Standard sirens with a running Planck mass

Macarena Lagos,^{1,*} Maya Fishbach,^{2,†} Philippe Landry,^{1,3,‡} and Daniel E. Holz^{1,2,3,4,§}

¹Kavli Institute for Cosmological Physics, University of Chicago, Chicago, Illinois 60637, USA

²Department of Astronomy and Astrophysics, University of Chicago, Chicago, Illinois 60637, USA

³Enrico Fermi Institute, University of Chicago, Chicago, Illinois 60637, USA

⁴Department of Physics, University of Chicago, Chicago, Illinois 60637, USA

(Received 18 January 2019; published 5 April 2019)

We consider the effect of a time-varying Planck mass on the propagation of gravitational waves (GWs). A running Planck mass arises naturally in several modified-gravity theories, and here we focus on those that carry an additional dark energy field responsible for the late-time accelerated expansion of the Universe, yet—like general relativity (GR)—propagate only two GW polarizations, both traveling at the speed of light. Because a time-varying Planck mass affects the amplitude of the GWs and therefore the inferred distance to the source, standard siren measurements of H_0 are degenerate with the parameter c_M characterizing the time-varying Planck mass, where $c_M = 0$ corresponds to GR with a constant Planck mass. The effect of nonzero c_M will have a noticeable impact on GWs emitted by binary neutron stars (BNSs) at the sensitivities and distances observable by ground-based GW detectors such as Advanced LIGO and A+, implying that standard siren measurements can provide joint constraints on H_0 and c_M . Assuming a Λ cold dark matter evolution of the Universe and taking *Planck*'s measurement of H_0 as a prior, we find that GW170817 constrains $c_M = -9^{+21}_{-28}$ (68.3% credibility). We also discuss forecasts, finding that if we assume H_0 is known independently (e.g., from the cosmic microwave background), then 100 BNS events detected by Advanced LIGO can constrain c_M to within ±0.9. This is comparable to the current best constraints from cosmology. Similarly, for 100 LIGO A+ BNS detections, it is possible to constrain c_M to ± 0.5 . When analyzing joint H_0 and c_M constraints we find that ~400 LIGO A+ events are needed to constrain H_0 to 1% accuracy. Finally, we discuss the possibility of a nonzero value of c_M biasing standard siren H_0 measurements from 100 LIGO A+ detections, and find that $c_M = +1.35$ could bias H_0 by 3σ to 4σ too low if we incorrectly assume $c_M = 0$.

DOI: 10.1103/PhysRevD.99.083504

I. INTRODUCTION

Einstein's general theory of relativity (GR) is the foundation of gravity. On Solar System scales, not only do its predictions show remarkable agreement with astrophysical data, but precise measurements of phenomena such as the deflection of light around the Sun and the perihelion shift of Mercury rule out many modifications to GR [1,2]. Nonetheless, GR exhibits weaknesses at both the very high and the very low energy regimes. At high energies, unavoidable singularities arise during gravitational collapse, and the so-called renormalization problem limits our understanding of quantum gravity [3–5]. In order to fit observational data on cosmological scales, GR relies on the presence of exotic unknown matter components, namely, dark matter and dark energy, to make up 95% of the total energy content of the Universe [6]. These issues

show the current limitations in our understanding of how gravity behaves and interacts with matter in extreme energy regimes. As a result, a number of modified-gravity theories have been proposed (see, e.g., [7–9] for summaries and reviews), and it is necessary to analyze their consistency, viability, and consequences.

Recently, multimessenger astrophysics has shown great potential for revealing new details of physical phenomena and testing gravity. In particular, combined gravitational wave (GW) and electromagnetic (EM) science is becoming a central topic, allowing us to test different aspects of cosmology and fundamental physics, including alternative dark energy candidates, spatial curvature, the expansion rate of the Universe, strong lensing sources, and the graviton mass [10–13], among others. For instance, the recent detection of GWs from a binary neutron star (BNS) merger, GW170817 [14], by the Advanced Laser Interferometer Gravitational Wave Observatory (LIGO) [15] and Advanced Virgo [16], in conjunction with the detection of an EM counterpart [17,18], constrained the propagation speed of GWs, c_T , to be $|c_T/c - 1| \leq 10^{-15}$

mlagos@kicp.uchicago.edu

mfishbach@uchicago.edu

landryp@uchicago.edu

holz@uchicago.edu

relative to the speed of light c. This high-precision constraint provides information about possible modifications to GR and strongly disfavors a number of gravity theories proposed in the literature [19–23].

The detection of GW170817 and its EM counterpart enabled the first standard siren measurement [24] of the current rate of expansion of the Universe, H_0 , assuming Λ cold dark matter cosmology and general-relativistic GW propagation. Besides [24]'s result, independent methods have been used to constrain the Hubble constant, falling into two major categories: large-scale and local observations. From the cosmic microwave background (CMB), the *Planck* mission [25] found $H_0 = 67.4 \pm 0.5$ km/s/Mpc [6], whereas from local observations of Type-Ia supernovae, the SHoES survey [26] found $H_0 = 73.48 \pm$ 1.66 km/s/Mpc [27]. These two measurements disagree at the 3.5 σ level. Consequently, obtaining independent GW constraints on H_0 with ~1% accuracy could substantially improve understanding of this tension and potentially reveal new physics or sources of systematic error. However, if gravity is described by a theory other than GR, an accurate inference of H_0 could be hampered by degeneracies with modified-gravity effects. Accordingly, in this paper we constrain H_0 with combined GW and EM observational data in the context of alternative theories of gravity with modified GW propagation.

The value of H_0 can be obtained if we know the redshift of the source and its luminosity distance. The GW amplitude is inversely related to the luminosity distance, and the scaling constant can be directly inferred from the evolution of the gravitational waveform, which depends on the theory of gravity [28]. While the source's redshift cannot be inferred directly from GWs, for events with EM counterparts it is possible to obtain the redshift from the EM spectrum. Sources of this kind are known as "standard sirens" [29], after their EM analogues known as "standard candles." In this context, the first BNS detection, GW170817, has already enabled the first standard siren measurement, $H_0 = 70.0^{+12.0}_{-8.0} \text{ km s}^{-1} \text{ Mpc}^{-1}$ [24,30] suggested that a detection of ~ 100 BNS events could yield a measurement with percent-level accuracy (see also [31,32]). This target may be attainable in as little as five years, as scheduled improvements bring the LIGO and Virgo detectors to their design sensitivity [30]. Within the next decade, the addition of two more detectors, KAGRA [33] and LIGO-India [34], to the LIGO-Virgo network, as well as the planned upgrade of Advanced LIGO to LIGO A+ [35], will further increase sensitivity to BNS mergers, which occur at an astrophysical rate of 110 Gpc⁻³ yr⁻¹ or greater [36].

Inspired by modified-gravity models that introduce new degrees of freedom as an alternative to dark energy, we analyze how modified propagation of GWs affects the standard siren estimation of H_0 . In the context of cosmology, some alternative models have indeed been found to

affect H_0 measurements and reduce the tension between the cosmological Λ CDM and local H_0 values (see [37] for a recent review and discussion). Since the estimated luminosity distance depends on the gravitational theory, we expect it to be different in models where the GW propagation changes due to the presence of additional fields. The impact of modified GW propagation on the measurement of H_0 was recently considered in [38], which studied a specific model where the amplitude of the GWs is damped due to modified-gravity effects in addition to the damping caused by the expansion of the Universe. Specifically, this work considered a nonlocal gravity model and analyzed how constraints on H_0 are affected by modifications to gravity and to the equation of state of dark energy.

In this paper, we stay agnostic regarding the specific underlying gravity theory and study H_0 in a modelindependent manner, although for simplicity we assume the background Universe to evolve according to the ACDM model, while allowing for general modifications for cosmological perturbations and gravitational waves. We compare constraints on H_0 with and without considering cosmological data, and quantify the impact of damping effects caused by modified gravity. In particular, we identify the extra damping effect with an effective running of the Planck mass, as it is typically found in common modified-gravity theories, whose time evolution is given by the fractional dark energy density Ω_{DE} . This time evolution will have one constant arbitrary parameter c_M , representing the Planck mass rate today, with $c_M = 0$ corresponding to GR with a constant Planck mass. The observable consequences of a running Planck mass have been studied in a number of regimes (see, e.g., [39] for a review), and its effect on the propagation of gravitational waves has been considered in [40–44]. We find that external cosmological data from Planck, in conjunction with GW170817, constrain c_M to be $-81 < c_M < 28$ at the 95% credible level. These constraints are very weak compared to those from cosmological data alone when assuming a specific modified-gravity theory, as c_M also affects CMB and structure formation. For instance, for Horndeski theories, current cosmological constraints give $-0.62 < c_M < +1.35$ at 95% confidence level [45].

In addition, we consider populations of events and discuss future forecasts for standard sirens with Advanced LIGO and LIGO A+. We find that with A+, 100 BNSs with detected EM counterparts can lead to cosmology-independent constraints on H_0 with an accuracy of ~3%, and on c_M with $\sigma(c_M) \sim 0.9$. From these results we estimate the need for ~400 events in order to obtain a 1%-accurate constraint on H_0 in the presence of a running Planck mass, thereby matching current local and cosmological constraints. Furthermore, we find that H_0 and c_M are highly degenerate, which highlights the importance of testing for the parameter c_M to avoid biasing the inferred value of H_0 by assuming GR (i.e., $c_M = 0$) in a setting

where the true gravitational wave physics is described by c_M of $\mathcal{O}(1)$. In particular, we show that if we have a population of 100 events detected by LIGO A+ with $c_M = 1.35$, then the inferred H_0 , assuming $c_M = 0$, will typically be >3 σ away from the true value. In this case, the true value of H_0 would be outside the posterior 99% credible interval due to the misplaced assumption of $c_M = 0$.

The paper is structured as follows. In Sec. II we describe how a time-dependent Planck mass modifies the propagation of GWs, as well as other local and cosmological observables. In Sec. III we discuss the use of BNS mergers as standard sirens in the context of a running Planck mass. We describe our inference of H_0 in Sec. IV, and in Sec. V we show how estimates of H_0 change compared to GR. Finally, in Sec. VI we summarize our results and give an outlook for future work. We set the speed of light to unity (c = 1) throughout.

