Probing leptoquarks and heavy neutrinos at the LHeC

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We explore leptoquark production and decay for the \tilde{R}_2 class of models at the proposed e^-p collider LHeC, planned to operate with 150 GeV electron and 7 TeV proton beams. In addition to the coupling of the leptoquark with the lepton and jet, the model also has right-handed neutrinos coupled to the leptoquark. We analyze the collider signatures of a number of final states that can originate from leptoquark decay into the standard model particles, as well as the final states that originate from further decay of the heavy neutrinos produced from the leptoquark. We find that the final state $l^+ + n - \text{jets}(1 \le n \le 2)$ has the largest discovery prospect, more than 5σ with only a few fb⁻¹ of data to probe a leptoquark of mass 1.1 TeV, even with a generic set of cuts. The significance falls sharply with increasing leptoquark mass. However, with 100 fb⁻¹ of data, a 5σ discovery for leptoquarks of mass up to 1.4 TeV is still achievable. Also, for the same luminosity final state $\bar{b}e^+\tau^- + n - \text{jets}(n \geq 2) + \mathcal{E}_T$, resulting from the cascade decay of the leptoquark to a \bar{t} and right-handed neutrino, followed by further decays of \bar{t} and the neutrino, is expected to yield a rather large number of events (≈ 180) .

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I. INTRODUCTION

Discovery of physics beyond the Standard Model (SM) continues to be the aim of most high energy physicists today. In spite of the so far unsuccessful direct searches for new particles or clear indications for the existence of any kind of new physics at the Large Hadron Collider (LHC), issues of the existence of dark matter, baryon asymmetry of the Universe, nonzero neutrino masses, etc., are compelling enough for one to believe that there must exist physics beyond the SM. A number of beyond Standard Model extensions have been proposed in the literature. The minimal supersymmetric standard model, large extra dimensions, seesaw models of neutrino mass generation, leptoquarks, and grand unified theories, are a few among them.

Leptoquarks (LQs) are hypothetical particles, which make leptons couple directly to quarks and vice versa [\[1](#page-13-0)–3]. In the Pati-Salam model, they emerged from the unification of quarks and leptons [\[4\].](#page-13-1) They also exist in grand unification theories based on SU(5) [\[5\]](#page-13-2) and SO(10) [6–[15\].](#page-13-3) They are also expected to exist at the TeV scale in extended technicolor models [16–[19\].](#page-13-4) LQs can be either of scalar or vector nature. Using the SM representation of quarks and leptons, all possible LQ states can be classified, with six scalar and six vector LQ multiplets under the SM gauge group [\[20\].](#page-13-5) Among the different classes, the scalar LQ \tilde{R}_2 is interesting, as it is one of the multiplets that allows for matter stability [\[21\]](#page-13-6). Moreover, it also couples to righthanded neutrinos (RH neutrinos). The RH neutrinos can generate light neutrino masses through the seesaw mechanism [22–[35\].](#page-13-7) In seesaw, light neutrino masses are generated through the $d = 5$ lepton number violating operator [\[28\]](#page-13-8). The high scale UV completed models include the gauge singlet RH neutrino (type-I, inverse seesaw), $SU(2)_L$ triplet scalar, and fermion (type-II and type-III).

In the case of type-I seesaw [\[22](#page-13-7)–25], the light neutrinos acquire masses through mixings with additional Majorana RH neutrinos. To account for the tiny neutrino masses, the mass scale of these Majorana neutrinos has to be very close

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to the gauge coupling unification scale, in which case these massive RH neutrinos will remain inaccessible at LHC and at other near future colliders. For the present and near future colliders to be able to probe the RH neutrinos their masses have to be within the experimental reach, and the mixing with the active neutrinos, referred to as active-sterile mixing, has to be sizable. TeV scale RH neutrinos with substantially large active-sterile mixings are, however, possible to accommodate in type-I seesaw if cancellation exists in the light neutrino mass matrix [\[36\]](#page-13-9). The inverse seesaw mechanism [\[33](#page-13-10)–35] is another such scenario, where the TeV scale or even smaller RH neutrino masses with sizable active-sterile mixing can exist. In this scheme, in addition to the SM particles there are gauge singlet neutrinos with opposite lepton numbers $(+1 \text{ and } -1)$. The light neutrino mass matrix is given in terms of the Dirac neutrino mass term $m_D \sim Y_\nu v$ (with v being the electroweak vacuum expectation value and Y_{ν} a generic Yukawa coupling), the heavy neutrino mass scale M_R and, a small lepton number violating ($\Delta L = 2$) mass term μ , which ensures that the M_R scale remains close to TeV or less, with order one Yukawa coupling. The light neutrino mass matrix in this case is $m_{\nu} \sim (m_D^2/M_R^2)\mu$. While
the heavy neutrino states may lie within the kinematic reach the heavy neutrino states may lie within the kinematic reach of the LHC, their production cross section falls rapidly with increasing masses and smaller active-sterile neutrino mixing. Large active-sterile mixing is possible to obtain in other seesaw secenarios as well, such as linear seesaw [\[37,38\]](#page-13-11) and extended seesaw [\[39](#page-13-12)–43]. A substantial rise in the production cross section of the RH neutrinos is feasible in the presence of LQs. This has been explored recently for the LHC in Ref. [\[44\]](#page-13-13) for inverse seesaw, where a number of final states have been analyzed in detail. Leptoquark models have also been tested recently for fitting the IceCube events [\[45\]](#page-13-14). For the heavy neutrino searches at LHeC in the inverse seesaw model, see Ref.[\[46\]](#page-13-15) and for the LNV signal at LHeC, see Ref. [\[47\]](#page-13-16). Similar studies for heavy neutrino searches also have been carried out in Refs. [\[48,49\].](#page-13-17)

In this work, we consider a particular type of scalar leptoquark \tilde{R}_2 , which transforms as $\tilde{R}_2 \in (3, 2, \frac{1}{6})$ under the
SM gauge group $SU(3) \times SU(2) \times U(1)$, and for the SM gauge group $SU(3)_c \times SU(2)_L \times U(1)_Y$, and for the RH neutrino, we adopt a model independent framework. \tilde{R}_2 is a genuine LQ with fermion number $F = 3B + L = 0$. The color charge of the LQ will enable their copious production at the LHC. Moreover, at e^-p colliders like LHeC, they can be resonantly produced. The LHeC is a proposed e^-p collider in the TeV regime after HERA, supposed to be built in the LHC tunnel [\[50\].](#page-14-0) LHeC will use a newly built electron beam of 60 GeV, up to possibly 150 GeV, to collide with the intense 7 TeV proton beam of the LHC. LHeC is expected to operate with 100 fb⁻¹ integrated luminosity, and is complementary to the pp collider LHC [\[51\].](#page-14-1) The RH neutrino, being coupled to the LQ, can be produced from LQ decay. The decay of LQ into a lepton and a jet, and the decay of the RH neutrino in different SM states give rise to a plethora of model signatures, that we study in detail. We show that among all the final states, $l^+ + n - \text{jets}(1 \le n \le 2)$ has the highest LQ discovery prospect, even with generic sets of cuts. Additionally, we also carry out an in-depth analysis for a few other channels that arise due to the decay of a heavy neutrino. We show that with judicious application of selection cuts the channels $l^+ + n - \text{jets}(n \geq 3)$, and $l^+\tau^-b + \mathcal{E}_T + n - \text{jets}(n \geq 2)$ can be made background free.

