Note on invisible decays of light mesons

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A search for the invisible decays of ω and ϕ mesons in $J/\psi \to \omega(\phi)\eta$ transitions was performed by the BESIII Collaboration very recently. Inspired by this experimental study, we compute the lowest-order contribution to branching ratios of $\mathcal{B}(V \to \bar{\nu}\nu)$ with V denoting ρ , ω , ϕ , as the standard model background to these invisible decays. Our predictions are far below the upper bounds given by the BESIII experiment. We also analyze the $J/\psi \to \eta(\eta')\bar{\nu}\nu$ processes and estimate their decay rates. Furthermore, the invisible decays of light pseudoscalar mesons P including π^0 , η , and η' are reexamined in the present paper. It is shown that, due to the helicity suppression of the two-neutrino final state, the standard model contributions to $P \to invisible$ decays are dominated by $P \to \bar{\nu}\nu\bar{\nu}\nu$ processes.

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The study of quarkonium decays to invisible final states is an interesting topic both theoretically and experimentally. The BESII [1] and *BABAR* [2] experiments have explored the invisible decays of heavy quarkonia including J/ψ and $\Upsilon(1S)$, and some interesting upper limits on the decay rates are obtained. These limits are still above the standard model (SM) predictions [3]. For the light mesons like pseudoscalar *P* with *P* denoting π^0 , η , η' , the current experimental upper bounds have been given by the E949 Collaboration [4] for $\pi^0 \rightarrow$ invisible decays and by the BESIII Collaboration [5] for $\eta(\eta') \rightarrow$ invisible decays, while branching ratios of these pseudoscalar invisible decays were calculated in Ref. [6] a long time ago.

Very recently, using a data sample of $(1310.6 \pm 7.0) \times 10^6 J/\psi$ events, the first experimental search for invisible decays of a light vector meson V was performed by the BESIII Collaboration [7] via $J/\psi \rightarrow V\eta$ ($V = \omega, \phi$) decays, and the upper limits on the ratio have been measured to be

$$\frac{\mathcal{B}(\omega \to \text{invisible})}{\mathcal{B}(\omega \to \pi^+ \pi^- \pi^0)} < 8.1 \times 10^{-5} \tag{1}$$

and

$$\frac{\mathcal{B}(\phi \to \text{invisible})}{\mathcal{B}(\phi \to K^+ K^-)} < 3.4 \times 10^{-4}, \tag{2}$$

at the 90% confidence level, for ω and ϕ mesons, respectively. Using the branching ratios of $\mathcal{B}(\omega \rightarrow \pi^+\pi^-\pi^0)$ and $\mathcal{B}(\phi \rightarrow K^+K^-)$ by the Particle Data Group (PDG) [8], we get

$$\mathcal{B}(\omega \to \text{invisible}) < 7.3 \times 10^{-5}$$
 (3)

and

$$\mathcal{B}(\phi \to \text{invisible}) < 1.7 \times 10^{-4}.$$
 (4)

In general, these invisible final states can be neutrinos in the SM and also some new particles beyond the SM, which, for instance, could be the candidate of light dark matter, as discussed in Refs. [9,10]. The decays $V \rightarrow \chi \chi$ with χ denoting the light dark matter particles have been estimated, and the branching ratio is predicted to be up to the order of 10^{-8} [9]. The authors of Refs. [10,11] have analyzed invisible decays of heavy mesons B(D) and strange meson K_L , in order to search for light dark matter particles in these processes. Thus, the investigation of invisible meson decays may help us to explore the novel dynamics or impose useful constraints on some models beyond the SM.

The first motivation of the present paper is to study the invisible decays of light vector mesons including ρ , ω , and ϕ in the SM. Since neutrinos are the only invisible particles in the SM, we will focus on the analysis of the neutrino contributions for these processes. It is expected that these contributions should be very small; however, a quantitative analysis, to our knowledge, has not been done yet. Only after we fully understand the SM background can the future precise experimental investigations of the invisible decays possibly provide us with some interesting information on new physics.