II. RUNNING PLANCK MASS

Let us start by considering a perfectly homogeneous and isotropic spatially flat cosmological background. In this case, the metric line element in conformal time τ takes the form of the Friedmann-Robertson-Walker (FRW) solution:

$$ds^{2} = a(\tau)^{2} [-d\tau^{2} + d\vec{x}^{2}], \qquad (1)$$

where $a(\tau)$ is the scale factor determining the expansion of the Universe. We next suppose that gravity is described by a modified theory with a time-dependent Planck mass. As previously mentioned, alternative theories typically include new degrees of freedom, which can interact nontrivially with the metric to produce an effective running of the Planck mass. In such a case, there is an ambiguity when defining the stress-energy tensor: the new effects can be interpreted as modifying gravity (i.e., the Einstein tensor $G_{\mu\nu}$), or as modifying the matter content of the Universe (i.e., the stress-energy tensor $T_{\mu\nu}$). However, without loss of generality, we can always adopt the latter perspective and write the background equations of motion in the standard form

$$3\mathcal{H}^2 M_P^2 = a^2 (\rho_m + \rho_{\rm DE}),\tag{2}$$

where $\mathcal{H} = a'/a$ is the conformal Hubble rate (with $l \equiv d/d\tau$), M_P is the constant Planck mass, $\rho_m(\tau)$ is the energy density of CDM, and $\rho_{\text{DE}}(\tau)$ is the energy density of dark energy, which is to encapsulate all modified-gravity effects. According to this definition, each of the fluid energy-density components is separately conserved:

$$\rho'_i + 3\mathcal{H}(\rho_i + P_i) = 0, \qquad i = m, \text{DE}.$$
 (3)

We note that the choice to write the background equation as in Eq. (2) is arbitrary, and we could have instead defined it with an effective time-dependent mass $M_*(\tau)$ instead of M_P on the left-hand side and a different $\rho_{\rm DE}$ on the right-hand side. However, in that case, the energy-density components would not have been separately conserved, and thus for simplicity we avoid this choice.

Here we have assumed that there is an additional degree of freedom that couples to the metric in a nontrivial way, which leads to an arbitrary ρ_{DE} . In contrast, standard matter components such as baryons and photons have been assumed to be minimally coupled to the metric, as usual, and therefore the way they contribute to the background equations is unchanged. Furthermore, their propagation and evolution are determined by standard geodesics in the given metric background. In particular, for perturbations about FRW, light still propagates at speed *c*.

Next, let us consider small cosmological perturbations around this background universe, and write the total metric as

$$g_{\mu\nu} = \bar{g}_{\mu\nu} + h_{\mu\nu}, \qquad |h| \ll |\bar{g}|,$$
 (4)

where $\bar{g}_{\mu\nu}$ is the background FRW metric and $h_{\mu\nu}$ is a linear perturbation whose transverse and traceless part $h_{\mu\nu}^{TT}$ encodes the GW amplitude. The other components of $h_{\mu\nu}$ determine the amplitude of matter energy-density perturbations, which will be ignored for our purposes.

GR is a single metric theory for a massless spin-2 particle, and hence $h_{\mu\nu}^{TT}$ propagates 2 physical degrees of freedom corresponding to two tensor polarizations. We consider modified-gravity theories that do not propagate additional tensor modes, and therefore $h_{\mu\nu}^{TT}$ alone carries all the information on the evolution of the metric polarizations. Generically, such theories have the following quadratic action,

$$S = \frac{1}{2} \int d^3x d\tau M_*^2 a^2 [h_A'^2 - c_T^2 (\vec{\nabla} h_A)^2], \qquad (5)$$

where we have expanded $h_{\mu\nu}^{TT}$ into two independent polarization components h_A with $A = +, \times$. The equation of motion for GWs will thus be given by

$$h_A'' + [2 + \alpha_M(t)]\mathcal{H}h_A' + k^2 c_T^2 h_A = 0, \qquad (6)$$

where we have transformed h_A to the spatial 3D Fourier space; its amplitude therefore implicitly depends on time τ and wave number k. Here α_M has been defined as

$$\alpha_M \equiv \frac{d \ln(M_*/M_P)^2}{d \ln a} = \frac{2}{\mathcal{H}} \frac{M'_*}{M_*}.$$
 (7)

We recover GR when $M_* = M_P$ (i.e., $\alpha_M = 0$) and $c_T = 1$. However, in modified-gravity theories, additional gravitational fields such as scalars or vectors will generically have a time-dependent solution in cosmological backgrounds, which can induce a running of the Planck mass $M_*(\tau)$ due to conformal couplings, even in a local frame. Additional fields can also modify the propagation speed of GWs $c_T(\tau)$ due to nonminimal and nonconformal couplings. We remark that, in this background, both M_* and c_T are functions of time only, and are thus isotropic and polarization independent.

Note that we have not added any nonderivative terms to Eq. (5). This is a consequence of our assumption that the graviton remains massless in the modified theory, and propagates only two polarizations, like in GR. Nonderivative terms like $m^2 h_A^2$ can appear in massive gravity theories [46,47], but their GWs are described by five different polarization modes, instead of the two modes h_A . More complicated models have also been developed, such as ones in which GWs are directly coupled to additional fields; the perturbations of these fields would appear explicitly in Eq. (5). This is the case of bigravity theories [48], which propagate one massless and one massive graviton. In these models, GWs can oscillate between the two gravitons (by analogy with neutrinos) and lead to distinctive signals in the waveform [49,50]. A similar phenomenon is present in multivector theories with internal SU(2) symmetry [51]. Nonetheless, we will not consider such cases in this paper, focusing exclusively on gravity theories that lead to the action of Eq. (5).

Due to the aforementioned constraints on the speed of GWs from GW170817, we will focus only on running Planck mass models where $c_T = 1$. Well-known modifiedgravity theories that lead to Eq. (5) with $c_T = 1$ are scalartensor theories in the Horndeski [52,53] and beyond Horndeski [54,55] families that have $c_T = 1$ [19]. Their action takes the form

$$S_s = \int d^4x \sqrt{-g} [G_4(\phi)R + K(X,\phi) - G_3(X,\phi)\Box\phi],$$
(8)

where ϕ is an additional scalar gravitational field responsible for dark energy, $X = -\nabla_{\mu}\phi\nabla^{\mu}\phi/2$ is the kinetic term of the scalar field, and G_4 , K, and G_3 are arbitrary functions. In this case, $\alpha_M = G_4(\phi)$. Specific models belonging to this category are quintessence, f(R) gravity, kinetic gravity braiding, and Jordan-Brans-Dicke theory [19]. Ignoring the matter sector, generalizations of the gravitational action in Eq. (8) can be obtained by performing a disformal transformation of the metric (see, e.g., [22]) to obtain theories belonging to the degenerate higher order scalar-tensor theory family [56–58], which retain the same structure for the GW action. See, e.g., [59–61] for reviews on the status of scalar-tensor gravity theories after GW170817.

We also mention that vector-tensor theories belonging to the generalized Proca [62] family with $c_T = 1$ have an action of the form [19]

$$S_v = \int d^4x \sqrt{-g} [R + G_2(X, F, Y) + G_3(X)\nabla_{\mu}A^{\mu}], \qquad (9)$$

where A^{μ} is an additional vector gravitational field responsible for dark energy; G_2 and G_3 are arbitrary functions of $X = -A^{\mu}A_{\mu}/2$, $F = -F_{\mu\nu}F^{\mu\nu}/4$, or $Y = A^{\mu}A^{\nu}F^{\alpha}_{\mu}F_{\nu\alpha}$, where $F_{\mu\nu} = \nabla_{\mu}A_{\nu} - \nabla_{\nu}A_{\mu}$. Since there are no conformal couplings between the vector field and the metric, it is straightforward to see that these models will also have constant M_* , and hence no modification will be seen for tensor polarizations (although the evolution of energydensity matter perturbations will be modified) [43].

The same happens for Lorentz-breaking vector-tensor theories of the Einstein-aether family [63,64]. In this case, the vector field is timelike, and hence defines a preferred frame of reference, and the subclass satisfying $c_T = 1$ also has constant M_* . We emphasize, however, that theories involving multiple vector fields do allow for nontrivial derivative couplings while still maintaining $c_T = 1$ [51]. However, this case is not encompassed by Eq. (5), as such models have an additional field explicitly coupled to h_A . Extended scalar-vector-tensor theories can also have $c_T = 1$ and a nontrivial $M_*(t)$; these are encompassed by Eq. (5) [65]. Generalizations to action (9) including higher derivative interactions have been also studied in [66], where theories with $c_T = 1$ and nontrivial predictions for GW astronomy have been found.

Having discussed examples of dark energy theories that can lead to an effective running Planck mass, we now turn to the observable consequences of such a modification. The time variation of fundamental constants has previously been studied in different regimes. Below, we survey its effect on various observables (see, e.g., [39] for a detailed review).

Cosmology: The effects of a running Planck mass on cosmology have been considered in [40,67–69] among others. The time dependence of the Planck mass arises due to the presence of additional fields, which can modify the background evolution of the Universe through a timedependent energy density $\rho_{\rm DE}$, in addition to modifying the evolution of perturbations propagating in the background. Early-time background modifications are well constrained by big bang nucleosynthesis (see, e.g., [70]), and the latetime background modifications are usually constrained using simple parametrizations for the equation of state of dark energy, such as $w_{\text{DE}} = w_0 + (1 - a)w_a$, with w_0 and w_a two free constants. We recover the standard Λ CDM model with $w_0 = -1$ and $w_a = 0$. The tightest constraints come from combined CMB, supernova, and baryon acoustic oscillation measurements yielding $w_0 = -0.961 \pm 0.077$ and $w_a = -0.28^{+0.31}_{-0.27}$ [6]. Since only small nonvanishing w_a are allowed, from now on we will assume that the background evolution is exactly ACDM. This has the added benefit of disentangling effects coming from the modified background and those coming from the evolution of the perturbations.

