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# Lepton number violation, lepton flavor violation, and baryogenesis in left-right symmetric model

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We did a model independent phenomenological study of baryogenesis via leptogenesis, neutrinoless double beta decay (NDBD) and charged lepton flavor violation (CLFV) in a generic left-right symmetric model (LRSM) where neutrino mass originates from the type I + type II seesaw mechanism. We studied the new physics contributions to NDBD coming from the left-right gauge boson mixing and the heavy neutrino contribution within the framework of LRSM. We have considered the mass of the RH gauge boson to be specifically 5 TeV, 10 TeV, and 18 TeV and studied the effects of the new physics contributions on the effective mass and baryogenesis and compared with the current experimental limit. We tried to correlate the cosmological baryon asymmetry of the universe from resonant leptogenesis with the low energy observables, notably, NDBD and lepton flavor violation with a view to finding a common parameter space where they coexist.

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#### I. INTRODUCTION

The landmark discovery of neutrino flavor oscillations from neutrino experiments like MINOS [1], T2K [2], Double Chooz [3], Daya Bay [4], RENO [5], etc. and hence the evidence of neutrino mass and mixing have immense impact on our perception of the dynamics of the universe. Regardless of its enormous success, the standard model (SM) of particle physics is considered an insufficient theory, owing to the fact that it fails to address some of the vital questions like, the origin of the tiny neutrino mass, baryon asymmetry of the universe (BAU), dark matter (DM), lepton number violation (LNV), lepton flavor violation (LFV) and various other cosmological problems.

There are many beyond standard model (BSM) frameworks to realize these observables. Amongst them, the seesaw mechanism is the simplest way to understand the smallness of neutrino masses, which is further categorized into type I, type II, type III, Inverse seesaw (SS) mechanisms [6–9]. In type I seesaw, the introduction of SM gauge singlet RH neutrinos, gives rise to the light neutrino mass matrix of the form,  $M_{\nu} \approx -M_D M_{RR}^{-1} M_D^T$ , with a heavy-light neutrino mixing of order  $M_D M_{RR}^{-1}$ , where  $M_D$  and  $M_{RR}$  are the Dirac and Majorana masses respectively. Notwithstanding, one of the most appealing frameworks BSM, in which the seesaw mechanisms arises naturally is the left-right symmetric model (LRSM) which is based on the gauge group,  $SU(3)_c \times SU(2)_L \times SU(2)_R \times$  $U(1)_{R-I}$ . Here, the RH neutrinos are a necessary part of the model, which acquires a Majorana mass when the  $SU(2)_R$ symmetry is broken at a scale  $v_R$ . This is quite analogous to the way in which the charged fermions get masses in the SM by Higgs mechanism when  $SU(2)_L$  gauge symmetry is broken at a scale v.

The RH neutrinos which exist in the seesaw mechanism, besides explaining the neutrino flavor oscillation and neutrino mass can also throw light on one of the most enthralling problems of particle physics and cosmology, the matter-antimatter asymmetry of the universe, i.e, excess of baryons over antibaryons in the universe. The decay of the lightest right handed neutrino,  $N_1$  can naturally give rise to an excess of baryons over antibaryons in the universe consistent with the cosmological observable constrained by big bang nucleosynthesis and determined recently with a good precision by WMAP experiment as,

$$\eta_B = \frac{n_B}{n_\gamma} = (6.5^{+0.4}_{-0.3}) \times 10^{-10}.$$
(1)

The decay of  $N_1$  can satisfy all the three Sakharov conditions [10] as required for successful generation of  $\eta_B$  as there is sufficient CP and C violation, there is baryon number violation and can also occur out of thermal equilibrium. TeV scale LRSM provides an alluring class of SS models which can be probed at LHC. Matter antimatter asymmetry is now generated by a resonant baryogenesis mechanism with at least two quasidegenerate RH neutrinos in TeV range with a mass difference comparable to their decay widths [11]. The TeV scale new particles in LRSM also leads to interesting collider signals.

The possible observation of NDBD would play an important role in understanding the origin of BAU as it would imply that lepton number indeed is not conserved (one of the essential conditions for leptogenesis [12]). Furthermore, the Majorana nature [13] of neutrinos would also be established from NDBD. The latest experiments [14] that have improved the lower bound of the half life of

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the decay process include KamLAND-Zen [15] and GERDA [16] which uses Xenon-136 and Germanium-76 nuclei respectively. Incorporating the results from first and second phase of the experiment, KamLAND-Zen imposes the best lower limit on the decay half life using Xe-136 as  $T_{1/2}^{0\nu} > 1.07 \times 10^{26}$  yr at 90% CL and the corresponding upper limit of effective Majorana mass in the range (0.061-0.165) eV.

The observation of *CP* violation in lepton sector, in neutrino osillation experiment and NDBD would suggest the existence of *CP* violation at high energy which might be related to the one responsible for leptogenesis. The observation of LNV in NDBD and in addition possibly of *CP* violation in lepton sector would be a strong indication of leptogenesis as an explaination of baryon asymmetry. It would be interesting to explore the existence of *CP* violation in leptonic sector due to Majorana *CP* phases in the light of leptogenesis.

Another important issue of discussion in collider is the relative values of mass of the gauge bosons and heavy right handed neutrinos. However there are theoretical arguments based on vacuum stability which suggests that the heavy neutrinos are lighter than the RH gauge bosons that appears in the LRSM for a large parameter space. Again, it has been pointed out in literature that to account for a successful leptogenesis in TeV scale LRSM, the mass of the RH gauge boson,  $M_{W_p}$  has to be larger than the value obtainable at the LHCs. They have found a lower bound of 18 TeV for successful leptogenesis from the decay of heavy RH neutrino with maximum *CP* asymmetry,  $\varepsilon = 1$ . [17]. This result is much significant as it can provide a way to falsify leptogenesis, if mass of a gauge boson below this limit is found in experiments. From the significant outcome of the work, [17], the authors of [18] have shown that for specific symmetry textures of  $M_D$  and  $M_{RR}$  in the seesaw formula and by considering larger Yukawa couplings, the bound for leptogenesis can be largely weaker, i.e.  $M_{W_R} > 3$  TeV and  $M_N \le M_{W_R}$  which is possible owing to the sizeable reduction of dilution effects from  $W_R$  mediated decays and scatterings. They have again reanalyzed their work [18] in [19] and came out with a lower bound of  $M_{W_R} > 10$  TeV for successful leptogenesis in a generic LRSM with large light- heavy mixing. The consistency has also been pointed out for other low energy constraints like NDBD, LFV etc.

In LRSM, there are several contributions to NDBD that involve left and right handed sectors individually as well as others that involve both sectors through left-right mixing accompanied by both light and heavy neutrinos. Left-right mixing is always a ratio of the Dirac and Majorana mass scales  $(M_D M_{RR}^{-1})$  which appears in the type I seesaw formula. NDBD involving left-right mixing can be enhanced for specific Dirac matrices. For large left right mixing, significant contributions to NDBD arises from the mixed diagrams with simultaneous mediation of  $W_L$  and

 $W_R$  accompanied by light left handed neutrino and heavy right handed neutrinos, known as  $\lambda$  and  $\eta$  contributions to NDBD, although the latter is a bit suppressed by the mixing between left and right handed gauge bosons. It has been studied in many of the earlier works in the framework of LRSM (see Refs. [20–22]) The other new physics contributions are also suppressed for a larger gauge boson mass,  $M_{W_R} > 10$  TeV which gives sizeable baryogenesis. Furthermore, the LFV processes are seeking great interest in recent times as the experiments to detect them are becoming increasingly precise. The decay processes,  $(\mu \rightarrow 3e)$  and  $(\mu \rightarrow e\gamma)$  are simplest to detect with the current experimental limits for these low energy processes as  $< 1.0 \times 10^{-12}$  and  $< 4.2 \times 10^{-13}$  respectively.

Apart from the new physics contributions to NDBD in LRSM as available in literature, it is important to study the linkage between baryogenesis and other low scale phenomenon like NDBD, LFV, etc. In this context, with the previous results aforementioned in mind [17-22] we have done a phenomenological study of leptogenesis in TeV scale LRSM by considering different values of RH gauge boson mass within and above the current collider limits. In particular we have considered the  $SU(2)_R$  breaking scale to be 5 TeV, 10 TeV and 18 TeV (the bounds as available in literature) in order to check the consistency of the results and thereby tried to link baryogenesis with NDBD for these particular values of gauge boson mass. Again regarding the  $\lambda$  and  $\eta$  contributions to be valid, we need to have a large left-right mixing. But for a generic TeV scale seesaw model, without considering any particular structure for the Dirac and Majorana masses, in order to account for neutrino mass of the order of sub eV, keeping the heavy masses of TeV scale, the Dirac mass is of the order of MeV. This leads to a not so large left-right mixing parameter,  $\zeta \approx 10^{-6}$ . Since we have seen non-negligible effects of the momentum dependent mechanisms in NDBD for not so large left light mixing, we studied all the possible contributions to NDBD. To co-relate with baryogenesis, we have considered only the momentum dependent mechanisms of NDBD, i.e., the  $\lambda$  and  $\eta$  contributions to NDBD due to light-heavy and gauge boson mixing. Since the effective mass governing NDBD is dependent upon the Majorana phases,  $\alpha$  and  $\beta$ , it would be compelling to examine if there exist a link between NDBD and BAU. Besides, the study of LFV processes will also provide insights about the mechanism of NDBD. LRSM at the TeV scale interlinks high energy collider physics to the low energy observables like NDBD and other LFV processes. So we tried to correlate all these high and low energy phenomenon and find out if there exist a common parameter space accessible at colliders where leptogenesis can be simultaneously realized.

