial conditions except that the density profile starts from $0.14n_c$ instead of $0.01n_c$ [the region on the right hand side of the green vertical dashed line in Fig. 1(a)]. Both simulations showed a lower T_h than the experiment. Without the low-density (<0.14 n_c) plasma, the average SRS reflectivity for the plane-wave case [(ii), (short)] rose to 20%, and the SBS reflectivity decreased to 32% as shown in Fig. 3(b). Hot electrons were now mainly generated by SRS in $n_e = 0.14-0.2n_c$ [Fig. 3(c)], which contrasts to Fig. 2(c). TPD can still be observed near $n_c/4$, but they were no longer the main cause for hot electrons. Compared to Simulation (i), η increased from 3% to 5% [Fig. 3(d)], and T_h decreased from 46 to 35 keV [Fig. 2(d)], both trending away from the experiment's values.

Comparing Simulations (i) and (ii) shows the importance of including the low-density region. This also shows the competition in SBS and SRS. Reducing SBS not only reduced the overall reflectivity, but also increased SRS, which, in turn, would soften the hot-electron spectrum. From hot-electron locations in the simulation domain [Figs. 2(c) and 3(c)], we can separate SRS and TPD hot electrons. We find SRS hot electrons had $T_h = 20-25$ keV lower than $T_h = 45-65$ keV of TPD hot electrons. Consequently, the accumulated hot electrons in Simulation (i) showed higher $T_h \sim 46$ keV compared to moderate $T_h \sim 35$ keV in Simulation (ii) [Fig. 2(d)]. This

- R. Betti, C. D. Zhou, K. S. Anderson, L. J. Perkins, W. Theobald, and A. A. Solodov, Phys. Rev. Lett. 98, 155001 (2007).
- [2] L. J. Perkins, R. Betti, K. N. LaFortune, and W. H. Williams, Phys. Rev. Lett. **103**, 045004 (2009).

shows the critical effects of LPI in the low-density region on the hot-electron properties in the long-scale-length plasma.

We performed Simulation (iii) (Table I) to qualitatively study how the effects of potential laser filaments and speckles on SBS and hot-electron generation. We used a single Gaussian laser speckle focused at $n_c/4$ with a spot size of 3 μ m, and the transverse size of the simulation domain was doubled compared to Simulation (ii). The maximum laser intensity at the incident plane was $I \sim 2 \times 10^{16}$ W/cm², keeping the transversely averaged intensity at 1×10^{16} W/cm². All other initial conditions were the same with Simulation (ii). The SRS and SBS reflectivities are plotted in Fig. 3(b). Compared to the plane-wave case (ii), the SBS reflectivity increased from 32% to 50%, and SRS reflectivity decreased from 20% to 15%. The conversion efficiency reduced to 3 to 4% [Fig. 3(d)], but $T_h = 37$ keV did not change much [Fig. 2(d)].

To summarize, the large-scale PIC simulations, here, show the importance of the low-density region in shock ignition LPI hot-electron generation. Only when it was included can the simulations reproduce the experiment measurements of the hot-electron conversion efficiency and temperature. Excluding it would increase the conversion efficiency by reducing the overall pump depletion and lower the temperature by increasing the SRS hot-electron fraction to levels inconsistent with the experiments. The strong pump depletion was supported by the experiments [28]. Our research shows that high convective gains of LPI for SI high laser intensity in the long-scale low-density region is a concern. However, it should be noted that both the simulations and the experiments described in this paper used a single beam as the main interaction pulse. Recent planar target experiments on OMEGA performed by this team [20] using multiple and overlapped UV beams as the interaction pulses with $I_0 = 1 \times 10^{16}$ W/cm², $L_n \sim 230 \ \mu$ m, and $T_e = 3$ keV have doubled laser-to-electron energy conversion efficiency $\eta = 4 \pm 2\%$ compared to the single-beam experiment on OMEGA EP. This warrants further investigation. Future LPI experiments on OMEGA are planned to directly probe electron plasma and ion acoustic waves using optical Thomson scattering together with time-resolved full aperture backscattering diagnostics.