Nonetheless, even if the background evolution of the Universe is unmodified, the evolution of linear cosmological perturbations can still differ from Λ CDM. It is customary to encode the modifications determining the evolution of the energy-density matter perturbations in two parameters, which affect the evolution of the two Newtonian potentials Φ and Ψ in the metric

$$ds^{2} = -a(\tau)^{2}[(1+2\Phi)d\tau^{2} + (1-2\Psi)d\vec{x}^{2}], \quad (10)$$

which describes the modifications relative to the FRW solution. The first parameter is an effective Newton's strength G_{eff} such that the Poisson equation becomes

$$\bar{\Box}\Phi = 4\pi G_{\rm eff}\rho_m \Delta_m,\tag{11}$$

where \Box is the d'Alembert operator using the covariant derivatives of the background metric (1), $\Delta_m = \delta \rho_m / \rho_m + 3Hv_m$ is the comoving gauge-invariant matter perturbation, $\delta \rho_m$ is the energy-density perturbation, and v_m is its velocity potential. The effective Newton's strength depends on time only for subhorizon perturbations with wave number k > aH.

The second parameter, γ , describes an effective anisotropic stress which makes the two metric potentials differ:

$$\gamma = \Psi/\Phi. \tag{12}$$

The parameter γ depends on time only for subhorizon scales as well. Matter and metric perturbations behave in the same way as general relativity when $\gamma = 1$ and $G_{\text{eff}} = G_N$, where G_N is Newton's constant. In scalar-tensor theories, it can be seen that the running of the Planck mass causes dark energy to cluster, leading to $G_{\text{eff}} \neq G_N$, and also induces anisotropic stress, making $\gamma \neq 1$ (see, e.g., [71,72]).

These two parameters are independent of the background evolution, and can differ from GR even when $w_{\text{DE}} = -1$. In this unmodified background, we can therefore still obtain different predictions, for instance, for the CMB temperature anisotropies, or large-scale galaxy distributions. If we knew exactly the gravitational theory leading to these modifications, we could calculate exactly how α_M affects matter perturbations and use EM cosmological data to constrain the running Planck mass (e.g., [45,73] for scalar-tensor theories). However, in this paper we will remain agnostic about the underlying gravity theory, and instead constrain α_M using gravitational wave data.

Solar System: The effects of a running Planck mass at Solar System and laboratory scales have been studied in [74–76]. The relevant modification is a time-varying Newton's constant, which affects, for instance, the period and radius of planetary orbits. However, to remain consistent with the remarkable agreement between GR and observations in this regime, modified-gravity theories come equipped with a "screening mechanism" that hides all modified-gravity effects in dense regions, where one recovers $M_* = M_P$ (see, e.g., [9,77] for reviews). The mechanism can be due to the additional field acquiring a large mass in dense environments, and effectively mediating an undetectable short-range force (chameleon mechanism); due to changing its coupling with matter in this regime, becoming negligible (symmetron mechanism); or having dominant nonlinear kinetic terms effectively produce a negligible coupling to matter (Vainshtein mechanism), among other possibilities. These screening mechanisms are expected to act in the Solar System as well as clusters of galaxies. Currently, observations of the Solar System and laboratory experiments constrain variations of the Planck mass to be of order 10^{-3} [74,76].

Gravitational waves: The presence of an additional dark energy field may affect the original emission of the waveform from binary mergers as well as GW propagation. In this paper, we will assume that the additional gravitational degrees of freedom will not modify the emitted waveform, and hence we can use GR to predict the emission of the waveform. Consistency checks must be performed in the future for specific dark energy models to make sure that this is the case, as it has been previously shown that even when stationary black hole solutions may not be affected by the dark energy field, dynamical situations may excite it and leave an imprint [78]. Under our assumptions, we can still use compact binaries with EM counterparts as standard sirens.

Regarding the propagation of gravitational waves, modifications can occur even if the original emitted waveform is the same as in GR. In particular, as shown in Eq. (6) and considered previously in [40–44], a running Planck mass can affect GW propagation. In this paper, we will assume that the propagation can be modified inside and outside galaxies, where screening will not be active for GWs and hence the effects of the dark energy field become relevant. However, we will assume that today, in our Galaxy, the effective Planck mass is given by M_P (although the present-day value of α_M need not vanish). Multimessenger observations allow us to place independent constraints on the running of the Planck mass [42–44] as well as constraints on the present Hubble constant H_0 (see [38] for a specific model).

III. STANDARD SIRENS

In this section, we show explicitly how a running Planck mass affects standard siren measurements. Since we take the running of the Planck mass to be the result of a new dark energy field, we expect α_M to change over cosmological timescales and only affect the late-time Universe. We will consider a specific parametrization for $M_*(t)$ satisfying these requirements, and discuss in detail its consequences.

Following the approach in [38,43], we start by canonically normalizing the field h_A in Eq. (5), and obtain the

following equation of motion for the propagation of the two GW polarizations:

$$\hat{h}_{A}^{\prime\prime} + \left(k^{2} - \frac{a_{\rm GW}^{\prime\prime}}{a_{\rm GW}}\right)\hat{h}_{A} = 0.$$
 (13)

Here, a_{GW} is an effective scale factor given by $a_{GW}(z) = a(z)(M_*(z)/M_P)$, and $\hat{h}_A = a_{GW}h_A$ is the canonically normalized amplitude of GWs. For very small wavelengths, namely, for $k^2 \gg a''_{GW}/a_{GW}$ with $a''_{GW}/a_{GW} = [2\alpha'_M \mathcal{H} + 2\mathcal{H}'(1 + \alpha_M) + \mathcal{H}^2(2 + \alpha_M)^2]/4$,¹ the solution for \hat{h}_A simply is a plane wave with constant amplitude. This means that the original metric perturbation h_A is also a plane wave with a decreasing amplitude due to the factor of $1/a_{GW}$. In GR, the amplitude would simply decay as 1/a, so we can interpret a_{GW} as the effective scale factor felt by GWs due to the combined effects of the background metric and the background's additional degree of freedom. In this case, the present-day observed amplitude h_A^{α} is given by

$$h_A^o = \frac{M_*(z)}{M_*(z=0)} h_{A,\text{GR}}^o \propto \frac{M_*(z)}{M_*(z=0)} \frac{1}{d_L(z)} \equiv \frac{1}{d_{\text{GW}}}, \quad (14)$$

where z is the redshift of the source and $h_{A,GR}^o$ is the expression for the observed amplitude in GR; $h_{A,GR}^o$ decays as $1/d_L$, with

$$d_L = \frac{1+z}{H_0} \int_0^z \frac{d\tilde{z}}{\hat{H}(\tilde{z})}$$
(15)

the luminosity distance. $\hat{H}(z) = H(z)/H_0$ is the normalized Hubble rate, which is explicitly

$$\hat{H}(z) = \sqrt{\Omega_{m,0}(1+z)^3 + \rho_{\rm DE}(z)/\rho_c}.$$
 (16)

We have introduced the fractional energy-density parameter $\Omega = \rho/(3H^2M^2)$, and the critical energy density $\rho_c = 3H_0^2M_P^2$. We have also used the fact that $a = (1 + z)^{-1}$, with a = 1 today.

The omitted proportionality factor in Eq. (14) characterizes the emitted waveform (which is a function of the GW frequency, chirp mass, the effective Newton's constant felt by the compact binary, and the equation of state for neutron stars), and we assume that it is the same as in GR.

We note that Eq. (14) depends only on the value of M_* at the source and observation points, and not on the intermediate evolution. This is because we can only measure the cumulative change in the amplitude compared to GR, which depends exclusively on the initial and final values of M_* . In keeping with the previous section's discussion, we assume that $M_*(z = 0) = M_P$, and that M_* depends only on time. As a consequence, the result depends only on the distance to the source galaxy, not on the properties of the host galaxy itself. Furthermore, we assume that the effective Planck mass evolves in the same way as the cosmological one, and hence it does not depend on whether we are inside a galaxy or not.

In order to make a concrete estimation of the effect of the running Planck mass, we need to assume a specific functional form for M_* . Since we are interested in modified-gravity models of dark energy, a common time parametrization for α_M is [73,79]

$$\alpha_M(z) = c_M \frac{\Omega_{\rm DE}(z)}{\Omega_{\rm DE,0}},\tag{17}$$

where c_M is a free constant parameter and Ω_{DE} is the fractional dark energy density. So far the background has been kept arbitrary, but we now assume it to be given by a fiducial Λ CDM expansion history, and thus from now on we assume that ρ_{DE} is constant, and set $\Omega_{DE,0}$ to the best-fit Planck value [6]. Note that the parametrization in Eq. (17) is not well suited to f(R) models [80], and hence different time evolutions may also be of interest (see, for instance, [66]). In any case, simple parametrizations with a few free constants are sufficient for the time being, as observational data does not have the constraining power to test more complicated functions [81].

This parametrization assumes that there are no modifiedgravity effects at early times, but at late times new degrees of freedom come into play and modify the evolution of the Universe through $\Omega_{\text{DE}}(z)$. Other parametrizations with early-time modifications can also be considered (see, for instance, [79]).

For the specific case of scalar-tensor theories, it is known how α_M affects the effective Newton constant G_{eff} and the effective anisotropic stress γ , and thus cosmological data has been used to constrain c_M to the range $-0.62 < c_M <$ +1.35 at 95% C.L. [45], which means c_M is allowed to be of order unity. Thus, in contrast to constraints on the propagation speed of GWs, this kind of modified-gravity effect is not yet ruled out. Forecasts for this same parametrization were studied in [79], where it was found that the 1σ uncertainties on the parameter c_M may improve by a factor of 5 when taking into consideration future photometric redshift surveys such as LSST [82] and SKA [83], as well as the Stage IV CMB experiment [84].