The discussion of the paper goes as follows: in Sec. [II,](#page-1-0) and Sec. [III,](#page-2-0) we review the model and the theory constraints. Following that, in Sec. [IV,](#page-4-0) we discuss the production and decay of LQs at LHeC. In the subsequent sections, Sec. [V,](#page-5-0) Sec. [VI,](#page-6-0) and Sec. [VII](#page-10-0), we present a detailed collider analysis and discuss the discovery prospects of different final states. Finally, in Sec. [VIII](#page-12-0), we summarize.

II. MODEL

We consider the scalar LQ \tilde{R}_2 charged as (3, 2, 1/6) under the SM gauge group. In the presence of the RH neutrinos N_R the LQ has additional interaction [\[2,3,20\],](#page-13-18)

$$
\mathcal{L} = -Y_{ij}\bar{d}_R^i \tilde{R}_2^a \epsilon^{ab} L_L^{j,b} + Z_{ij} \bar{Q}_L^{i,a} \tilde{R}_2^a N_R^j + \text{H.c.,} \quad (1)
$$

where i, $j = 1, 2, 3$ are flavor indices and a, $b = 1, 2$ are $SU(2)_L$ indices. We assume that there are three right-chiral neutrinos N_R^j $(j = 1, 2, 3)$, Y_{ij} , and Z_{ij} are the elements of explicitly complex 3×3 . Vulcave coupling matrices. Note arbitrary complex 3×3 Yukawa coupling matrices. Note that \tilde{R}_2 comprises two LQs. One has $Q = \frac{2}{3}$, and the other has $Q = -\frac{1}{3}$. Upon expansion, the Lagrangian becomes

$$
\mathcal{L} = -Y_{ij}\bar{d}_{R}^{i}e_{L}^{j}\tilde{R}_{2}^{2/3} + (YU_{PMNS})_{ij}\bar{d}_{R}^{i}\nu_{L}^{j}\tilde{R}_{2}^{-1/3} \n+ (V_{CKM}Z)_{ij}\bar{u}_{L}^{i}N_{R}^{j}\tilde{R}_{2}^{2/3} + Z_{ij}\bar{d}_{L}^{i}N_{R}^{j}\tilde{R}_{2}^{-1/3} + \text{H.c.},
$$
\n(2)

where the superscript of the LQ fields denote the electric charge of a given $SU(2)_L$ doublet component of \tilde{R}_2 ; U_{PMNS} and V_{CKM} are the Pontecorvo-Maki-Nakagawa-Sakata (PMNS) and Cabibbo-Kobayashi-Maskawa (CKM) matrices. At the e^-p machine $\tilde{R}_2^{\frac{1}{3}}$ cannot be resonantly produced. Hence, the expected cross section for the production of $\tilde{R}_2^{\frac{1}{3}}$ is small. Therefore, in this work, we consider only $\tilde{R}_2^{\frac{2}{3}}$ and study its production and decay.

The charged current and neutral current interactions of the RH neutrinos are parametrized in a model-independent way as follows,

$$
-\mathcal{L}_{\text{CC}} = \frac{g}{\sqrt{2}} W_{\mu}^- \bar{\mathcal{E}} \gamma^{\mu} P_L V_{\ell j} N_j + \text{H.c.},\tag{3}
$$

and

$$
-\mathcal{L}_{NC} = \frac{g}{2\cos\theta_w} Z_\mu \{ (U_{PMNS}^\dagger V)_{ij} \bar{\nu}_i \gamma^\mu P_L N_j + \text{H.c.} \}.
$$
 (4)

The interaction of the heavy neutrinos with Higgs boson has the following form:

$$
-\mathcal{L}_H = \frac{gM_j}{4M_W} H\{ (U_{\text{PMNS}}^\dagger V)_{ij} \bar{\nu}_i P_R N_j + \text{H.c.} \} \tag{5}
$$

In the above, $P_{L/R}=(1 \mp \gamma^5)/2$ is the left and rightchirality projection operator, and V is the mixing matrix through which light neutrinos mix with the RH neutrinos. We consider a diagonal basis for the charged leptons.

For the RH neutrino, coupled with LQ, we do not assume any particular model. Instead, we are interested in different frameworks of RH neutrinos that can lead to large activesterile mixing, so that the heavy neutrinos decay inside the detector. It is widely known that a number of different frameworks can generate large active-sterile mixing, including inverse and linear seesaw [33–[35,37,38\]](#page-13-10), extended seesaw [\[39](#page-13-12)–43], and the cancellation framework [\[36\]](#page-13-9). In the inverse seesaw, light SM neutrino masses are extremely tiny, owing to the small lepton number violating parameter of the model. The active-sterile neutrino mixing is not constrained from light neutrino masses in this model. Active-sterile mixing up to $\mathcal{O}(10^{-2})$ is allowed from experimental data [\[52](#page-14-2)–63]. In extended seesaw, or double seesaw [\[64\]](#page-14-3), the RH neutrino gets mass due to seesaw, and light neutrino masses are generated due to twofold seesaw. In other frameworks, such as, cancellation, small light neutrino masses are generated due to cancellation between different RH neutrino contributions in the mass matrix [\[36\]](#page-13-9). The active-sterile mixing is yet unconstrained from neutrino data. In all the above mentioned frameworks, owing to the charged current and neutral current interactions as well as the interaction with the Higgs, specified above in Eqs. (3) , (4) , and (5) , the RH neutrino N can decay to a number of SM particles, including $l^{\pm}W^{\mp}$, νZ , and ν H. The branching ratio of these three decays is $Br(N \rightarrow lW): Br(N \rightarrow \nu Z): Br(N \rightarrow \nu H) \simeq 0.6:0.3:0.1,$ once RH neutrino mass becomes larger than the Higgs mass $M_N > M_H$ and $M_N < 200$ GeV [\[57,65\].](#page-14-4)

In the following sections, we first consider the resonant production of a LQ and its decay to a lepton and jet. We next consider the production of heavy neutrinos from LQ decay, and discuss the discovery prospect of the LQ in a number of channels. As mentioned before, we consider the prompt decays of heavy neutrino for the analysis of the RH neutrino signature, that occurs due to large active-sterile neutrino mixing. We compare between the usual charged current (CC) production of heavy neutrinos vs the alternate production from LQ decay. We show that the production from LQ decay dominates over the CC production mode by an order of magnitude for active-sterile mixing $V \lesssim 10^{-2}$.