We acknowledge useful discussions with Dr. L. Hao. This work was supported by the DOE Office of Science under Grants No. DE-SC0014666, No. DE-SC0012316, and NNSA NLUF Grants No. DE-NA0003600 and No. DE-NA0002730. This research used resources of the National Energy Research Scientific Computing Center (NERSC) and the Argonne Leadership Computing Facility, which are both the U.S. Department of Energy Office of Science User Facility but operated, respectively, under Contracts No. DE-AC02-05CH11231 and No. DE-AC02-06CH11357. The support of DOE does not constitute an endorsement by DOE of the views expressed in this paper.

[3] J. D. Lindl, P. Amendt, R. L. Berger, S. G. Glendinning, S. H. Glenzer, S. W. Haan, R. L. Kauffman, O. L. Landen, and L. J. Suter, Phys. Plasmas 11, 339 (2004).

^[4] W. L. Kruer, *The Physics of Laser Plasma Interactions* (Westview, Boulder, CO, 2003).

- [5] C. S. Liu, M. N. Rosenbluth, and R. B. White, Phys. Fluids 17, 1211 (1974).
- [6] D. W. Forslund, J. M. Kindel, and E. L. Lindman, Phys. Fluids 18, 1002 (1975).
- [7] M. N. Rosenbluth, Phys. Rev. Lett. 29, 565 (1972).
- [8] J. F. Drake and Y. C. Lee, Phys. Rev. Lett. **31**, 1197 (1973).
- [9] M. N. Rosenbluth, R. B. White, and C. S. Liu, Phys. Rev. Lett. 31, 1190 (1973).
- [10] A. Simon, R. W. Short, E. A. Williams, and T. Dewandre, Phys. Fluids 26, 3107 (1983).
- [11] R. S. Craxton and R. L. McCrory, J. Appl. Phys. 56, 108 (1984).
- [12] E. Llor Aisa, X. Ribeyre, G. Duchateau, T. Nguyen-Bui, V. T. Tikhonchuk, A. Colaïtis, R. Betti, A. Bose, and W. Theobald, Phys. Plasmas 24, 112711 (2017).
- [13] R. Nora, W. Theobald, R. Betti, F. J. Marshall, D. T. Michel, W. Seka, B. Yaakobi, M. Lafon, C. Stoeckl, J. Delettrez, A. A. Solodov, A. Casner, C. Reverdin, X. Ribeyre, A. Vallet, J. Peebles, F. N. Beg, and M. S. Wei, Phys. Rev. Lett. **114**, 045001 (2015).
- [14] W. L. Shang, R. Betti, S. X. Hu, K. Woo, L. Hao, C. Ren, A. R. Christopherson, A. Bose, and W. Theobald, Phys. Rev. Lett. 119, 195001 (2017).
- [15] O. Klimo, V. T. Tikhonchuk, X. Ribeyre, G. Schurtz, C. Riconda, S. Weber, and J. Limpouch, Phys. Plasmas 18, 082709 (2011).
- [16] S. Weber, C. Riconda, O. Klimo, A. Héron, and V. T. Tikhonchuk, Phys. Rev. E 85, 016403 (2012).
- [17] D. Batani, S. Baton, A. Casner, S. Depierreux, M. Hohenberger, O. Klimo, M. Koenig, C. Labaune, X. Ribeyre, C. Rousseaux, G. Schurtz, W. Theobald, and V. Tikhonchuk, Nucl. Fusion 54, 054009 (2014).
- [18] C. Riconda, S. Weber, V. T. Tikhonchuk, and A. Héron, Phys. Plasmas 18, 092701 (2011).
- [19] R. Yan, J. Li, and C. Ren, Phys. Plasmas 21, 062705 (2014).
- [20] S. Zhang, C. M. Krauland, J. Li, J. L. Peebles, F. N. Beg, S. Muller, N. B. Alexander, C. Ren, W. R. Theobald, R. Betti, D. J. Haberberger, E. M. Campbell, R. Yan, E. B. Borwick, J. Trela, D. Batani, P. Nicolai, R. Scott, and M. S. Wei, Bull. Am. Phys. Soc. 63(11), JO6.00012 (2018).
- [21] L. Hao, J. Li, W. D. Liu, R. Yan, and C. Ren, Phys. Plasmas 23, 042702 (2016).
- [22] L. Hao, R. Yan, J. Li, W. D. Liu, and C. Ren, Phys. Plasmas 24, 062709 (2017).
- [23] J. Li, R. Yan, and C. Ren, Phys. Plasmas 24, 052705 (2017).
- [24] W. Theobald, R. Nora, W. Seka, M. Lafon, K. S. Anderson, M. Hohenberger, F. J. Marshall, D. T. Michel, A. A. Solodov,