Regardless of the underlying modified-gravity theory causing α_M , from standard sirens we can also place constraints on c_M by measuring the difference between the luminosity distance and the GW distance. As shown in [38], according to Eq. (14) we have that

$$\frac{d_{\rm GW}}{d_L} = \frac{M_P}{M_*} = \exp\left\{\frac{1}{2}\int_0^z \frac{dz'}{1+z'} \alpha_M(z')\right\},$$
 (18)

¹Note that this condition limits how large α_M can be, and how quickly it can evolve in time. Typically, we will consider evolution over cosmological times, and $\alpha_M \ll k^2/\mathcal{H}^2$.

and for the specific parametrization (17), we explicitly obtain

$$\frac{d_{\rm GW}}{d_L} = \exp\left\{\frac{c_M}{2\Omega_{\rm DE,0}}\ln\frac{1+z}{(\Omega_{m,0}(1+z)^3 + \Omega_{\rm DE,0})^{1/3}}\right\},\qquad(19)$$

where we have used the assumption that ρ_{DE} is constant. This ratio describes the cumulative difference in the GW amplitude in GR compared to that in modified gravity, if the wave had the same emitted amplitude. In order to illustrate the effect of c_M on this ratio, we Taylor expand this expression for low redshifts $z \ll 1$ to find

$$\frac{d_{\rm GW}}{d_L} \approx 1 + \frac{1}{2}c_M z + \frac{1}{8}c_M (c_M - 2 - 6\Omega_{m,0})z^2 + \mathcal{O}(z^3).$$
(20)

From here we explicitly see that if $c_M = 0$, then $d_{\text{GW}}/d_L = 1$, and the leading-order correction is proportional to *z*, hence, no considerable modifications are expected for low-redshift events.

When estimating H_0 from standard sirens, we first obtain d_{GW} from the waveform and the redshift *z* from the EM counterpart. Then, we combine Eqs. (19) and (15) to obtain H_0 . At low redshifts, we have that

$$H_0 = \frac{z}{d_{\rm GW}} + z^2 \frac{[1 - (3/4)\Omega_{m,0} + (1/2)c_M]}{d_{\rm GW}} + \mathcal{O}(z^3),$$
(21)

and thus the estimates of H_0 in GR and modified gravity would differ by a factor $z^2 c_M / (2d_{GW})$ for a given value of d_{GW} . We note that the sign of c_M determines whether the measured H_0 in the modified-gravity model will be larger or smaller than the GR value. In particular, if $c_M < 0$, then c_M contributes with a negative term to H_0 , yielding a smaller H_0 , and vice versa.

Going beyond the low-redshift limit, Fig. 1 shows the evolution of the fractional difference $(d_{\rm GW} - d_L)/d_{\rm GW}$ as a function of $d_{\rm GW}$ for different values of c_M (blue, green, and orange lines), up to a GW distance of 1.5 Gpc. For comparison, the GW distances for BNSs detected by aLIGO at design sensitivity and A+ are expected to follow the distributions in Fig. 2 under the assumptions discussed in Sec. IV. The ratio $(d_{\rm GW} - d_L)/d_{\rm GW}$ illustrates the fractional cumulative difference in the GW amplitude that would be detected in GR compared to that detected in modified gravity, for a source at a given distance with the same emitted amplitude. As expected, the larger the $|c_M|$, the larger the fractional difference between the GW distance and d_L , indicating a larger deviation from GR. We note that for values of $c_M \gtrsim -3$, the ratio flattens out at large distances due to the fact that our α_M in Eq. (17) decreases with redshift (or, equivalently, with distance), and



PHYS. REV. D 99, 083504 (2019)

 $(d_{\rm GW} - d_L) / d_{\rm GW}$ 0.20.0 $c_M = 10$ $c_M = 50$ -0.2GW170817 -0.4aLIGO horizor A+ horizon -0.60.0 0.2 0.4 0.6 0.8 1.0 1.2 1.4 $d_{\rm GW}$ (Gpc) FIG. 1. Fractional change in $d_{\rm GW}$ due to modified-gravity

0.6

0.4

effects as a function of $d_{\rm GW}$, for different values of c_M . Here we have fixed cosmological parameters to the best-fit values from *Planck*. The yellow (pink) region corresponds to the range of $1\sigma \ d_{\rm GW}$ measurement uncertainties for aLIGO (LIGO A+). The sharp cutoff at $\pm 22.5\%$ is due to our assumption that only systems with a single-detector SNR > 8 are detected; lower-SNR systems, if included in the sample, will yield broader $d_{\rm GW}$ measurements (see Sec. IV).

hence the accumulated difference between GR and modified gravity becomes negligible at large distances. The distance at which a given curve starts flattening out depends on the value of c_M and the cosmological parameters. Explicitly, from Eq. (19), we find that the maximum fractional difference is given by

$$\lim_{z \to \infty} \frac{|d_{\rm GW} - d_L|}{d_{\rm GW}} = \left| 1 - \exp\left\{ -\frac{c_M}{2\Omega_{\rm DE,0}} \ln \Omega_{m,0}^{-1/3} \right\} \right|.$$
 (22)

Using best-fit *Planck* cosmological parameters, we find that if $c_M = 1$, for instance, then the maximum fractional difference will be about 32%. However, for sources at aLIGO or LIGO A+ horizons (dotted vertical lines,



FIG. 2. Distance distribution of the BNS events detected by Advanced LIGO at design sensitivity and LIGO A+, assuming 1.4–1.4 M_{\odot} mergers and that the underlying merger rate density follows $\frac{dN}{dV_c dt} \propto (1 + z)^{2.7}$ and *Planck* cosmology.

corresponding to the largest detectable distances in Fig. 1), the fractional difference will be about 4% or 7%, respectively, for $c_M = 1$.

Due to the aforementioned behavior, we conclude that more distant events have a priori more constraining power on c_M than nearby events; however, this effect starts to diminish for events at distances much greater than a few gigaparsecs. We note that the measurement uncertainties in $d_{\rm GW}$ tend to grow with distance, as the signal to noise ratio (SNR) of a GW signal scales inversely with the source distance. The range of expected 1σ uncertainties in the measured GW distance is shown as solid colored regions in Fig. 1: yellow for aLIGO and pink for LIGO A+, under the simplified assumptions discussed in Sec. IV. The boundary closest to zero of each colored region corresponds to the best sources, which produce the optimal SNR and the smallest distance uncertainties, and thus the tightest constraints on c_M . In the above discussion, we assumed that the uncertainty in the EM distance, d_L , is negligible, and that all the uncertainty in the fraction $(d_{\rm GW} - d_L)/d_{\rm GW}$ comes from d_{GW} . Indeed, for a fixed cosmology, the uncertainty on d_L comes exclusively from the peculiar velocity of the source, which is typically around 150-250 km/s at all distances, and therefore for a fixed background cosmology the fractional error of the luminosity distance σ_{d_L}/d_L decreases with distance.

From Fig. 1, we see that in order to distinguish GR from a nonzero c_M , we need to measure d_{GW} to a precision better than the deviation caused by the nonzero value of c_M . For a single event, this is only possible for the most extreme values of c_M , because we will rarely get an event with a 1σ distance uncertainty that is comparable to the deviation caused by $-1 < c_M < 1$. However, by combining a population of events, it will be possible to place tight constraints on c_M , as discussed in Sec. V B. A population of BNS events detected by LIGO A+ is especially promising, because the typical source detected by A+ at a given distance has a much higher SNR, and therefore a smaller relative distance uncertainty, than the typical source detected by aLIGO. However, it becomes less useful to extend the detection horizon much beyond A+, because the effect of nonzero $c_M \sim \mathcal{O}(1)$ starts to saturate at ~1.5 Gpc (additionally, it is increasingly difficult to find counterparts and identify host galaxies for events at high redshift).

Finally, we recall that we have a schematic relationship between d_{GW} and redshift z of the form

$$d_{\rm GW} = d_L(z, H_0, \Omega_{m,0}) R(z, c_M, \Omega_{m,0}), \qquad (23)$$

where *R* is a function corresponding to the ratio of d_{GW}/d_L given on the right-hand side of Eq. (19). It is clear that, given cosmological parameters (H_0 , $\Omega_{m,0}$), we can constrain c_M by measuring d_{GW} and *z*. We emphasize that if the cosmological parameters are fixed by some cosmological data, then the resulting constraint on c_M is not independent

of these cosmological datasets. However, if the cosmological parameters H_0 and $\Omega_{m,0}$ are taken to be free constants, then Eq. (23) can be used to find joint constraints on c_M , H_0 , and $\Omega_{m,0}$ which are completely independent from the cosmological datasets. Note that the constraints would still depend on the cosmological model (assumed to be Λ CDM here), but not on the best-fit values from external data. If $c_M = 0$, then R = 1, and we can use this relationship to find independent constraints on the cosmological parameters, as has been done for H_0 in [24].

While for low-redshift sources $\Omega_{m,0}$ has a negligible effect and the only relevant cosmological parameter is H_0 , for high-redshift sources $\Omega_{m,0}$ does become relevant and must be taken into consideration. For simplicity, in the rest of the paper we will always fix $\Omega_{m,0} = 0.315$, the best-fit value from *Planck* 2018 [6], while keeping H_0 free. In this sense, the constraints that we quote are not fully cosmology independent, although we have checked that if we free $\Omega_{m,0}$ and use a flat prior with a 6σ width around the best-fit *Planck* value, i.e., $0.330 < \Omega_{m,0} < 0.372$, our results are unaffected, as the uncertainty on $\Omega_{m,0}$ is subdominant, affecting the distance-redshift relation to less than 1% over the redshift range of interest ($z \leq 0.1$ for aLIGO and $z \leq$ 0.2 for LIGO A+) for BNSs. For this reason, in the rest of the paper we will focus on the joint constraints for c_M and H_0 only, and these will be referred to as cosmologyindependent constraints. In particular, we will analyze the data from GW170817 as well as forecasts for Advanced LIGO and LIGO A+.