This paper is outlined as follows. In the next section, we present the left-right symmetric model framework with its particle contents and the origin of neutrino mass. In Sec. III,

we summarized the implications of TeV scale LRSM in processes like BAU and other low energy observables like NDBD, LFV. In Sec. IV, we present our numerical analysis and results and then give our conclusion in Sec. V.

# II. LEFT RIGHT SYMMETRIC MODEL(LRSM) AND NEUTRINO MASS

In the generic LRSM [23], the fermions are assigned to the gauge group  $SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$ [23,24] which is a very simple extension of the standard model gauge group,  $SU(3)_c \times SU(2)_L \times U(1)_Y$ , that provides a UV complete seesaw model where the type I and II seesaw arises naturally. Most of the problems like parity violation of weak interaction, masssless neutrinos, CP problems, hierarchy problems etc can be realized in the framework of LRSM. The seesaw scale is identified as the breaking of the  $SU(2)_R$  symmetry. In this model, the electric charge takes a form, $Q = T_{3L} + T_{3R} + \frac{B-L}{2}$  [25], where  $T_{3L}$  and  $T_{3R}$  are the 3rd components of isospin under  $SU(2)_L$  and  $SU(2)_R$ . In LRSM, the left and right handed components of the fields are treated on the same footing. The leptons (LH and RH) that transform in L-R symmetric gauge group are assigned with quantum numbers (1,2,1,-1) and (1,1,2,-1) respectively under  $SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$ . The Higgs sector in LRSM consists of two scalar triplets,  $\Delta_L(1,2,1,-1)$ ,  $\Delta_R(1,1,2,-1)$  and a Bidoublet with quantum number  $\phi(1,2,2,0)$ . A 2 × 2 matrix representation for the Higgs bidoublets and the  $SU(2)_{L,R}$  triplets is given as,

$$\phi = \begin{bmatrix} \phi_1^0 & \phi_1^+ \\ \phi_2^- & \phi_2^0 \end{bmatrix} \equiv (\phi_1, \tilde{\phi}_2),$$

$$\Delta_{L,R} = \begin{bmatrix} \delta_{\underline{L},R}^+ & \delta_{L,R}^{++} \\ \delta_{L,R}^0 & -\delta_{\underline{L},R}^{-+} \end{bmatrix}.$$
(2)

The VEVs of the neutral component of the Higgs field are  $v_R$ ,  $v_L$ ,  $k_1$ ,  $k_2$  respectively. The VEV  $v_R$  breaks the SU(2) $_R$  symmetry and sets the mass scale for the extra gauge bosons ( $W_R$  and Z') and for right handed neutrino field ( $v_R$ ). The VEVs  $k_1$  and  $k_2$  serves the twin purpose of breaking the remaining the SU(2) $_L \times$  U(1) $_{B-L}$  symmetry down to U(1) $_{\rm em}$ , thereby setting the mass scales for the observed  $W_L$  and Z bosons and providing Dirac masses for the quarks and leptons. Clearly,  $v_R$  must be significantly larger than  $k_1$  and  $k_2$  in order for  $W_R$  and Z' to have greater masses than the  $W_L$  and Z bosons.  $v_L$  is the VEV of  $\Delta_L$ , it plays a significant role in the seesaw relation which is the characteristics of the LR model and can be written as,

$$\langle \Delta_L \rangle = v_L = \frac{\gamma k^2}{v_R}.$$
 (3)

The Yukawa Lagrangian in the lepton sector is given by,

$$\mathcal{L} = h_{ij}\bar{\Psi}_{L,i}\phi\Psi_{R,j} + \widetilde{h}_{ij}\bar{\Psi}_{L,i}\tilde{\phi}\Psi_{R,j} + f_{L,ij}\Psi_{L,i}^{T}Ci\sigma_{2}\Delta_{L}\Psi_{L,j} + f_{R,ij}\Psi_{R,i}^{T}Ci\sigma_{2}\Delta_{R}\Psi_{R,j} + \text{H.c.}$$
(4)

Where the family indices i, j are summed over, the indices i, j=1, 2, 3 represents the three generations of fermions.  $C=i\gamma_2\gamma_0$  is the charge conjugation operator,  $\tilde{\phi}=\tau_2\phi^*\tau_2$  and  $\gamma_\mu$  are the Dirac matrices. Considering discrete parity symmetry, the Majorana Yukawa couplings  $f_L=f_R$  (for left-right symmetry) gives rises to Majorana neutrino mass after electroweak symmetry breaking when the triplet Higgs  $\Delta_L$  and  $\Delta_R$  acquires nonzero vacuum expectation value. Then equation (5) leads to  $6\times 6$  neutrino mass matrix as shown in reference 2 of [20]

$$M_{\nu} = \begin{bmatrix} M_{LL} & M_D \\ {M_D}^T & M_{RR} \end{bmatrix}, \tag{5}$$

where

$$M_D = \frac{1}{\sqrt{2}}(k_1 h + k_2 \tilde{h}), \qquad M_{LL} = \sqrt{2} v_L f_L,$$

$$M_{RR} = \sqrt{2} v_R f_R, \qquad (6)$$

where  $M_D$ ,  $M_{LL}$  and  $M_{RR}$  are the Dirac neutrino mass matrix, left handed and right handed mass matrix respectively. Assuming  $M_L \ll M_D \ll M_R$ , the light neutrino mass, generated within a type I + II seesaw can be written as,

$$M_{\nu} = M_{\nu}^{\mathrm{I}} + M_{\nu}^{\mathrm{II}}, \tag{7}$$

$$M_{\nu} = M_{LL} + M_D M_{RR}^{-1} M_D^T$$
  
=  $\sqrt{2} v_L f_L + \frac{k^2}{\sqrt{2} v_R} h_D f_R^{-1} h_D^T$ , (8)

where the first and second terms in Eq. (8) corresponds to type II seesaw and type I seesaw mediated by RH neutrino respectively. Here,

$$h_D = \frac{(k_1 h + k_2 \tilde{h})}{\sqrt{2}k}, \qquad k = \sqrt{|k_1|^2 + |k_2|^2}.$$
 (9)

In the context of LRSM both type I and type II seesaw terms can be written in terms of  $M_{RR}$  which arises naturally at a high energy scale as a result of spontaneous parity breaking. In LRSM the Majorana Yukawa couplings  $f_L$  and  $f_R$  are same (i.e.,  $f_L = f_R$ ) and the VEV for left-handed triplet  $v_L$  can be written as,

$$v_L = \frac{\gamma M_W^2}{v_R}.\tag{10}$$

Thus Eq. (8) can be written as

$$M_{\nu} = \gamma \left(\frac{M_W}{v_R}\right)^2 M_{RR} + M_D M_{RR}^{-1} M_D^T.$$
 (11)

In literature, (Refs. [22,26]) author define the dimensionless parameter  $\gamma$  as,

$$\gamma = \frac{\beta_1 k_1 k_2 + \beta_2 k_1^2 + \beta_3 k_2^2}{(2\rho_1 - \rho_3)k^2}.$$
 (12)

Here the terms  $\beta$ ,  $\rho$  are the dimensionless parameters that appears in the expression of the Higgs potential.

Again, the neutrino mass matrix as given in 5 can be digonalized by a  $6 \times 6$  unitary matrix, as follows,

$$\mathcal{V}^T M_{\nu} \mathcal{V} = \begin{bmatrix} \hat{M}_{\nu} & 0\\ 0 & \hat{M}_{RR} \end{bmatrix}, \tag{13}$$

where,  $\mathcal V$  represents the diagonalizing matrix of the full neutrino mass matrix,  $M_{\nu}$ ,  $\hat{M}_{\nu}=\mathrm{diag}(m_1,m_2,m_3)$ , with  $m_i$  being the light neutrino masses and  $\hat{M}_{RR}=\mathrm{diag}(M_1,M_2,M_3)$ , with  $M_i$  being the heavy RH neutrino masses. The diagonalizing matrix is represented as,

$$\mathcal{V} = \begin{bmatrix} U & S \\ T & V \end{bmatrix} \approx \begin{bmatrix} 1 - \frac{1}{2}RR^{\dagger} & R \\ -R^{\dagger} & 1 - \frac{1}{2}R^{\dagger}R \end{bmatrix} \begin{bmatrix} V_{\nu} & 0 \\ 0 & V_{R} \end{bmatrix}, \tag{14}$$

where, R describes the left-right mixing and given by,

$$R = M_D M_{RR}^{-1} + \mathcal{O}(M_D^3 (M_{RR}^{-1})^3). \tag{15}$$

The matrices U, V, S, and T are as follows,

$$U = \left[1 - \frac{1}{2} M_D M_{RR}^{-1} (M_D M_{RR}^{-1})^{\dagger}\right] V_{\nu}, \tag{16}$$