III. CONSTRAINTS ON LEPTOQUARK COUPLINGS

The couplings of the LQs to fermions are constrained by low energy precision observables such as atomic parity violation, Kaon decays, etc. We assume the Yukawa coupling matrix elements $Y_{ij} = \delta_{ij}Y_{ii}$ and $Z_{ij} = \delta_{ij}Z_{ii}$, where, $i, j = 1, 2, 3$. Hence the LQ couples exclusively to a lepton and a quark of the same generation, although it can have nonzero couplings to fermions of more than one generation.

(i) LQs have been searched for and studied in the context of e^+e^- [66–[70\],](#page-14-5) ep [71–[76\],](#page-14-6) p \bar{p} [\[77](#page-14-7)–81], and pp [82–[87\]](#page-14-8) colliders. The present tightest bounds are from the LHC [88–[92\]](#page-14-9). The LHC has studied the process $p p \to L\overline{O} \overline{LO} \to \ell i \ell i$ for LQs of first, second, and third generations. Nonobservation of any new physics at the LHC has ruled out LQs of masses up to 1.1 TeV at 95% C.L. for the LQ decaying to ej with 100% branching ratio [\[89\]](#page-14-10). For the second generation, the bound is even more stringent $M_{LO} > 1.5$ TeV at 95% C.L. [\[92\].](#page-14-11) For the third generation, the bound is $M_{\text{LO}} >$ 900 GeV at 95% C.L. [\[91\]](#page-14-12). At the LHC, numerous QCD diagrams contribute to the LQ pair production. For illustration, we show only one representative gluon initiated diagram in the left panel of Fig. [1.](#page-3-0) However, with nonzero Yukawa couplings, significantly large contribution to the LQ pair production may arise through a single t channel diagram (see the right panel of Fig. [1](#page-3-0)). The pair production cross section at the LHC can be parametrized as [\[93\]](#page-14-13)

$$
\sigma_{\text{pair}}(Y_{ii}, M_{\text{LQ}}) = a_0(M_{\text{LQ}}) + a_2(M_{\text{LQ}})|Y_{ii}|^2
$$

+ $a_4(M_{\text{LQ}})|Y_{ii}|^4$, (6)

where the three terms correspond to the QCD pair production, an interference term, and t-channel production. In Fig. [2](#page-3-1), we show the variation of the LQ pair-production cross section with the Yukawa coupling Y_{11} .

For small Yukawa coupling Y_{11} , LQ pair production is mostly governed by QCD, as can be seen from the straight line up to $Y_{11} \sim 0.5$ in Fig. [2](#page-3-1). For intermediate Yukawa couplings there exists a region with negative interference between QCD diagrams and the t-channel diagram, where the total cross section decreases [\[93\],](#page-14-13) resulting in a mild dip in the cross section for coupling beyond 0.5, which is seen in Fig. [2](#page-3-1). For large Yukawa coupling Y_{ii} , the *t*-channel process dominates and significantly enhances the cross section. The right panel of Fig. [2](#page-3-1) shows the limit on the firstgeneration scalar LQ pair production times the branching fraction to the ej final state as a function of the mass. For the branching fraction $LQ \rightarrow e\dot{\jmath}$ as 100%, the bound on the pair production of LQ becomes $\sigma(pp \to LQ LQ) \lesssim 3$ fb, for LQ mass 1.1 TeV. Comparing the left and right

FIG. 1. Left panel: Feynman diagram for the gluon-initiated LQ pair-production process at the LHC. Right panel: the same, but for the quark-initiated processes.

FIG. 2. Left panel: variation of the production cross section with Yukawa coupling for $\sqrt{s} = 13$ TeV. Right panel: limit on the scalar I O pair-production time branching fraction to eq final state as a function of mass f LQ pair-production time branching fraction to eq final state as a function of mass for first-generation LQs. The yellow and green bands represent the 2σ and 1σ expected limits. The NLO prediction is shown in the blue curve with uncertainty due to the choice of the PDF set and the renormalization or factorization scale [\[89\]](#page-14-10).

panel of Fig. [2](#page-3-1), one can see that the limit on the cross section for a LQ of mass 1.1 TeV will be inconsistent with a Yukawa coupling larger than 1.

It is obvious from Eq. [\(1\)](#page-1-3) that for the LQ to have 100% branching ratio in the LQ \rightarrow *ej* decay mode, the coupling Z needs to be zero. Allowing a nonzero value for coupling Z will open up new decay modes, such as $\bar{t}N$ for LQs, and hence will lower the stringent bound on LQs. We, however, adopt a conservative approach, and in order to be consistent with the LHC results for the first generation of LQs, throughout our study, we consider $M_{\text{LO}} \geq 1.1$ TeV. Additionally, we also keep both the couplings nonzero.

(ii) The present bound on coupling Y from atomic parity violation are $Y_{de} < 0.34(\frac{M_{LQ}}{1 \text{ TeV}})$, $Y_{ue} < 0.36(\frac{M_{LQ}}{1 \text{ TeV}})$ Figure 1.1 TeV $T_{de} \sim 0.54(\frac{1}{1 \text{ TeV}})$, $T_{ue} \sim 0.50(\frac{1}{1 \text{ TeV}})$
[\[93\]](#page-14-13). These bounds are extracted under the assumption that only one of the two contributions is present at a given moment. These bounds allow large coupling for a larger mass of LQs, and place a stringent constraint for lighter LQs.

(iii) The most stringent bound on the diagonal couplings of $\tilde{R_2}^2$ comes from the LFV decay mode $K_L \rightarrow \mu^- e^+$, as this is a tree-level process. Follow-ing Refs. [\[93,94\]](#page-14-13), the bound is given by $|Y_{s\mu}Y_{de}^*| <$
2.1 $(1.10^{-5}e^{M_{10}})^2$, $(1.100^{14}e^{M_{10}})^2$ $2.1 \times 10^{-5} \left(\frac{M_{\text{LO}}}{1 \text{ TeV}}\right)^2$. In order to satisfy both the APV
and LEV constraints for $Y_{\text{LO}} \approx (2)(0.1)$, the other 2.1 × 10 $\frac{1}{1}$ TeV) · in order to satisfy both the XI v
and LFV constraints, for $Y_{de} \sim \mathcal{O}(0.1)$, the other coupling Y_{su} has to be tiny. We consider Y_{su} to be zero and a large value (0.3) for Y_{de} to get a large production cross section of LQs at LHeC.