IV. METHOD

In this section, we describe the method used for our standard siren inference of H_0 in the context of a running Planck mass. Throughout the analysis, we fit only for c_M and H_0 , assuming that the other cosmological parameters in the Λ CDM background (namely, Ω_k , Ω_m , and Ω_Λ), collectively denoted by Ξ , are known to a few percent. We note that c_M is not expected to correlate with these other cosmological parameters in their impact on CMB observables [69], and it is therefore self-consistent to fix the background cosmology to the Planck 2018 values while measuring c_M with standard sirens. Allowing these parameters to vary by up to 10% from their best-fit Planck 2018 values has a $\leq 1\%$ effect on the distance-redshift relation over the detectable redshift range, and so even if the current measurement errors were several times larger, marginalizing over the extra uncertainty would have a negligible impact on our results. Within the current Planck 2018 uncertainties, the distance-redshift relation only varies by <0.05% over the detectable redshift range. In the future, however, especially if standard sirens with counterparts are detectable to much higher redshifts z > 1 by, e.g., LISA, one could carry out a joint CMB-standard siren analysis that would incorporate all cosmological parameters.

PHYS. REV. D 99, 083504 (2019)

GW measurements: We assume that the GW measurement uncertainty of distance scales as $1.8/\rho$ (at 1σ) where ρ is the single-detector SNR of the source. We assume a threshold SNR of $\rho_{\rm th} = 8$ for detection. From Fisher matrix arguments, we expect the GW distance to scale inversely with the SNR, with the proportionality factor >1 because of the distance-inclination degeneracy [85]. We choose the 1σ uncertainty of $1.8/\rho$ to match the expected H_0 convergence rate of $(13\%-15\%)/\sqrt{N}$, where N is the number of GW detections [30]. For simplicity, when simulating a mock population of sources, we assume that the GW distance likelihood is approximated by a Gaussian distribution:

$$p(d_{\rm GW}^{\rm obs}|d_{\rm GW}) = N_{[\mu=d_{\rm GW},\sigma=1.8/\rho]}(d_{\rm GW}^{\rm obs}),$$
 (24)

where $N_{[\mu,\sigma]}$ denotes the standard normal distribution with mean μ and standard deviation σ . While this is not a realistic approximation for individual sources, when combining tens to hundreds of detections, it yields the expected convergence rate for the recovered cosmological parameters.

Likelihood: We denote the GW data by x_{GW} and the EM data by x_{EM} . The likelihood of the GW data depends on the source's GW distance d_{GW} , sky position ω , inclination ι , and all other parameters of the signal, including its redshift z (which affects the frequency of the waveform), and the source-frame masses, spins, etc., which we collectively denote by ξ . The likelihood given the extrinsic parameters (sky localization and inclination) is largely independent of the intrinsic parameters [86,87], and we marginalize over these other parameters to get the GW likelihood given its distance and sky position:

$$p(x_{\rm GW}|d_{\rm GW},\omega) = \int p(x_{\rm GW}|d_{\rm GW},\omega,\iota,z,\xi) d\iota dz d\xi.$$
(25)

Meanwhile, the likelihood of the EM data depends on the host galaxy's sky position and luminosity distance, which is related to its cosmological redshift (the redshift it would have if it were in the Hubble flow, corrected for any peculiar velocities) by the standard ACDM relation.

We put a prior $p(z, \omega)$ on the redshifts and sky positions of the host galaxies. We choose this prior to match a merger rate density that is isotropic and roughly follows the starformation rate (see the Appendix). To avoid a biased measurement of the cosmological parameters, this prior must match the true redshift distribution of the host galaxies; however, we find that any likely deviation from a uniform merger rate density, including a merger rate that traces the star-formation rate, is too small to cause a noticeable bias. Similarly, deviations from an isotropic distribution of sources on the sky (e.g., due to large-scale structure) are largely irrelevant to this analysis unless there are significant correlations between the underlying distribution of sources on the sky and the antenna power patterns of the detectors. Moreover, a significant deviation from the assumed merger rate density will be easily detectable with hundreds of host galaxies with well-measured redshifts and sky positions, and can be used to update our prior accordingly.

The relationship between d_L and d_{GW} is given in Eq. (19), where d_L is given by z, H_0 , and the standard Λ CDM parameters Ξ . We denote the function that returns d_{GW} given z, H_0 , c_M , and Ξ by \hat{d}_{GW} .

The likelihood for the data given c_M and H_0 is

$$p(x_{\rm GW}, x_{\rm EM}|c_M, H_0) = \frac{\int p(x_{\rm GW}|d_{\rm GW} = \hat{d}_{\rm GW}(z, c_M, H_0, \Xi), \omega) p(x_{\rm EM}|z, \omega) p(z, \omega) p(\Xi) dz d\omega d\Xi}{\beta(H_0, c_M)},$$
(26)

where $\beta(H_0, c_M)$ ensures that the likelihood integrates to unity over detectable datasets, and accounts for selection effects in the GW detection and measurement process (see the Appendix).

We take $p(\Xi)$ to be the posterior on these parameters from *Planck* 2018, although, as noted earlier, we can approximate these as being measured exactly and given by a δ function centered on their mean values. We also assume that the sky position is measured exactly, and that the redshift uncertainty is small (i.e., spectroscopic redshifts, so that the only significant source of uncertainty in the cosmological redshift is in the peculiar velocity correction, typically around 200 km/s [88]). For a population where the majority of detected sources are at redshifts $z \gtrsim 0.05$ and the redshift uncertainty is subdominant to the d_{GW} uncertainty, we can therefore approximate the EM likelihood term, $p(x_{\rm EM}|z, \omega)$ by a δ function centered at the true redshift and sky position:

$$p(x_{\rm EM}|z,\omega) = \delta(z - z_{\rm obs})\delta(\omega - \omega_{\rm obs}).$$
(27)

When analyzing GW170817, a very nearby event at redshift $z \sim 0.01$, we include the peculiar velocity uncertainty in the calculations, taking the EM likelihood to be

$$p(x_{\rm EM}|z,\omega) = N_{[\mu=z,\sigma=\sigma_z]}(z_{\rm obs})\delta(\omega-\omega_{\rm obs}), \quad (28)$$

where $z_{\rm obs}$ is the observed, peculiar-velocity corrected redshift, σ_z is the uncertainty, and $\omega_{\rm obs}$ is the observed sky position. For this analysis, we also choose priors that match the default priors in [24]: $p(d_{\rm GW}) \propto d_{\rm GW}^2$ and $p(H_0) \propto 1/H_0$.

V. RESULTS

In this section we analyze the one BNS detection so far, GW170817, as well as a simulated population of BNSs detected by aLIGO at design and A+ sensitivities. In each case, we present joint constraints on c_M and H_0 and highlight the correlations between them. Section VA discusses constraints from the single event GW170817, detected at $d_{GW} \sim 40$ Mpc. Then, in Sec. V B we discuss forecast constraints from populations of standard sirens detected with design-sensitivity LIGO and A+.

A. Single event

In this section we study joint constraints on c_M and H_0 from a single multimessenger signal. We start by considering GW170817, which has a measured² GW distance of $d_{GW} = 41^{+4}_{-7}$ Mpc and a "Hubble" velocity of $v_H =$ 3017 ± 166 km/s [24]. Combining the GW distance samples with the redshift of the host galaxy, we can calculate the joint posterior on H_0 and c_M . If we assume an H_0 prior given by *Planck* (2018) [25], we find $c_M = -9^{+21}_{-28}$ (68.3% credible interval); alternatively, taking a H_0 prior given by *SHoES* (2018) [26] gives $c_M = 8^{+21}_{-30}$. The c_M posterior under each assumption is shown in Fig. 3. The 95% credible interval under the *Planck* (*SHoES*) H_0 prior is $c_M = -9^{+37}_{-72}$ ($c_M = 8^{+39}_{-74}$).

We see that even though this event had a high SNR of 32.4, since it was very close by (~40 Mpc), the constraints on c_M are very broad. As Fig. 1 shows, at 40 Mpc, a large range of c_M values would produce GW distances that are consistent with the ~15% distance uncertainty from GW170817. As a comparison, we mention that constraints on c_M have been obtained for scalar-tensor theories from cosmological data, where it was found that $-0.62 < c_M < +1.35$ at 95% C.L. [45]. Therefore, current GW constraints allow for c_M of $\mathcal{O}(10)$, whereas cosmological data require c_M of $\mathcal{O}(1)$.

However, future detector networks with improved sensitivity, such as A+, will detect events out to much higher distances with comparable measurement uncertainties. For example, a single event detected by A+ at $d_{\rm GW} = 400$ Mpc with a 1σ distance uncertainty of 15% would constrain $-4 < c_M < 4$ for a true $c_M = 0$, assuming the *Planck* H_0 measurement as a prior.

We can also obtain constraints on c_M independently of other datasets by using an uninformative prior on H_0 . In this case, we find a strong positive correlation between c_M and H_0 , as shown in Fig. 4. This correlation arises because a given pair (z, d_{GW}) can also be achieved in a universe where H_0 is larger (and hence the source is closer) but the friction term c_M is correspondingly larger too (and hence the amount of amplitude decay during its travel is larger).



FIG. 3. Posterior probability of c_M from the multimessenger detection of GW170817, with an H_0 prior given by the *Planck* (2018) measurement (blue) and the *SHoES* (2018) measurement (green).

Equivalently, the same data could also be fitted by a universe with a smaller H_0 and a smaller c_M .

The posterior probability of H_0 , with c_M marginalized over a flat prior in the range $c_M \in [-150, 150]$ and a flat-inlog prior on H_0 , is shown in Fig. 5. In this case, the constraints become $H_0 = 76^{+53}_{-28}$ km/s/Mpc (68.3% highest density posterior interval). As a comparison, we also show the constraint on H_0 found by marginalizing over a narrow c_M prior, $-2 < c_M < 2$, and assuming $c_M = 0$. In both of these cases, we find $H_0 = 70^{+13}_{-7}$ km/s/Mpc, in agreement with [89]. In this case, we find that for this one event the uncertainties on H_0 grow by a factor of > 2when marginalizing over a very broad prior on c_M , but are unaffected by a more reasonable prior $-2 < c_M < 2$.