$$V = \left[1 - \frac{1}{2} (M_D M_{RR}^{-1})^{\dagger} M_D M_{RR}^{-1}\right] V_R, \tag{17}$$

$$S = M_D M_{RR}^{-1} v_R f_R, (18)$$

$$T = -(M_D M_{RR}^{-1})^{\dagger} V_{\nu}. \tag{19}$$

The leptonic charged current interaction in flavor basis is given by,

$$\mathcal{L}_{CC}^{\text{lepton}} = \frac{g}{\sqrt{2}} [\bar{l}' \gamma^{\mu} P_L \nu' W_{L_{\mu}}^{-} + \bar{l}' \gamma^{\mu} P_R \nu' W_{R_{\mu}}^{-}] + \text{H.c.}, \quad (20)$$

where,

$$\begin{bmatrix} W_L^{\pm} \\ W_R^{\pm} \end{bmatrix} = \begin{bmatrix} \cos \zeta & \sin \zeta e^{i\alpha} \\ -\sin \zeta e^{-i\alpha} & \cos \zeta \end{bmatrix} \begin{bmatrix} W_1^{\pm} \\ W_2^{\pm} \end{bmatrix}, \quad (21)$$

characterizes the mixing between L-R gauge bosons with,

$$\tan 2\zeta = -\frac{2k_1k_2}{v_R^2 - v_L^2}. (22)$$

With negligible mixing, the gauge boson masses become,

$$M_{W_L} \approx M_{W_1} \approx \frac{g}{2} k_+, \qquad M_{W_R} \approx M_{W_2} \approx \frac{g}{\sqrt{2}} v_R.$$
 (23)

Assuming  $k_2 < k_1 \Rightarrow \zeta \approx -\frac{k_1 k_2}{v_R^2} \approx -2 \frac{k_2}{k_1} (\frac{M_{W_L}}{M_{W_R}})^2$ . T and S in Eq. (14) describes the left-right mixing and can be written as  $\frac{L}{R}$ , gauge boson mixing angle  $\zeta$  is of order  $(\frac{L}{R})^2$ .

## III. RESONANT LEPTOGENESIS, NDBD, AND LFV IN TEV SCALE LRSM

As illustrated in several earlier works, for TeV scale seesaw models, a simple approach for generating adequate lepton asymmetry is to use resonant leptogenesis (RL) [27], which craves for at least two heavy RH Majorana neutrinos to be nearly degenerate, which we have already considered in our analysis. With quasidegenerate RH neutrino masses for at least two RH neutrinos, BAU/leptogenesis can be efficient at lower mass scales, but for this case generally a specific flavor structure is generally considered which allows for large Yukawa couplings which serves the twin purpose of leptogenesis to be efficient as well as it can be tested in experiments. Nevertheless, as far as Dirac neutrino mass matrix is concerned, we have not considered any particular structure of the matrix but a general form which is obtained from the type I seesaw when the Majorana mass matrix and the light neutrino mass matrix is considered to be known. The neutrino mass matrices is such that it fits the current neutrino oscillation data. The basic focus of our work is to relate the lepton asymmetry with the low observable phenomenons like NDBD, rather than only BAU and NDBD or LFV and to find a common parameter space where all them holds true.

In the framework of TeV scale LRSM, the presence of the RH neutrinos (type I SS) and the scalar triplets (type II SS) suggests their decays which give rise to lepton asymmetry. However we will only consider the decay of the heavy RH neutrinos for generating lepton asymmetry. The decay of the scalar triplet  $\Delta_L$  would not much affect on our result as above TeV scale, decay of RH neutrinos are in thermal equilibrium and hence they would wash out any kind of preexisting lepton asymmetry and so we have ignored it [19]. So the dominant contribution would come from the type I seesaw term.

The two heavy RH Majorana neutrinos decay via the decay modes,  $N_i \rightarrow l + \phi^c$  and its CP conjugate process,  $N_i \rightarrow l^c + \phi$  which can occur at both tree and one loop levels. Hence, their CP violating asymmetry  $\epsilon_i$  which arises from the interference between the tree level amplitude and its self-energy [28] correction is defined as [29],

$$\epsilon_i = \frac{\Gamma(N_i \to l + \phi^c) - \Gamma(N_i \to l^c + \phi)}{\Gamma(N_i \to l + \phi^c) + \Gamma(N_i \to l^c + \phi)}.$$
 (24)

The decay rates of the heavy neutrino decay processes are governed by the Yukawa couplings, and is given by,

$$\Gamma_i = (Y_\nu^\dagger Y_\nu)_{ii} \frac{M_i}{8\pi}.$$
 (25)

An essential condition for RL is that the mass difference between the two heavy RH neutrinos must be comparable to the decay width (i.e., $M_i - M_j \approx \Gamma$ ). In this case, the *CP* aymmetry becomes very large (even of order 1). The *CP* violating asymmetry  $e_i$  is thus given by,

$$\epsilon_{i} = \frac{\operatorname{Im}[(Y_{\nu}^{\dagger}Y_{\nu})_{ij}^{2}]}{(Y_{\nu}^{\dagger}Y_{\nu})_{11}(Y_{\nu}^{\dagger}Y_{\nu})_{22}} \cdot \frac{(M_{i}^{2} - M_{j}^{2})M_{i}\Gamma_{j}}{(M_{i}^{2} - M_{j}^{2}) + M_{i}^{2}\Gamma_{j}^{2}},$$
(26)

where,

$$\frac{\text{Im}[(Y_{\nu}^{\dagger}Y_{\nu})_{ij}^{2}]}{(Y_{\nu}^{\dagger}Y_{\nu})_{11}(Y_{\nu}^{\dagger}Y_{\nu})_{22}} \approx 1.$$
 (27)

The variables i, j run over 1 and 2,  $i \neq j$ .

The CP violating asymmetries  $\epsilon_1$  and  $\epsilon_2$  can give rise to a net lepton number asymmetry, provided the expansion rate of the universe is larger than  $\Gamma_1$  and  $\Gamma_2$ . This can further be partially converted into baryon asymmetry of the universe by B + L violating sphaleron [30] processes.

Now that there are several new heavy particles in LRSM, many new physics contributions to NDBD arises in addition to the standard contribution. It has been extensively studied in many of the earlier works (see Refs. [21,22]). Amongst the new physics contributions to  $0\nu\beta\beta$  decay, notable are the contributions coming from the exchange of the heavy gauge bosons ( $W_L^-$  and  $W_R^-$ ), the both the left and right handed gauge bosons (mixed diagrams,  $\lambda$  and  $\eta$ ) as well the scalar triplet ( $\Delta_L$  and  $\Delta_R$ ) contributions. The amplitude of these processes mostly depends upon the mixing between light and heavy neutrinos, the leptonic mixing matrix elements, the mass of the heavy neutrino ( $M_i$ ), the mass of the gauge bosons,  $W_L^-$  and  $W_R^-$ , the mass of the triplet Higgs as well as their coupling to leptons,  $f_L$  and  $f_R$ .

However in our present work, we have considered only three of the aforesaid contributions to NDBD. The ones mediated by  $W_R^-$  and the momentum dependent mechanisms, i.e., the contributions to NDBD from  $\lambda$  and  $\eta$  diagrams which involves the light and heavy neutrino mixings and the mixing between  $W_L^-$  and  $W_R^-$  bosons

(considering a small light heavy neutrino mixing of  $\mathcal{O}(10^{-6})$ . The amplitudes of the contributions are given in several earlier works like [22]. The mass scales for the heavy particles has been assumed to be  $\approx$ TeV, with  $M_{W_R} > M_N$ . Under these assumptions, the amplitude for the light-heavy mixing contribution which is proportional to  $\frac{m_D^2}{M_R}$  remains very small (since  $m_{\nu} \approx \frac{m_D^2}{M_R} \approx (0.01-0.1)$  eV,  $m_D \approx (10^5-10^6)$  eV which implies  $\frac{m_D}{M_R} \approx (10^{-7}-10^{-6})$  eV).

Again, the contribution from  $\Delta_L^-$ ,  $W_L^-$  is suppressed by the type II seesaw contribution to light neutrino mass and hence neglected here. Considering these contributions we have studied the NDBD and tried to correlate the effective mass governing the process with the BAU for different gauge boson masses in TeV scale LRSM.

As has been pointed out that successful low scale RL requires an absolute lower bound of 18 TeV on the mass of the RH gauge boson and recent work predicted that it can be produced for considerably lower value of  $M_{W_n}$ accessible at LHCs considering relatively large Yukawa couplings. Again, although it has been illustrated as the light-heavy neutrino mixing to be sufficiently large in TeV scale LRSM inorder to get dominant NDBD contributions from the momentum dependent mixed diagrams,  $\lambda$  and  $\eta$ , we have seen that a sizeable amount of BAU and effective mass governing NDBD (from  $\lambda$  and  $\eta$  diagrams) consistent with the experimental value is observed by considering a general structure of the Dirac mass matrix and not so large light-heavy neutrino mixing parameter. Without considering any special structure of  $M_D$  and  $M_{RR}$  in generic TeV scale LRSM, in order to get light neutrino mass of the order of sub eV,  $M_D$  has to be fine tuned to be very small which results in a lower value of the light heavy neutrino mixing parameter,  $\zeta$ . But, in our present work, by considering a smaller  $\zeta$  value, we have tried to correlate the effective mass from purely RH contribution and the suppressed effective mass coming from  $\lambda$  and  $\eta$  contributions with leptogenesis at a TEV scale LRSM.