We discuss the production of LQs and its decay to different final states in the next section, for the benchmark points, which are in agreement with the described constraints.

FIG. 3. Feynman diagram for $e^-p \rightarrow \ell j$.

FIG. 4. Comparison of the cross section for LQ production at the LHC and the LHeC. The c.m. energy for the LHC is \sqrt{s} = 13 TeV. For the LHeC, we use an electron beam of 150 GeV and proton beam of 7 TeV respectively. The coupling 150 GeV and proton beam of 7 TeV, respectively. The coupling Y_{de} has been varied as $0.3 \frac{M_{LQ}}{1 \text{ TeV}}$, in agreement with the APV constraints.

IV. LEPTOQUARK PRODUCTION AND ITS DECAYS

At e^-p colliders, scalar LQs can be resonantly produced through the s-channel process as shown in the left panel of Fig. [3](#page-4-1), and decay to a lepton and a jet. In addition, LQs can also be a *t*-channel mediator for the process $e^-p \rightarrow l^-j$, that we consider in our analysis (shown in the right panel of Fig. [3\)](#page-4-1).

The production cross section of a LQ at LHeC, as well as that for both the single and pair production at LHC, are shown in Fig. [4](#page-4-2) for varying LQ mass. Clearly, the LHeC cross section is more than both the pair production, as well as the single production of LQs associated with a charged lepton at LHC. The higher LQ production cross section as well as the lower background at LHeC will allow more precise studies for probing LQs and RH neutrinos. Once produced, the LQ can decay into a number of final states, including (a) a quark-lepton pair that gives rise to a single charged lepton and a light jet, (b) a light jet and a heavy neutrino, and (c) a top quark accompanied with a heavy neutrino. These heavy neutrinos appearing from the decays of the LQ can again be more easily probed at LHeC through its decay products. Note that, for all these processes, the LQ can also mediate as a t-channel mediator. For (b) and (c) , there is also a *t*-channel contribution from a W gauge boson mediator, but significantly smaller for the active-sterile mixing $V \lesssim 10^{-2}$. We give numerical estimates in Sec. [VI](#page-6-0). However, during computation (in Fig. [5](#page-5-1) and for the collider analysis), we consider all the contributions together.

For our computations, the LQ mass has been set to 1.1 TeV. We choose three benchmark points, with the three heavy neutrino masses and the LQ couplings Y_{ii} and Z_{ii} chosen such that they are consistent with all the constraints mentioned in Sec. [III](#page-2-0), as well as with the neutrino oscillation data [\[46\]](#page-13-15). These parameters for the benchmark points have been specified in Table [I.](#page-4-3) The production cross section for these three processes at LHeC, with electron and proton beam energies of 150 GeV and 7 TeV, respectively, are also shown in Fig. [5](#page-5-1) and in Fig. [6](#page-5-2) as a function of the couplings and LQ mass respectively.

The general expression for the two body decay of a scalar LQ to $\ell_i q$ and $N_i q$ final states is given by

$$
\Gamma(LQ \to e_{iq}) = \frac{|Y_{ii}|^2}{16\pi M_{LQ}^3} \lambda^{\frac{1}{2}} (M_{LQ}^2, m_{e_i}^2, m_{q^2}) (M_{LQ}^2 - m_{e_i}^2 - m_q^2), \quad (7)
$$

$$
\Gamma(\text{LQ} \to N_i q) = \frac{|Z_{ii}|^2}{16\pi M_{\text{LQ}}^3} \lambda^{\frac{1}{2}} (M_{\text{LQ}}^2, M_{N_i}^2, m_{q^2}) (M_{\text{LQ}}^2 - M_{N_i}^2 - m_q^2). \tag{8}
$$

In the massless limit of leptons and quarks, the branching ratios are given by

$$
\beta(\text{LQ} \to \ell_i q) = \frac{|Y_{ii}|^2}{\sum_i (|Y_{ii}|^2 + |Z_{ii}|^2)} \quad \text{and}
$$

$$
\beta(\text{LQ} \to N_i q) = \frac{|Z_{ii}|^2}{\sum_i (|Y_{ii}|^2 + |Z_{ii}|^2)}.
$$
(9)

TABLE I. Benchmark parameters and production cross section for ℓj , jN_1 , and $\bar{i}N_3$ at the LHeC with electron and proton beam energy 150 GeV and 7 TeV, respectively. The LQ mass is considered as 1.1 TeV.

Benchmarks	$M_{N_{1,2,3}}$			Process	σ (fb)
BP1	(150, 1000, 1000)	(0.3, 0, 0)	(0, 0, 0)		221
BP ₂	(150, 1000, 1000)	(0.3, 0, 0)	(1, 0, 0)	iN_1	242
BP3	(1000, 1000, 150)	(0.3, 0, 0)	(0, 0, 1)	$\bar{t}N_{3}$	222

FIG. 5. Production cross section for ℓj , jN_1 , and $\bar{t}N_3$ at the LHeC with varying coupling Z_{11} . We have considered a 150 GeV electron beam colliding with a 7 TeV proton beam. The LQ mass has been set to 1.1 TeV. For l^-j , jN_1 , the coupling $Y_{11} = 0.3$, Z_{11} is varying and for $\bar{t}N_2$ production, the coupling $Y_{11} = 0.3$, Z_{12} is varying for $\bar{t}N_3$ production, the coupling $Y_{11} = 0.3$, Z_{33} is varying; the rest of the Yukawa couplings have been set to zero.

At an e^-p collider LQs can be resonantly produced, followed by their decay. Hence, we can write the cross section approximately as

$$
\sigma(e^-p \to e_i q \text{ or } N_i q)
$$

$$
\approx \sigma(e^-p \to \text{LQ}).\beta(\text{LQ} \to e_i q \text{ or } N_i q).
$$
 (10)

As can be seen from Eq. [\(9\)](#page-4-4), with increasing coupling Z_{11} the branching ratio of $\sigma(e^-p \rightarrow jN_1)$ increases, while $\sigma(e^-p \rightarrow l\bar{j})$ decreases. This results in a larger cross section for $\sigma(e^-p \to jN_1)$ for larger Z_{11} . Cross section for the other channel $e^-p \rightarrow \bar{t}N_3$ is also large for a large value of Z_{33} . The values of the cross section in fb, for three benchmark points are given in the last column of Table [I](#page-4-3). As can be seen, the production cross section at LHeC is fairly large, approximately $\sigma \sim 221-242$ fb for the chosen benchmark points. As we will show in the next section, folded with branching ratios of heavy neutrino, top quark,

FIG. 6. Production cross section for ℓj , jN_1 , and tN_3 with varying LQ mass M_{LQ} . For l^-j , jN_1 , and $\bar{t}N_3$ production we adopt BP1, BP2, and BP3, respectively.

the total cross section for the different final states will be sizable.