C. Stoeckl, D. H. Edgell, B. Yaakobi, A. Casner, C. Reverdin, X. Ribeyre, A. Shvydky, A. Vallet, J. Peebles, F. N. Beg, M. S. Wei, and R. Betti, *Phys. Plasmas* **22**, 056310 (2015).

- [25] W. Theobald, A. Bose, R. Yan, R. Betti, M. Lafon, D. Mangino, A. R. Christopherson, C. Stoeckl, W. Seka, W. Shang, D. T. Michel, C. Ren, R. C. Nora, A. Casner, J. Peebles, F. N. Beg, X. Ribeyre, E. Llor Aisa, A. Colaïtis, V. Tikhonchuk, and M. S. Wei, Phys. Plasmas 24, 120702 (2017).
- [26] W. Theobald, R. Nora, M. Lafon, A. Casner, X. Ribeyre, K. S. Anderson, R. Betti, J. A. Delettrez, J. A. Frenje, V. Y. Glebov, O. V. Gotchev, M. Hohenberger, S. X. Hu, F. J. Marshall, D. D. Meyerhofer, T. C. Sangster, G. Schurtz, W. Seka, V. A. Smalyuk, C. Stoeckl, and B. Yaakobi, Phys. Plasmas 19, 102706 (2012).
- [27] J. Trela, W. Theobald, K. S. Anderson, D. Batani, R. Betti, A. Casner, J. A. Delettrez, J. A. Frenje, V. Y. Glebov, X. Ribeyre, A. A. Solodov, M. Stoeckl, and C. Stoeckl, Phys. Plasmas 25, 052707 (2018).
- [28] S. Zhang, J. Li, C. M. Krauland, F. N. Beg, S. Muller, W. Theobald, J. Palastro, T. Filkins, D. Turnbull, D. Haberberger, C. Ren, R. Betti, C. Stoeckl, E. M. Campbell, J. Trela, D. Batani, R. Scott, and M. S. Wei, arXiv:1909.00094.
- [29] R. A. Fonseca, L. O. Silva, F. S. Tsung, V. K. Decyk, W. Lu, C. Ren, W. B. Mori, S. Deng, S. Lee, T. Katsouleas, and J. C. Adam, Computational science iccs 2002: International conference amsterdam, the netherlands, april 21–24, 2002 proceedings, part iii, (Springer Berlin Heidelberg, Berlin, Heidelberg, 2002) Chap. OSIRIS: A Three-Dimensional, Fully Relativistic Particle in Cell Code for Modeling Plasma Based Accelerators, pp. 342–351.
- [30] B. Fryxell, K. Olson, P. Ricker, F. X. Timmes, M. Zingale, D. Q. Lamb, P. MacNeice, R. Rosner, J. W. Truran, and H. Tufo, Astrophys. J. Suppl. Ser. 131, 273 (2000).
- [31] H. X. Vu, J. M. Wallace, and B. Bezzerides, Phys. Plasmas 1, 3542 (1994).
- [32] R. L. Berger, E. A. Williams, and A. Simon, Phys. Fluids B 1, 414 (1989).
- [33] D. R. Nicholson and A. N. Kaufman, Phys. Rev. Lett. **33**, 1207 (1974).
- [34] D. R. Nicholson, Phys. Fluids 19, 889 (1976).
- [35] E. a. Williams, J. R. Albritton, and M. N. Rosenbluth, Phys. Fluids 22, 139 (1979).
- [36] G. Picard and T. W. Johnston, Phys. Fluids 28, 859 (1985).
- [37] J. Moody, B. MacGowan, S. Glenzer, R. Kirkwood, W. Kruer, a. Schmitt, E. Williams, and G. Stone, Phys. Rev. Lett. 83, 1783 (1999).
- [38] C. L. Tang, J. Appl. Phys. 37, 2945 (1966).