FIG. 4. Joint posterior probability of c_M and H_0 from GW170817, for a flat prior $-150 < c_M < 150$ and a flat-inlog prior in the range $10 < H_0 < 250$ km/s/Mpc. The black and green contours indicate 90% and 50% credibility levels, respectively.

²We use the publicly available posterior samples released with [89] and available at http://dcc.ligo.org/LIGO-P1800061/public.



FIG. 5. Posterior probability of H_0 from GW170817, marginalizing over a wide, flat prior on $c_M \in [-150, 150]$ (solid blue line), a narrow prior on $c_M \in [-2, 2]$, and constant $c_M = 0$ (dashed line; corresponding to GR).

B. Population

We now consider a population of BNS events detected by aLIGO at design and A+ sensitivities, with EM counterparts that allow us to identify unique redshifts of the host galaxies. As the GW network sensitivity reaches design sensitivity for aLIGO and later upgrades to A+, a GW event at a given distance will be detected with higher SNR and yield a better-constrained $d_{\rm GW}$ measurement, meaning that although GW170817 is only sensitive to $c_M \sim \mathcal{O}(50)$, a single event detected by aLIGO at design (A+) sensitivity will typically constrain c_M to a 1σ width of $\lesssim 10 \ (\lesssim 5)$. In Fig. 6 we show the joint and marginalized constraints on c_M and H_0 for a simulated population of 250 BNSs detected by aLIGO, where the injected values are $c_M = 0$ and $H_0 = 67.4 \text{ km/s/Mpc}$ (indicated by solid black lines). We assume flat priors on both c_M and H_0 .

The bottom left panel shows the joint posterior probability on c_M and H_0 , with the contours indicating 90% and 50% credibility levels. As expected, there is a positive correlation between H_0 and c_M , which leads to a broader recovered posterior on H_0 when marginalizing over c_M , as opposed to fixing $c_M = 0$ (the correct value in this case). This is shown in the top left panel. When fixing $c_M = 0$, the 1σ constraints on H_0 scale roughly as $(13\%-15\%)/\sqrt{N}$ (for aLIGO and A+), giving a 1σ interval of 0.6 for 250 events (green dotted line); however, when marginalizing over a completely uninformative prior on c_M , the same number of events yields a 1σ interval that is twice as broad



FIG. 6. Joint and marginalized posterior probabilities of c_M and H_0 (solid blue lines) for 250 mock BNS mergers detected by aLIGO at design sensitivity, with true values of H_0 and c_M indicated with solid black lines. The contours in the bottom left panel denote 90% and 50% confidence levels. In the top left panel we also show the posterior probability of H_0 when fixing $c_M = 0$ with a green dotted line. In the bottom right panel we show the posterior probability of c_M when $H_0 = 67.4 \pm 0.5$ km/s/Mpc (*Planck* 2018).

(solid blue line). This implies that with no external knowledge of c_M , it would take 4 times as many events to reach the same precision in the standard siren H_0 measurement, or around 200 events to reach 2% as opposed to only ~50 events if fixing $c_M = 0$ [30].

Meanwhile, the bottom right panel shows the posterior probability of c_M when marginalizing over H_0 with a flat, broad prior (solid blue line), as well as when fixing the H_0 prior to the *Planck* (2018) posterior (green dotted line). In the former case, taking the *Planck* H_0 measurement as a prior, this realization gives $c_M = 0.16^{+0.58}_{-0.60}$ (68.3% credible interval), whereas the latter case, which assumes no external measurement of H_0 , gives $c_M = 0.35^{+1.08}_{-1.10}$. Including an external constraint on H_0 reduces the uncertainties on c_M by almost a factor of 2.

Although Fig. 6 shows only a single realization of 250 simulated BNSs detected by design-sensitivity aLIGO, we find that the expected constraints on c_M and H_0 and the $1/\sqrt{N}$ scalings are typical across many realizations for aLIGO. Generically, for aLIGO, we find constraints on c_M with a 1σ width that scale roughly as $\sim 9.3/\sqrt{N}$ for an informative H_0 prior, and $\sim 16/\sqrt{N}$ for a flat H_0 prior. In particular, with 100 BNS events detected by aLIGO, assuming that H_0 is obtained

from external information (such as from the cosmic microwave background), we would find that $|c_M| \leq 0.9$. This number is comparable to the current constraints for scalartensor theories obtained from cosmological observations [45]. Similarly, with A+ sensitivity, we find that the same number of events yields constraints on c_M that are tighter by a factor of 2, constraining c_M with a 1σ width that scales roughly as $\sim 4.7/\sqrt{N}$ for an informative H_0 prior, and $\sim 9.5/\sqrt{N}$ for a flat H_0 prior. In this case, we find that 100 BNS events would allow us to get a limit $|c_M| \leq 0.5$ when assuming H_0 is known.

For the previous example, we chose the true $c_M = 0$ (i.e., assumed that GWs propagate as predicted by general relativity), and so by fitting a model with an uninformative prior for c_M and H_0 , we recovered the true values with a larger uncertainty than if we had assumed GR and fixed $c_M = 0$. However, if the true $c_M \neq 0$ but GR is assumed in the usual standard siren analysis, we will recover a biased H_0 measurement. Due to the previously shown positive correlation between H_0 and c_M , if the true $c_M > 0$, the H_0 measurement will be biased to low values if falsely assuming $c_M = 0$, and if $c_M < 0$, the H_0 measurement will be biased to large values. As an example, Fig. 7 shows



FIG. 7. Joint and marginalized posterior probabilities of c_M and H_0 (solid blue lines) for 100 mock BNS mergers detected by LIGO A+, with true values of H_0 and c_M indicated with solid black lines. The contours in the bottom left panel denote 90% and 50% confidence levels. In the top left panel we also show the posterior probability of H_0 when $c_M = 0$ with a green dotted line. In the bottom right panel we show the posterior probability of H_0 when $c_M = 0$ with a green dotted line. In the bottom right panel we show the posterior probability of r_M when taking the informative prior $H_0 = 67.4 \pm 0.5$ km/s/Mpc (*Planck* 2018).

the joint and marginalized constraints on c_M and H_0 for a simulation in which we injected $c_M = 1.35$. We emphasize that this value of c_M is currently allowed within the 95% confidence interval inferred by [45] for scalar-tensor theories of gravity. For this simulation, we take 100 mock BNS events detected by LIGO A+.

As in the previous figure, in the bottom left panel we show the joint posterior probability, where the contours indicate 50% and 90% levels. The bottom right panel shows the posterior probability of c_M marginalizing over an uninformative prior on H_0 (solid blue line), as well as when adopting the *Planck* (2018) measurement as the prior on H_0 (green dotted line). In the former case, it is found that $c_M = 1.3 \pm 0.8$ (68.3% credible interval), whereas in the latter case $c_M = 1.5 \pm 0.5$.

In the top left panel, we see that the posterior probability of H_0 is significantly biased away from its true value if we falsely assume $c_M = 0$ (green dotted line). If we properly marginalize over a flat c_M prior, we find $H_0 = 66.9^{+1.6}_{-1.5}$ km/s/Mpc, whereas fixing $c_M = 0$ gives $H_0 = 64.8^{+0.8}_{-0.8}$ km/s/Mpc. In the latter case, the true H_0 is outside the 99% credible interval. In other words, incorrectly assuming $c_M = 0$ yields an H_0 measurement that is biased by more than 3σ with only 100 events detected by A+. In general, if the true value is positive ($c_M > 0$) and we fit a model with $c_M = 0$, we bias H_0 towards lower values than the true one. Conversely, if the true value is negative ($c_M < 0$), we bias H_0 towards higher values.

VI. DISCUSSION

In this paper we describe a modification to GR which impacts the propagation of GWs. This extension corresponds to a possible running of the Planck mass, which we describe with one free parameter c_M , where $c_M = 0$ represents GR with a constant Planck mass. This modification affects the friction of GW amplitudes when they propagate through a homogeneous and isotropic universe, and also affects the evolution of matter perturbations in different ways depending on the theory of interest. Here we focus on GW standard siren measurements, studying how a $c_M \neq 0$ modification is degenerate with the value of the local Hubble expansion rate, H_0 . We also explore the ability to constrain both these quantities with future standard siren events detected by LIGO at design and A+ sensitivities.

Studying the event GW170817, we find that if we include external cosmological data, namely, the *Planck* 2018 H_0 posterior, then we find $-81 < c_M < 28$ at 95% credibility. This constraint is very weak compared to existing constraints from cosmological data when a specific modified-gravity theory is considered. Since c_M affects matter perturbations, it leaves potentially detectable imprints on CMB and structure formation. For Horndeski theories, current cosmological constraints give

 $-0.62 < c_M < +1.35$ at 95% C.L. [45]. Hence, current GW constraints allow for c_M of $\mathcal{O}(10)$, whereas cosmological data require c_M of $\mathcal{O}(1)$. On the other hand, for cosmology-independent results, we find that c_M and H_0 are highly degenerate, and constraints on H_0 are degraded from $H_0 = 70^{+12}_{-8} \text{ km/s/Mpc}$ (when $c_M = 0$, that is, when GR is assumed to be correct) to $H_0 = 76^{+53}_{-28} \text{ km/s/Mpc}$ (when marginalizing over a very broad c_M prior, $-150 < c_M < 150$).

In addition, we consider populations of events and discuss future forecasts for standard sirens with aLIGO and LIGO A+. We find that 100 BNSs detected by A+ with identified EM counterparts can lead to cosmologyindependent constraints on H_0 with an accuracy of ~3%, and on c_M with $\sigma(c_M) \sim 0.9$ (or $\sigma(c_M) \sim 1.6$ with 100 aLIGO detections). From these results we estimate the need for 400 detections in order to obtain a $\sim 1\%$ constraint on H_0 , or 4 times what is required if c_M is known exactly to be zero. Furthermore, we find that H_0 and c_M are highly degenerate, which highlights the importance of testing for the parameter c_M to avoid biasing the inferred value of H_0 by wrongly assuming GR. In particular, we show that if we have a population of 100 events with $c_M = 1.35$, then the inferred H_0 , assuming $c_M = 0$, will be > 3σ below the true value. In this case, the actual H_0 of the population may be ruled out at more than 99% confidence due to the incorrect assumption that $c_M = 0$. This result emphasizes the importance of testing the minimal assumptions of one's models. Finding a bias of this magnitude could help arbitrate the current discrepancy between local and cosmological H_0 constraints.