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FIG. 1. Lowest-order diagrams for the decay $V \rightarrow \bar{\nu}\nu$. For $V \rightarrow e^+e^-$ decays, replace *Z* with the photon γ , and the final states will be the charged leptons.

One can easily find that the invisible decays of V in the SM, $V \rightarrow \bar{\nu}\nu$, are given by the neutral current interactions, which can be expressed as

$$\mathcal{L}_{\rm NC} = e J_{\mu}^{\rm em} A^{\mu} + \frac{g}{\cos \theta_W} J_{\mu}^Z Z^{\mu} \tag{5}$$

with

$$J_{\mu}^{\rm em} = \sum_{f} Q_{f} \bar{f} \gamma_{\mu} f \tag{6}$$

and

$$J_{\mu}^{Z} = \frac{1}{2} \sum_{f} \bar{f} \, \gamma_{\mu} (g_{V}^{f} - g_{A}^{f} \gamma_{5}) f, \qquad (7)$$

where *e* is the coupling constant of electromagnetic interaction, *g* is the $SU(2)_L$ coupling constant, θ_W is the Weinberg angle, and *f* denotes fermions including leptons and quarks. Also, $g_V^f = T_3^f - 2Q_f \sin^2 \theta_W$ and $g_A^f = T_3^f$, where Q_f is the charge and T_3^f is the third component of the weak isospin of the fermion.

For $V \rightarrow \bar{\nu}\nu$ decays, only the intermediate Z boson can contribute, which has been shown in Fig. 1. For the charged leptonic decays, $V \rightarrow e^+e^-$, both the photon and Z contribute; however, contributions from Z boson could be negligible. Thus, direct calculations will give the ratio as

$$R_V \equiv \frac{\mathcal{B}(V \to \bar{\nu}\nu)}{\mathcal{B}(V \to e^+e^-)} = \frac{G_F^2 m_V^4}{4\pi^2 \alpha_{\rm em}^2} \frac{G_V^2}{Q_V^2} \cdot 3 \tag{8}$$

for $V = \rho$, ω , and ϕ , where the factor 3 in the equation is due to the neutrino flavors, $\alpha_{\rm em} = e^2/4\pi$, and G_F is Fermi coupling constant with

$$\frac{G_F}{\sqrt{2}} = \frac{g^2}{8m_W^2} = \frac{g^2}{8m_Z^2 \cos^2 \theta_W}.$$
 (9)

 G_V and Q_V are listed in Table I, and the values of R_V have been calculated. By employing the branching ratios of $V \rightarrow e^+e^-$ from Ref. [8], one can get

$$\mathcal{B}(\rho \to \bar{\nu}\nu) = (2.41 \pm 0.02) \times 10^{-13},$$
 (10)

TABLE I. Ratios of the decay rates R_V for ρ , ω , and ϕ mesons.

Meson V	G_V	Q_V	R_V
ρ	$\frac{1}{\sqrt{2}}\left(\frac{1}{2}-\sin^2\theta_W\right)$	$\frac{1}{\sqrt{2}}$	5.10×10^{-9}
ω	$\frac{-\sin^2\theta_W}{3\sqrt{2}}$	$\frac{1}{3\sqrt{2}}$	3.84×10^{-9}
ϕ	$-\frac{1}{4}+\frac{1}{3}\sin^2\theta_W$	$-\frac{1}{3}$	$5.65 imes 10^{-8}$

$$\mathcal{B}(\omega \to \bar{\nu}\nu) = (2.79 \pm 0.05) \times 10^{-13},$$
 (11)

$$\mathcal{B}(\phi \to \bar{\nu}\nu) = (1.67 \pm 0.02) \times 10^{-11}.$$
 (12)

Here, the uncertainty is due to the experimental value of $\mathcal{B}(V \to e^+e^-)$ only. These are quite small branching ratios, which means a big experimental challenge. Meanwhile, comparing with the present experimental bound in Eqs. (3) and (4) reported by the BESIII Collaboration and theoretical predictions $\mathcal{B}(V \to \chi\chi) \sim 10^{-8}$ given in Ref. [9], some interesting room for new physics in these invisible decays might be expected.