V. COLLIDER ANALYSIS

We implemented the model in FeynRules [\[95\]](#page-14-14) and generated the model files for MadGraph5_aMC@NLO $(v2 \t5 \t5)$ [\[96\]](#page-14-15) to calculate the parton level cross section for signals and background. For the collider simulation part, we passed the MadGraph generated parton level events to PYTHIA (v6.4.28) [\[97\]](#page-14-16), where subsequent decay, initial state radiation, final state radiation, and hadronization have been carried out. The jets are reconstructed by an anti- κ_t algorithim [\[98\]](#page-14-17) implemented in the Fastjetpackage [\[99\]](#page-14-18) with radius parameter $R = 0.4$. For the analysis of signal and background events we use the following set of basic cuts:

- (1) Electrons and muons in the final state should have the following transverse momentum and pseudorapidity $p_T^e > 20$ GeV, $|\eta^e| < 2.5$.
Lets are ordered in p_T jets sh
- (2) Jets are ordered in p_T , jets should have p_T^j > 40 GeV and $|\eta^j| < 2.5$.
Photons are counted if *n*
- (3) Photons are counted if $p_T^{\gamma} > 10$ GeV and $|\eta^{\gamma}| < 2.5$.
(4) Lets should be separated by $\Delta R_{\gamma} > 0.5$
- (4) Jets should be separated by $\Delta R_{ij} > 0.5$.
- (5) Leptons should be separated by $\Delta R_{\ell\ell} > 0.2$.
- (6) Leptons and photons isolation $\Delta R_{\ell\gamma} > 0.2$.
- (7) Jets and leptons should be separated by $\Delta R_{\ell i} > 0.4$.
- (8) Hadronic activity within a cone of radius 0.3 around a lepton must be limited to $\sum p_T^{\text{hadron}} < 0.2 p_T^e$, where p_T^{ℓ} is the transverse momentum of lepton within the specified cone.

Because of the initial and final state radiations, additional jets will be present in the final states considered. For the inverse seesaw framework, lepton number violation (LNV) is dictated by the parameter μ_X , which is negligibly small. Therefore, the cross section for LNV dilepton final states will be suppressed. For the framework where light neutrino masses are generated as a result of cancellation, sizable lepton number violation can, however, be present. Below,

Cuts	Final states	Signal (fb)	Background (fb)	
No cuts	$\ell^- + n - \text{jets}(1 \le n \le 2)$	220	2.96×10^{6}	
Basic cuts	$\ell^- + n - \text{jets}(1 \le n \le 2)$	159	4.08×10^{5}	
Leading lepton p_T cut	$+p_T^{\ell^-}$ (> 400 GeV)	118	178	
LQ invariant mass cut	$+ M_{\text{LO}} - M_{\ell_1 i_1} \leq 100 \text{ GeV}$	101		

TABLE II. Signal and background cross sections for the final state $l^+ + n - \text{jets}(1 \le n \le 2)$ after different cuts. BP1 has been used for this final state.

we adopt a conservative approach, and only consider lepton number conserving signatures. A number of signatures, including single lepton and multijet, dilepton associated with multijet and missing energy, and multilepton associated with missing energy and b jet have been analyzed in the subsequent sections.

VI. SIGNALS AND BACKGROUND

A. Signal I: $l^-\ + n - \text{jets}(1 \le n \le 2)$

The single-lepton associated with jet is the easiest channel to probe LQs. LQs, once produced resonantly, can directly decay to a charged lepton and a jet. Additionally, the t-channel contribution, as shown in Fig. [3](#page-4-1) will also be present. Therefore, the parton level final state is $l^+ + n - \text{jets}(n = 1)$. Additional jets will be present due to ISR, FSR. We demand the final state should contain ℓ^- and number of jets 1 ≤ n − jets ≤ 2. The main backgrounds arise from the SM process, such as, $e^-p \rightarrow \ell^-j, \ell^-jj$, which are significantly larger as compared to the signal. From Table [II](#page-6-1), the signal cross section is 220 fb, while the background cross section is 3×10^6 fb. We use a number of cuts on different kinematic variables to reduce the background.

In Fig. [7](#page-6-2) we have shown the transverse momentum of the leading lepton, leading and subleading jet, as well as the invariant mass distribution of the leading jet and leading lepton, both for the signal and background. Evidently, for a very heavy LQ, a high- p_T cut on the

FIG. 7. Distribution of transverse momentum p_T of the leading lepton, leading and subleading jet p_T distribution, and invariant mass distribution of the leading lepton and leading jet for the final state $l^+ + n -$ jets $(1 \le n \le 2)$.

FIG. 8. Feynman diagram for various final states from $e^-p \to jN$. For this case, a t-channel LQ mediated diagram can also contribute.

FIG. 9. Invariant mass distribution of a LQ p_T distribution of leading, subleading jet, and of the leading lepton. We also show the invariant mass distribution of N for the final state $l^+ + n - \text{jets}(n \geq 3)$.

leading jet or lepton, and LQ invariant mass cut will reduce the SM background drastically. In Table. [II,](#page-6-1) we have shown how we can reduce the SM background to zero using p_T cut— $p_T^{\ell^-}$ (>400GeV) on the leading
lepton and invariant mass cut— $|M_{\ell,0} - M_{\ell,0}|$ < 100 GeV lepton and invariant mass cut— $|M_{LQ} - M_{\ell_1j_1}| \leq 100 \text{ GeV}$ simultaneously after using the basic sets of cuts mentioned in the previous section.

B. Signal II

If the coupling Z_{ij} is nonzero, the LQ can also decay to a RH neutrino and a jet, as shown in the right panel of Fig. [8](#page-7-0). The considered final state, can also arise from the *t*-channel W exchange diagram as shown in left panel of Fig. [8](#page-7-0). For active-sterile mixing $V \sim 10^{-2} - 10^{-3}$, the contribution from the LQ, however, dominates. For example, with the BP2, the CC production cross section is \approx 12.7 fb, while the production cross section from LQ decay is \approx 240 fb. The subsequent decays of the RH neutrino, followed by hadronic and leptonic decays of gauge bosons gives rise to a number of partonic states that we list below.

