# IceCube can constrain the intrinsic charm of the proton

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The discovery of extraterrestrial neutrinos in the ~30 TeV–PeV energy range by IceCube provides new constraints on high energy astrophysics. An important background to the signal are the prompt neutrinos which originate from the decay of charm hadrons produced by high energy cosmic-ray particles interacting in the Earth's atmosphere. It is conventional to use the calculations of charm hadroproduction using gluon splitting  $g \rightarrow c\bar{c}$  alone. However, QCD predicts an additional "intrinsic" component of the heavy quark distribution which arises from diagrams where heavy quarks are multiply connected to the proton's valence quarks. We estimate the prompt neutrino spectrum due to intrinsic charm. We find that the atmospheric prompt neutrino flux from intrinsic charm is comparable to those calculated using QCD computations not including intrinsic charm, once we normalize the intrinsic charm differential cross sections to the ISR and the LEBC-MPS collaboration data. In the future, IceCube will constrain the intrinsic charm content of the proton and will contribute to one of the major questions in high energy physics phenomenology.

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# I. INTRODUCTION

Astrophysical neutrinos  $(\equiv \nu + \bar{\nu})$  discovered by IceCube provide new insights on profound astrophysics and particle physics questions [1–7]. Many astrophysical models have been proposed to explain these events [8–33] and to constrain various processes [34–55]. These have spurred development of new signatures such as the through-going tracks caused by  $\tau$  leptons [25] and the echo technique [56].

IceCube has detected an excess of neutrinos over the atmospheric neutrino background; however: how well do we know the background? The contribution of conventional atmospheric neutrinos, produced from the decays of  $\pi$ 's and K's, is known to ~20%–30% precision depending on the energy [57–59]. The major background uncertainty comes from  $pp \rightarrow cX$ , which results in prompt neutrinos produced from the decay of charm hadrons [60–85]. The flavor ratio of prompt neutrinos is  $\nu_e:\nu_\mu:\nu_\tau \approx 1:1:0.1$ , and  $\nu:\bar{\nu} = 1:1$ .

Most calculations of the prompt neutrino spectrum from charm hadroproduction are based within perturbative QCD (pQCD) gluon splitting  $g \rightarrow c\bar{c}$  alone [62–70,72–80,84– 86]. Inclusion of nonperturbative effects, for e.g., intrinsic charm [87–90], have received much less consideration [60,61]. Recently attention has been drawn to forward production of charm hadrons by Refs. [82,83]. Intrinsic charm is a rigorous prediction of QCD (see Supplemental Material [91]) and it is important to estimate its effect on atmospheric prompt neutrinos.

The important distinction between intrinsic charm and gluon splitting is that intrinsic charm uses the incoming proton energy much more efficiently due to its harder  $d\sigma/dx_F$  distribution. Inclusion of nonperturbative effects are important since the amount of intrinsic charm is an important uncertainty in QCD simulations. Due to its inherent nonperturbative nature, it has not yet been calculated from first principles, and thus its normalization must be inferred from experiment. Experiments have not yet decisively measured the normalization of intrinsic charm in the proton, which typically dominates the differential cross section at high  $x_F$ .

Various experimental techniques have been suggested for measuring atmospheric prompt neutrinos [92–95]. These studies illustrate how measurements can constrain the underlying QCD mechanism in regions of the parameter space where it is difficult to obtain constraints from colliders [79].

IceCube compares the prompt neutrino spectrum derived by Enberg, Reno and Sarcevic (with modifications by Gaisser) (ERS w/G) [68,69,81] with their data. The present upper limits on the prompt neutrinos are near the nominal predictions [6,7,96]. An additional contribution to the prompt neutrino spectrum can change the interpretation of the astrophysical neutrinos.