Note that this experimental search at BESIII [7] was performed via $J/\psi \rightarrow V\eta$ ($V = \omega, \phi$) decays. By taking the current experimental measurements of $J/\psi \rightarrow V\eta$ by the PDG [8], together with our predictions, we obtain

$$\mathcal{B}(J/\psi \to \eta \rho \to \eta \bar{\nu} \nu) = \mathcal{B}(J/\psi \to \eta \rho) \cdot \mathcal{B}(\rho \to \bar{\nu} \nu)$$
$$= (4.65 \pm 0.55) \times 10^{-17}, \qquad (13)$$

$$\mathcal{B}(J/\psi \to \eta \omega \to \eta \bar{\nu} \nu) = \mathcal{B}(J/\psi \to \eta \omega) \cdot \mathcal{B}(\omega \to \bar{\nu} \nu)$$
$$= (4.85 \pm 0.56) \times 10^{-16}, \qquad (14)$$

$$\mathcal{B}(J/\psi \to \eta \phi \to \eta \bar{\nu} \nu) = \mathcal{B}(J/\psi \to \eta \phi) \cdot \mathcal{B}(\phi \to \bar{\nu} \nu)$$
$$= (1.25 \pm 0.14) \times 10^{-14}. \tag{15}$$

This indicates that, on the other hand, it will be of interest to investigate the $J/\psi \rightarrow \eta \bar{\nu} \nu$ decay in which $\bar{\nu} \nu$ is not from any resonances, and the analysis may provide some complementary information for the future experimental study.

In the SM, it is natural to believe that, at the leading order, this process proceeds through $J/\psi \rightarrow Z^*\eta$, followed by $Z^* \rightarrow \bar{\nu}\nu$. Considering charge conjugate invariance in $J/\psi \rightarrow Z^*\eta$ transition, one can effectively write

$$\mathcal{L}_{JZ\eta} = \frac{g_{JZ\eta}}{m_J} \epsilon^{\mu\nu\alpha\beta} J_{\mu\nu} Z_{\alpha\beta} \eta, \qquad (16)$$

where $J_{\mu\nu} = \partial_{\mu}J_{\nu} - \partial_{\nu}J_{\mu}$, $Z_{\alpha\beta} = \partial_{\alpha}Z_{\beta} - \partial_{\beta}Z_{\alpha}$, and $g_{JZ\eta}$ is an unknown dimensionless coupling. Thus, the differential decay rate of the transition $J/\psi \rightarrow \eta Z^* \rightarrow \eta \bar{\nu} \nu$ is expressed as



FIG. 2. Representative diagrams for $J/\psi \rightarrow \gamma/Z + gg$ transitions with the wave line denoting γ or Z and the curly line denoting the gluon. By exchanging the γ/Z line with the gluon line, one can totally get three diagrams.

$$\frac{d\Gamma(J/\psi \to \eta \bar{\nu} \nu)}{dq^2} = \frac{G_F^2 g_{JZ\eta}^2 q^2}{144\pi^3 m_J^5} \lambda^{3/2}(m_J^2, m_\eta^2, q^2), \quad (17)$$

where q^2 is the neutrino pair invariant mass squared with its range $0 \le q^2 \le (m_J - m_\eta)^2$ and $\lambda(a, b, c) = a^2 + b^2 + c^2 - 2ab - 2bc - 2ac$. Consequently, we have

$$\Gamma(J/\psi \to \eta \bar{\nu} \nu) = \frac{G_F^2 m_J^5 g_{JZ\eta}^2}{144\pi^3} f(r_\eta) \cdot 3 \tag{18}$$

with $r_{\eta} = m_{\eta}^2/m_J^2$, $f(x) = (1-x)(x^4 - 14x^3 - 94x^2 - 14x + 1)/20 - 3x^2(1+x)\log x$, and the factor 3 is also due to the neutrino flavors. To predict this decay rate, one has to fix the unknown coupling $g_{JZ\eta}$.