The heavy Majorana neutrinos that takes part in explaining BAU as well as NDBD also plays a significant role in giving rise to experimentally testable rates of LFV processes like,  $\mu \to e\gamma$ ,  $\mu \to 3e$ ,  $\mu \to e$  etc. The different neutrino Yukawa couplings for each lepton flavour have a considerable impact on leptogenesis with nearly degenerate heavy neutrino mass. Owing to the presence of some new heavy particles in the LRSM, the LFV processes are mediated by these heavy neutrinos and doubly charged triplet Higgs bosons.

The relevant BR for the process  $(\mu \rightarrow 3e)$  is defined as, [31]

$$BR(\mu \to 3e) = \frac{1}{2} |h_{\mu e} h_{ee}^*|^2 \left( \frac{m_{W_L}^4}{M_{\Delta_L}^{++4}} + \frac{m_{W_R}^4}{M_{\Delta_P}^{++4}} \right).$$
 (28)

Where  $h_{ij}$  describes the lepton Higgs coupling in LRSM and is given by,

$$h_{ij} = \sum_{n=1}^{3} V_{in} V_{jn} \left( \frac{M_n}{M_{W_R}} \right), \quad i, j = e, \mu, \tau.$$
 (29)

For  $\mu \to e\gamma$ , the BR is given by, [31]

BR(
$$\mu \to e\gamma$$
) = 1.5 × 10<sup>-7</sup>| $g_{lfv}$ |<sup>2</sup> $\left(\frac{1 \text{ TeV}}{M_{W_p}}\right)^4$ , (30)

where,  $g_{lfv}$  is defined as,

$$g_{lfv} = \sum_{n=1}^{3} V_{\mu n} V_{en}^* \left( \frac{M_n}{M_{W_R}} \right)^2 = \frac{[M_R M_R^*]_{\mu e}}{M_{W_R}^2}. \quad (31)$$

The sum is over the heavy neutrinos only.  $M_{\Delta_{L,R}}^{++}$  are the masses of the doubly charged bosons,  $\Delta_{L,R}^{-++}$ , V is the mixing matrix of the right-handed neutrinos with the electrons and muons.  $M_n(n=1,2,3)$  are the right handed neutrino masses.

Several new sources of LFV are present in new physics BSM in LRSM due to the additional RH current interactions, which could lead to considerable LFV rates for TeV scale  $v_R$ . LFV in the LRSM has been studied in many previous works. There are various LFV processes providing constraints on the masses of the right-handed neutrinos and doubly charged scalars. It turns out that the process  $\mu \to 3e$  induced by doubly charged bosons  $\Delta_L^{++}$  and  $\Delta_R^{++}$ and  $\mu \rightarrow e \gamma$  provides the most relevant constraint. The upper limits of branching ratio of the process  $\mu \to 3e$  is  $< 1.0 \times 10^{-12}$  [32] at 90% CL was obtained by the SINDRUM experiment. Furthermore, the Mu3e collaboration has also submitted a letter of intent to PSI to perform a new improved search for the decay  $\mu \rightarrow 3e$  with a sensitivity of  $10^{-16}$  at 95% CL [33] which corresponds to an improvement by four orders of magnitude compared to the former SINDRUM experiment. While for the LFV process,  $\mu \to e\gamma$ , the BR is established to be  $< 4.2 \times 10^{-13}$ [34] at 90% CL by the MEG collaboration. Considering these contributions from heavy righthanded neutrinos and Higgs scalars, the expected branching ratios and conversion rates of the above processes have been calculated in the LRSM in the work (first reference in [35]).

#### IV. NUMERICAL ANALYSIS AND RESULTS

With reference to several earlier works [17–19,22,36] for TeV scale LRSM, we carried out an extensive study for RL, NDBD, and LFV, with a view to finding a common parameter space for these observabes. It is reasonable to check if the mass matrices that can explain the BAU of the universe can also provide sufficient parameter space for

other low energy observables like NDBD, LFV, etc. For NDBD, we have considered the mixed LH-RH contribution along with the purely RH neutrino contribution, considering a generalized structure for the Dirac mass matrix. The Dirac and Majorana mass matrices in our case are determined using the type I seesaw formula (as shown in the Appendix) and type II seesaw [Eq. (37)] respectively which satisfies the recent neutrino oscillation data. Whereas, in the previous works, the authors have considered specific Dirac and Majorana textures resulting in light neutrinos via type I seesaw with large light heavy neutrino mixing. They have chosen large Yukawa couplings as allowed by specific textures for calculation of the lepton asymmetry. As stated in [19], we have been found that it is possible to observe BAU with a lower  $W_R$  mass, in our case it is 5 TeV. Further, we have also correlated the LFV of the process,  $\mu \rightarrow 3e$ ,  $\mu \rightarrow e \gamma$  and with lightest neutrino mass and atmospheric mixing angle. In this section we present a detailed analysis of our work by dividing it into several subsections, firstly BAU, then NDBD and then LFV.

#### A. Baryogenesis via leptogenesis

The formula for light  $\nu$  masses in LRSM can be written as,

$$M_{\nu} = M_{\nu}{}^{I} + M_{\nu}{}^{II}, \tag{32}$$

where the type I seesaw mass term is,

$$M_{\nu}^{I} = M_{D} M_{RR}^{-1} M_{D}^{T}. {33}$$

We have considered a tribimaximal mixing (TBM) pattern, such that,

$$M_{\nu}^{\ I} = U_{(\text{TBM})} U_{\text{Maj}} M_{\nu}^{\ I(\text{diag})} U_{\text{Maj}}^{\ T} U_{(\text{TBM})}^{\ T}, \quad (34)$$

where  $M_{\nu}^{I(\text{diag})} = X M_{\nu}^{(\text{diag})}$  [37], the parameter X is introduced to describe the relative strength of the type I and II seesaw terms. It can take any numerical value provided the two seesaw terms gives rise to correct light neutrino mass matrix. In our case, we have considered X = 0.5 [37], i.e., equal contributions from both the seesaw terms. Thus, equation (32) can be written as,

$$U_{\text{PMNS}} M_{\nu}^{\text{(diag)}} U_{\text{PMNS}}^{T}$$

$$= M_{\nu}^{II} + U_{\text{(TBM)}} U_{\text{Maj}} X M_{\nu}^{\text{(diag)}} U_{\text{Maj}}^{T} U_{\text{(TBM)}}^{T}, \quad (35)$$

where,  $U_{\text{PMNS}}$  is the diagonalizing matrix of the light neutrino mass matrix,  $M_{\nu}$  and is given by,

$$U_{\text{PMNS}} = \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -c_{23}s_{12} - s_{23}s_{13}c_{12}e^{i\delta} & -c_{23}c_{12} - s_{23}s_{13}s_{12}e^{i\delta} & s_{23}c_{13} \\ s_{23}s_{12} - c_{23}s_{13}c_{12}e^{i\delta} & -s_{23}c_{12} - c_{23}s_{13}s_{12}e^{i\delta} & c_{23}c_{13} \end{bmatrix} U_{\text{Maj}}.$$
 (36)

TABLE I. Global fit  $3\sigma$  values of  $\nu$  oscillation parameters [38].

Parameters	3σ Ranges	Best FIT $\pm 1\sigma$	
$\Delta m_{21}^2 [10^-5 \text{ eV}^2]$	6.93-7.97	7.37	
$\Delta m_{31}^2 [10^-3 \text{ eV}^2] \text{ (NH)}$	2.37-2.63	2.50	
$\Delta m_{23}^2 \ [10^-3 \text{ eV}^2] \ (\text{IH})$	2.33-2.60	2.46	
$\sin^2 \theta_{12}$	0.250-0.354	0.297	
$\sin^2 \theta_{23}$ (NH)	0.379-0.616	0.437	
(IH)	0.383-0.637	0.569	
$\sin^2\theta_{13}$ (NH)	0.0185-0.0246	0.0214	
(IH)	0.0186-0.0248	0.0218	
$\delta/\pi$	0–2 (NH)	1.35	
	0–2 (IH)	1.32	

The abbreviations used are  $c_{ij} = \cos \theta_{ij}$ ,  $s_{ij} = \sin \theta_{ij}$ ,  $\delta$  is the Dirac *CP* phase while the diagonal phase matrix,  $U_{\text{Maj}}$  is diag $(1, e^{i\alpha}, e^{i(\beta+\delta)})$ , contains the Majorana phases  $\alpha$  and  $\beta$ . We have adopted the recent neutrino oscillation data in our analysis as in the Table I.