It is important to discuss some caveats of our results and calculations. In general, all population results depend on the time evolution of the background, assumed to be Λ CDM here. They also depend on the specific values of the cosmological parameters considered, and in some cases we also assumed H_0 to be fixed. One possible extension to the analysis made in this paper could involve a change in the background, e.g., changing Λ (w = -1) to a more general form of dark energy, $w_{\text{DE}} = w_0 + w_a(1 - a)$.

In addition, the numbers quoted here also depend on the parametrization adopted for $\alpha_M(t)$, which means that even if these constraints are found to be in tension with future measurements, we cannot conclude that all models with nonzero α_T are disfavored, but rather that the specific time behavior assumed here, $\alpha_M(t) = c_M \frac{\Omega_{\text{DE}}(z)}{\Omega_{\text{DE},0}}$, is disfavored. This is why alternative parametrizations, such as the ones considered in [45], must also be tested.

Furthermore, we have made the crucial assumption that the GW emission of the BNS source is the same in GR as in the modified-gravity theory. One typically justifies this by arguing that some compact object solutions, such as those for black holes, are exactly the same as the solutions in GR. However, as shown in [78], even if the stationary solutions in the strong-field regime of modified gravity look the same as in GR, the emission of GWs in dynamical environments can still differ. Another argument is that the extra gravitational field may be suppressed due to a screening mechanism in the intermediate and high-energy regimes. However, even if this is true, one should check that the suppressed effects are negligible given LIGO's current measurement uncertainty. To date, GR waveforms have been found to describe all detected compact binary GWs. Nonetheless, it would be interesting to have analytical or numerical calculations (for instance, for Horndeski theories) that allow us to estimate the size of modified-gravity effects in the waveform, and determine whether they can be seen with LIGO A+ or next-generation detectors.

Finally, we highlight that given the current constraints on the propagation speed of gravitational waves $|c_T/c - 1| \leq 10^{-15}$, a constraint on α_M would have a large impact on modified-gravity theories, as this is the only possible effect that could be detected with GW data for second-orderderivative scalar-tensor theories, and the only remaining nontrivial extension to GR that can be achieved in this case. For the model in Eq. (8), a constraint pointing to $\alpha_M \approx 0$ (i.e., no modification to GW propagation) would disallow all scalar-tensor interactions but those given by

$$S_s = \int d^4x \sqrt{-g} [R + K(X,\phi) - G_3(X,\phi)\Box\phi]. \quad (29)$$

In the subhorizon regime, these models always give $\gamma = 1$, as well as $G_{\text{eff}} = G_N$ for structure formation when the coupling term G_3 is sufficiently small, and hence modified gravity would only affect scales near the cosmological horizon.

ACKNOWLEDGMENTS

We would like to thank Ignacy Sawicki for useful discussions during the development of this work. M. L., M. F., P. L., and D. E. H. are supported by the Kavli Institute for Cosmological Physics at the University of Chicago through an endowment from the Kavli Foundation and its founder, Fred Kavli. M. F. was also supported by the NSF Graduate Research Fellowship Program under Grant No. DGE-1746045. P. L. was supported in part by the Natural Sciences and Engineering Research Council of Canada, and by NSF Grant No. PHY-1505124. M. F., P. L., and D. E. H. were supported by NSF Grant No. PHY-1708081.

APPENDIX: STATISTICAL FORMALISM

In this Appendix, we give additional details regarding the statistical formalism summarized in Sec. IV. In order to arrive at the likelihood [Eq. (26)] for a given EM and GW dataset given values of c_M and H_0 , we follow the formalism of [24,30,90,91] for incorporating measurement uncertainty and selection effects.

In the likelihood equation (26), we include a term $\beta(H_0, c_M)$ to account for selection effects in the measurement process. This term is given by the integral of the numerator over all detectable EM and GW datasets [91]:

$$\beta(c_M, H_0) = \int_{x_{\rm GW} > x_{\rm GW}^{\rm thresh}, x_{\rm EM} > x_{\rm EM}^{\rm thresh}} p(x_{\rm GW} | d_{\rm GW}$$
$$= \hat{d}_{\rm GW}(z, c_M, H_0, \Xi), \omega) p(x_{\rm EM} | z, \omega)$$
$$\times p(z, \omega) p(\Xi) dz d\omega d\Xi dx_{\rm GW} dx_{\rm EM}, \qquad (A1)$$

where we assume that a given EM or GW dataset is detected if and only if it is above certain threshold. In reality, the detectability of an EM counterpart to a GW event may depend on details such as the inclination, masses, and apparent magnitude of the source, but for simplicity we assume that all BNS mergers detected in GWs will have an observed EM counterpart and an identified host galaxy. If such counterparts are similar to the kilonova associated with GW170817, their detection is certainly feasible with current telescopes for aLIGO sources (which will be at redshifts $z \leq 0.1$), and with future telescopes such as LSST for higher-redshift A+ sources [30]. We therefore assume that the integral over $x_{\rm EM}$ is independent of the other terms, and ignore it. However, if it becomes the case with future detections that only a subset of GW BNS events have identified host galaxies, this term must be modeled and incorporated into the likelihood.

For the GW selection effects, we assume that a BNS is detected if it produces a single-detector SNR $\rho > 8$. When a real population of BNSs is detected in GWs, this assumption can be easily modified to consider the network SNR, or calibrated to injection campaigns in real data [92]. As in [30], we define

$$P_{\rm det}(d_{\rm GW}) \equiv \int_{x_{\rm GW} > x_{\rm GW}^{\rm thresh}} p(x_{\rm GW}|d_{\rm GW},\omega) p(\omega) d\omega dx_{\rm GW}.$$
(A2)

(Recall that our assumed prior $p(z, \omega)$ is separable, $p(z, \omega) = p(z)p(\omega)$.) We evaluate the term $P_{det}(d_{GW})$ with the procedure described in [30]. In particular, we make the simplifying assumptions that the detectability of a GW waveform is independent of its redshift, which affects the observed frequency and therefore the SNR of the source, but only by a negligible amount for the redshifts $z \leq 0.2$ considered here. We assume that all BNS sources are nonspinning (the dimensionless spin is expected to be very small, a < 0.05, for BNS sources) and 1.4–1.4 M_{\odot} in mass. The mass distribution will, in general, affect the term $P_{det}(d_{GW})$, since the SNR of a GW source is a strong function of the binary's mass. However, to leading order the SNR depends only on the chirp mass, and so the term $P_{det}(d_{GW})$ depends only on the underlying distribution of BNS chirp masses. The chirp mass of each source is measured extremely well, and so with $\mathcal{O}(100)$ sources, the distribution of chirp masses will be accurately determined and can be used to update the function $P_{det}(d_{GW})$ used in standard siren analyses. Note that we also assume that any running of the Planck mass (nonzero c_M) only affects the amplitude of the signal and not the frequency evolution of the waveform; otherwise, the recovered masses would be affected.

We therefore have that the $\beta(c_M, H_0)$ term in the likelihood is given by

$$\beta(c_M, H_0) = \int P_{\text{det}}(d_{\text{GW}} = \hat{d}_{\text{GW}}(z, c_M, H_0, \Xi))$$
$$\times p(z)p(\Xi)dzd\omega d\Xi.$$
(A3)

The prior on the redshift of the source, p(z), enters into this equation. In general, to avoid a biased measurement, the prior p(z) must match the true redshift distribution.

[1] C. M. Will, Living Rev. Relativity 17, 4 (2014).

- [2] E. Berti *et al.*, Classical Quantum Gravity **32**, 243001 (2015).
- [3] P. S. Joshi and D. Malafarina, Int. J. Mod. Phys. D 20, 2641 (2011).
- [4] G. 't Hooft and M. J. G. Veltman, Ann. Inst. Henri Poincaré, A 20, 69 (1974).
- [5] S. Deser, Ann. Phys. (Berlin) 9, 299 (2000).
- [6] N. Aghanim *et al.* (Planck Collaboration), arXiv:1807 .06209.
- [7] T. Clifton, P. G. Ferreira, A. Padilla, and C. Skordis, Phys. Rep. 513, 1 (2012).
- [8] K. Koyama, Rep. Prog. Phys. 79, 046902 (2016).
- [9] A. Joyce, B. Jain, J. Khoury, and M. Trodden, Phys. Rep. 568, 1 (2015).
- [10] J.-J. Wei, Astrophys. J. 868, 29 (2018).
- [11] J.-J. Wei and X.-F. Wu, Mon. Not. R. Astron. Soc. 472, 2906 (2017).
- [12] T. Baker and M. Trodden, Phys. Rev. D 95, 063512 (2017).
- [13] T. E. Collett and D. Bacon, Phys. Rev. Lett. 118, 091101 (2017).
- [14] B. P. Abbott *et al.* (LIGO Scientific and Virgo Collaborations), Phys. Rev. Lett. **119**, 161101 (2017).
- [15] J. Aasi, B. P. Abbott, R. Abbott, T. Abbott, M. R. Abernathy, K. Ackley, C. Adams, T. Adams, P. Addesso *et al.*, Classical Quantum Gravity **32**, 074001 (2015).
- [16] F. Acernese, M. Agathos, K. Agatsuma, D. Aisa, N. Allemandou, A. Allocca, J. Amarni, P. Astone, G. Balestri, G. Ballardin *et al.*, Classical Quantum Gravity **32**, 024001 (2015).
- [17] A. Goldstein et al., Astrophys. J. Lett. 848, L14 (2017).