It is assumed that the radiative J/ψ decays like $J/\psi \rightarrow \gamma \eta(\eta')$, which are suppressed by the Okubo-Zweig-Iizuka rule, are dominated by the process $J/\psi \rightarrow \gamma gg$ with $gg \rightarrow \eta(\eta')$ [12–14]. It is expected that $J/\psi \rightarrow Z^*\eta(\eta')$ transitions can be described in the same way, and the corresponding diagrams have been displayed in Fig. 2. One can parametrize the effective vertex of radiative decays as

$$\mathcal{L}_{J\gamma\eta} = \frac{g_{J\gamma\eta}}{m_J} \epsilon^{\mu\nu\alpha\beta} J_{\mu\nu} F_{\alpha\beta} \eta, \qquad (19)$$

where $g_{J\gamma\eta}$ is an effective coupling. Because of charge conjugate invariance, the leading-order contribution to $J/\psi \rightarrow Z^*\eta$ is only given by the vector part of J^Z_{μ} in Eq. (7). Then, it is easy from Fig. 2 to see

$$\frac{g_{JZ\eta}}{g_{J\gamma\eta}} = \frac{gg_V^c/2\cos\theta_W}{eQ_C} = \frac{3/8 - \sin^2\theta_W}{\cos\theta_W\sin\theta_W}.$$
 (20)

This relation would help us estimate the decay rate of $J/\psi \rightarrow \eta \bar{\nu} \nu$ using the experimental information of $J/\psi \rightarrow \eta \gamma$ decay. It is thus straightforward to get

$$R^{\eta}_{\bar{\nu}\nu} \equiv \frac{\mathcal{B}(J/\psi \to \eta\bar{\nu}\nu)}{\mathcal{B}(J/\psi \to \eta\gamma)} = \frac{G_F^2 m_J^4}{16\pi^2} \frac{f(r_{\eta})}{(1 - r_{\eta})^3} \left(\frac{g_{JZ\eta}}{g_{J\gamma\eta}}\right)^2 = 3.4 \times 10^{-13}.$$
(21)

Accordingly, taking $\mathcal{B}(J/\psi \rightarrow \eta \gamma) = (1.104 \pm 0.034) \times 10^{-3}$ from Ref. [8], we have



FIG. 3. The decay spectrum for $J/\psi \to \eta \bar{\nu} \nu$ normalized by $\Gamma(J/\psi \to \eta \gamma)$ denoted by Γ_{η} as the function of the neutrino pair invariant mass squared q^2 .

$$\mathcal{B}(J/\psi \to \eta \bar{\nu} \nu) = (3.8 \pm 0.1) \times 10^{-16},$$
 (22)

which can be compared with the results in Eqs. (13), (14), and (15). Also, the decay spectrum normalized by $\Gamma(J/\psi \rightarrow \eta \gamma)$ has been plotted, as the function of the neutrino pair invariant mass squared q^2 in Fig. 3 and as the function of the energy of η meson E_{η} in Fig. 4.

Similar analysis can be applied to the $J/\psi \rightarrow \eta' \bar{\nu} \nu$ decay. Replacing η in Eq. (21) by η' , one has

$$R^{\eta'}_{\bar{\nu}\nu} \equiv \frac{\mathcal{B}(J/\psi \to \eta' \bar{\nu}\nu)}{\mathcal{B}(J/\psi \to \eta' \gamma)} = 2.0 \times 10^{-13}, \qquad (23)$$

which, using the data $\mathcal{B}(J/\psi \rightarrow \eta' \gamma) = (5.13 \pm 0.17) \times 10^{-3}$ given in Ref. [8], gives

$$\mathcal{B}(J/\psi \to \eta' \bar{\nu} \nu) = (10.2 \pm 0.3) \times 10^{-16}.$$
 (24)



FIG. 4. The decay spectrum for $J/\psi \to \eta \bar{\nu} \nu$ normalized by $\Gamma(J/\psi \to \eta \gamma)$ denoted by Γ_{η} as the function of the energy of η meson E_{η} .