From type II seesaw mass term,  $M_{RR}$  can be written in the form (from Ref. [39]) as,

$$M_{RR} = \frac{1}{\gamma} \left( \frac{v_R}{M_{W_t}} \right)^2 M_{\nu}^{II},$$
 (37)

$$U_R M_{RR}^{\text{(diag)}} U_R^T = \frac{1}{\gamma} \left( \frac{v_R}{M_{W_I}} \right)^2 M_{\nu}^{II},$$
 (38)

$$\begin{split} M_{\nu}{}^{II} &= U_{\text{PMNS}} M_{\nu}{}^{(\text{diag})} U_{\text{PMNS}}{}^{T} \\ &- U_{(\text{TBM})} U_{\text{Maj}} X M_{\nu}{}^{(\text{diag})} U_{\text{Maj}}{}^{T} U_{(\text{TBM})}{}^{T}, \quad (39) \end{split}$$

where  $M_{RR}^{\text{(diag)}} = \text{diag}(M_1, M_2, M_3)$ . We have fine tuned the dimensionless parameter,  $\gamma \sim 10^{-10}$ . The variation of the RH gauge boson mass with heavy RH neutrino mass as shown in Fig. 1, corresponds to the condition  $M_{W_R} > M_N$ . As previously mentioned we have considered three different values of the  $SU(2)_R$  breaking scale,  $v_R$  for our further analysis, specifically 5 TeV, 10 TeV, and 18 TeV respectively, which will be useful to study the common parameter space of the phenomenon we have considered, i.e., BAU, NDBD, LFV. The left-handed gauge boson is  $M_{W_I} = 80$  GeV and determined the RHS of equation terms of lightest neutrino mass by varying the Majorana phases from 0 to  $2\pi$ . By considering a very tiny mass splitting of the Majorana masses  $M_1$  and  $M_2$  as per requirement of resonant leptogenesis, we equated both sides of Eq. (37) and obtained  $M_1$ ,  $M_2$ , and  $M_3$ , where,  $M_1 \approx M_2$ .

We considered the lepton number violating and CP violating decays of two heavy RH Majorana neutrinos,  $N_1$  and  $N_2$  via the decay modes,  $N_i \rightarrow l + \phi^c$  and its CP conjugate process,  $N_i \rightarrow l^c + \phi$ , i = 1, 2. First, we determined the leptonic CP asymmetry,  $\epsilon_1$  and  $\epsilon_2$  using

equation (26) where  $Y_{\nu} = \frac{M_D}{v}$ , v being the VEV of Higgs bidoublet and is 174 GeV. The decay rates in Eq. (26) can be obtained using Eq. (40). The Dirac mass,  $m_D$  as mentioned before is not of any specific texture, but we have obtained it from the type I seesaw equation in which we have considered the light neutrino mass  $M_{LL}$  and the heavy right handed Majorana neutrino mass to be known, which satisfies the current neutrino oscillation data.

The CP violating asymmetries  $\epsilon_1$  and  $\epsilon_2$  can give rise to a net lepton number asymmetry, provided the expansion rate of the universe is larger than  $\Gamma_1$  and  $\Gamma_2$ . The net baryon asymmetry is then calculated using [29,39],

$$\eta_B \approx -0.96 \times 10^{-2} \sum_i (k_i \epsilon_i),$$
(40)

 $k_1$  and  $k_2$  being the efficiency factors measuring the washout effects linked with the out of equillibrium decay of  $N_1$  and  $N_2$ . We can define the parameters,  $K_i \equiv \frac{\Gamma_i}{H}$  at temperature,  $T = M_i$ ,  $H \equiv \frac{1.66 \sqrt{g_* T^2}}{M_{\text{Planck}}}$  is the Hubble's constant with  $g_* \simeq 107$  and  $M_{\text{Planck}} \equiv 1.2 \times 10^{19}$  GeV is the Planck mass. The decay width can be estimated using Eq. (25). For simplicity, the efficiency factors,  $k_i$  can be calculated using the formula [40],

$$k_1 \equiv k_2 \equiv \frac{1}{2} \left( \sum_i K_i \right)^{-1.2},$$
 (41)

which holds validity for two nearly degenerate heavy Majorana masses and  $5 \le K_i \le 100$ . We have used the formula (40) in calculating the baryon asymmetry. The result is shown as a function of lightest neutrino mass by varying the Majorana phases from 0 to  $2\pi$  in Fig. 2 for different values of RH gauge boson mass. It is evident from the figure that the cosmological observed BAU from RL can be obtained for varying gauge boson mass  $M_{W_R}$ , distinctively, 5, 10 and 18 TeV in our case, which is in accordance to several prior works. In the case of mass hierarchy, IH seems to give better results in our analysis. The required amount of BAU is perceived for lightest neutrino mass of around (0.05-0.1) eV. For  $M_{W_R}=18$  TeV,

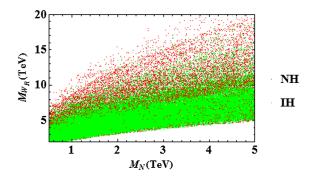


FIG. 1.  $M_{W_R}$  against heavy Majorana neutrino mass  $M_1$  in TeV For NH and IH.

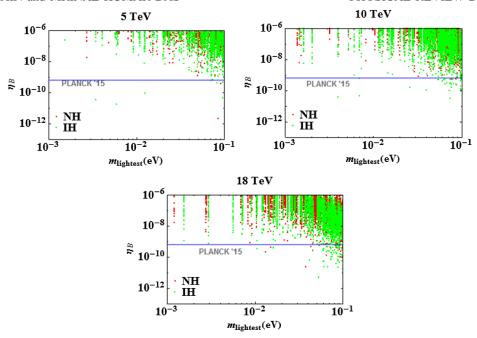


FIG. 2. BAU as a function of lightest neutrino mass,  $m_1/m_3$  (in eV)for NH/IH. The blue solid line represents the observed BAU in PLANCK '15[41] for different values of RH gauge boson mass, 5, 10, and 18 TeV respectively.

greater parameter space satisfies the observed BAU than for 5 TeV.

# B. NDBD from heavy RH neutrino not so large left-right mixing

In LRSM, owing to the presence of several new heavy particles, many new contributions arises to NDBD

amplitudes. In a previous work (second reference of [37]) we have considered the new physics contributions coming from the ones mediated by  $W_R^-$  and  $\Delta_R$  respectively. In the present work, besides the heavy RH neutrino contribution coming from the exchange of  $W_R$  bosons, we also considered the momentum dependent mechanisms also, i.e., the  $\lambda$  and  $\eta$  contributions to NDBD due to

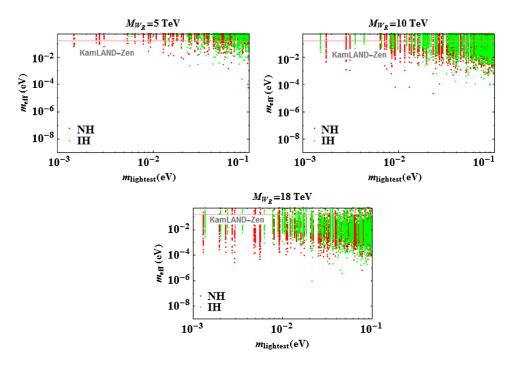


FIG. 3. Effective Majorana mass for  $0\nu\beta\beta$  as a function of lightest neutrino mass, for new physics contribution coming from RH  $\nu$  for both NH and IH. The pink solid line represents the KamLAND-Zen upper bound on the effective neutrino mass.

gauge boson mixing since we have seen non-negligible contributions from these momentum dependent mechanisms in our case.

The effective neutrino mass corresponding to the heavy RH neutrino contribution from the exchange of  $W_R$  gauge bosons is given by,

$$M_{\text{eff}}^{N} = p^{2} \frac{M_{W_{L}}^{4}}{M_{W_{R}}^{4}} \frac{U_{\text{Rei}}^{*} 2}{M_{i}}.$$
 (42)

Here,  $\langle p^2 \rangle = m_e m_p \frac{M_N}{M_\nu}$  is the typical momentum exchange of the process, where  $m_p$  and  $m_e$  are the mass of the proton and electron respectively and  $M_N$  is the NME corresponding to the RH neutrino exchange. The allowed value of p (the virtuality of the exchanged neutrino) is in the range  $\sim (100-200)$  MeV. In our analysis, we have taken  $p \simeq 180$  MeV [22]. As in case of BAU, herein, we have considered different values of  $M_{W_R}$ , namely, 5, 10 and 18 TeV respectively.  $U_{\rm Rei}$  are the first row elements of the

diagonalizing matrix of the heavy right handed Majorana mass matrix  $M_{RR}$  and  $M_i$  is its mass eigenvalues,  $M_i$ .