In this paper, we calculate the prompt neutrino contribution from intrinsic charm after normalizing the differential cross section to the ISR and the LEBC-MPS collaboration data [97,98]. This contribution must be added to the  $g \rightarrow c\bar{c}$  contribution to obtain the total atmospheric

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prompt neutrino spectrum. We show that the prompt neutrino flux from intrinsic charm can be comparable to those calculated within QCD computations not including intrinsic charm. The inclusion of this component as a background in the atmospheric neutrino flux can have important implications on the flux and spectral shape of the "IceCube excess neutrinos."

We emphasize that IceCube can test these differential cross sections which have proven to be difficult to measure in colliders. This synergy between IceCube and the collider searches [99–102] can constrain the normalization of the intrinsic charm contribution and contribute to the investigation of a  $\sim$ 36 year old puzzle in QCD.

# **II. CALCULATIONS OF NEUTRINO FLUXES**

The earliest prompt neutrino calculations employed a proton-only cosmic ray flux known as the "broken powerlaw" [61,62,68,103,104]. Recent observations of cosmic ray flux indicate a mixed composition [105–107]: the Gaisser 2012 fit [105] with (i) the third component being proton (H3P), or (ii) mixed (H3A), and the Stanev *et al.*, 2014 fit [107] fit with (iii) three (H14A), or (iv) four cosmic ray populations (H14B). We convert these to an equivalent allproton flux,  $\phi_p(E, X)$ , where *E* and *X* denote the proton energy and the atmospheric column depth, respectively [74].

Assuming that the fluxes are separable in energy and column depth, we write the cascade equations as [61,62,68, 74,76,108,109]

$$\frac{d\phi_p(E,X)}{dX} = -\frac{\phi_p(E,X)}{\lambda_p(E)} + Z_{pp}(E)\frac{\phi_p(E,X)}{\lambda_p(E)},\quad(1)$$

$$\frac{d\phi_m(E,X)}{dX} = -\frac{\phi_m(E,X)}{\rho(X)\delta_m(E)} - \frac{\phi_m(E,X)}{\lambda_m(E)} + Z_{mm}(E)\frac{\phi_m(E,X)}{\lambda_m(E)} + Z_{pm}(E)\frac{\phi_p(E,X)}{\lambda_p(E)},$$
(2)

$$\frac{d\phi_{\ell}(E,X)}{dX} = \sum_{m} Z_{m\ell}(E) \frac{\phi_m(E,X)}{\rho(X)\delta_m(E)},$$
(3)

where  $\lambda_p(E)$  [ $\lambda_m(E)$ ] denotes the nucleon [charm hadron] attenuation length. The charm hadron flux [lepton flux from the decay of charm hadron] are denoted by  $\phi_m(E, X)$  [ $\phi_{\ell}(E, X)$ ]. The atmospheric density and charm hadron decay length is denoted by  $\rho(X)$  and  $\delta_m(E)$ , respectively. The sum includes the contribution of all the relevant charm hadrons.

The production moments  $Z_{pp}(E)$ ,  $Z_{mm}(E)$ , and  $Z_{pm}(E)$ are defined as [62]

$$Z_{kj}(E) = \int_0^1 \frac{dx_E}{x_E} \frac{\phi_k(\frac{E}{x_E}, 0)}{\phi_k(E, 0)} \frac{\lambda_k(E)}{\lambda_k(\frac{E}{x_E})} \frac{dn_{kj}}{dx_E} (E/x_E), \quad (4)$$

where  $x_E = E/E_k$ , and  $dn_{kj}(E/x_E)/dx_E$  denote the production spectrum of *j* from the interaction of *k* with the air nucleon. The decay moments  $Z_{m\ell}(E)$  are calculated following Refs. [62,68].

For  $\lambda_p(E)$ , we take the mean atomic number of air molecules,  $\langle A \rangle = 14.5$ . For the proton—air cross section, we take the values from QGSJet0.1c [110]. Additional parameters required to calculate  $Z_{pp}(E)$ ,  $Z_{mm}(E)$  and  $\lambda_m(E)$  are taken from Refs. [62,73].