This can be compared with

$$\mathcal{B}(J/\psi \to \eta' \rho \to \eta' \bar{\nu} \nu) = \mathcal{B}(J/\psi \to \eta' \rho) \cdot \mathcal{B}(\rho \to \bar{\nu} \nu)$$
$$= (1.95 \pm 0.19) \times 10^{-17}, \qquad (25)$$

$$\mathcal{B}(J/\psi \to \eta' \omega \to \eta' \bar{\nu} \nu) = \mathcal{B}(J/\psi \to \eta' \omega) \cdot \mathcal{B}(\omega \to \bar{\nu} \nu)$$
$$= (5.27 \pm 0.51) \times 10^{-17}, \qquad (26)$$

$$\mathcal{B}(J/\psi \to \eta' \phi \to \eta' \bar{\nu} \nu) = \mathcal{B}(J/\psi \to \eta' \phi) \cdot \mathcal{B}(\phi \to \bar{\nu} \nu)$$
$$= (7.68 \pm 0.84) \times 10^{-15}, \qquad (27)$$

where we have combined the experimental data of $J/\psi \rightarrow V\eta'$ for $V = \rho$, ω , ϕ by the PDG [8] with our predictions in Eqs. (10), (11), and (12).

Our theoretical estimations in Eqs. (22) and (24) also indicate that it is interesting to search for $J/\psi \rightarrow \eta(\eta') +$ invisible decays to explore new physics beyond the SM, by using very huge J/ψ samples at BESIII. Actually, some model studies, for instance, $J/\psi \rightarrow P\gamma'$ with γ' called a dark photon, which is a singlet under the SM gauge groups but couples to the SM photon via kinetic mixing [15], were performed in Ref. [16] very recently. Theoretical analysis was done in Ref. [17].

The remainder of the present paper revisits the invisible decays of light pseudoscalar mesons including π^0 , η , and η' . As mentioned above, experimentally,

$$\mathcal{B}(\pi^0 \to \bar{\nu}\nu) < 2.7 \times 10^{-7} \tag{28}$$

has been obtained, at the 90% confidence level, by the E949 Collaboration [4], and the upper limits

$$\frac{\mathcal{B}(\eta \to \text{invisible})}{\mathcal{B}(\eta \to \gamma\gamma)} < 2.6 \times 10^{-4}$$
(29)

and

$$\frac{\mathcal{B}(\eta' \to \text{invisible})}{\mathcal{B}(\eta' \to \gamma\gamma)} < 2.4 \times 10^{-2}$$
(30)

have been determined, at the 90% confidence level, by the BESIII Collaboration [5]. Recently, an interesting experimental project, by searching for invisible decays of π^0, η , η' , K_S , and K_L to probe new physics, has been proposed [18] and is designed for the NA64 experiment at the CERN Super Proton Synchrotron. Theoretically, calculation of the $P \rightarrow \bar{\nu}\nu$ decay rate in the SM was performed in Ref. [6] more than 30 years ago. Because of the helicity suppression, this mode is forbidden for the massless neutrino in the SM. Such suppression does not happen in the above case for light vector mesons. If the Z boson couples to a massive neutrino with the standard weak interaction, one will get, for π^0 decaying into the neutrino pair [6],

$$\Gamma(\pi^0 \to \bar{\nu}\nu) = \frac{G_F^2 f_\pi^2 m_\pi^3}{16\pi} r_\nu^2, \tag{31}$$

where $r_{\nu} = m_{\nu}/m_{\pi}$ and $f_{\pi} = 93$ MeV is the pion decay constant. For neutrino masses, if assuming $m_{\nu} \sim \sum_{i} m_{\nu_{i}} < 0.62$ eV given in Ref. [19], we get

$$\mathcal{B}(\pi^0 \to \bar{\nu}\nu) \sim 6.3 \times 10^{-25}.$$
 (32)

The authors of Ref. [6] obtained a larger branching ratio for $\pi^0 \rightarrow \bar{\nu}\nu$ since they used a larger bound for neutrino masses. Similarly, one can have $\mathcal{B}(\eta/\eta' \rightarrow \bar{\nu}\nu)$, which is of the same order of magnitude as Eq. (32) or even smaller. These predictions are far from the present experimental upper bounds shown in Eqs. (28) and (29).