(i) In case of  $\lambda$  contribution, the particle physics parameter that measures the lepton number violation is given by,

$$|\eta_{\lambda}| = \left(\frac{M_{W_L}}{M_{W_R}}\right) \left| \sum_{i} U_{e_i} T_{e_i}^* \right|. \tag{43}$$

(ii) While the  $\eta$  contribution to NDBD due to  $W_L - W_R$  mixing is described by the parameter,  $\tan \zeta$ , as in Eq. (22), with particle physics parameter,

$$|\eta_{\eta}| = \tan \zeta \Big| \sum_{i} U_{ei} T_{ei}^* \Big|. \tag{44}$$

In the above equations,  $U_{e_i}$  represents the elements of the matrix as defined by Eq. (16), and T is represented by Eq. (19), the term  $|\sum_i U_{ei} T^*_{ei}|$  can be simplified to the form  $-[M_D M_{RR}^{-1}]_{ee}$  (as in second reference of [31]).  $V_{\nu}$  in the

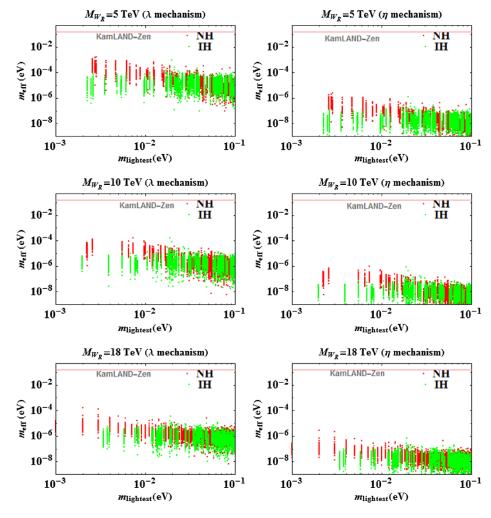


FIG. 4. Effective Majorana mass for  $0\nu\beta\beta$  as a function of lightest neutrino mass, for new physics contribution coming from  $\lambda$  (left figures) and  $\eta$  mechanisms (right figures) for NH and IH for different RH gauge boson masses. The pink solid line represents the KamLAND-Zen upper bound on the effective neutrino mass.

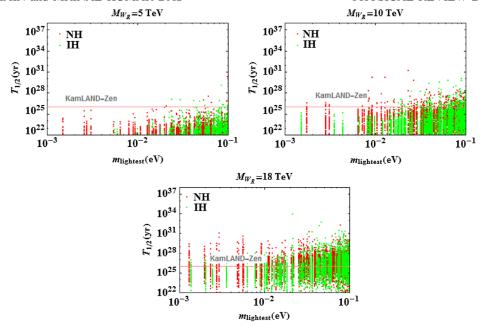


FIG. 5. Half life for  $0\nu\beta\beta$  as a function of lightest neutrino mass for NH and IH for heavy RH neutrino contribution. The horizontal pink line represents the KamLAND-Zen lower bound on the half life of NDBD.

expression for T is the diagonalizing matrix of  $M_{\nu}$ . The effective Majorana neutrino mass due to  $\lambda$  and  $\eta$  contribution is thus given by,

$$M_{\rm eff}^{\lambda} = \frac{\eta_{\lambda}}{m_e}, \qquad M_{\rm eff}^{\eta} = \frac{\eta_{\eta}}{m_e}.$$
 (45)

The half lives corresponding to these effective mass values is given by,

$$[T_{\frac{1}{2}}^{0\nu}]^{-1} = G^{0\nu}(Q, Z) |M_N^{0\nu}|^2 \frac{|M_{\text{eff}}^N|_N^2}{m_e^2}, \tag{46}$$

$$[T_{\frac{1}{2}}^{0\nu}]^{-1} = G^{0\nu}(Q, Z) |M_{\lambda}^{0\nu}|^2 \frac{|M_{\text{eff}}^{\lambda}|_N^2}{m_e^2}, \tag{47}$$

$$[T_{\frac{1}{2}}^{0\nu}]^{-1} = G^{0\nu}(Q, Z) |M_{\eta}^{0\nu}|^2 \frac{|M_{\text{eff}}^{\eta}|_N^2}{m_e^2}, \tag{48}$$

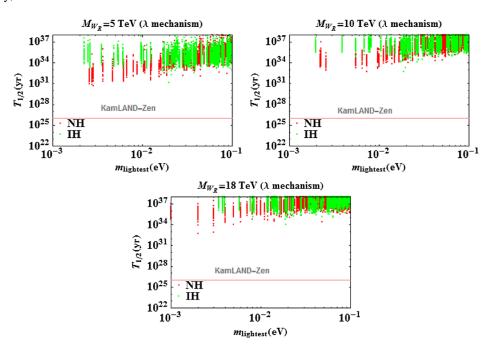


FIG. 6. Half life for  $0\nu\beta\beta$  as a function of lightest neutrino mass for NH and IH for  $\lambda$  mechanism. The horizontal line represents the KamLAND-Zen lower bound on the half life of NDBD.

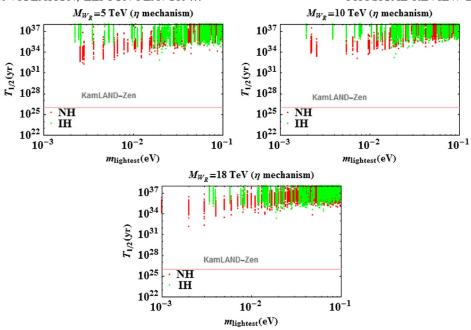


FIG. 7. Half life for  $0\nu\beta\beta$  as a function of lightest neutrino mass for NH and IH for  $\eta$  mechanism. The horizontal line represents the KamLAND-Zen lower bound on the half life of NDBD.

where,  $G^{0\nu}$  and  $|M^{0\nu}|$  represents the phase space factor and the nuclear matrix elements of the processes which holds different values as in [42].

Figures 3 to 7 shows the effective mass and half life governing NDBD from RH neutrino,  $\lambda$  and  $\eta$  contribution against the lightest neutrino mass. For new physics contribution coming from purely RH current, the effective mass governing NDBD is consistent with the experimental

results as propounded by KamLAND-Zen for all the cases  $(M_{W_R}=5,\ 10,\ 18\ \text{TeV})$  although better results is obtained for 18 TeV. It is not much dependent on the mass hierarchy. Whereas, for NDBD contributions from  $\lambda$  and  $\eta$  mechanisms, the effective mass is found to be within the experimental limit but of lower magnitude than the RH neutrino contributions. We have seen that  $\eta$  contribution  $(10^{-6}-10^{-8})$  eV is around two orders of magnitude less than the  $\lambda$  contribution

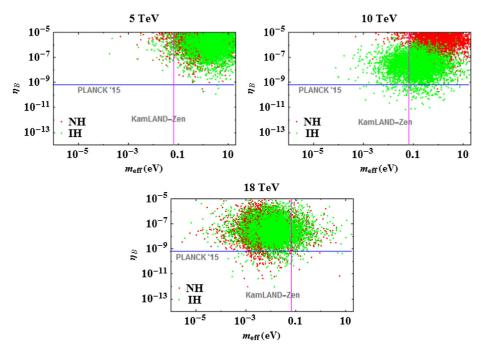


FIG. 8. BAU against effective Majorana neutrino mass for RH  $\nu$  contribution. The solid blue and pink line represents the observed BAU and the KAMLAND upper bound on effective Majorana neutrino mass.

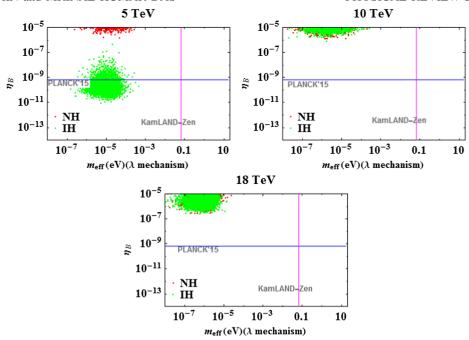


FIG. 9. BAU against effective Majorana neutrino mass (for  $\lambda$  mechanism). The solid blue and pink line represents the observed BAU and the KAMLAND upper bound on effective Majorana neutrino mass.

 $(10^{-4}-10^{-6})$  eV in all the cases shown in Fig. 4 irrespective of the mass hierarchies. Similar results are obtained for the half lives of the process as shown in Figs. 5,6.

Figures 8–10 shows the correlation of NDBD and BAU for the different contributions. It is seen that BAU and NDBD (for RH  $\nu$  contribution) can simultaneously satisfy

the experimental results for  $M_{W_R} = 10$  and 18 TeV in our case, although for 10 TeV case only IH is consistent with the experimental bounds. As far as the mixed contributions are concerned, a common parameter space for NDBD and BAU is observed only for RH gauge boson mass to be 5 TeV and for IH only.

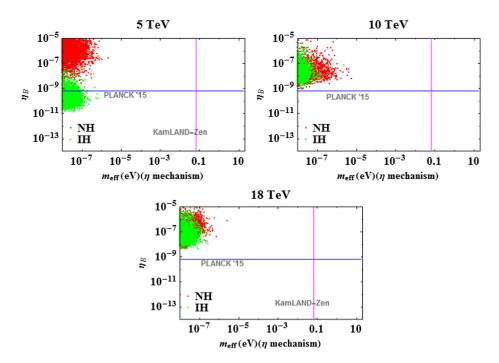


FIG. 10. BAU against effective Majorana neutrino mass (for  $\eta$  mechanism). The solid blue and pink line represents the observed BAU and the KAMLAND upper bound on effective Majorana neutrino mass.

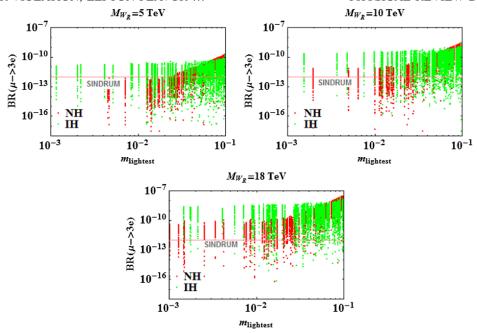


FIG. 11. BR for  $\mu \to 3e$  shown as a function of the lightest neutrino mass. The solid pink line represents the limit of BR as given by SINDRUM experiment.