The calculation of  $Z_{pm}(E)$  involves the differential cross section  $\frac{d\sigma}{dx_F}(pp \to cX)$ . There are substantial uncertainties in this differential cross section, especially at high  $x_F$ . Modern colliders are not capable of measuring this differential cross section in the forward region (high  $x_F$ ) [79]. State of the art calculations, which incorporate various different constraints, are also lacking for these differential cross sections at high  $x_F$ . Taking these uncertainties into account, we adopt three test cases using the data presented by the ISR experiments and the LEBC-MPS collaboration.

Case (A): For  $\Lambda_c$  production, we use Ref. [111] which normalizes their differential cross section to the ISR data [97]. For *D* mesons, we use the shape of the differential cross sections as calculated in Ref. [112], and normalize them to the data at the highest  $x_F (d\sigma/dx_F \approx 17^{+18}_{-9} \ \mu b at x_F \approx 0.32)$ as measured by the LEBC-MPS collaboration [98].

Although the LEBC-MPS measurements extend to the forward region,  $x_F \approx 0.32 \pm 0.08$ , yet due to the uncertainties in the theoretical prediction and experimental measurements, it is difficult to estimate the contribution of intrinsic charm from this. Our strategy is to use the best-fit prediction following Ref. [73] ( $\approx 10 \ \mu b$  at  $x_F = 0.32$ ), and use the error bars of the LEBC-MPS measurement to maximize the intrinsic charm contribution. This sets the normalization for the *D* mesons.

Case (B): We use the charm hadron differential cross section spectral shapes as derived by Ref. [112]. To normalize these, we assume that the intrinsic charm cross section  $d\sigma/dx_F \approx 25 \ \mu$ b at  $x_F \approx 0.32$  for the *D* mesons. Since we are using the same model for the *D* mesons and the  $\Lambda_c$  production, this also gives the normalization of the  $\Lambda_c$  cross section.

Case (C): We again use the charm hadron differential cross section spectral shape as derived by Ref. [112]. We normalize the cross section such that the intrinsic charm cross section  $d\sigma/dx_F \approx 7 \ \mu b$  at  $x_F \approx 0.32$  for the *D* mesons. This corresponds to the best fit point of the LEBC-MPS measurement. Similar to Case (B), we use the same production model for *D* mesons and  $\Lambda_c$  production. The above mentioned differential cross section for the *D* mesons also set the normalization for the  $\Lambda_c$  production.

The cross sections for various charm mesons and hadrons at  $\sqrt{s} \approx 39$  GeV for the three cases discussed

TABLE I. Production cross sections (in  $\mu$ b) at  $\sqrt{s} \approx 39$  GeV for the various charm mesons and baryons via the intrinsic charm models discussed in the text. Here  $\sigma(D_{(s)}^{\pm}) = \sigma(D_{(s)}^{+}) + \sigma(D_{(s)}^{-})$ and  $\sigma(\Lambda_c^{\pm}) = \sigma(\Lambda_c^{+}) + \sigma(\Lambda_c^{-})$ .

Case	$\sigma(D^{\pm})$	$\sigma(D^0+ar D^0)$	$\sigma(D_s^{\pm})$	$\sigma(\Lambda_c^{\pm})$
Case A	3.88	3.88	2.29	183.54
Case B	3.88	3.88	2.29	4.99
Case C	1.09	1.09	0.64	1.47

above are given in Table I. The cross section for the production of  $\Lambda_c^+ + \Lambda_c^-$  in Case A is anomalously high as the normalization is fit to the ISR data. The production cross section for these charmed bound states in the other cases are  $\sim \mathcal{O}(\mu b)$  and these are normalized to the LEBC-MPS data.