In our simulations, we assume that the underlying redshift distribution matches a merger rate that roughly traces the low-redshift star-formation rate:

$$p(z) = \frac{dV_c}{dz} \frac{1}{1+z} (1+z)^{2.7},$$
 (A4)

where V_c is the comoving volume, $(1 + z)^{2.7}$ approximates the Madau-Dickinson star-formation rate [93] at low redshift and the factor of $\frac{1}{1+z}$ accounts for difference in clocks between the source frame and the detector frame. In reality, for the redshifts considered here, $z \leq 0.2$, any reasonable redshift distribution, including one that traces the starformation rate, is a very small deviation from the uniformin-comoving volume and source-frame time redshift distribution, and is unlikely to significantly affect the results. Furthermore, the true redshift distribution will be accurately measured given a precise redshift measurement of each identified host galaxy, and can be used to update the prior p(z).

- [18] V. Savchenko et al., Astrophys. J. Lett. 848, L15 (2017).
- [19] T. Baker, E. Bellini, P. G. Ferreira, M. Lagos, J. Noller, and I. Sawicki, Phys. Rev. Lett. **119**, 251301 (2017).
- [20] P. Creminelli and F. Vernizzi, Phys. Rev. Lett. 119, 251302 (2017).
- [21] J. Sakstein and B. Jain, Phys. Rev. Lett. 119, 251303 (2017).
- [22] J. M. Ezquiaga and M. Zumalacárregui, Phys. Rev. Lett. 119, 251304 (2017).
- [23] H. Wang et al., Astrophys. J. 851, L18 (2017).
- [24] B. P. Abbott *et al.* (LIGO Scientific, VINROUGE, Las Cumbres Observatory, DES, DLT40, Virgo, 1M2H, Dark Energy Camera GW-E, and MASTER Collaborations), Nature (London) 551, 82 (2017).
- [25] J. Tauber *et al.* (Planck Collaboration), arXiv:astro-ph/ 0604069.
- [26] A. Riess, HST Proposal No. 10802, 2006.
- [27] A. G. Riess, S. Casertano, W. Yuan, L. Macri, J. Anderson, J. W. MacKenty, J. B. Bowers, K. I. Clubb, A. V. Filippenko, D. O. Jones, and B. E. Tucker, Astrophys. J. 855, 136 (2018).
- [28] B. F. Schutz, Nature (London) 323, 310 (1986).
- [29] D. E. Holz and S. A. Hughes, Astrophys. J. 629, 15 (2005).
- [30] H.-Y. Chen, M. Fishbach, and D. E. Holz, Nature (London) 562, 545 (2018).
- [31] S. Nissanke, D. E. Holz, N. Dalal, S. A. Hughes, J. L. Sievers, and C. M. Hirata, arXiv:1307.2638.
- [32] S. M. Feeney, H. V. Peiris, A. R. Williamson, S. M. Nissanke, D. J. Mortlock, J. Alsing, and D. Scolnic, Phys. Rev. Lett. **122**, 061105 (2019).
- [33] Y. Aso, Y. Michimura, K. Somiya, M. Ando, O. Miyakawa, T. Sekiguchi, D. Tatsumi, and H. Yamamoto, Phys. Rev. D 88, 043007 (2013).

- [34] B. Iyer, T. Souradeep, C. S. Unnikrishnan, S. Dhurandhar, S. Raja, and A. Sengupta, LIGO Report No. M1100296-v2, 2011.
- [35] D. McClelland, M. Evans, B. Lantz, I. Martin, V. Quetschke, and R. Schnabel, LIGO Report No. T1500290-v3, 2015.
- [36] B. P. Abbott *et al.* (LIGO Scientific and Virgo Collaborations), arXiv:1811.12907.
- [37] J. M. Ezquiaga and M. Zumalácarregui, Front. Astron. Space Sci. 5, 44 (2018).
- [38] E. Belgacem, Y. Dirian, S. Foffa, and M. Maggiore, Phys. Rev. D 98, 023510 (2018).
- [39] J.-P. Uzan, Living Rev. Relativity 14, 2 (2011).
- [40] V. Pettorino and L. Amendola, Phys. Lett. B 742, 353 (2015).
- [41] A. Nishizawa, Phys. Rev. D 97, 104037 (2018).
- [42] S. Arai and A. Nishizawa, Phys. Rev. D 97, 104038 (2018).
- [43] L. Amendola, I. Sawicki, M. Kunz, and I.D. Saltas, J. Cosmol. Astropart. Phys. 08 (2018) 030.
- [44] E. V. Linder, J. Cosmol. Astropart. Phys. 03 (2018) 005.
- [45] J. Noller and A. Nicola, arXiv:1811.12928.
- [46] C. de Rham, G. Gabadadze, and A. J. Tolley, Phys. Rev. Lett. 106, 231101 (2011).
- [47] C. de Rham and G. Gabadadze, Phys. Rev. D 82, 044020 (2010).
- [48] S. Hassan and R. A. Rosen, J. High Energy Phys. 02 (2012) 126.
- [49] K. Max, M. Platscher, and J. Smirnov, Phys. Rev. Lett. 119, 111101 (2017).
- [50] K. Max, M. Platscher, and J. Smirnov, Phys. Rev. D 97, 064009 (2018).
- [51] J. Beltran Jimenez and L. Heisenberg, J. Cosmol. Astropart. Phys. 09 (2018) 035.
- [52] G. W. Horndeski, Int. J. Theor. Phys. 10, 363 (1974).
- [53] C. Deffayet, X. Gao, D. A. Steer, and G. Zahariade, Phys. Rev. D 84, 064039 (2011).
- [54] J. Gleyzes, D. Langlois, F. Piazza, and F. Vernizzi, Phys. Rev. Lett. **114**, 211101 (2015).
- [55] M. Zumalacarregui and J. Garcia-Bellido, Phys. Rev. D 89, 064046 (2014).
- [56] D. Langlois and K. Noui, J. Cosmol. Astropart. Phys. 02 (2016) 034.
- [57] M. Crisostomi, K. Koyama, and G. Tasinato, J. Cosmol. Astropart. Phys. 04 (2016) 044.
- [58] J. B. Achour, D. Langlois, and K. Noui, Phys. Rev. D 93, 124005 (2016).
- [59] R. Kase and S. Tsujikawa, arXiv:1809.08735.
- [60] D. Langlois, arXiv:1811.06271.
- [61] T. Kobayashi, arXiv:1901.07183.
- [62] L. Heisenberg, J. Cosmol. Astropart. Phys. 05 (2014) 015.
- [63] T. Jacobson and D. Mattingly, Phys. Rev. D 64, 024028 (2001).
- [64] T. G. Zlosnik, P. G. Ferreira, and G. D. Starkman, Phys. Rev. D 74, 044037 (2006).

- [65] L. Heisenberg, R. Kase, and S. Tsujikawa, Phys. Rev. D 98, 024038 (2018).
- [66] C. D. Kreisch and E. Komatsu, J. Cosmol. Astropart. Phys. 12 (2018) 030.
- [67] P. A. R. Ade *et al.* (Planck Collaboration), Astron. Astrophys. 580, A22 (2015).
- [68] P. A. R. Ade *et al.* (Planck Collaboration), Astron. Astrophys. **594**, A14 (2016).
- [69] Z. Huang, Phys. Rev. D 93, 043538 (2016).
- [70] C. J. Copi, A. N. Davis, and L. M. Krauss, Phys. Rev. Lett. 92, 171301 (2004).
- [71] E. Bellini and I. Sawicki, J. Cosmol. Astropart. Phys. 07 (2014) 050.
- [72] M. Lagos, E. Bellini, J. Noller, P. G. Ferreira, and T. Baker, J. Cosmol. Astropart. Phys. 03 (2018) 021.
- [73] E. Bellini, A. J. Cuesta, R. Jimenez, and L. Verde, J. Cosmol. Astropart. Phys. 02 (2016) 053; 06 (2016) E01.
- [74] J. G. Williams, S. G. Turyshev, and D. H. Boggs, Phys. Rev. Lett. 93, 261101 (2004).
- [75] R. W. Hellings, P. J. Adams, J. D. Anderson, M. S. Keesey, E. L. Lau, E. M. Standish, V. M. Canuto, and I. Goldman, Phys. Rev. Lett. 51, 1609 (1983).
- [76] A. Bonanno and H.-E. Froehlich, arXiv:1707.01866.
- [77] B. Jain and J. Khoury, Ann. Phys. (Amsterdam) 325, 1479 (2010).
- [78] O. J. Tattersall, P. G. Ferreira, and M. Lagos, Phys. Rev. D 97, 044021 (2018).
- [79] D. Alonso, E. Bellini, P. G. Ferreira, and M. Zumalacarregui, Phys. Rev. D 95, 063502 (2017).
- [80] E. V. Linder, Phys. Rev. D 95, 023518 (2017).
- [81] J. Gleyzes, Phys. Rev. D 96, 063516 (2017).
- [82] P. A. Abell *et al.* (LSST Science and LSST Project Collaborations), arXiv:0912.0201.
- [83] C. L. Carilli and S. Rawlings, New Astron. Rev. 48, 979 (2004).
- [84] K. N. Abazajian *et al.* (CMB-S4 Collaboration), arXiv: 1610.02743.
- [85] C. Cutler and É. E. Flanagan, Phys. Rev. D 49, 2658 (1994).
- [86] L. P. Singer and L. R. Price, Phys. Rev. D 93, 024013 (2016).
- [87] H.-Y. Chen and D. E. Holz, Astrophys. J. 840, 88 (2017).
- [88] H.-Y. Wu and D. Huterer, Mon. Not. R. Astron. Soc. 471, 4946 (2017).
- [89] B. P. Abbott *et al.* (LIGO Scientific and Virgo Collaborations), Phys. Rev. X 9, 011001 (2019).
- [90] K. Pardo, M. Fishbach, D. E. Holz, and D. N. Spergel, J. Cosmol. Astropart. Phys. 07 (2018) 048.
- [91] I. Mandel, W. M. Farr, and J. R. Gair, arXiv:1809.02063.
- [92] B. P. Abbott *et al.* (LIGO Scientific and Virgo Collaborations), arXiv:1811.12940.
- [93] P. Madau and M. Dickinson, Annu. Rev. Astron. Astrophys. 52, 415 (2014).