(1) $l^+ + n - \text{jets}(n = 3)$ (For hadronic decays of W⁺) (2) $l^+ + l^+ + n - \text{jets}(n = 1) + \not{E}_T$ (For leptonic decays of W^+)

1. $l^-\ + n - \text{jets}(n \geq 3)$

For the case of the hadronic decays of the charged gauge boson, we demand a charged lepton and at least three jets as the final state. The invariant mass of the three jets and the charged lepton must be equal to that of the mass of the LQ. Hence, a cut on the invariant mass distribution allows the separation of the signal from the backgound. For the background we generate $e^-p \rightarrow l^$ $n -$ jets up to $n = 3$. The distribution is given in the top
left panel of Fig. 9. Additionally, the leading jet that is left panel of Fig. [9.](#page-7-1) Additionally, the leading jet that is directly generated from LQ decay has a very high transverse momentum (see Fig. [9](#page-7-1)). Therefore, a large cut on the transverse momentum of the leading jet reduces the background. As can be seen from Table [III](#page-8-0), the large p_T cut on the leading jet itself reduces the background by $\mathcal{O}(10^4)$. Further reduction in background is achieved though a cut on the invariant mass distribution of the heavy neutrino. Stringent cuts, such as the cuts on the invariant mass of the LQ and the heavy neutrino make the background negligibly small.

2. $l^-\ell^+ + n - \text{jets}(n \geq 1) + E_T$

For the scenario, when a charged gauge boson produced in the decay of the RH neutrino decays leptonically, the signal will have 2 opposite sign charged leptons, jets (one or more), and missing energy. The dominant SM background comes from the processes like $e^-p \to \ell^- \ell^+ j \nu_\ell$ and $e^-p \rightarrow e^-e^+j j \nu_e$. The reduction of the background in this case is achieved by applying proper cuts on the missing energy, transverse momentum of the leading jet, and effective mass M_{EFF} . The M_{EFF} variable is defined as

$$
M_{\text{EFF}} = \sum_i p_{T_i}^j + \sum_i p_{T_i}^e + \cancel{E}_T,
$$

where $p_{T_i}^j$, $p_{T_i}^{\ell}$ are the transverse momentum of the jet and lepton, and E_T is the missing transverse energy. We expect a hard distribution for M_{EFF} , since the p_T of the lepton and jets coming mostly from resonantly produced LQs (as the t-channel contribution is small) is significantly large. The peak of the M_{EFF} shifts towards higher values with increasing LQ mass. We have shown in Fig. [10](#page-9-0) the missing energy E_T , M_{EFF} , leading jet, and leading lepton p_T distributions. The effect of different cuts on the signal and background cross sections are given in Table [IV.](#page-9-1)

C. Signal III

For the LQ mass more than $M_N + M_t$, it can further decay to $\bar{t}N_3$, which enables a final state with large lepton or large jet multiplicity, see Fig. [11](#page-10-1). The large lepton multiplicity is promising due to the suppressed SM background. For the $\bar{t}N_3$ production channel, considering subsequent decays of N_3 and \bar{t} , where N_3 is assumed to decay to $\tau^{\pm}W^{\mp}$, the following final states at the parton level are possible:

- (1) $\bar{b}\ell^-\tau^-\ell^+ + \not{E}_T$ (for leptonic decays of both the W bosons, $W^- \to \ell^- \nu$, $W^+ \to \ell^+ \nu$),
- (2) $\bar{b}\ell^-\tau^- + n \text{jets}(n = 2) + \not{E}_T$ (for the W boson decays, $W^- \rightarrow \ell^- \nu$ and $W^+ \rightarrow jj$,
- (3) $b\tau^{-}t^{+} + n \text{jets}(n = 2) + \mathcal{E}_T$ (for the W boson decays, $W^- \rightarrow jj$ and $W^+ \rightarrow \ell^+ \nu$),
- (4) $\bar{b}\tau^- + n \text{jets}(n = 4)$ (for the W boson decays, $W^- \rightarrow i j$ and $W^+ \rightarrow i j$).

We do not consider the last final states in our study because of very small cross section and very large SM background due to large jet multiplicity.

TABLE III. Signal and background cross sections for the final state $l^+ + n - \text{jets}(n \geq 3)$ with cuts. BP2 has been used for this final state.

Cuts	Final states	Signal (fb)	Background (fb)	
No cuts	ℓ^- + n – jets(n \geq 3)	24.8	2.99×10^{6}	
Basic cuts	ℓ^- + n – jets(n \geq 3)	7.65	2.9×10^{3}	
Leading Jet p_T cut	$+p_T^{j_1}$ (> 200 GeV)	6.56	180	
LQ invaraint mass cut	$+ M_{\text{LQ}} - M_{\ell_1 j_1 j_2 j_3} \leq 100 \text{ GeV}$	3.65	60	
N invaraint mass cut	$+ M_{N_1} - M_{\ell_1 i_a j_b} \leq 30$ GeV	3.08	θ	

FIG. 10. Missing transverse energy distribution, M_{EFF} distribution, p_T distribution of the leading jet, and leading lepton for the final state $l^-\ell^+ + n - \text{jets}$ $(n \ge 1) + E_T$.

1. $\bar{b}t^2 \tau^- t^+ + E_T$

For the final states involving τ and b, tagging can reduce the SM background significantly. We consider the p_T for the b and τ jets, as $p_T > 40$ GeV. In this work, we adopt a minimalistic approach and consider a flat 75% efficiency for b tagging and 60% efficiency for τ tagging. Similar to the previous case, the M_{EFF} distribution is hard due to the large missing energy and large transverse momenta of final state particles. For this signal, the most dominant SM backgound comes from the process $\bar{t}\ell$ [−]W⁺, $\bar{t}Z\nu$ and $\bar{t}h\nu$ with $\bar{t} \to \bar{b}\tau^-\nu$, $W^+ \to \ell^+\nu$, $Z \to \ell^+\ell^-$, and $h \to \ell^+\ell^-$. After applying the basic cuts only, the SM background drops significantly. In addition, we use missing energy E_T , leading jet p_T , and M_{EFF} distribution to further reduce the SM background.

2. $\bar{b}\ell^{-} \tau^{-} + n - \text{jets}(n \geq 2) + E_T$

For this case, due to large jet multiplicity, the SM background is greater than the previous signal and the background mainly comes from the process \bar{t} ℓ [−]W⁺. However, using missing energy E_T , cuts on leading jet p_T

TABLE IV. Signal and background cross section after various cuts for the final state $l^-\ell^+ + n -$ jets $(n \ge 1) + E_T$. BP2 has been used for this final state.