We illustrate the uncertainty of the intrinsic charm flux by the three cases as mentioned above. The Case (C) does not represent a lower limit to the intrinsic charm contribution to the differential cross section. It is possible that the intrinsic charm contribution is lower, and this will correspond to a lower contribution to the atmospheric prompt neutrino flux compared to what is presented here. As is evident from our discussion, the intrinsic charm cross section is not at all well known. Despite decades of effort, colliders have not yet been able to definitively measure its normalization. We examine the role of IceCube in this search.

The intrinsic charm cross section scales with the mass number, *A*, approximately as  $A^{0.755\pm0.016}$ , according to SELEX [113]. The energy dependence of the intrinsic charm contribution follows the inelastic cross section [114].

We solve Eqs. (1)–(3) separately in the low and high energy regime [61,62,68,74,76]. The final prompt neutrino flux is a geometric interpolation of the low and high energy solutions and includes the contribution of all the charm hadrons,  $D^0$ ,  $\bar{D}^0$ ,  $D^{\pm}$ ,  $D_s^{\pm}$ ,  $\Lambda_c^{\pm}$ . The  $\Lambda_c$  shares a c-quark from the |uudcc̄⟩ state of the proton, and thus has a harder differential cross section  $d\sigma/dx_F$  when compared to that of the *D* mesons.

Our calculation improves over the previous estimates [60,61,82,83,86] in various important ways. We normalize our calculations to the ISR and the LEBC-MPS collaboration data [97,98], which were not used in the earliest works. We employ the latest cosmic ray flux measurement, and the experimentally measured nuclear scaling of the cross section, and a theoretically motivated energy dependence of the cross section. We use a more updated calculation of the intrinsic charm cross section which takes into account the inherent nonperturbativeness of the process [111,112], whereas some of these earlier works [82,83] used a modified pQCD prescription to account for the high  $x_F$  data.

#### **III. RESULTS**

Our predictions for the flux of neutrinos  $(\nu_{\mu} + \bar{\nu}_{\mu})$  or  $\nu_e + \bar{\nu}_e$  are shown in Fig. 1. The three flux scenarios are

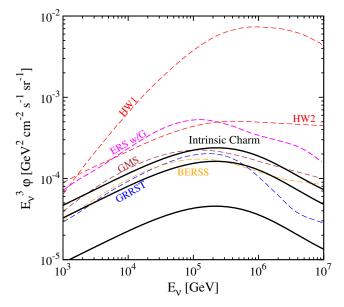


FIG. 1. Predictions for the atmospheric prompt neutrino  $(\nu_e + \bar{\nu}_e \text{ or } \nu_\mu + \bar{\nu}_\mu)$  spectrum,  $\varphi$ , as a function of the neutrino energy  $E_\nu$  using the H3A cosmic ray input flux. We show (i) GRRST [74], (ii) BERSS [73], (iii) GMS [76], (iv) ERS w/G [68,69], (v) HW1 [82], (vi) HW2 [83], and (vii) our calculation (Intrinsic Charm). The highest, intermediate, and the lowest flux from the intrinsic charm contribution correspond to Case (A), Case (B), and Case (C) respectively. See text for details. The upper limit from the IceCube data on the prompt neutrino flux is 1.06 times the ERS w/G flux [7].

given by Case (A), Case (B), and Case (C). We also show the best-fit flux calculated by BERSS [73], GMS [76], GRRST [74], HW1 [82], HW2 [83], and ERS w/G [6,96], all of which have large theoretical error bars. Remarkably, we find that the atmospheric prompt neutrino flux due to intrinsic charm can be at the same level as those estimated within QCD calculations not including intrinsic charm.

The neutrino fluxes due to intrinsic charm can be large enough to be detectable by IceCube. The detectability depends on the contribution of the fluxes arising from QCD not including intrinsic charm. For example, if the best fit prediction follows the BERSS flux, and the intrinsic charm contribution is as large as Case (B), then IceCube can get a strong constraint on intrinsic charm provided the uncertainties in BERSS are made smaller. It is important to decrease the uncertainties within the various pQCD predictions in order to obtain a robust constraint on intrinsic charm; global analyses of laboratory data also have this same requirement [115,116].