However, this is not the whole story for $P \rightarrow$ invisible decays from the neutrino background. Besides $P \rightarrow \bar{\nu}\nu$, there could also exist $P \rightarrow \bar{\nu}\nu\bar{\nu}\nu$ or even more numbers of neutrino pairs. As shown above, the decay to one neutrino pair is strongly helicity suppressed due to the very tiny neutrino mass, while such helicity suppression can be overcome for the four-neutrino final state. In the SM, the lowest-order contribution to $P \rightarrow \bar{\nu}\nu\bar{\nu}\nu$ is given by the transition $P \rightarrow Z^*Z^*$ with the virtual $Z^* \rightarrow \bar{\nu}\nu$.

It is well known that $P \rightarrow \gamma \gamma$ decays are generated from chiral anomaly, which can be expressed as

$$\mathcal{L}_{P\gamma\gamma} \sim \frac{e^2}{16\pi^2 f_P} \varepsilon^{\mu\nu\alpha\beta} F_{\mu\nu} F_{\alpha\beta} P.$$
(33)

Analogously, one may get

$$\mathcal{L}_{PZZ} \sim \frac{g^2}{16\pi^2 f_P \cos^2 \theta_W} \epsilon^{\mu\nu\alpha\beta} Z_{\mu\nu} Z_{\alpha\beta} P.$$
(34)

Thus, using naive dimensional analysis, we obtain

$$R_P \equiv \frac{\mathcal{B}(P \to \bar{\nu}\nu\bar{\nu}\nu)}{\mathcal{B}(P \to \gamma\gamma)} \sim \frac{G_F^4 m_P^8}{\alpha_{\rm em}^2}.$$
 (35)

In general, some different factors should appear in Eqs. (33) and (34) for $P = \pi^0$, η , η' . However, as an order of magnitude estimation of Eq. (35) in the present paper, we neglect these factors. Numerically, we have $R_{\pi^0} \sim 3.8 \times 10^{-23}$, $R_{\eta} \sim 2.9 \times 10^{-18}$, and $R_{\eta'} \sim 2.5 \times 10^{-16}$, which gives

$$\mathcal{B}(\pi^0 \to \bar{\nu}\nu\bar{\nu}\nu) \sim 4 \times 10^{-23},\tag{36}$$

$$\mathcal{B}(\eta \to \bar{\nu}\nu\bar{\nu}\nu) \sim 1 \times 10^{-18},$$
 (37)

$$\mathcal{B}(\eta' \to \bar{\nu}\nu\bar{\nu}\nu) \sim 5 \times 10^{-18},\tag{38}$$

by using the experimental data of $P \rightarrow \gamma \gamma$ [8]. Although these branching ratios are still small and far from the present experimental bounds, comparing with Eq. (32) for one neutrino pair, one can find that there is a large enhancement for the four-neutrino final states, and the enhancement could be increasing when the decaying pseudoscalar particle gets heavier. Therefore, for heavy pseudoquarkonia like η_c or η_b , a much stronger enhancement may be expected. Similar enhancement has been pointed out in the neutral *B* and *D* invisible decays by the authors of Ref. [20].

To summarize, we have calculated the lowest-order SM contribution to the branching ratios of the light vector meson invisible decays, $\mathcal{B}(V \to \bar{\nu}\nu)$, for $V = \rho$, ω , ϕ . Our theoretical results for $\mathcal{B}(V \to \bar{\nu}\nu)$ are about $10^{-13} \sim 10^{-11}$, which are far below the upper limits given by the BESIII experiment very recently. The $J/\psi \to \eta(\eta')\bar{\nu}\nu$ decays have

been studied, and their decay rates were estimated. We also revisited the light pseudoscalar invisible decays. It is known that $P \rightarrow \bar{\nu}\nu$ is strongly helicity suppressed; however, such suppression does not happen in $P \rightarrow \bar{\nu}\nu\bar{\nu}\nu$. These results may provide some complementary information for the future experimental and theoretical investigations of the invisible decays of light mesons, in order to explore new physics scenarios beyond the SM.

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