Cuts	Final states	Signal (fb)	Background (fb)	
No cuts	$\ell^{-} \ell^{+} + n - \text{jets}(n \geq 1) + \not{E}_{T}$	11.2	5.22×10^{2}	
Basic cuts	$\ell^{-} \ell^{+} + n - \text{jets}(n \geq 1) + E_T$	7.84	258	
Missing energy cut	$\ell^{-} \ell^{+} + n - \text{jets}(n \ge 1) + \mathcal{E}_T$ (> 100 GeV)	4.26	57.5	
Leading Jet p_T cut	$+p_T^{j_1}$ (> 300 GeV)	3.24	3.73	
M_{EFF} cuts	$+M_{\text{EFF}}(> 500 \text{ GeV})$	2.88	2.54	

and M_{EFF} distribution, the SM background can be reduced significantly.

3.
$$
\bar{b}\ell^+ \tau^- + n - \text{jets}(n \geq 2) + \not{E}_T
$$

For this final state, the SM background is actually negligibly small at the e^-p collider for the beam energies considered. The result is shown in Table [VII.](#page-12-1)

VII. SIGNAL STRENGTH FOR HIGHER LQ MASS

Bounds on LQs parameter space are expected to improve in the future with increasing luminosity at the LHC. Hence, we repeat our study for higher LQ masses. Though for higher LQ mass we can allow for large Yukawa coupling, we use the same coupling as for the 1.1 TeV LQ mass to compare our result for different LQ masses. Using the same set of cuts for each final state as we did for LQ mass 1.1 TeV, we have calculated the cross section for LQ mass of $1.2, 1.3, \ldots$, up to 1.7 TeV. The partonic cross sections and the effect of different cuts are shown in Tables [VIII](#page-12-2) and [IX.](#page-12-3)

A. Zero background case

First, we consider only final states for which the SM background is zero or can be reduced to zero using an invariant mass cut of LQ and RH neutrinos. The SM background is practically zero for final state $\bar{b}\ell^+\tau^- + n - \text{jets}$ $(n \geq 2) + \not\!{E}_T$. For the final state $l^2 + n - \text{jets}(1 \le n \le 2)$, using p_T^{ℓ} cut and LQ invariant mass cut (for corresponding I Q mass), the SM background mass cut (for corresponding LQ mass), the SM background can be reduced to zero. Similarly, for the final state, $l^+ + n - \text{jets}(n \ge 3)$, selection cut on p_T^j , along with on
LO invariant mass, and the invariant mass of the RH neutrino LQ invariant mass, and the invariant mass of the RH neutrino can make the SM background negligibly small. The results are given in Table [VIII.](#page-12-2) We have also shown the cross section as a function of LQ masses in Fig. [12](#page-10-2). As can be seen, the cross section for the $l^+ + n - \text{jets}(1 \le n \le 2)$ channel is the largest and varies $10^2 - 0.42$ fb for a wide range of LQ mass. With 100 fb⁻¹ luminosity, this predicts 10^4 number of events at LHeC. The other channel with jet multiplicity

FIG. 11. Feynman diagram for various final states from $e^-p \rightarrow \overline{t}N_3$. For this case also, the t-channel mediated diagram with gauge boson and LQ will contribute.

FIG. 12. Signal cross section as a function of LQ mass for different final states.

 $(n \geq 3)$ also offers a large cross section, and a large number of events $\mathcal{O}(10^2)$.

B. Nonzero background case

For the final states, $l^+ + n - \text{jets}(1 \le n \le 2)$ and $l^+ + n - \text{jets}(n \geq 3)$, the SM background is nonzero if we do not use the invariant mass of the LQ and RH neutrino. Since the LQ and RH neutrino masses are unknown, we do not implement the mass cut, rather in this section we show the cross sections with a very generic set of cuts. Assuming LQ mass to be more than 1 TeV, all the other cuts that we considered can be easily applied. For the above two final states we applied cuts only on p_T^{ℓ} and p_T^j . For final states, $\ell^- \ell^+ + n - \text{jets}$ $(n \ge 1) + \cancel{E}_T$,
 $\bar{b}\ell^- \tau^- \ell^+ + \cancel{E}_T$ and $\bar{b}\ell^- \tau^- + n - \text{jets}$ $(n \ge 2) + \cancel{E}_T$, $\bar{b}\ell^-\tau^-\ell^+ + \not E_T$ and $\bar{b}\ell^-\tau^- + n - \text{jets}$ $(n \geq 2) + \not E_T$ we used the same cuts as in Tables [IV,](#page-9-1) [V,](#page-11-0) and [VI](#page-11-1), respectively. We show the signal cross section and statistical significance with integrated luminosity of 100 fb⁻¹ in Fig. [13](#page-11-2). We also show the required luminosity to achieve 3σ and 5σ statistical significance in Fig. [14](#page-11-3). The statistical significance has been calculated using the following expression:

$$
S_{\text{sig}} = \frac{S}{\sqrt{S+B}},\tag{11}
$$

where, S and B denote the number of signal and background events, respectively.

1. Results

We discuss the discovery prospect of LQs in the mass range 1.1–1.7 TeV at LHeC. We have shown the significance for different final states with integrated luminosity 100 and 1000 fb⁻¹ for each LQ mass in the range 1.1–1.7 TeV in Table. [X.](#page-12-4) The channel $l^-\ + n$ jets $(1 \le n \le 2)$ is the most promising. For the final states

TABLE V. Signal and background cross section after various cuts for the final state $\bar{b}\ell^-\tau^-\ell^+ + E_T$. BP3 has been used for this final state.

Cuts	Final states	Signal (fb)	Background (fb)	
No cuts	$\bar{b}\ell^-\tau^-\ell^+ + \not\!{E}_T$	1.57	0.323	
Basic cuts	$\bar{b}\ell^-\tau^-\ell^+ + E_T$	0.83	7.51×10^{-3}	
Missing energy cut	$\bar{b}\ell^{-}\tau^{-}\ell^{+} + \bar{E}_{T} (> 100 \text{ GeV})$	0.502	4.46×10^{-3}	
Leading Jet p_T cut	$+p_T^{j_1}$ (> 100 GeV)	0.476	2.16×10^{-3}	
M_{EFF} cuts, b and τ tagging	$+M_{\text{EFF}}(> 500 \text{ GeV})$	0.21	7.7×10^{-4}	

TABLE VI. Signal and background cross section after various cuts for the final state $\bar{b}e^-\tau^- + n - \text{jets}(n \geq 2) + \mathcal{E}_T$. BP3 has been used for this final state.

FIG. 13. Left panel: the signal cross section as a function of LQ mass for different final states. Right panel: the significance with 100 fb[−]¹ luminosity.

FIG. 14. The required luminosity to achieve 3σ (left panel) and 5σ (right panel) for different final states.

TABLE VII. Signal and background cross section after various cuts for the final state $\bar{b}\ell^+\tau^- + n - \text{jets}(n \geq 2) + \mathbb{E}_T$. BP3 has been used for this final state.