For case (A), the dominant contribution to the flux comes from the production of  $\Lambda_c^{\pm}$ , followed by  $D^{\pm}$ ,  $D^0 + \bar{D}^0$ , and  $D_s^{\pm}$ . For cases (B) and (C), the production of  $D^{\pm}$ ,  $D^0 + \bar{D}^0$ ,  $D_s^{\pm}$ , and  $\Lambda_c^{\pm}$  contribute to the atmospheric prompt neutrino flux in decreasing order. These contributions can be simply understood by comparing their respective production cross

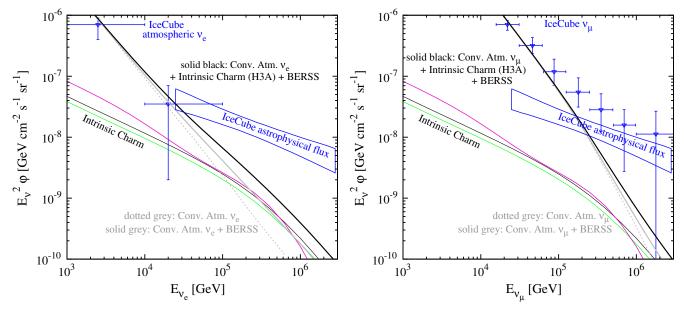


FIG. 2. Left: Comparison of the total atmospheric  $\nu_e + \bar{\nu}_e$  data (IceCube-86 for 332 days) with calculations. The contribution to the  $\nu_e + \bar{\nu}_e$  flux from intrinsic charm for Case (A) for various cosmic ray spectra is shown by the dashed lines (H3A = magenta, H3P = green, H14A = brown, and H14B = magenta. H14A and H14B are on top of each other). The conventional  $\nu_e + \bar{\nu}_e$  flux [117], conventional  $\nu_e + \bar{\nu}_e + BERSS$  (H3A), and conventional  $\nu_e + \bar{\nu}_e + BERSS + intrinsic charm contribution for H3A are shown. Right: Same as the left panel, but for <math>\nu_\mu + \bar{\nu}_\mu$  [6] (IceCube-79/86 for 2 years). This measurement also includes the astrophysical neutrino flux. The astrophysical flux shown in these panels is from Refs. [4].

sections (see Table I) multiplied by the decay branching fractions to neutrinos.

If the intrinsic charm contribution follows Case (C), and the nonintrinsic charm contribution follows the BERSS flux, then it will be difficult to measure the intrinsic charm unless very precise measurements of the atmospheric prompt neutrino fluxes are made. Even in this pessimistic case, weak upper limits on intrinsic charm can be obtained from the data. Encouragingly, present IceCube constraints have already started to constrain the forward production within the various QCD computations not including intrinsic charm [80,84,85]. It is expected that near future measurements of the prompt atmospheric neutrino flux will further constrain these various contributions in pQCD.

In the intrinsic charm picture, the proton preferentially forms a charm hadron with a similar energy. In the  $g \rightarrow c\bar{c}$ picture, due to its steeply falling  $d\sigma/dx$  distribution, the charm hadron comes dominantly from a proton at much higher energy. Our results are slightly lower than the calculation presented in Ref. [83] due to the above mentioned refinements.