### C. Lepton flavor violation

In our analysis, we further studied the LFV processes,  $\mu \to 3e$  and  $\mu \to e\gamma$  and correlated the branching ratios (BR) with the lightest neutrino mass and the atmospheric mixing angle respectively as in our previous work (second reference of [37]). For calculating the BR, we used the expression given in Eq. (28). The lepton Higgs coupling  $h_{ij}$ 

in (29) can be computed explicitly for a given RH neutrino mass matrix as shown in Eq. (37) by diagonalizing the RH neutrino mass matrix and obtaining the mixing matrix element,  $V_i$  and the eigenvalues  $M_i$ . For evaluating  $M_{RR}$ , we need to know  $M_{\nu}^{\text{II}}$ , as evident from Eq. (37). We computed  $M_{\nu}^{\text{II}}$  from Eq. (38). For determining the BR for  $\mu \to 3e$ , we imposed the best fit values of the parameters,

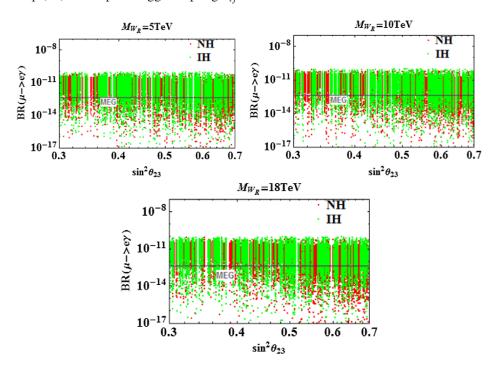


FIG. 12. BR for  $\mu \to e \gamma$  shown as a function of the atmospheric mixing angle. The horizontal solid line shows the limit of BR as given by MEG experiment.

TABLE II. summarized form of the results for NDBD, BAU, LFV for both NH and IH. The  $\checkmark$  and x symbol are used to denote if the observables are (not are) in the current experimental limit.

Observables	5 TeV NH (IH)	10 TeV NH (IH)	18 TeV NH (IH)
NDBD $(N_R)$	<b>√</b> ( <b>√</b> )	√(√)	<b>√</b> ( <b>√</b> )
NDBD (λ)	$\checkmark(\checkmark)$	$\checkmark(\checkmark)$	$\checkmark(\checkmark)$
NDBD (η)	$\checkmark(\checkmark)$	$\checkmark(\checkmark)$	$\checkmark(\checkmark)$
BAU	$\checkmark(\checkmark)$	$\checkmark(\checkmark)$	$\checkmark(\checkmark)$
BAU and NDBD $(N_R)$	$\mathbf{X}(\mathbf{X})$	<b>X</b> ( <b>✓</b> )	$\checkmark(\checkmark)$
BAU and NDBD (λ)	<b>X</b> ( <b>√</b> )	X(X)	X(X)
BAU and NDBD (η)	<b>X</b> ( <b>✓</b> )	$\mathbf{X}(\mathbf{X})$	$\mathbf{X}(\mathbf{X})$
$BR(\mu \rightarrow 3e)$	$\checkmark(\checkmark)$	$\checkmark(\checkmark)$	$\checkmark(\checkmark)$
$BR(\mu \to e\gamma)$	<b>√</b> ( <b>√</b> )	√(√)	<b>√</b> ( <b>√</b> )

 $\Delta m_{\rm sol}^2$ ,  $\Delta m_{\rm atm}^2$ ,  $\delta$ ,  $\theta_{13}$ ,  $\theta_{23}$ ,  $\theta_{12}$  in  $M_{\nu}$ . The numerical values of  $M_{\nu}^{T}$  can be computed considering TBM mixing pattern in our case. Thus, we get  $M_{\nu}^{\text{II}}$  as a function of the parameters  $\alpha$ ,  $\beta$  and  $m_{\text{lightest}}$ . Then varying both the Majorana phases,  $\alpha$ ,  $\beta$  from 0 to  $2\pi$ , we obtained  $M_{\nu}^{II}$ as a function of  $m_{\text{lightest}}$ . Similarly, for  $\mu \to e \gamma$  we substituted the values of the lightest mass (m1/m3) for (NH/IH) as (0.07 eV/0.065 eV) and best fit values for the parameters  $\Delta m_{\rm sol}^2$ ,  $\Delta m_{\rm atm}^2$ ,  $\delta$ ,  $\theta_{13}$ , while varying both the Majorana phases,  $\alpha$ ,  $\beta$  from 0 to  $2\pi$  and thus obtained  $M_{\nu}^{\text{II}}$  and hence  $M_{RR}$  as a function of the atmospheric mixing angle  $\theta_{23}$ . Thus BR can be obtained as a function of  $\sin^2 \theta_{23}$  from Eq. (28). We have varied the value of  $\sin^2 \theta_{23}$  in its  $3\sigma$  range as in [43] and the lightest neutrino mass from  $10^{-3}$  to  $10^{-1}$ and obtained the values of BR. Like the previous cases (BAU and NDBD), we have considered three values of the right-handed gauge boson mass, 5 TeV, 10 TeV and 18 TeV respectively and different results have been obtained for these different values.

The variation is shown in Figs. 11 and 12 for both NH and IH. It is obvious from the figures that for both the LFV process, a good amount of parameter space is consistent with the experimental results for the different RH gauge boson mass we have considered i.e. 5, 10, and 18 TeV.

We have shown a summarized form of our results in tabular form in Table II.

### V. DISCUSSION AND CONCLUSION

While calculating the NDBD contribution and BAU we concentrated on an important issue that whether both the phenomena can be correlated in TeV scale or not. As addressed by the author in [17] TeV-scale LRSM, there are complications due to the presence of RH gauge interactions that contribute to the dilution and washout of the primordial lepton asymmetry generated via resonant leptogenesis. Combined with the dilution effects from inverse decays and entropy, this implies that even for maximal CP asymmetry the observed baryon-to-photon ratio can be obtained only if  $M_{W_p} \ge 18$  TeV. They have basically

focused on the possibilities of falsification of leptogenesis owing to the possible experimental observation of RH gauge boson mass of around (3–5) TeV. But in the recent papers [18,19] authors have taken up this issue and claim that one can generate the baryon asymmetry within the experimental limit even if RH gauge boson mass is as low as 5 TeV. In their work, instead of assuming maximal CP asymmetry, they calculated the premordial CP asymmetry as demanded by their specific neutrino fix. Furthermore, they have also shown the consistency of their model with other low energy constraints like NDBD, LFV etc. thereby specifying the fact that just the possible observation of  $W_R$  at LHC alone cannot falsify leptogenesis as a mechanism to generate matterantimatter asymmetry of the universe. Since the main purpose of our work is to see if there is a common parameter space where we can establish a linkage between baryogenesis and the low scale phenomenon like NDBD and LFV, we have done a phenomenological study of these phenomenon at a TeV scale LRSM considering some specific values of RH Gauge boson mass, 5 TeV, 10 TeV, and 18 TeV (as found separately in the earlier works) and check the consistency of the previous results. Based on our study, we could arrive at the following conclusions,

- (i) For a low scale model independent seesaw model, one can account for successful leptogenesis and also the constraints that comes after regarding mass of the RH gauge bosons is that larger parameter space for BAU with the observed cosmological value is obtained for  $M_{W_R} = 18$  TeV than for 5 TeV.
- (ii) New physics contributions to NDBD in TeV scale LRSM for different  $M_{W_R}$  shows that dominant contribution comes from the exchange of RH gauge boson rather than the mixed, LH-RH gauge boson mixing contributions. The  $\lambda$  contributions to NDBD is a bit suppressed, owing to the less Yukawa coupling and not so large left-right mixing in our analysis while  $\eta$  contribution is further suppressed by two orders of magnitude that the  $\lambda$  contribution.
- (iii) It is possible to obtain a common parameter space for both NDBD and BAU. This corresponds to the NDBD contribution coming from the heavy RH neutrino for both NH and IH. However, in this case better results are obtained for 18 TeV RH gauge boson mass. Whereas, as far as the momentum dependent  $\lambda$  and  $\eta$  mechanisms are concerned, both NDBD and BAU can be simultaneously explained for  $M_{W_R} = 5$  TeV or < 10 TeV and only for IH.
- (iv) Sizeable implications for other low energy observable, charged LFV of the processes,  $\mu \rightarrow 3e$  and  $\mu \rightarrow e\gamma$  are obtained for a minimal TeV scale LRSM which simultaneously accounts for BAU and NDBD.

For LFV, the BR prediction for  $\mu \rightarrow e \gamma$  is not much dependent on the atmospheric mixing angle,  $\theta_{23}$ .

Having done an extensive study of several of the earlier works, we have found that our results are in accordance with the previous works where low scale phenomena are discussed. That successful leptogenesis can be found within the vicinity of the experimental limit for RH gauge boson mass as low as 5 TeV and is not much dependent on the mass hierarchy, NH or IH. However, both low scale BAU and effective mass governing NDBD can be simultaneously obtained for only some parameter space that depends on the mass hierarchy and the  $W_R$  mass as mentioned in the above points. Notwithstanding a more detailed study is preferred in order to give a strong concluding remark.