Final states	Signal (fb)	Background (fb)	
$\bar{b}\ell^+\tau^- + n - \text{jets}(n \geq 2) + \not{E}_T$	4.07		
$\bar{b}\ell^+\tau^- + n - \text{jets}(n \geq 2) + \not{E}_T$. 83		

TABLE VIII. Cross sections (in fb) after all the cuts as a function of LQ mass.

Final states	1.1 TeV	1.2 TeV	1.3 TeV	1.4 TeV	1.5 TeV	1.6 TeV	1.7 TeV
$\ell^- + n - \text{jets}(1 \le n \le 2)$	101	47.53	18.37	6.148	2.04	0.82	0.42
ℓ^- + n – jets(n \geq 3)	3.08	.98	0.83	0.47	0.322	0.24	0.18
$\bar{b}\ell^+\tau^- + n - \text{jets}(n \geq 2) + \not{E}_T$	l.83	0.74	0.29	0.12	0.06	0.03	0.02

TABLE IX. Cross sections in fb, after all the cuts (except invariant LQs and right-handed neutrinos mass cut) as a function of LQ mass. Backgrounds are same as for 1.1 TeV as the beam energies are same.

Final states	1.1 TeV	1.2 TeV	1.3 TeV	1.4 TeV	1.5 TeV	1.6 TeV	1.7 TeV
$\ell^- + n - \text{jets}(1 \le n \le 2)$	118	57	23		2.8	1.16	0.62
ℓ^- + n – jets(n \geq 3)	6.56	2.36		0.5	0.32	0.23	0.18
$\ell^- \ell^+ + n - \text{jets}(n \geq 1) + \mathbb{E}_T$	2.88	1.38	0.57	0.23	0.102	0.057	0.039
$\bar{b}\ell^-\tau^-\ell^+ + \not\!{E}_T$	0.21	0.08	0.03	0.012	0.007	0.003	0.0018
$\bar{b}\ell^{-} \tau^{-} + n - \text{jets}(n \geq 2) + \not{E}_{\tau}$	0.522	0.175	0.063	0.025	0.013	0.008	0.006

TABLE X. Significance for different final states with integrated luminosity $\mathcal{L} = 100$ fb⁻¹ (1st column corresponding to each LQ mass) and $\mathcal{L} = 1000$ fb⁻¹ (2nd column corresponding to each LQ mass), respectively, for the LQ mass range [1.1–1.7] TeV.

 $l^+ + n - \text{jets}(1 \le n \le 2)$, even with integrated luminosity 2 fb⁻¹, the statistical significance is 9.69 σ for the LQ of mass 1.1 TeV.

For final states $l^+ + n - \text{jets}(n \geq 3)$ and $l^-l^+ + n$ jets $(n \ge 1) + \mathbf{E}_T$, statistical significance drastically decreases with higher LQ masses. Similarly for the final states $\bar{b}\ell^-\tau^-\ell^+ + \not{E_T}$ and $\bar{b}\ell^-\tau^- + n - \text{jets}(n \geq 2) + \not{E_T}$, in spite of the small SM background, as the signal cross section is itself small for higher LQ masses, it is difficult to observe these final states for higher LQ masses.

VIII. CONCLUSIONS

In this work, we study the discovery prospect of the \tilde{R}_2 class of the LQ model at the LHeC. The model contains two LQs with $Q = \frac{2}{3}$ and $Q = -\frac{1}{3}$. The LQ with $Q = \frac{2}{3}$ can be conjourly produced at LHeC due to its interaction with the copiously produced at LHeC due to its interaction with the electron and down-type quark. We study the production and its decay to different final states, including a lepton and a jet, a jet and a RH neutrino, and a RH neutrino and a top quark. The typical production cross sections for $e^-p \rightarrow$ $lj, jN_1, \bar{t}N_3$ are 221, 242, and 222 fb for $M_{\text{LQ}} = 1.1 \text{ TeV}$, $M_{N_{13}} = 150$ GeV, and the couplings $Y_{11} = 0.3, Z_{33} = 1.$ The produced RH neutrino further decays and gives a plethora of model signatures. For the RH neutrinos, we adopt a model independent framework, and a large activesterile mixing to ensure its decay within the detector. For the LQs, the higher production cross section as well as the lower backgrounds at the LHeC result in a much higher statistical significance for a few of the signals studied.

We have analyzed a number of final states, including $l^2 + n - \text{jets}$ (1≤n≤2), $l^{\pm} + n - \text{jets}(n \ge 3)$, $l^{\pm} l^{\mp} + n - \text{jets}(n > 1) + k^{\pm}$, $\bar{b}l^{\pm} - \bar{c}l^{\pm} + k^{\pm}$, $\bar{b}l^{\pm} - \bar{c}l^{\pm} + n - \text{jets}(n > 2) + \bar{c}l^{\pm}$ jets $(n\geq 1)+E_T$, $\bar{b}\ell^-\tau^-\ell^++E_T$, $\bar{b}\ell^-\tau^-+n-\text{jets}(n\geq 2)+$ E_T , $\bar{b}\ell^+\tau^- + n - \text{jets}(n\geq 2) + \bar{E}_T$. Among these, the model signature $l^+ + n - \text{jets}(1 \le n \le 2)$ arises due to the direct decay of LQ to a lepton and a jet. All the other final states arise due to the decay of the LQ to a RH neutrino and a light jet, or to a RH neutrino and top quark, with successive decays of the RH neutrino, and a t quark into SM states.

We find that, among all the above mentioned final states, $l^+ + n - \text{jets}(1 \le n \le 2)$ has the highest discovery prospect even after giving a generic set of cuts. A LQ of mass up to 1.4 TeV in this channel can be discovered at more than 5σ C.L. with 100 fb⁻¹ of data. The LQs will also result in the enhancement of the RH neutrino production in association with a light jet, or with a top quark. If at LHeC the electron beam is polarized, the right-handed neutrino-light jet production cross section can substantially increase [\[46,47\].](#page-13-15) We find that among all the final states $l^+ + n - \text{jets}(n \geq 3)$, and $\bar{b}\ell^+ \tau^- + n - \text{jets}(n \geq 2) + \bar{E}_T$ are the most optimal, after implementing the selection cuts judiciously. With 100 fb⁻¹ integrated luminosity, for LO mass 1.1 TeV, the expected number of events for the final sates $l^+ + n - \text{jets}(n \ge 3)$, and $\bar{b}\ell^+ \tau^- + n - \text{jets}(n \ge 2) + \bar{E}_T$ are $10⁴$ and 180, respectively.

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Correction: The previously published Figure 4 contained a plotting error and has been replaced.