So far, IceCube has presented upper bounds on prompt neutrinos. IceCube assumes that the prompt neutrino flux is the ERS w/G spectrum and varies the normalization. The present limit on the prompt neutrino spectrum is 1.06 times the ERS w/G flux [7]. These IceCube limits are close to the intrinsic charm prompt neutrino spectrum predictions, implying that IceCube can give information about intrinsic charm content of the proton in the near future. In Fig. 2 (left), we compare our calculation for Case (A) and the measurement of the atmospheric  $\nu_e$  flux [117]. The conventional atmospheric  $\nu_e + \bar{\nu}_e$  flux (angular averaged) is taken from Refs. [57,58,117]. The conventional atmospheric  $\nu_e$  + BERSS flux, the prompt  $\nu_e$  flux due to intrinsic charm in case (A) for various different input cosmic ray model, the total atmospheric  $\nu_e$  flux including the BERSS and due to intrinsic charm in case (A) for the H3A cosmic ray input model are also shown. We also show the astrophysical neutrino spectrum from Ref. [4] in the energy range [25 TeV, 2.8 PeV]. This shows that although the inclusion of the intrinsic charm component can change the background for astrophysical neutrinos, yet atmospheric prompt neutrinos cannot explain the "IceCube excess neutrinos".

Normalizing to the ISR and the LEBC-MPS collaboration data does not contradict the atmospheric  $\nu_e$  measurements. The importance of atmospheric  $\nu_e$  measurement for prompt neutrinos was pointed out in Ref. [93], and we argue that it might be the best channel to search for intrinsic charm as well. We predict that the atmospheric  $\nu_e + \bar{\nu}_e$  flux due to intrinsic charm is larger than  $g \rightarrow c\bar{c}$  contribution at  $\gtrsim 50$  TeV. A more precise measurement of the atmospheric  $\nu_e$  spectrum at slightly higher energies can give strong constraints on the intrinsic charm content of the proton.

Atmospheric prompt neutrinos cannot explain the "IceCube excess neutrinos" since prompt neutrinos have a softer spectral shape and have accompanying muons. The "IceCube excess neutrinos" have an energy spectrum varying within  $\sim E^{-2.1}$  and  $E^{-2.6}$  between  $\sim 30$  TeV and 3 PeV and do not have any accompanying muons. The

prompt neutrino flux follows the much softer cosmic ray spectrum.

For downgoing events, the IceCube self-veto can discriminate between atmospheric and astrophysical neutrinos [118,119]. Every atmospheric neutrino is accompanied by a muon or an electromagnetic shower from the same interaction producing the neutrino. The muon or the shower detected in coincidence with the neutrino, reduces the atmospheric neutrino flux by a factor  $\gtrsim 2$  at energies  $\gtrsim 10$  TeV [3]. This also results in a difference in the zenith angle distributions of astrophysical and prompt neutrinos.

The angular distribution of atmospheric prompt neutrinos is approximately isotropic at  $\leq 10^7$  GeV. Conventional atmospheric neutrinos have a smaller vertical flux compared to the horizontal flux. Searching for atmospheric neutrinos in the vertical direction can more easily find the prompt component. More theoretical and experimental work is also required to narrow down the uncertainties of the predictions made within pQCD calculation to extract the contribution of intrinsic charm from the IceCube data.

A comparison of the  $\nu_{\mu} + \bar{\nu}_{\mu}$  flux from the Northern Hemisphere with calculations is shown Fig. 2 (right) [6]. The intrinsic charm component is shown for Case (A). The astrophysical neutrino spectrum in the energy range [25 TeV, 2.8 PeV] from Ref. [4] is shown. The neutrino flux due to intrinsic charm cannot increase, since it will be in contradiction with the ISR and the LEBC-MPS collaboration data. The inclusion of this contribution may result in a revision of the astrophysical neutrino spectrum. Since these events are upgoing, the atmospheric veto does not play any role, and one needs to model the astrophysical neutrino flux before inferring the prompt neutrino contribution using this detection channel.

In Fig. 2, we only show the intrinsic charm contribution to the prompt atmospheric neutrino flux for Case (A). This has the largest flux among the three cases that we have considered, and hence we are displaying the optimistic case. For this case, the total prompt atmospheric neutrino flux is dominated by the intrinsic charm contribution. The intrinsic charm contribution in Case (B) is comparable to the best fit BERSS flux. If the intrinsic charm contribution follows Case (C), then the total prompt atmospheric neutrino flux will be totally dominated by the BERSS flux. In such case, upper limits on intrinsic charm of the proton can only be obtained if the prompt atmospheric neutrinos are measured quite precisely.