#### **APPENDIX**

### 1. Determination of $M_D$

From type I SS term,  $M_{\nu}^{\rm I} \approx -M_D M_{RR}^{-1} M_D^T$  Again,  $M_{\nu}^{\rm I} = U_{\rm (TBM)} U_{\rm Maj} X M_{\nu}^{\rm (diag)} U_{\rm Maj}^{\rm T} U_{\rm (TBM)}^{\rm T}$ 

$$M_{RR} = \frac{1}{\gamma} \left( \frac{v_R}{M_{W_*}} \right)^2 M_{\nu}^{\text{II}} \tag{A1}$$

Where,  $M_{\nu}^{\text{II}} = U_{\text{PMNS}} M_{\nu}^{\text{(diag)}} U_{\text{PMNS}}^{T} - U_{\text{(TBM)}} U_{\text{Maj}} X M_{\nu}^{\text{(diag)}} U_{\text{Maj}}^{T} U_{\text{(TBM)}}^{T}$ . Considering, X = 0.5,  $M_{W_{L}} = 80$  GeV,  $v_{R} = 5$  TeV (for one case only), and expressing  $M_{\nu}^{\text{(diag)}}$  in terms of lightest neutrino mass,  $m_{1}(m_{3})$  for NH (IH), we obtained  $M_{RR}$  varying the Majorana phases  $\alpha$  and  $\beta$  from 0 to  $2\pi$  and lightest neutrino mass from  $10^{-3}$  to  $10^{-1}$ .

We have considered  $M_D$  as,

$$M_D = \begin{bmatrix} a_1 & a_2 & a_3 \\ a_2 & a_4 & a_5 \\ a_3 & a_5 & a_6 \end{bmatrix}, \tag{A2}$$

which is  $\mu - \tau$  symmetric. Equating both sides of type I seesaw equation and solving for  $a_1$ ,  $a_2$ ,  $a_3$ ,  $a_4$ ,  $a_5$ ,  $a_6$ , we obtain the matrix elements of one of the  $M_D$  of the form,

$$M_D = \begin{bmatrix} 24776.2 + 122368.i & 70524.8 + 76561.i & -12687.1 + 21472.4i \\ 70524.8 + 76561.i & 14308.4 + 138730.i & -45802.3 - 46293.4i \\ -12687.1 + 21472.4i & -45802.3 - 46293.4i & 87313.6 + 158166.i \end{bmatrix}, \tag{A3}$$

which we have implemented for our further analysis.

## 2. Elements of the type II seesaw mass matrix

$$S_{11} = (c_{12}^2 c_{13}^2 - X c_{12}^{2 \text{ TBM}}) m_1 + e^{2i(\beta - \delta)} s_{13}^2 m_3 + (c_{13}^2 s_{12}^2 - X s_{12}^2 {}^{\text{TBM}}) e^{2i\alpha} m_2$$
(A4)

$$S_{12} = (-c_{12}c_{13}c_{23}s_{12} - c_{12}^{2}c_{13}s_{13}s_{23}e^{i\delta} + Xc_{12}^{\text{TBM}}c_{23}^{\text{TBM}}s_{12}^{\text{TBM}})m_{1}$$

$$+ (-c_{13}s_{12}c_{12}c_{23}e^{2i\alpha} - c_{13}s_{12}^{2}s_{13}s_{23}e^{i(2\alpha+\delta)} + Xc_{12}^{\text{TBM}}c_{23}^{\text{TBM}}s_{12}^{\text{TBM}}e^{2i\alpha})m_{2}$$

$$+ (c_{13}s_{13}s_{23}e^{i(2\beta-\delta)})m_{3}$$
(A5)

$$S_{13} = (c_{12}^2 c_{13} c_{23} s_{13} e^{i\delta} + s_{12} s_{23} c_{12} c_{13} - X c_{12}^{\text{TBM}} s_{12}^{\text{TBM}} s_{23}^{\text{TBM}}) m_1 + (-c_{13} s_{12} c_{23} s_{12} s_{13} e^{i(2\alpha + \delta)} - X c_{12}^{\text{TBM}} s_{12}^{\text{TBM}} s_{23}^{\text{TBM}} e^{2i\alpha}) m_2 + (e^{i(2\beta - \delta)} c_{13} c_{23} s_{13}) m_3$$
(A6)

$$S_{21} = (-c_{12}c_{13}c_{23}s_{12} - c_{12}^2c_{13}s_{13}s_{23}e^{i\delta} + Xc_{12}^{TBM}c_{23}^{TBM}s_{12}^{TBM})m_1 + (c_{13}s_{12}c_{12}c_{23}e^{2i\alpha} - s_{12}^2s_{13}s_{23}c_{13}e^{i(2\alpha+\delta)} + Xc_{12}^{TBM}c_{23}^{TBM}s_{12}^{TBM}e^{2i\alpha})m_2(e^{i(2\beta-\delta)}c_{13}s_{23}s_{13})m_3$$
(A7)

$$\begin{split} S_{22} &= \left( (c_{23}s_{12} - e^{i\delta}c_{12}s_{13}s_{23})^2 - Xc_{23}^2{}^{\text{TBM}}s_{12}^2{}^{\text{TBM}} \right) m_1 + \left( -Xc_{12}^2{}^{\text{TBM}}c_{23}^2{}^{\text{TBM}} + \left( -c_{12}c_{23} - e^{i\delta}s_{12}s_{13}s_{23} \right)^2 \right) m_2 e^{2i\alpha} \\ &+ \left( c_{13}^2s_{23}^2 - Xs_{23}^2{}^{\text{TBM}}e^{2i\beta} \right) m_3 \end{split} \tag{A8}$$

$$\begin{split} S_{23} &= ((-c_{12}c_{23}s_{13}e^{i\delta} + s_{12}s_{23})(-c_{23}s_{12} - e^{i\delta}c_{12}s_{13}s_{23}) + Xc_{23}^{\text{TBM}}s_{12}^{2} \\ &\quad + ((-e^{i\delta}c_{23}s_{12}s_{13} + c_{12}s_{23})(-c_{12}c_{23} - e^{i\delta}s_{12}s_{13}s_{23}) + Xc_{12}^{2} \\ &\quad + (c_{13}^{2}c_{23}s_{23}e^{2i\beta} - c_{23}^{\text{TBM}}s_{23}^{\text{TBM}})m_{3} \end{split} \tag{A9}$$

$$\begin{split} S_{31} &= (c_{12}^2 c_{13} c_{23} s_{13} e^{i\delta} + s_{12} s_{23} c_{12} c_{13} - X c_{12}^{\text{TBM}} s_{12}^{\text{TBM}} s_{23}^{\text{TBM}}) m_1 \\ &+ (c_{13} s_{12}^2 e^{i\delta} c_{23} s_{13} + c_{12} s_{23} c_{13} s_{12} e^{2i\alpha} - X c_{12}^{\text{TBM}} s_{12}^{\text{TBM}} s_{23}^{\text{TBM}}) m_2 e^{2i\alpha} + (e^{2i\beta - i\delta} c_{13} c_{23} s_{13}) m_3 \end{split} \tag{A10}$$

$$\begin{split} S_{32} &= ((-e^{i\delta}c_{12}c_{23}s_{13} + s_{12}s_{23})(-c_{23}s_{12} - e^{i\delta}c_{12}s_{13}s_{23}) + c_{23}^{\text{TBM}}s_{12}^{2}^{\text{TBM}}s_{23}^{\text{TBM}})m_1 \\ &\times ((-e^{i\delta}c_{23}s_{12}s_{13} + c_{12}s_{23})(-c_{12}c_{23} - e^{i\delta}s_{12}s_{13}s_{23}) + Xc_{12}^{2}^{\text{TBM}}c_{23}^{\text{TBM}}s_{23}^{\text{TBM}})e^{2i\alpha}m_2 \\ &\times (c_{13}^2c_{23}s_{23} - Xc^{\text{TBM}}{}_{23}s^{\text{TBM}}{}_{23})e^{2i\beta}m_3 \end{split} \tag{A11}$$

$$\begin{split} S_{33} &= ((-e^{i\delta}c_{12}c_{23}s_{13} + s_{12}s_{23})^2 - Xs_{12}^2{}^{\text{TBM}}s_{23}^2{}^{\text{TBM}})m_1 \\ &+ ((-e^{i\delta}c_{23}s_{12}s_{13} + c_{12}s_{23})^2 - Xc_{12}^2{}^{\text{TBM}}s_{23}^2{}^{\text{TBM}})e^{2i\alpha}m_2 + (c_{13}^2c_{23}^2 - c_{23}^2{}^{\text{TBM}})e^{2i\beta}m_3 \end{split} \tag{A12}$$

Where,  $c_{ij}^{\text{TBM}} = \cos \theta_{ij}^{\text{TBM}}$ ,  $s_{ij}^{\text{TBM}} = \sin \theta_{ij}^{\text{TBM}}$  represents the mixing angles for TBM neutrino mass matrix.

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