We only plot the best fit BERSS flux in Fig. 2 for clarity. We do not show the uncertainty in this flux which is substantial [73]. It is essential to decrease the uncertainties in this calculation to obtain a more robust constraint on intrinsic charm from astroparticle measurements.

Present upper limits from IceCube have already started to constrain various pQCD computations not including intrinsic charm, and near future data will have stronger constraints [80,84,85]. There are spectral differences between astrophysical neutrinos and prompt atmospheric neutrinos. IceCube uses a veto which produces a different angular dependence for the astrophysical neutrinos when compared to the prompt atmospheric neutrinos. These distinct features help in determining the atmospheric prompt neutrino sample in the IceCube data. Various different analyses of IceCube give similar upper limits on prompt atmospheric neutrinos implying that the constraint is robust.

# **IV. CONCLUSIONS**

The landmark discovery of astrophysical neutrinos by IceCube opens up a new era. Due to the atmospheric veto employed by IceCube, any atmospheric neutrino spectrum shows an up v/s down asymmetry. The excess of neutrinos unveiled by IceCube is isotropic implying the astrophysical origin of these events. Careful consideration of the atmospheric neutrino background will impact the astrophysical neutrino flux interpretation.

The neutrino backgrounds considered so far by IceCube are the conventional atmospheric and prompt neutrinos predicted by  $g \rightarrow c\bar{c}$ . Intrinsic charm, rigorously predicted by QCD, has strong theoretical justification and some experimental indications. We find that this often neglected component can be as large as the component estimated within the various pQCD computations not including intrinsic charm, without violating any direct experimental constraints. This has important implications in interpreting the astrophysical neutrino flux, and inferring the atmospheric prompt neutrino component.

We present our calculation of the neutrino flux due to intrinsic charm in Fig. 1 after normalizing to the ISR and the LEBC-MPS collaboration data. We show the atmospheric prompt neutrino flux due to three different scenarios. The atmospheric prompt neutrino flux due to intrinsic charm is comparable to that estimated within various pQCD computations not including intrinsic charm. Our calculation is lower than Refs. [82,83] as we use improved theoretical and experimental input.

The measurement of atmospheric  $\nu_e + \bar{\nu}_e$  at higher energies is the most promising channel to discover prompt neutrinos and constrain the intrinsic charm of the proton (Fig. 2 left). The comparison of the total atmospheric flux with the  $\nu_{\mu} + \bar{\nu}_{\mu}$  data, including the intrinsic charm contribution, is shown in Fig. 2 (right). The total atmospheric neutrino flux including intrinsic charm can dominate the flux contribution within the pQCD framework at energies  $\gtrsim 200$  TeV and  $\gtrsim 2$  PeV for  $\nu_e + \bar{\nu}_e$  and  $\nu_{\mu} + \bar{\nu}_{\mu}$ respectively.

The conventional atmospheric  $\nu_e + \bar{\nu}_e$  flux is lower, implying that the prompt component is more visible in this channel. We estimate that a measurement of the atmospheric  $\nu_e + \bar{\nu}_e$  flux at ~200 TeV at ~50% accuracy will cleanly distinguish between the pQCD contribution and intrinsic charm component.

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The current upper limit on prompt neutrinos is 1.06 times the ERS w/G flux. The neutrino flux due to intrinsic charm is at the same level as the ERS w/G flux implying that IceCube can constrain intrinsic charm of the proton. This shows that IceCube can constrain QCD predictions in regions of parameter space which have been difficult to constrain in colliders for decades.

The multi-pronged approach consisting of IceCube data, collider physics, and global analysis will help us constrain the intrinsic charm of the proton, a  $\sim$ 36 year old problem in QCD. Using the weakly interacting neutrino to constrain the strong interactions also highlights the importance of cross disciplinary searches in physics.

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